

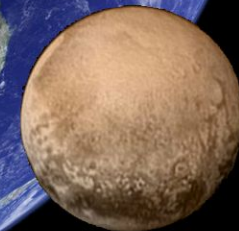
# 冥王星地下海の 安定性と進化

木村 淳(大阪大学・理)

Death Star I  
160 km



Charon  
1208 km



Pluto  
2370 km



Death Star II  
900 km

ACK for 鎌田さん

Earth  
12,742 km

# Background

- **Pluto:** icy dwarf planet
  - Radius = 1186 km
  - Bulk density = 1.88 g/cc (30-35 wt% of H<sub>2</sub>O)
  - No detectable flattening implies warm/deformable interior (ocean?) [Nimmo+ 2016]
  - Extensional tectonics with strong H<sub>2</sub>O spectral signature [Moore+ 2016, Grundy+ 2016]
  - Astrobiological/geophysical interests to investigate the conditions which Pluto may retain an ocean.

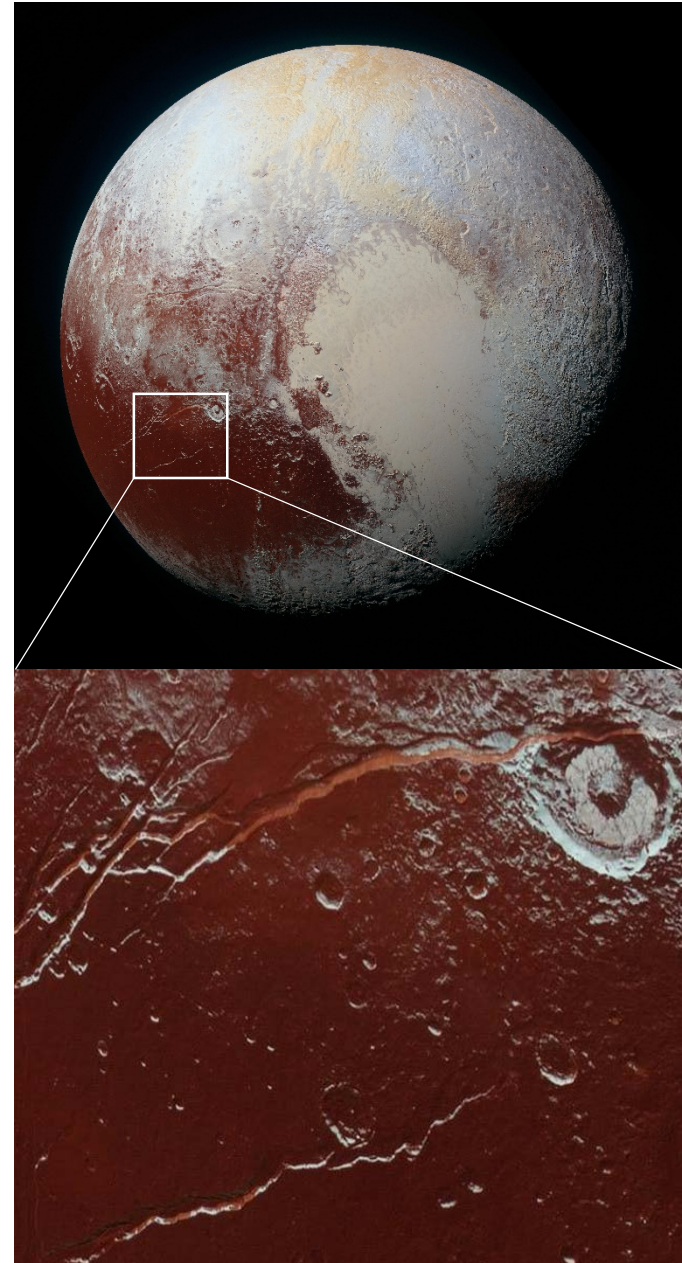


Image credit: NASA/JPL

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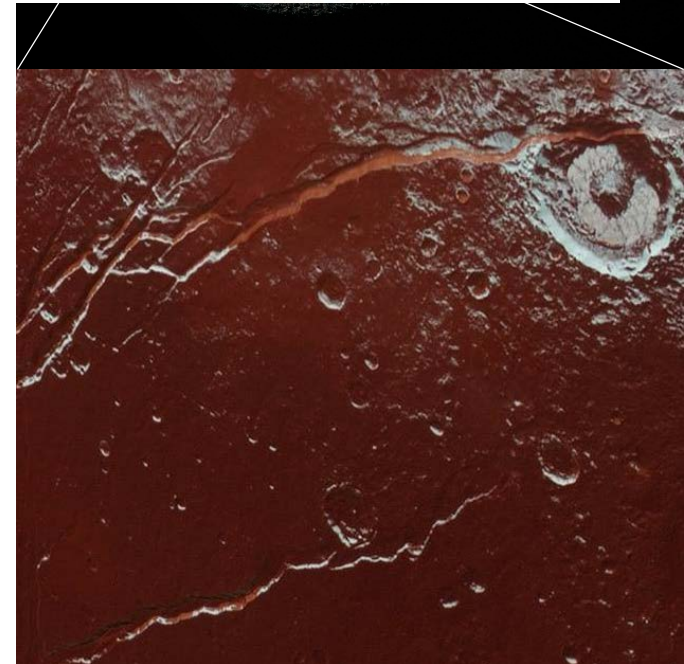
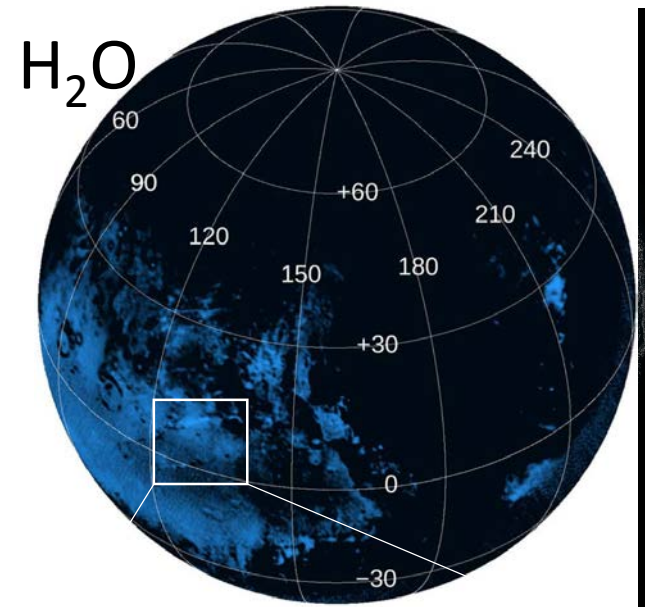


Image credit: NASA/JPL

# Previous study for Pluto's evolution

- Robuchon and Nimmo (2011)

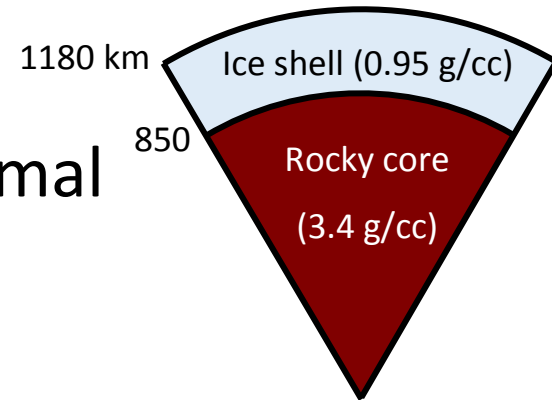
- Numerical simulation for interior thermal evolution w/ cold initial state using 2-layered interior model.

- If the ice shell has a large viscosity (reference vis  $>5 \times 10^{15}$  Pas), the ocean should be present.

- Caveat

- Only Ice-Ih appeared case is considered.
- Assumed rocky core is conductive (no convection included)

→ Needs a further investigations under various structural settings (HP-ice appeared case) and different initial thermal states (cold and hot).



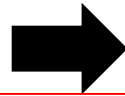
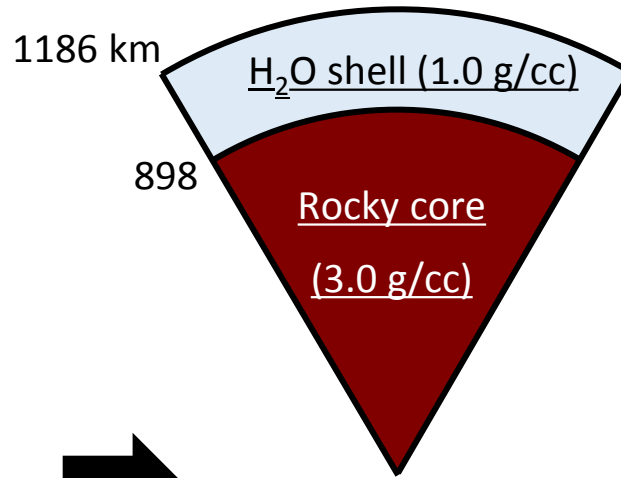
HP: high-pressure

# Structural settings

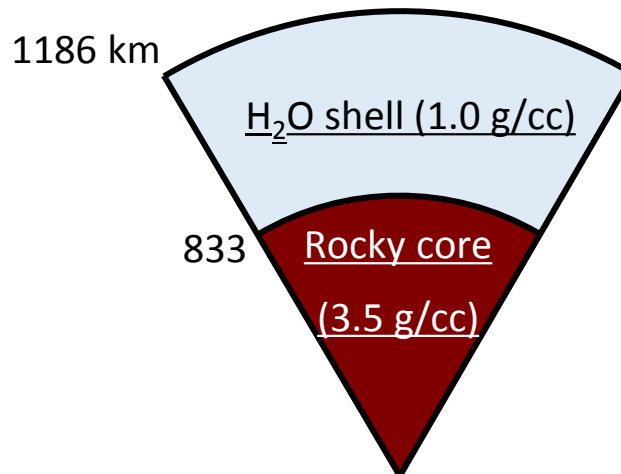
- Mean Radius  
= 1186 km

- Mass  
=  $1.305 \times 10^{22}$  kg

- Bulk density  
= 1.88 g/cc

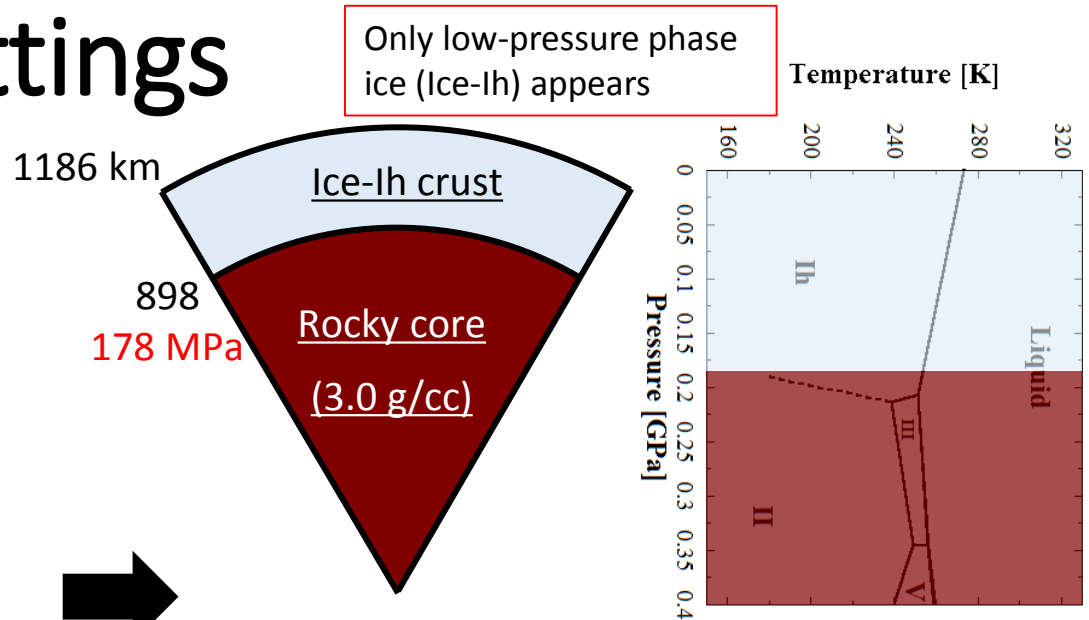


If 2-components are completely differentiated

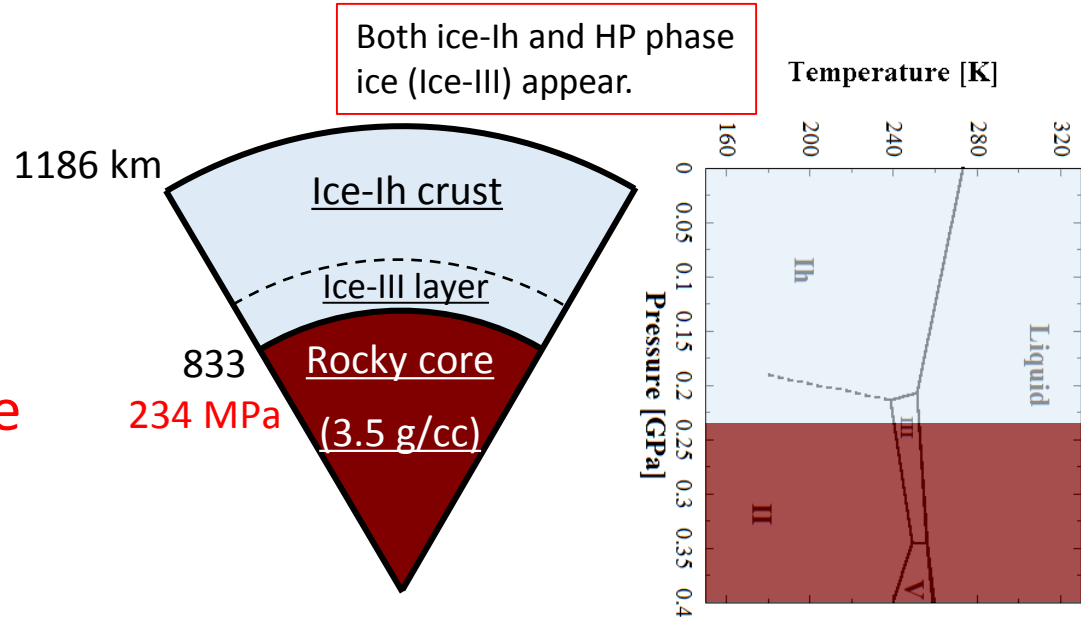
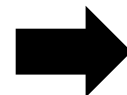


# Structural settings

- Mean Radius = 1186 km
- Mass =  $1.305 \times 10^{22}$  kg
- Bulk density = 1.88 g/cc



Only low-pressure phase ice (Ice-Ih) appears

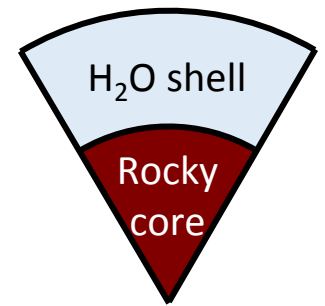


Both ice-Ih and HP phase ice (Ice-III) appear.

## → Considers

- a large core (only ice-Ih) case
- a small core (ice-Ih-III) case

# Model



- 1-D thermal-structural evolution model

- Mixing Length Theory for solid parts

$$\rho C_p \frac{\partial T}{\partial t} = \nabla \cdot \mathbf{F} + \rho Q$$

[e.g., Kimura+ 2009, Wagner+ 2011]

$$\mathbf{F} = F_{cond} + F_{conv}$$

$$F_{cond} = k_c \nabla T$$

$$F_{conv} = k_v (\nabla T - \nabla_{ad} T) \quad k_v = \begin{cases} 0 & \frac{\partial T}{\partial r} < \left(\frac{\partial T}{\partial r}\right)_{ad} \\ \frac{\rho C_p \alpha g l^4}{18\nu} \left[ \frac{\partial T}{\partial r} - \left(\frac{\partial T}{\partial r}\right)_{ad} \right] & \frac{\partial T}{\partial r} > \left(\frac{\partial T}{\partial r}\right)_{ad} \end{cases}$$

- Parametrized Convection Theory for liquid part

t: time  
 T: temperature  
 r: density  
 C<sub>p</sub>: specific heat  
 Q: heat generation  
 k<sub>c</sub>: thermal conductivity  
 n: kinetic viscosity  
 r: radius  
 a: thermal expansion coef.  
 l: mixing length  
 g: gravity

- conduction/convection, spherical symmetry

- Rheologies [Goldsby & Kohlstedt 2001; Karato+ 1986]

- Liquid water,  $\eta_w = 10^{-3}$  Pas

- Solid ices,  $\eta_{ice} = \eta_{ice0} \exp\left[25 \left(\frac{T_m}{T} - 1\right)\right]$

$$\eta_{ice0} = 1 \times 10^{15}, 5 \times 10^{17} \text{ Pas}$$

- Rock,  $\eta_{rock} = 4.9 \times 10^8 \exp(23.25 T_m / T)$

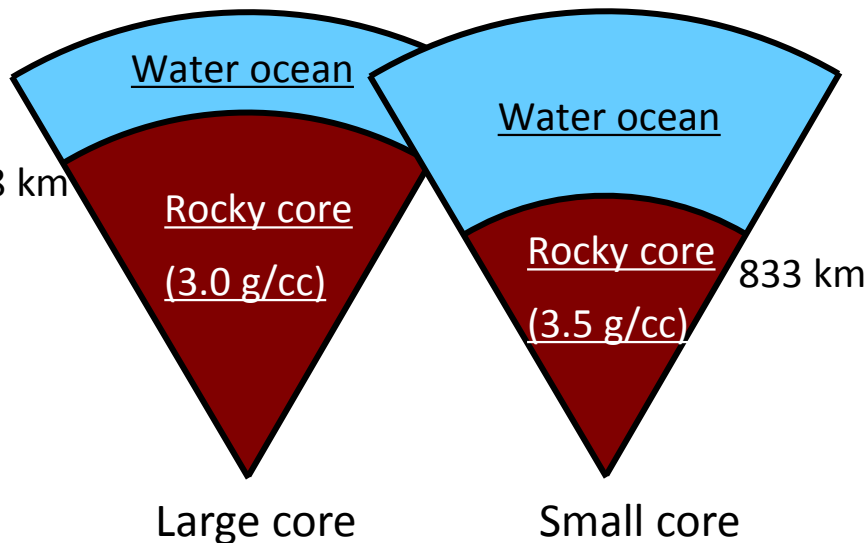
- Heat source

- U = 12.0 ppb, Th/U = 3.3,  
 K/U = 6.15x10<sup>4</sup>

(Carbonaceous chondritic)

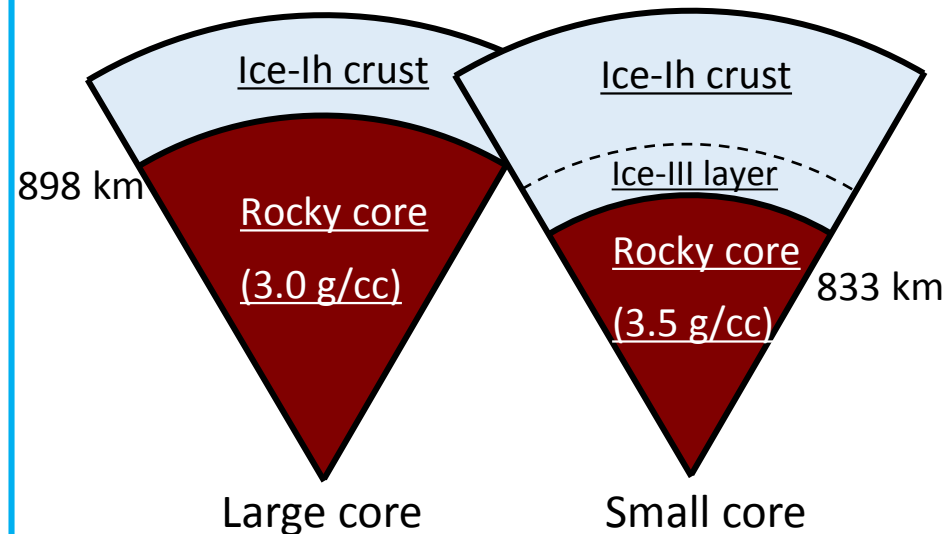
# Structural setting and initial state

- Hot (ocean) start  
No solid ice shell and vast ocean



- Surface: 273.15 K  $\rightarrow$  44 K
- Ocean: adiabatic T-grad
- Core: iso-T of the ocean-core boundary

- Cold (icy) start  
Initial H<sub>2</sub>O layer is entirely frozen

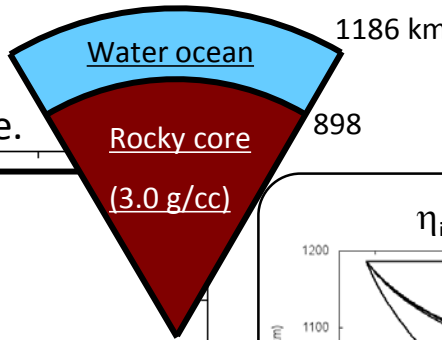


- Surface: 44 K
- Ice: iso-T of 250 K
- Core: iso-T of 250 K

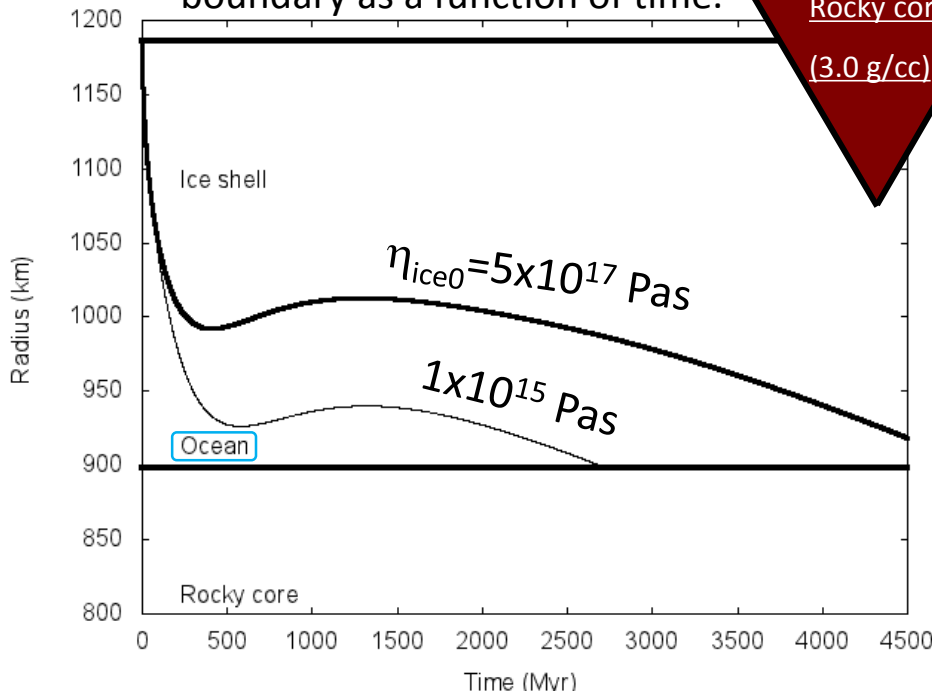
Track the change of boundary position between ocean and ice layer(s) with time.



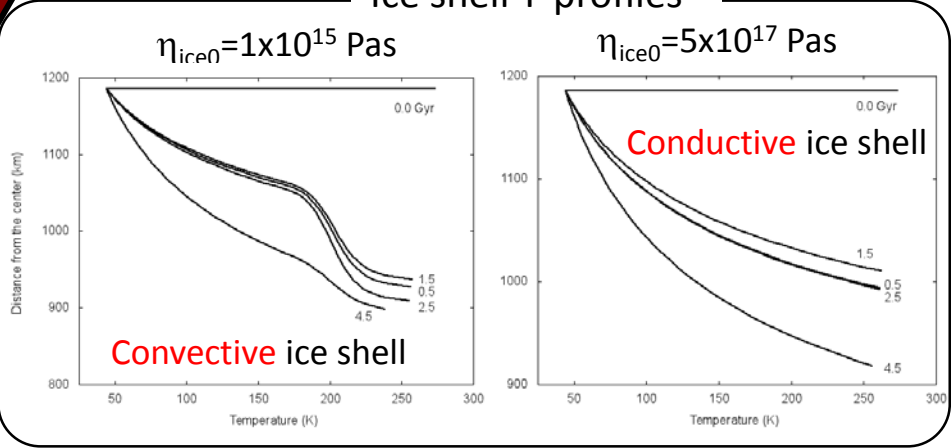
# Results: ocean stability, hot start w/ large core



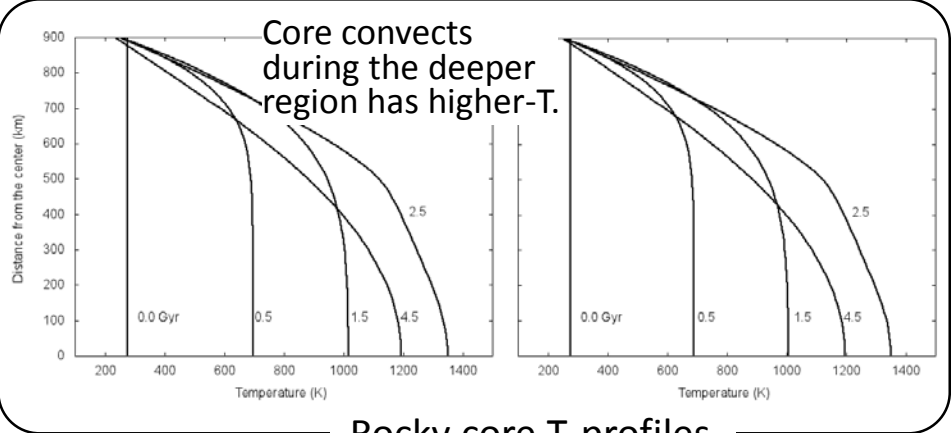
Position of the ocean-ice shell boundary as a function of time.



Ice shell T-profiles



Core convects during the deeper region has higher-T.

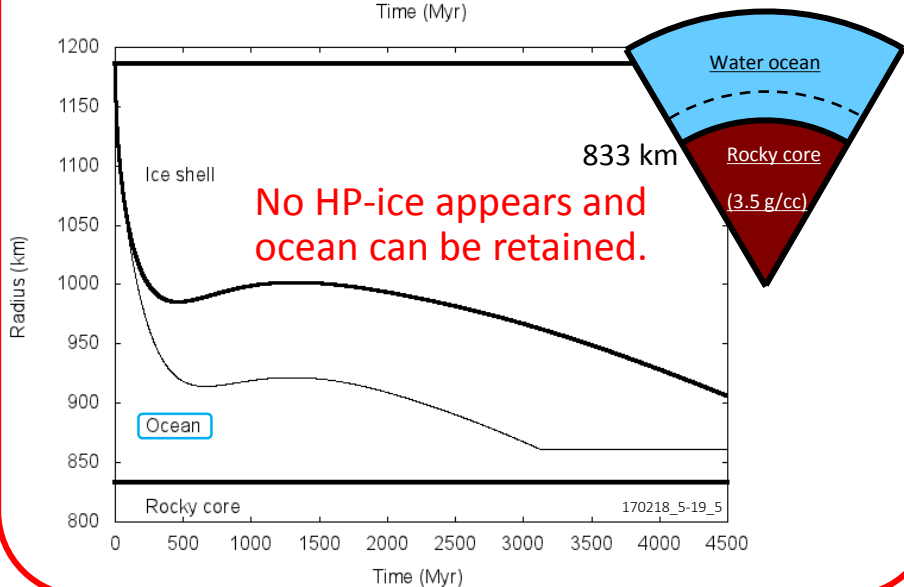
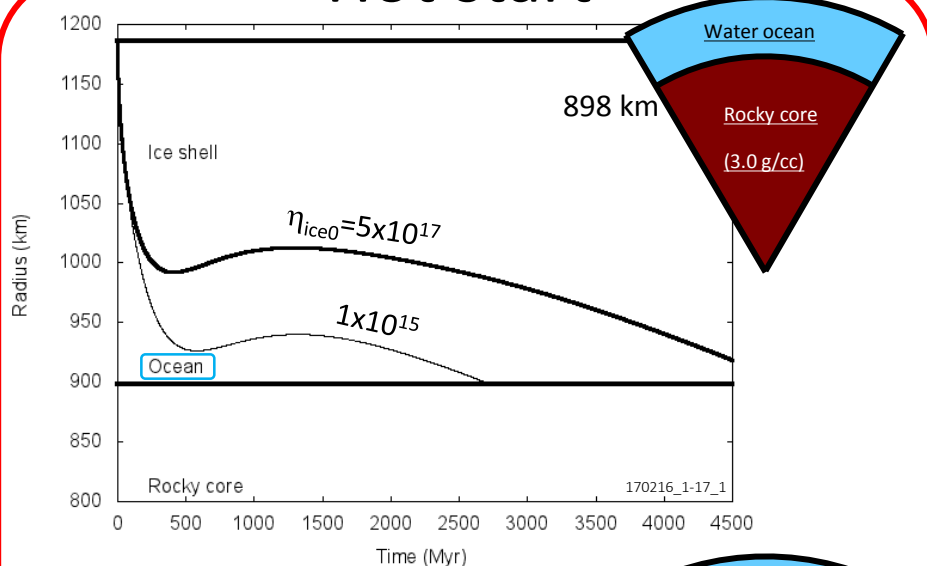


Rocky core T-profiles

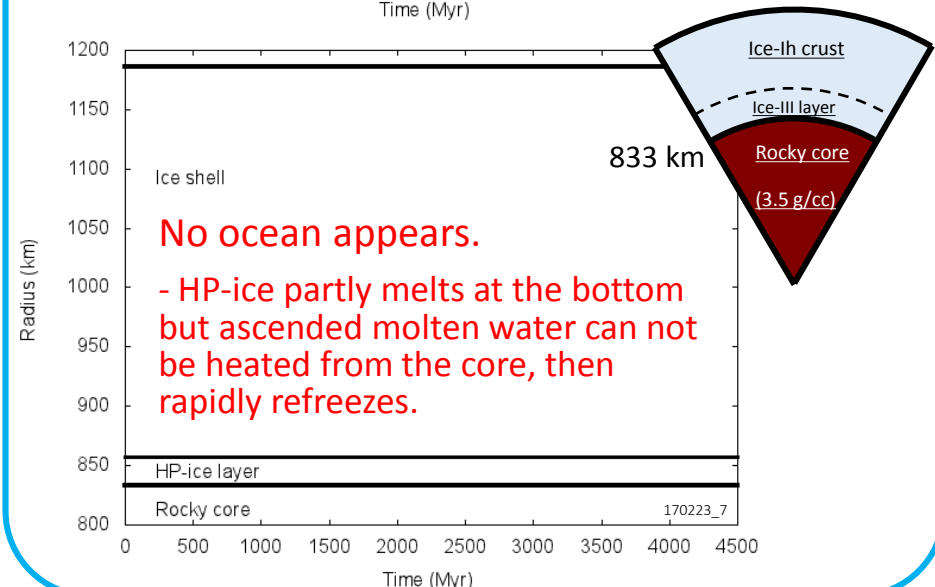
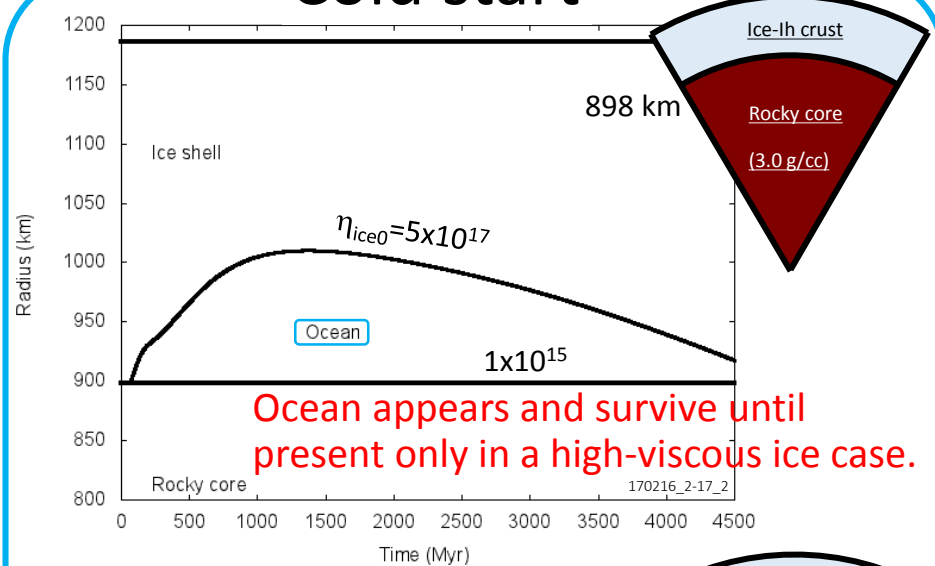
- If the solid ice has (extremely) large viscosity, the ocean can be survived by present.
- In the lower  $\eta_{ice0}$  case, the ocean can be retained until recently, but frozen at present.

# CI chondritic heat source

## Hot start



## Cold start



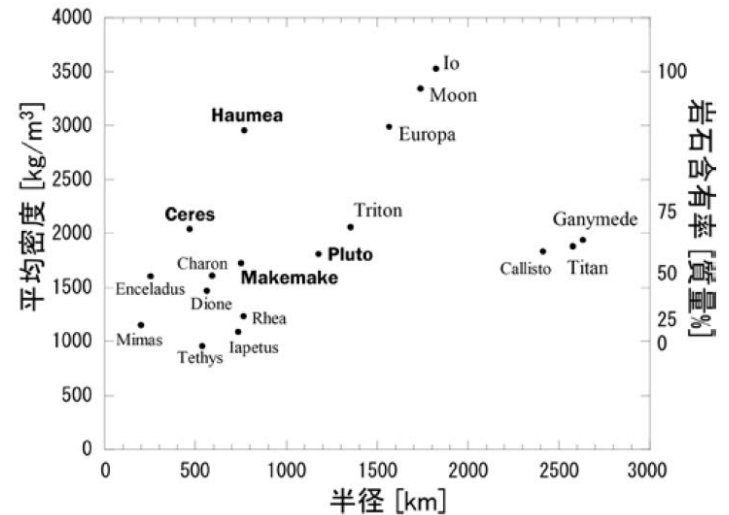
# Ice shell viscosity controls stability of subsurface ocean.

地下海が存在する

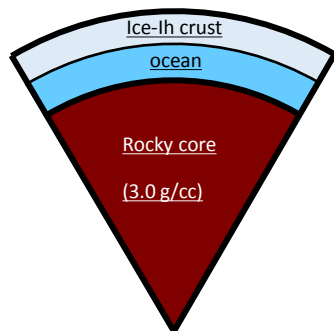
→ 氷を融点以上に保つ

→ 内部に熱を保持する

- たくさん発熱 …… 熱源を多く (岩石量大 or 潮汐変形大)
- 熱を逃げにくく …… 冷却率を小さく



氷地殻の粘性率が大きいほど保温性は高い



$$\eta_{ice} = \eta_{ice0} \exp \left[ A \left( \frac{T_m}{T} - 1 \right) \right]$$

$$\eta_{ice0} = 1 \times 10^{15}, 5 \times 10^{17} \text{ Pas}$$

$$A = 25$$

# Ice shell viscosity

$$\eta_{ice} = \eta_{ice0} \exp \left[ A \left( \frac{T_m}{T} - 1 \right) \right]$$

For  $d_0 = 0.1$  to  $1$  mm,  
 $\eta_{ice0} = 10^{13-15}$  Pas

$$\eta_{ice0} = \eta(d_0, T_m), \quad A = Q_V / RT_m$$

$$\eta = \frac{RTd^2}{42V_m D_{0,V}} \exp \left( \frac{Q_V}{RT} \right)$$

$\sigma$  : stress  
 $\varepsilon$  : strain rate  
 $V_m$  : molar vol.  
 $R$  : gas const.
 
 $d$  : grain size  
 $D_V$  : Vol. diffusion const.  
 $Q_V$  : Vol. diffusion activation energy  
 $T_m$  : melting point

$$D_V = D_{0,V} \exp(-Q_V/RT)$$

$$D_b = D_{0,b} \exp(-Q_b/RT)$$

$$\delta = 2b$$

(by analogy with terrestrial ice sheets)

For reasonable **grain sizes ~0.1 to 1 mm**,  
 the diffusion creep is overwhelmingly  
 dominated by **the vol. diffusion**.

- 氷地殻の粘性率が大きいほど保温性は高い

\* Stress-strain rate relationship

$$\eta = \frac{1}{3 \frac{n+1}{2}} \frac{\sigma}{\dot{\varepsilon}}$$

\* Diffusion creep = volume diffusion creep  
 (n=1) + grain boundary diffusion creep

$$\dot{\varepsilon} = \frac{42V_m\sigma}{3RTd^2} \left( D_V + \frac{\pi\delta}{d} D_b \right)$$

# Ice shell viscosity

$$\eta_{ice} = \eta_{ice0} \exp \left[ A \left( \frac{T_m}{T} - 1 \right) \right]$$

## 氷地殻の粘性率はどうすれば決まるか

$$\eta_{ice0} = \frac{RT_m d_0^2}{42V_m D_{0,V}} \exp \left( \frac{Q_V}{RT_m} \right)$$

$\sigma$  : stress

$\varepsilon$  : strain rate

$V_m$  : molar vol.

$R$  : gas const.

$d$  : grain size

$D_V$  : Vol. diffusion const.

$Q_V$  : Vol. diffusion activation energy

$T_m$  : melting point

For reasonable grain sizes  $d_0 = 0.1$  to  $1$  mm,  $\eta_{ice0} = 10^{13-15}$  Pas.

For Pluto's case and  $\eta_{ice0} = 5 \times 10^{17}$  Pas,  $d_0 \sim 20$  mm

融点に近くても、数cm粒径はなかなか・・・

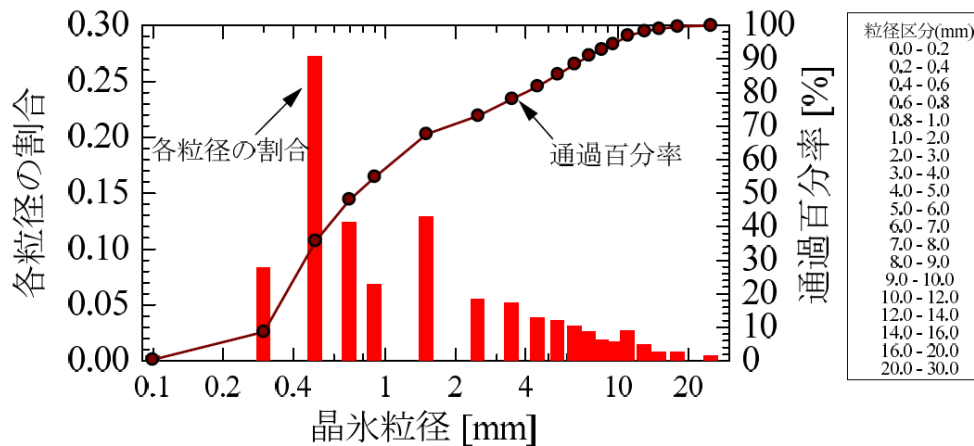
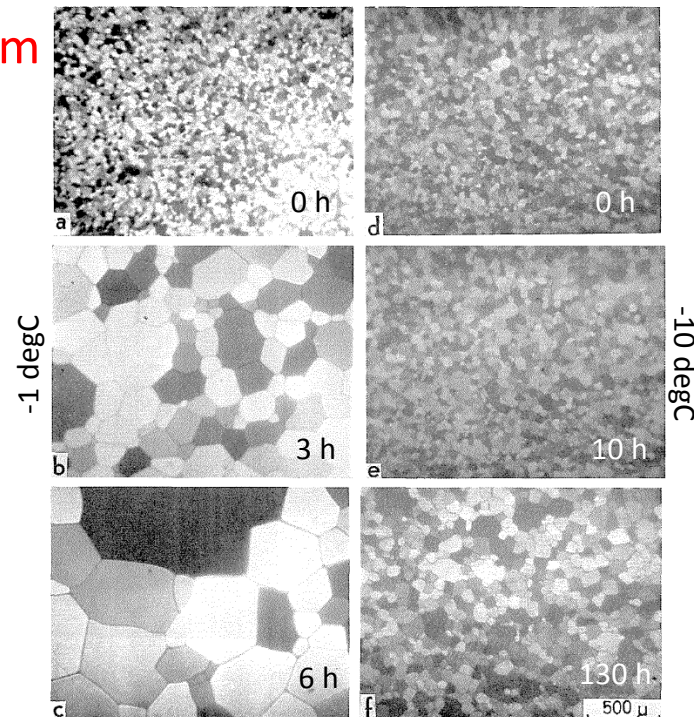


図-8 晶氷粒径の度数分布と加積曲線

吉川ら, 土木学会論文集B1, 69 (2013).



第2図 純水の微結晶の粗大化

鈴木, 低温科学, 27 (1970).

# Discussion 1: Extensional tectonics

- Volume increase (e.g., from liq H<sub>2</sub>O to ice-Ih) (Ice shell growth)
- Viscoelastic stress model for Europa
  - ex.) Ice shell growth at ~8 km/Gyr generates 1 MPa surface tensile stress for 0.5 Gyr
  - Pluto's shell growth ~30 km/Gyr [Kimura+, 2007]
  - Sufficient stress could be generated.

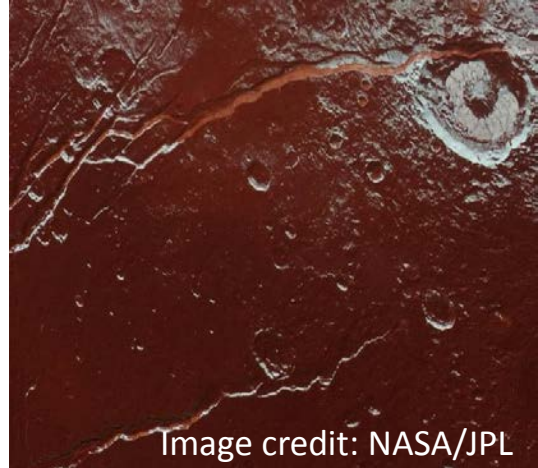
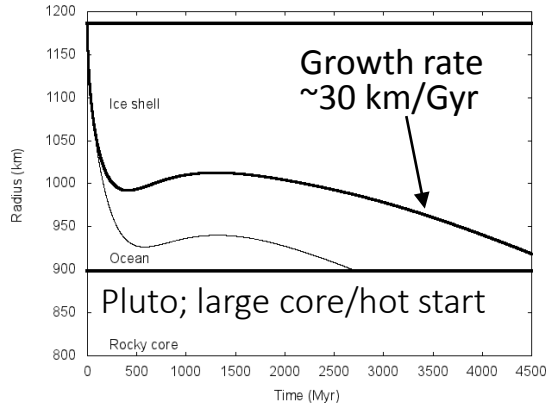
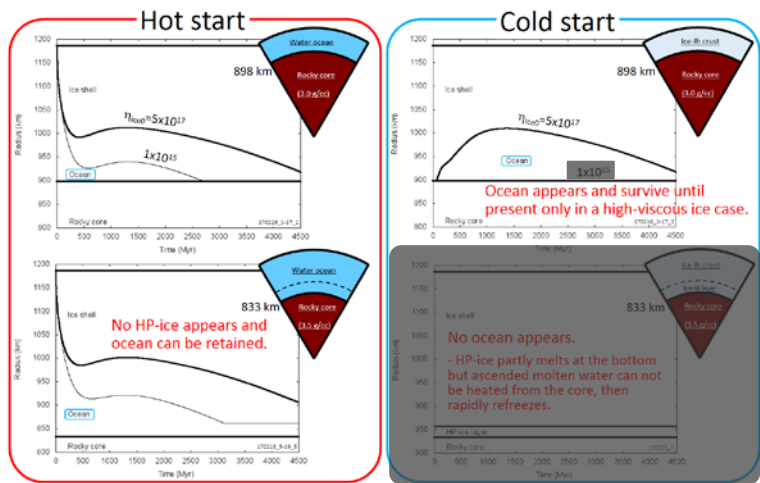


Image credit: NASA/JPL



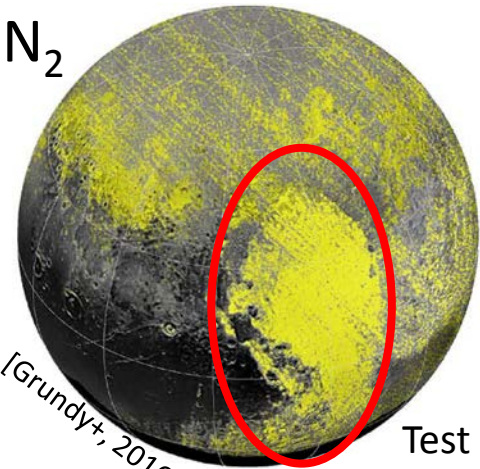
- No shell growth (no ocean appears) case can be ruled out.
- More precise estimation of tectonic age, better constraint to the interior evolution.



# Discussion 2; Nitrogen contribution

NASA

N<sub>2</sub>

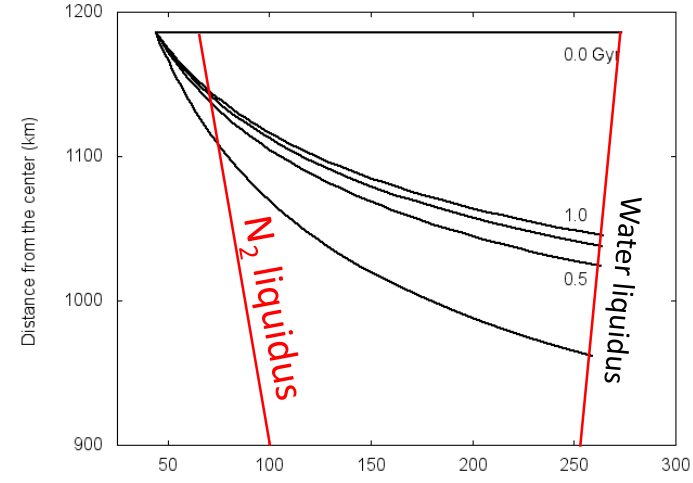
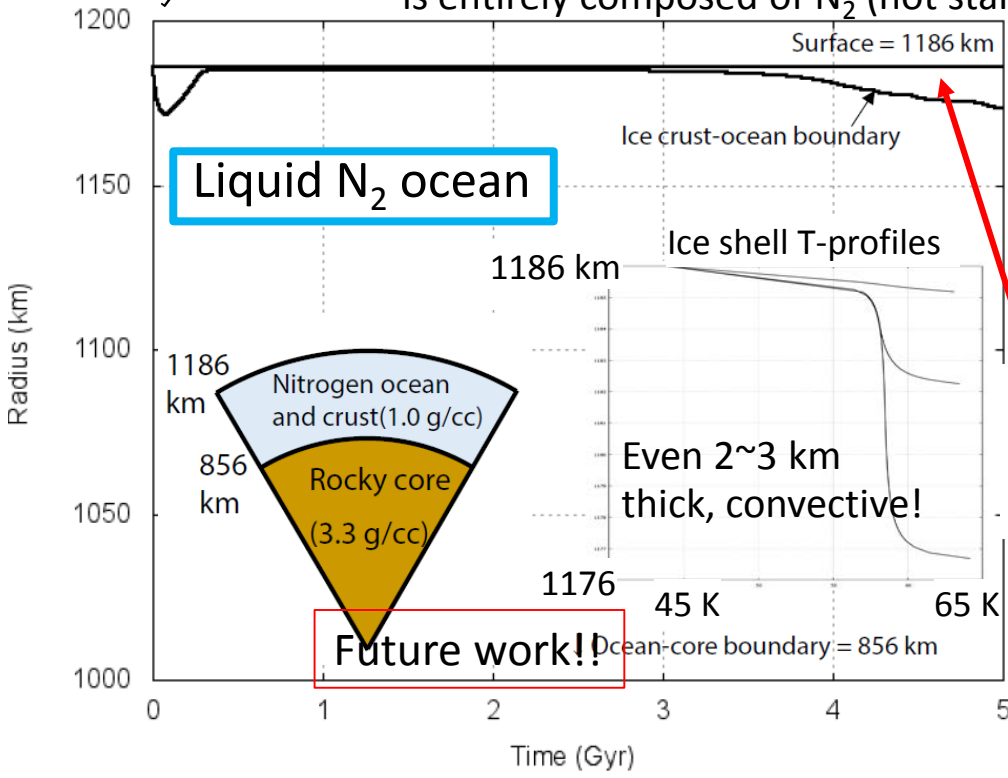


[Grundy+, 2016]



Smooth N<sub>2</sub> ice landscape showing polygons could be evidence of convection.

Test calculation assuming surficial layer is entirely composed of N<sub>2</sub> (hot start).



Huge N<sub>2</sub> ocean under the ~12 km thick solid convective N<sub>2</sub> shell exists at  $\left(\frac{T_m}{T} - 1\right)$  present.

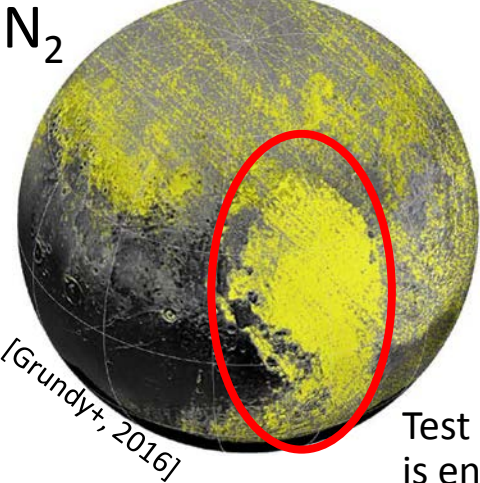
$$\eta_{ice} = \eta_0 \exp\left[\frac{T_m}{T} - 1\right]$$

$\eta_0 = 8.8 \times 10^{10}$  (Pas),  $A=24.9$ ,  $T_m=63.15$  (K)  
[Brown & Kirk, 1994]

Low melting point and viscosity.

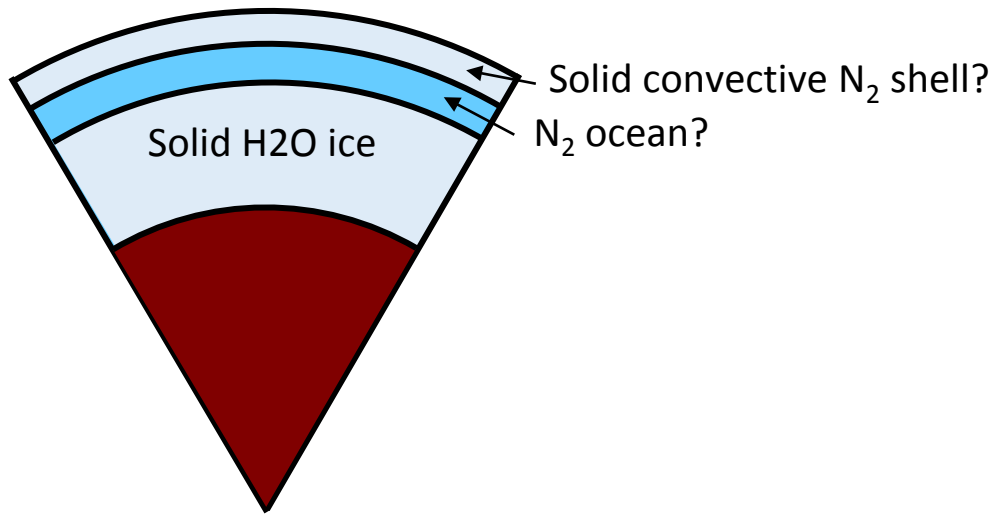
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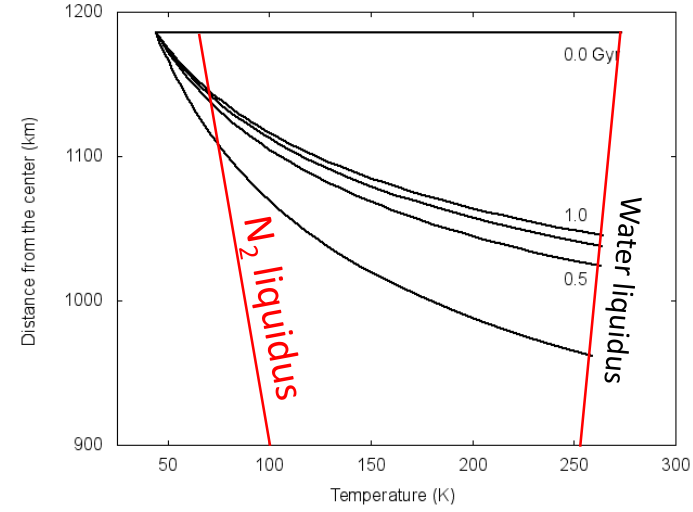


Smooth N<sub>2</sub> ice landscape showing polygons could be evidence of convection.

Test calculation assuming surficial layer is entirely composed of N<sub>2</sub> (hot start).



Future work!!



$$\eta_{ice} = \eta_0 \exp \left[ A \left( \frac{T_m}{T} - 1 \right) \right]$$

$\eta_0 = 8.8 \times 10^{10}$  (Pas),  $A=24.9$ ,  $T_m=63.15$  (K)  
[Brown & Kirk, 1994]

Low melting point and viscosity.



# Summary

- We investigated stability of the ocean of Pluto using a thermal/structural evolution model.
- In a large core/thin water shell model (only ice Ih appears case), the ocean should be present if the ice has large viscosity (reference visc.  $> 10^{17}$  Pas).
- In a small core/thick water shell model, the ocean should be present if the ocean presents from initial.
- If the initial Pluto was entirely frozen and HP ice covered the core, no ocean appears. It should be ruled out in terms of extensional tectonics.