
Planetary Seismology and Geophysics

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Presentation's outline

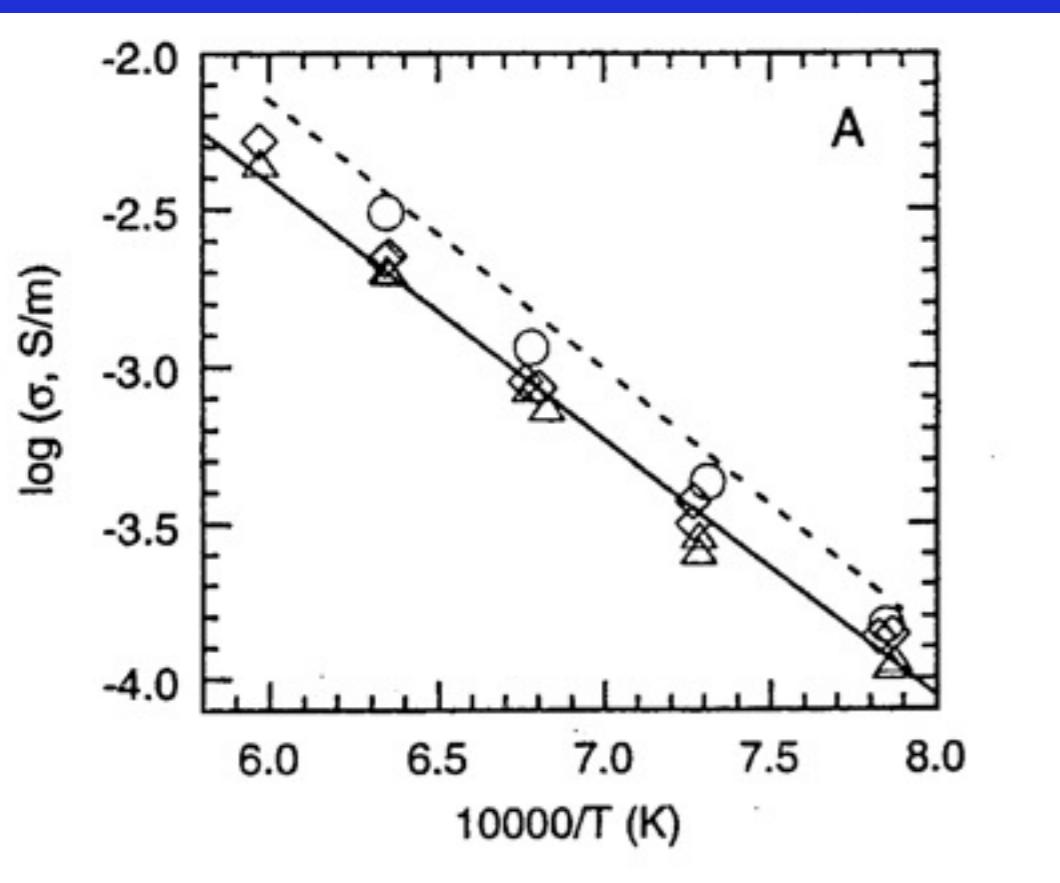
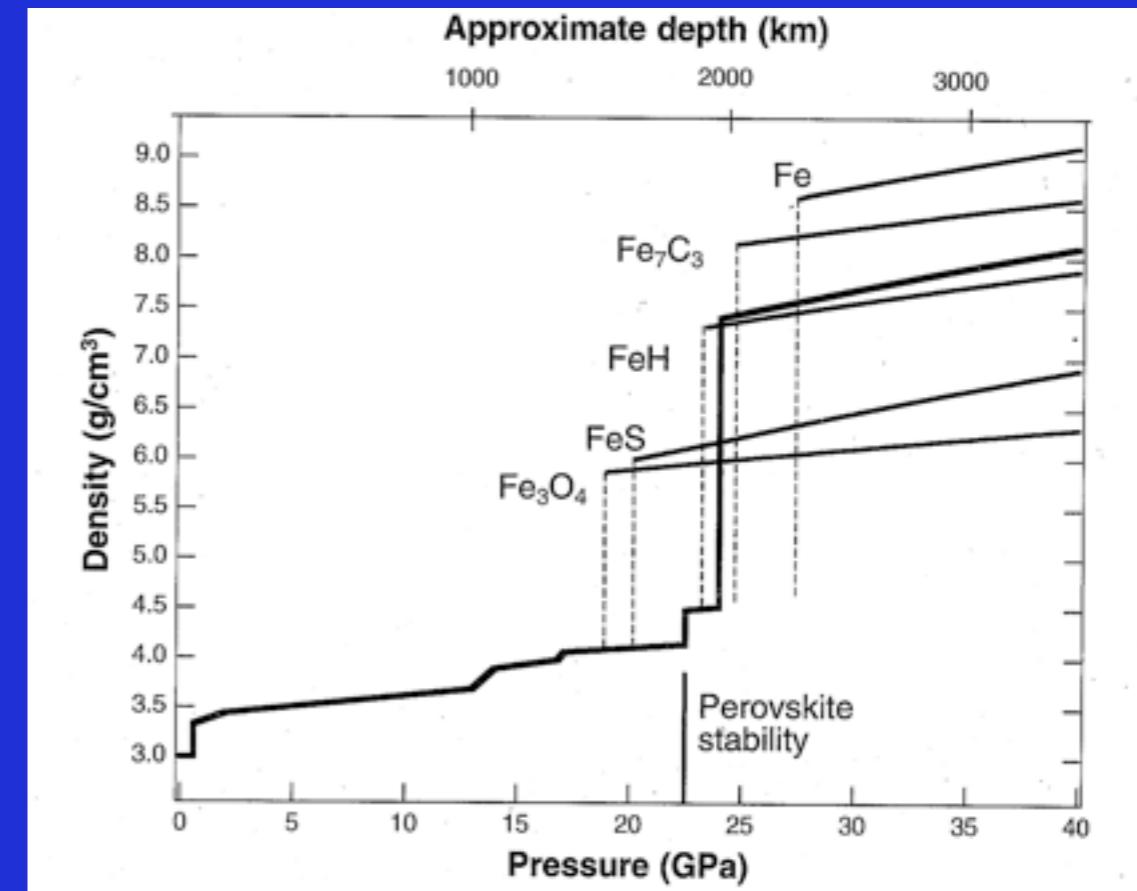
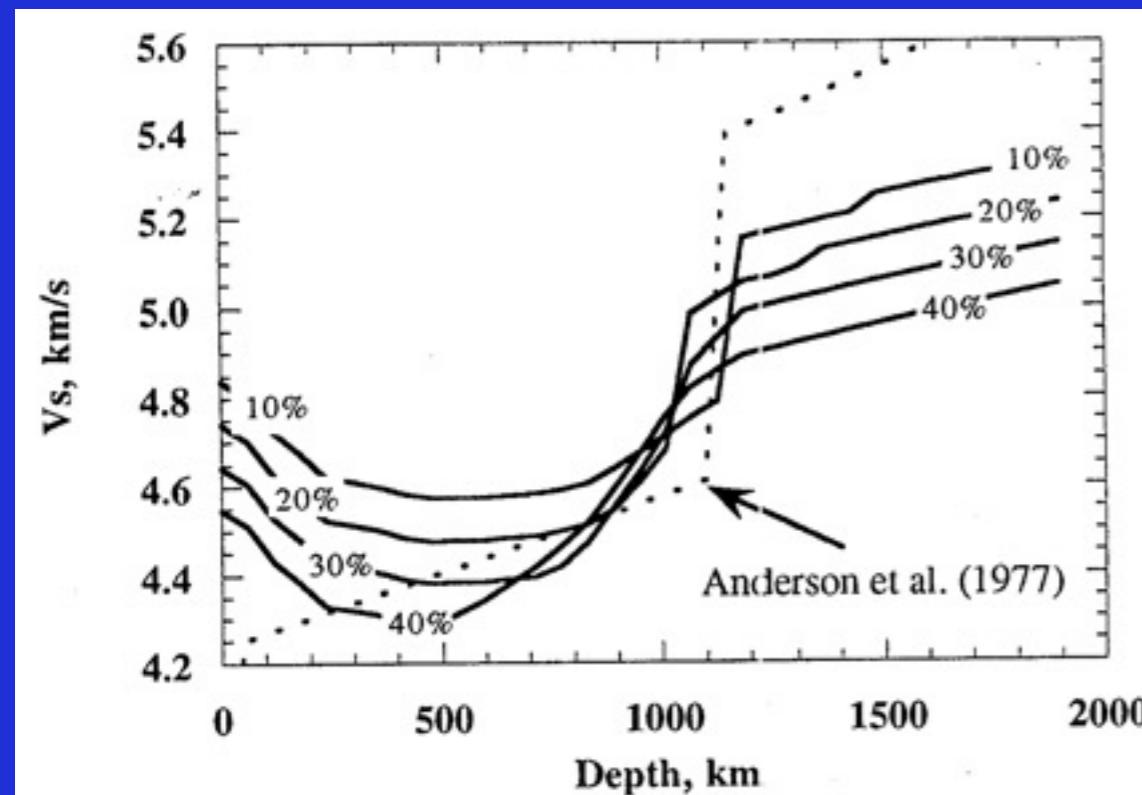
- What can we get from geophysical exploration and sounding of a planet other than Earth?
 - A complete illustration with the Moon
- What can we imagine from geophysical exploration and sounding of a planet other than Earth?
 - Dreams for Mars, the Moon and Venus...

In situ geophysical exploration

- Goal of in situ geophysical exploration is to determine the Internal structure of a planet
- Internal structure is
 - Thermodynamical state (pressure and temperature)
 - Mineralogy
- The approach is based
 - On geophysical methods determining the profile with depth (or the 3D models, for the earth case) of geophysical parameters such as
 - Seismic velocities
 - Shear modulus
 - Density
 - Electrical conductivity
 - For subsurface, permittivity
 - On remote sensing, in situ and sample analysis of the crustal radioactive material PLUS situ heat flow measurement to get the heat (and temperature) surface budget
 - On laboratory and theoretical studies determining the dependence of these geophysical parameters with respect to temperature and mineralogy (PLUS thermal evolution models)
 - On mineralogical and geochemical analysis constraining directly or indirectly the mineralogy with depth

-
- A geophysical field must penetrate in the planet, must be reflected/transmitted and then recorded
 - Magnetic sounding (electrical conductivity)
 - Seismic sounding (seismic velocities, seismic attenuation)
 - Electro-magnetic sounding (permittivity, electrical conductivity)
 - A geophysical signal must be produced by the planet with amplitude depending on its properties with depth
 - Gravity (density)
 - Heat flux (temperature, radioactivity, thermal conductivity)
 - An external force deform the planet with a response depending on its properties with depth and the shape (or deformations) of the planet is recorded
 - Tidal deformation, Precession, nutation, etc (density and elastic modulus)
 - Plate flexure (density, elastic thickness)
 - In planetology, data are generally limited.... All sources of information must be used

What is the mineralogy, structure and temperature?



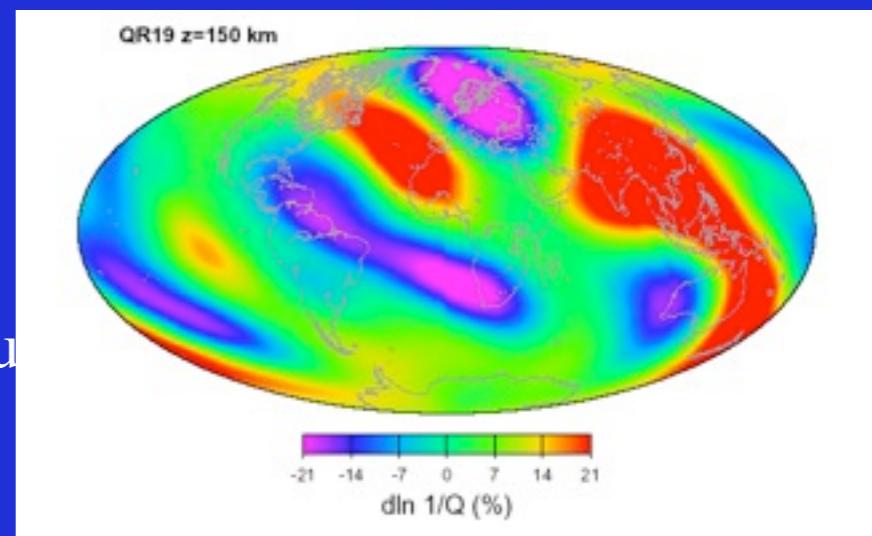
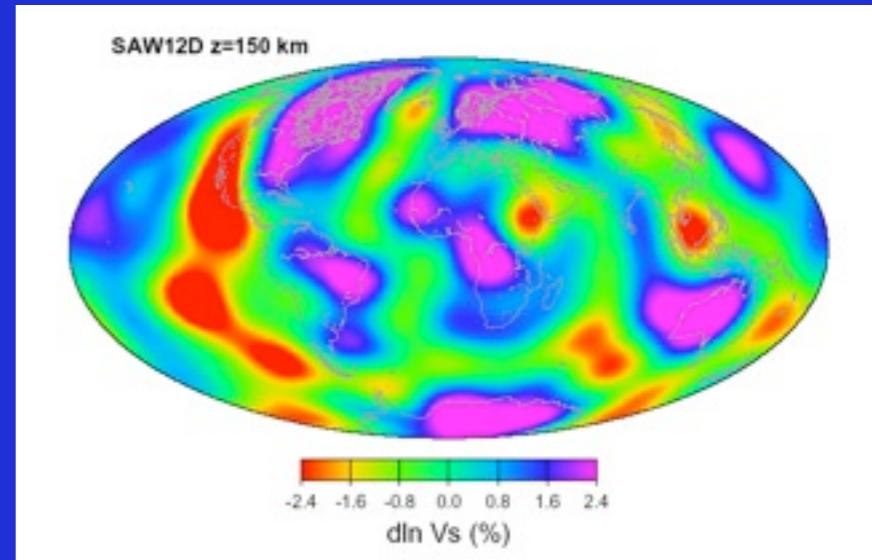
Magnetic sounding

- Principle:
 - An external, time dependant, magnetic field penetrates in an planet
 - Time variation of the magnetic field inside the planet generates currents in the conductive areas canceling partially the field
 - The induced magnetic field is measured by magnetometers
- Limitation
 - Magnetic field is diffusing inside the body
 - Only long periods magnetic field (hours) are sounding deep
 - Diffusion makes the reconstruction of discontinuities difficult
- Success
 - Detection of highly conducting part of a planet (iron metallic core, low velocity zone in a mantle associated to partial melting, liquid in the crust or below a crust)
- Sources
 - Moon: Magnetic field variations associated to the displacement of the Moon in the Earth magnetosphere
 - Moon: Magnetic field variations associated to the solar wind
 - Jovian satellites: Magnetic field variations associated to the tilted rotating Jovian magnetosphere

$$\nabla^2 \mathbf{B} = \mu\sigma \frac{\partial \mathbf{B}}{\partial t},$$

Seismic sounding

- Principle
 - Use active (impactors, explosive) or passive (quakes, meteorite impacts, crack) seismic sources
 - Record and analyse the seismic signals
- Key dates
 - Earth:
 - Von Reben Paschwitz, 1889, first signal
 - Oldham, 1906, discovery of the core
 - 1960, discovery of the normal modes
 - 1980+ Tomographic models (i.e. details of a few %)
 - Sun:
 - Leighton et al., 1962, discovery of the normal modes
 - Moon:
 - Latham et al., 1969, Apollo 11, first records and deep moonquakes
 - Jupiter:
 - Hammel et al., 1995, observation of Atmospheric Tsunamis
 - Mars:
 - Anderson et al., 1976, First installation of seismometer, single observation of a «quake» possibly not associated to wind burst...



The interior structure of the Moon

What did seismology and geophysics?

with contributions of
Mark Wieczorek, Jeannine Gagnepain-Beyneix, Tamara Gudkova, Catherine Johnson, Taichi Kawamura and other

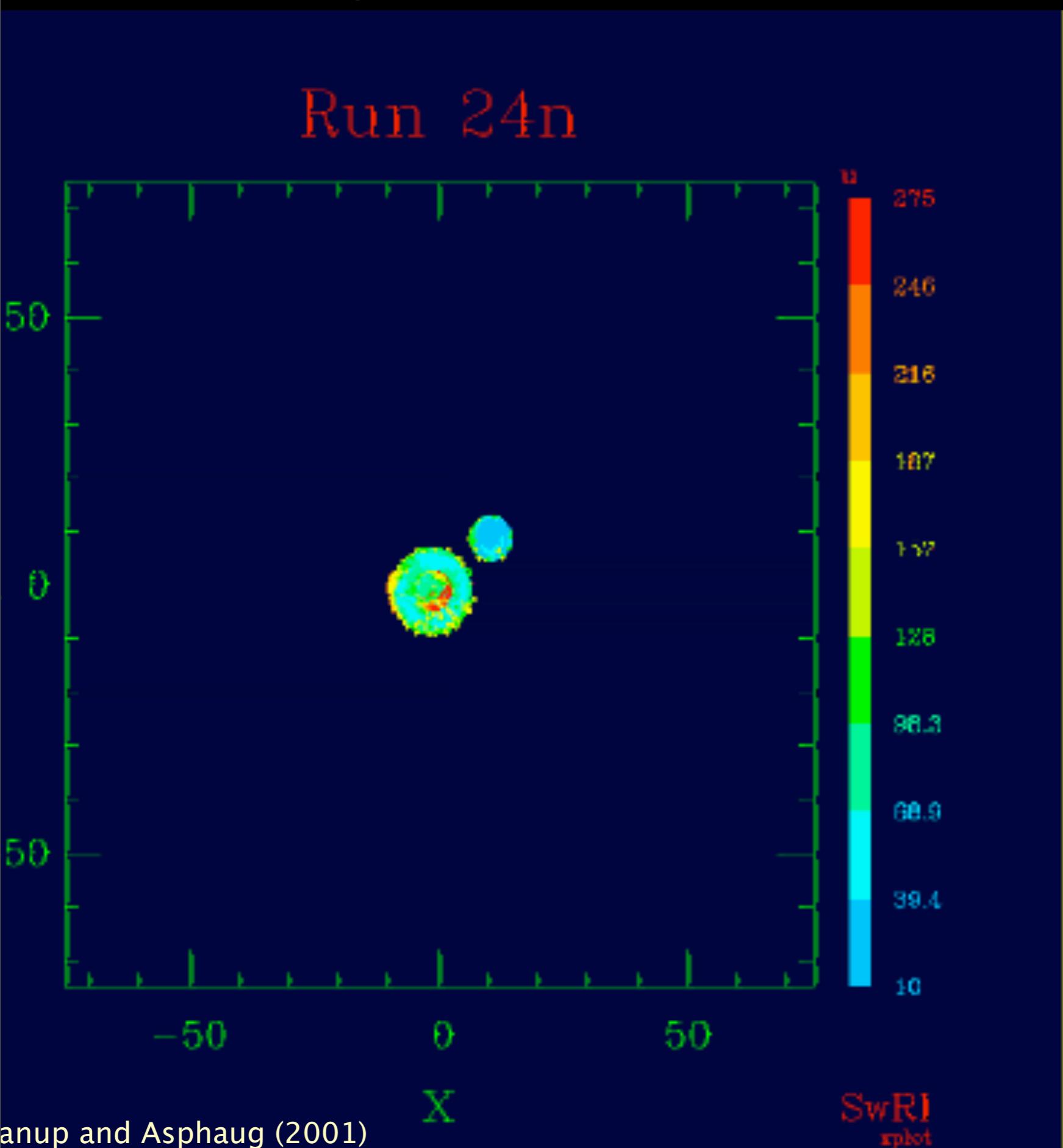


What might the interior of the Moon look like?

A few ideas and simple observations



The origin of the Moon: The first 24 hours



A Mars-sized object is postulated to have collided with the Earth 4.5 B.y.a.

The material put into circum-terrestrial orbit re-accretes to form the Moon on the time scale of about 1 month to 100 years.

As a result of the energy liberated during the impact, the energy associated with re-accretion, and the short re-accretion time scales, the Moon could have formed completely molten.

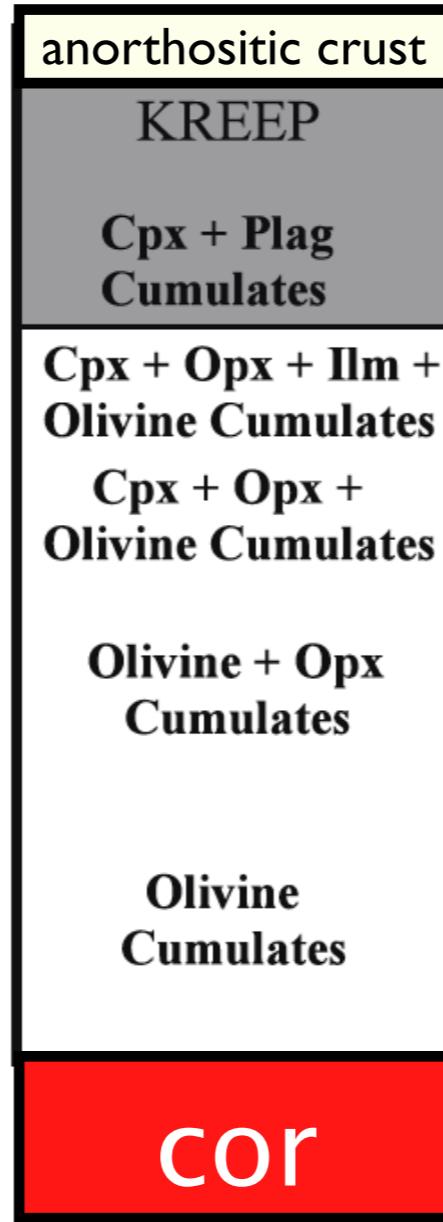
Magma Ocean Crystallization

initial state

completely or partially molten magma ocean

→
fractional crystallization

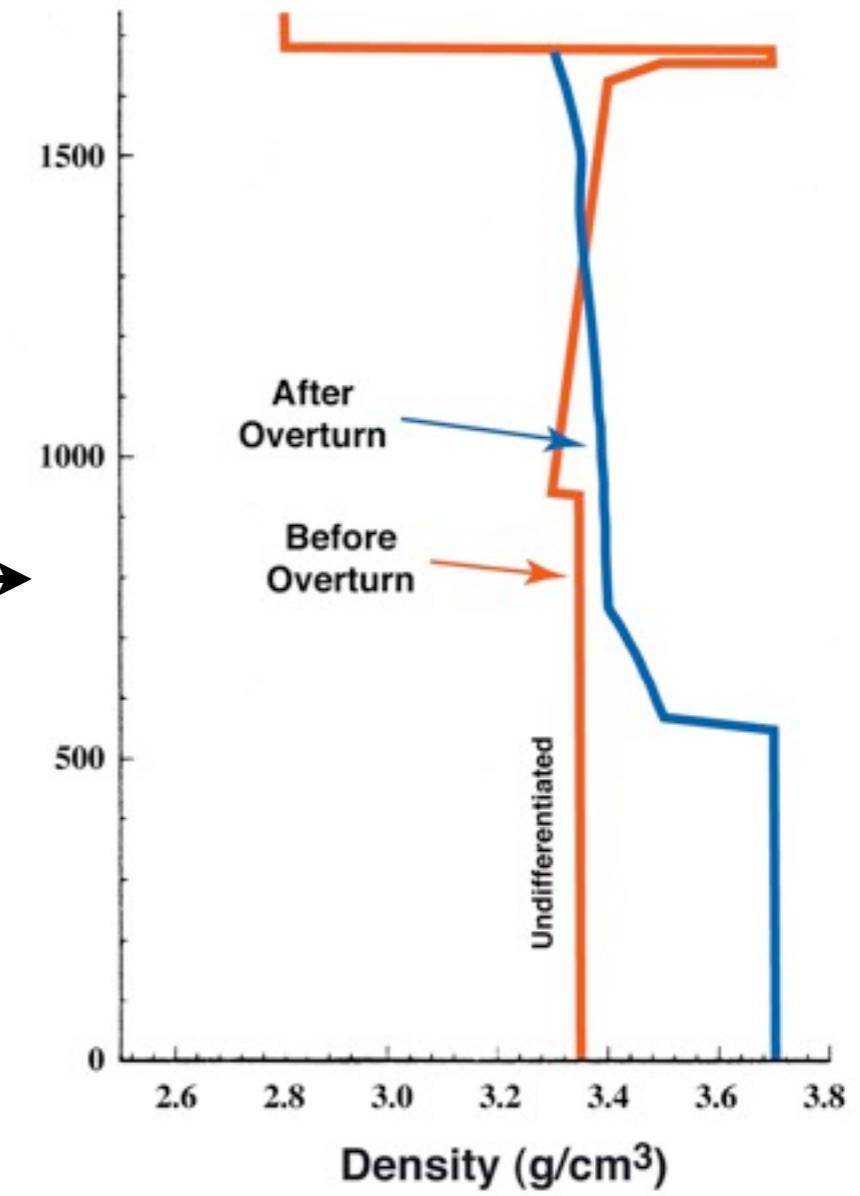
intermediary



Shearer et al. (2006)

gravitational overturn?

final state?

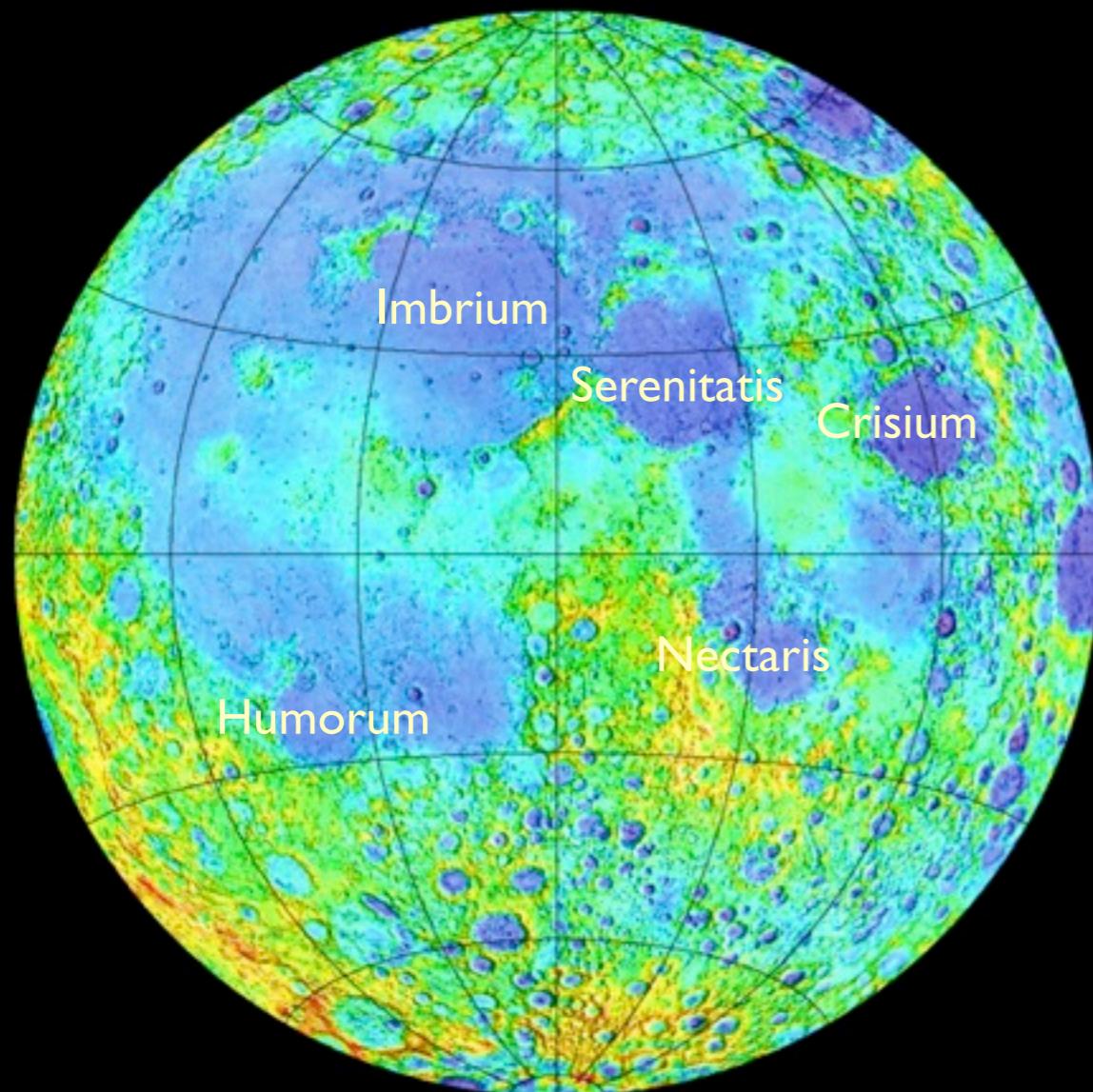


Hess and Parmentier (1995)

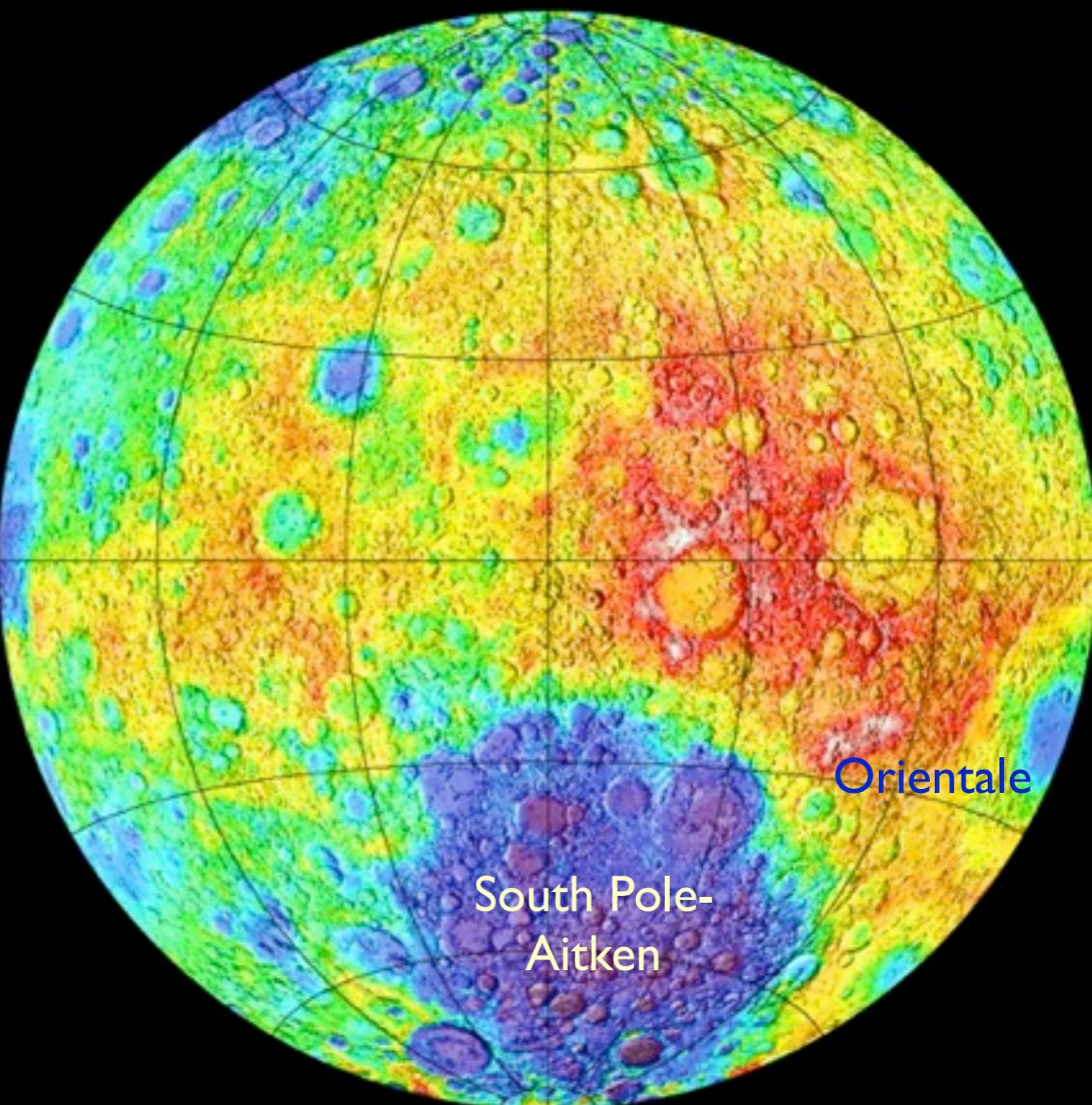
Crystallizing a magma ocean could have given rise to a layered mantle. The cumulates would have been gravitationally unstable and might have overturned.

Impact Cratering

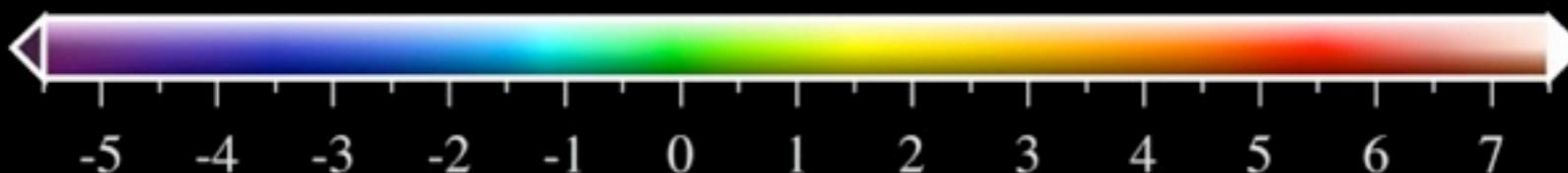
Near side



Far side

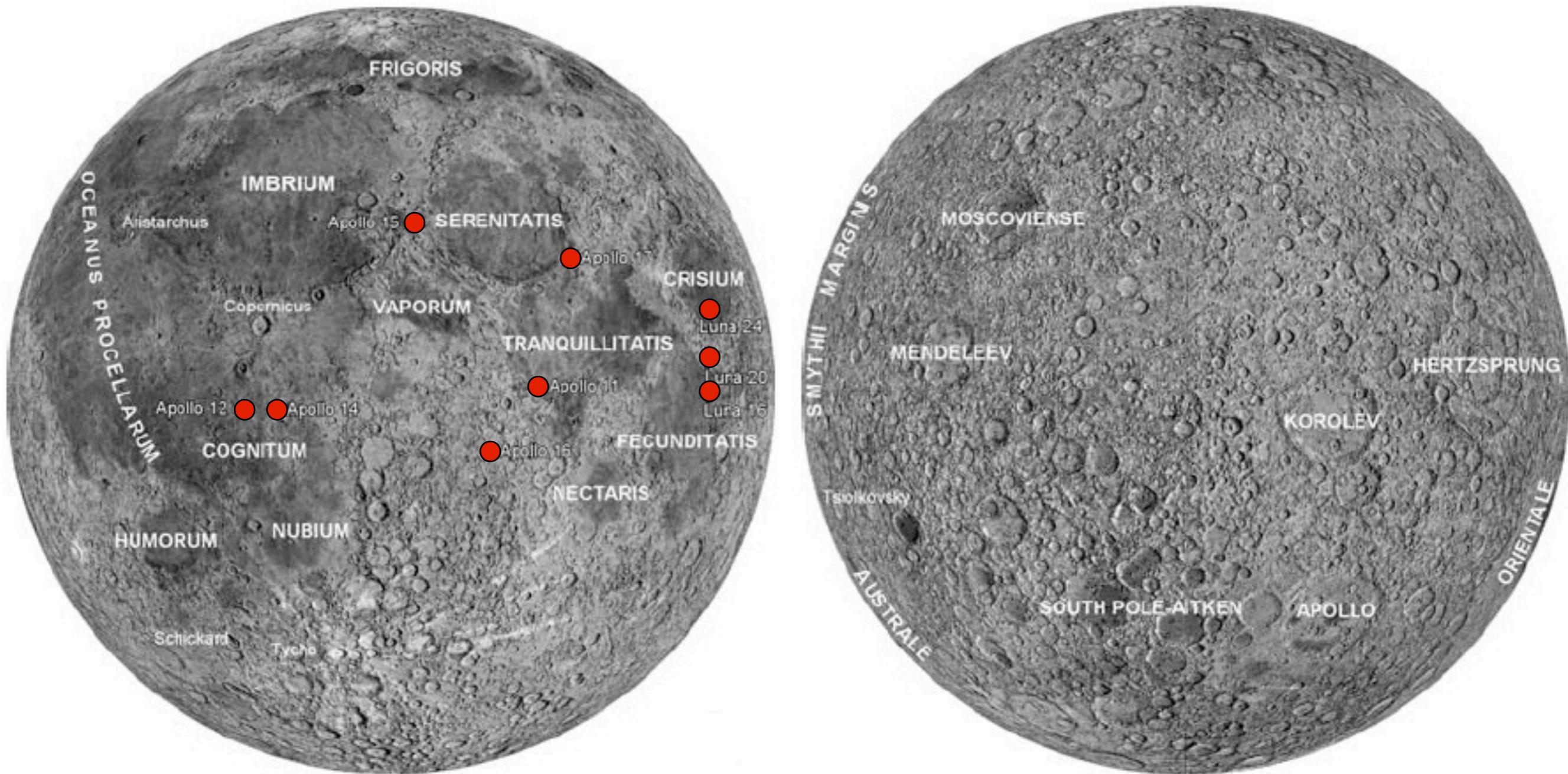


Topography (km)



Asteroidal and cometary impact events excavated deep into the crust. Large lateral variations in crustal thickness

Mare Volcanism



Almost all volcanic flows erupted on the near-side. Are there large variations in composition (i.e., heat producing elements) between the two hemispheres?

Geophysical investigations of the lunar interior

The Crust

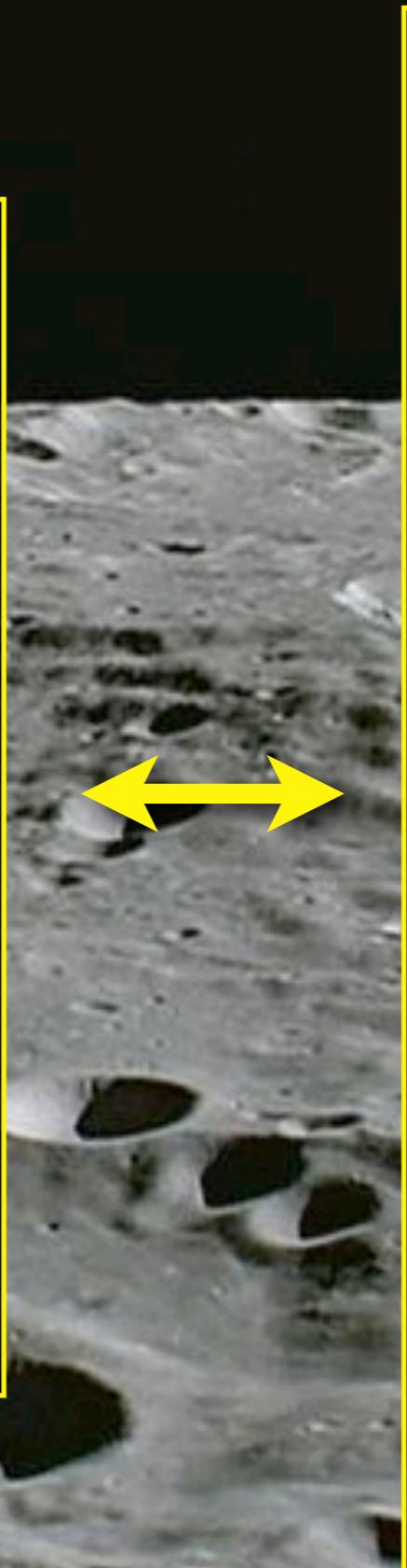
Composition, average thickness, lateral variations in thickness, magnetization.

The Mantle

Composition, layering, lateral variations in composition, temperature.

The Core

Composition, size, geodynamo.



Gravity

Crustal thickness variations, time variable gravity signatures related to the tides and core.

Seismology

Crustal thickness, seismic discontinuities in the mantle, core size.

Magnetics

Crustal magnetizations, electrical conductivity of the mantle and core.

Lunar Laser Ranging

Energy dissipation in the mantle (Q) and at the core-mantle boundary.

Heat flow

Distribution of heat producing elements in the crust and mantle.

Gravity

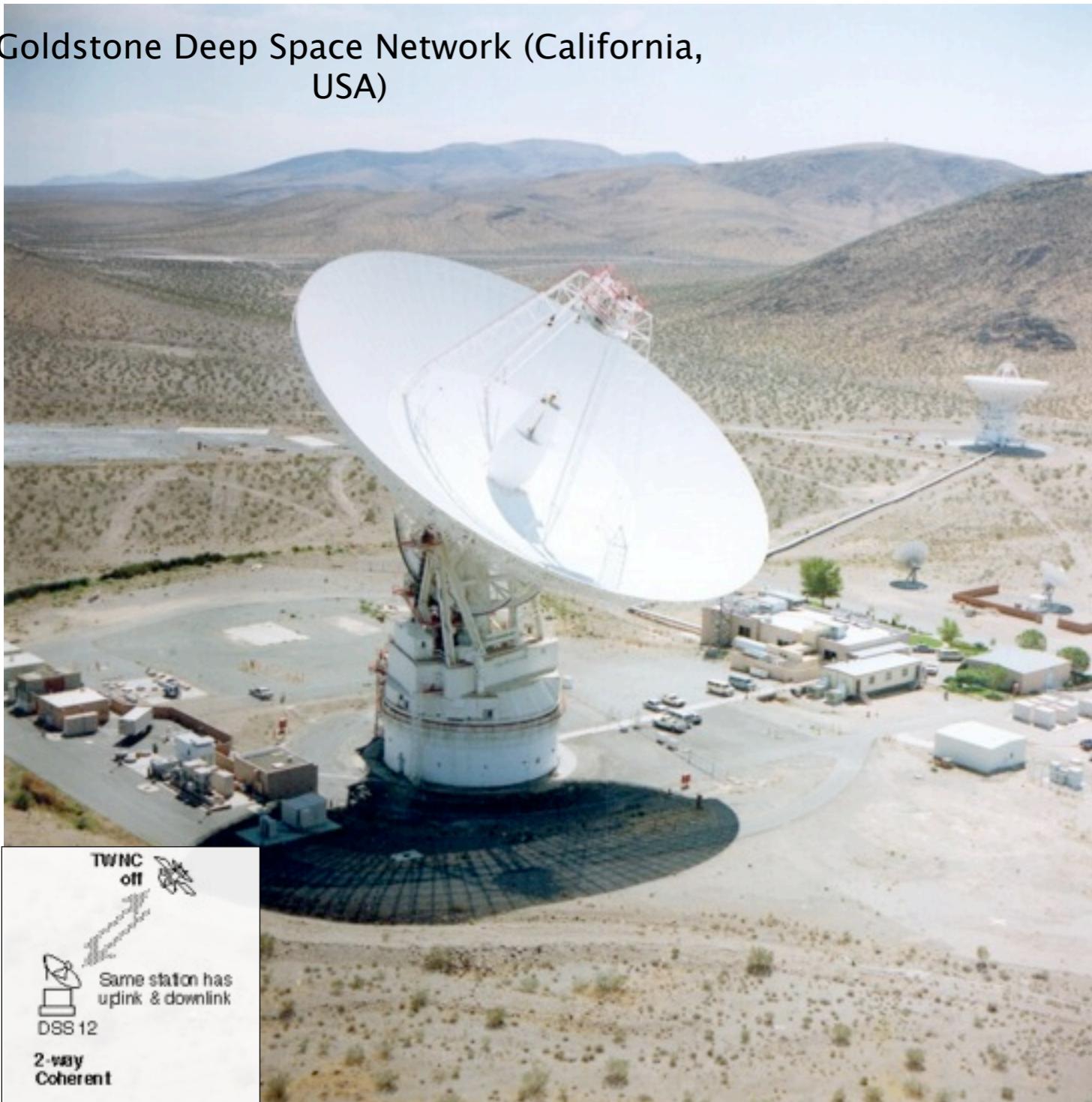
$$\mathbf{g}(\mathbf{r}) = \nabla U(\mathbf{r})$$

$$U(\mathbf{r}) = \int_V \frac{G \rho(\mathbf{r}')}{|\mathbf{r} - \mathbf{r}'|} dV'$$

The gravity field depends upon the distribution of mass within the planet.

Measurement principle

Goldstone Deep Space Network (California, USA)



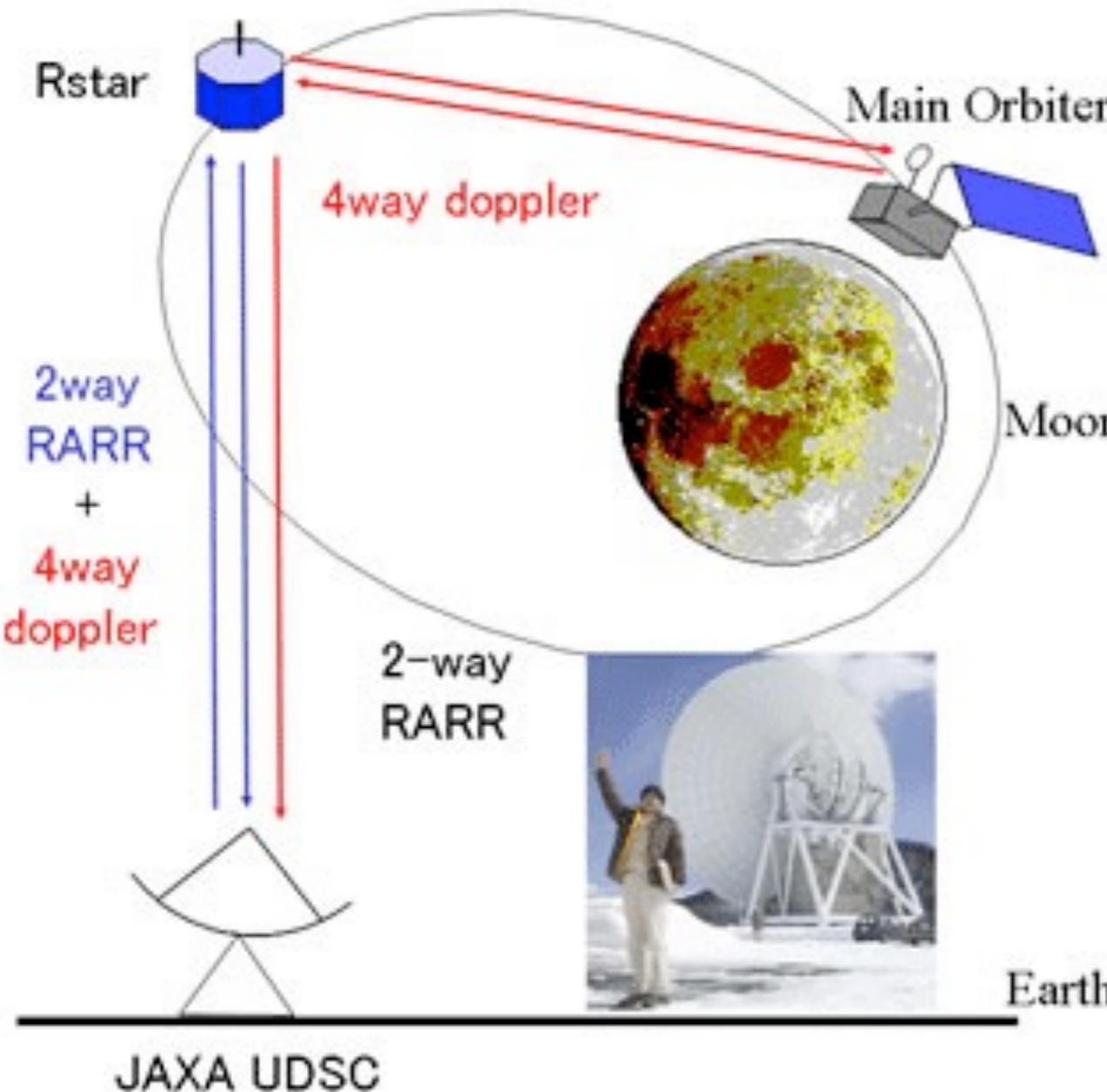
1. The frequency of radio signals transmitted by a spacecraft is doppler shifted according to the relative velocity.
2. The time-of-flight of the radio signal is related to the distance between the antenna and spacecraft.

These two measurements are used to reconstruct the orbit of a spacecraft, and the “residuals” are modeled as spatial variations in the gravity field of the planet.

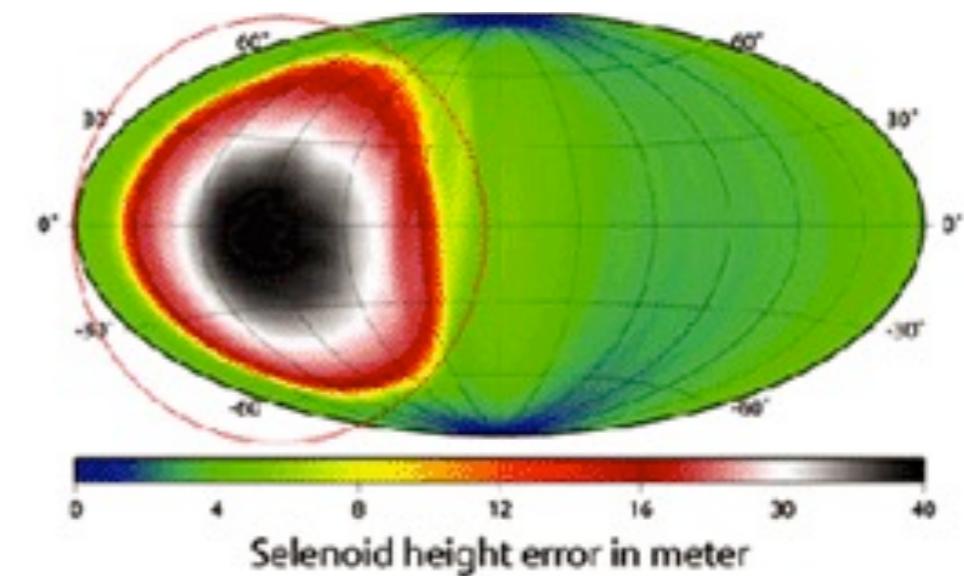
No data is available over the far-side hemisphere of the Moon when using a single satellite!

Kaguya (SELENE, Japan)

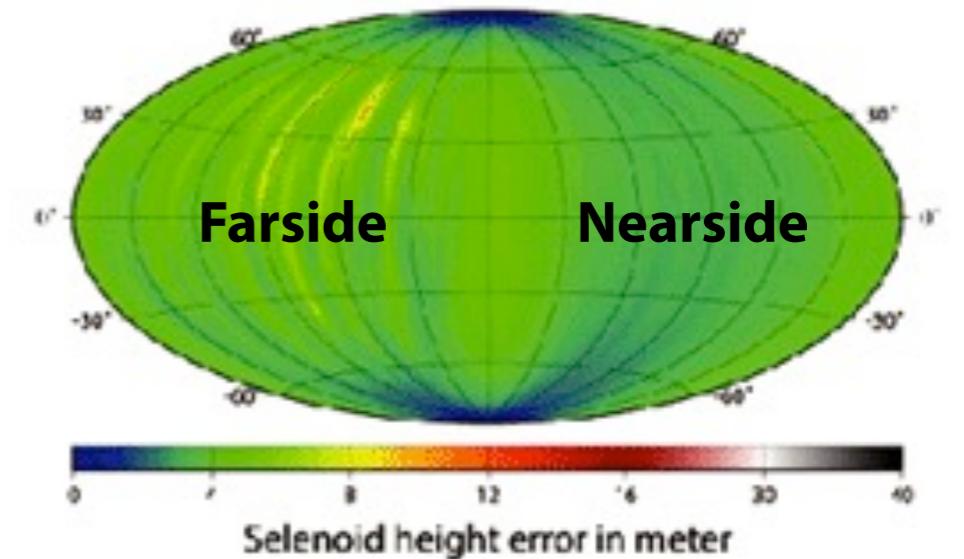
4-way tracking



previous gravity uncertainty

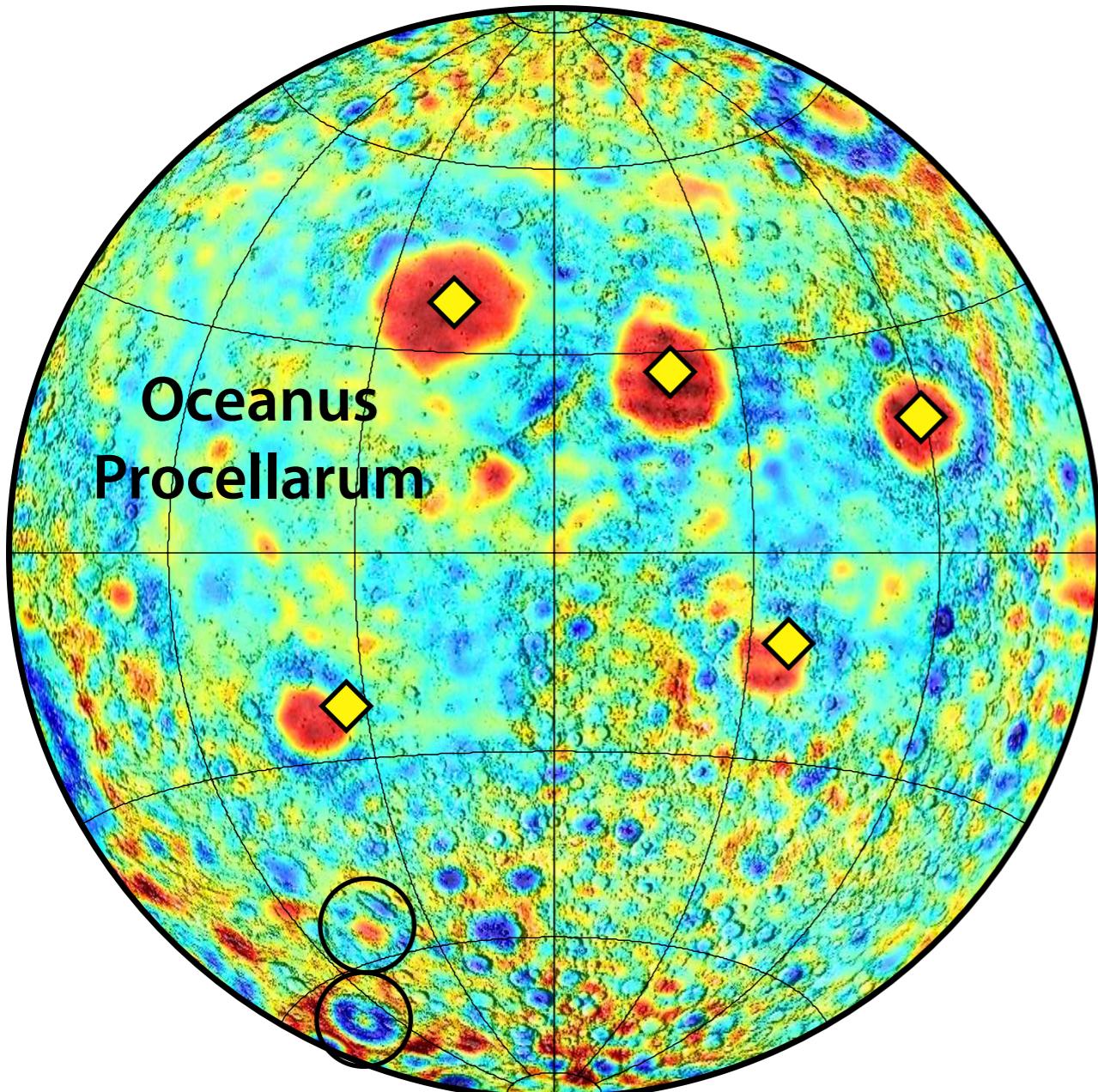


Kaguya gravity uncertainty

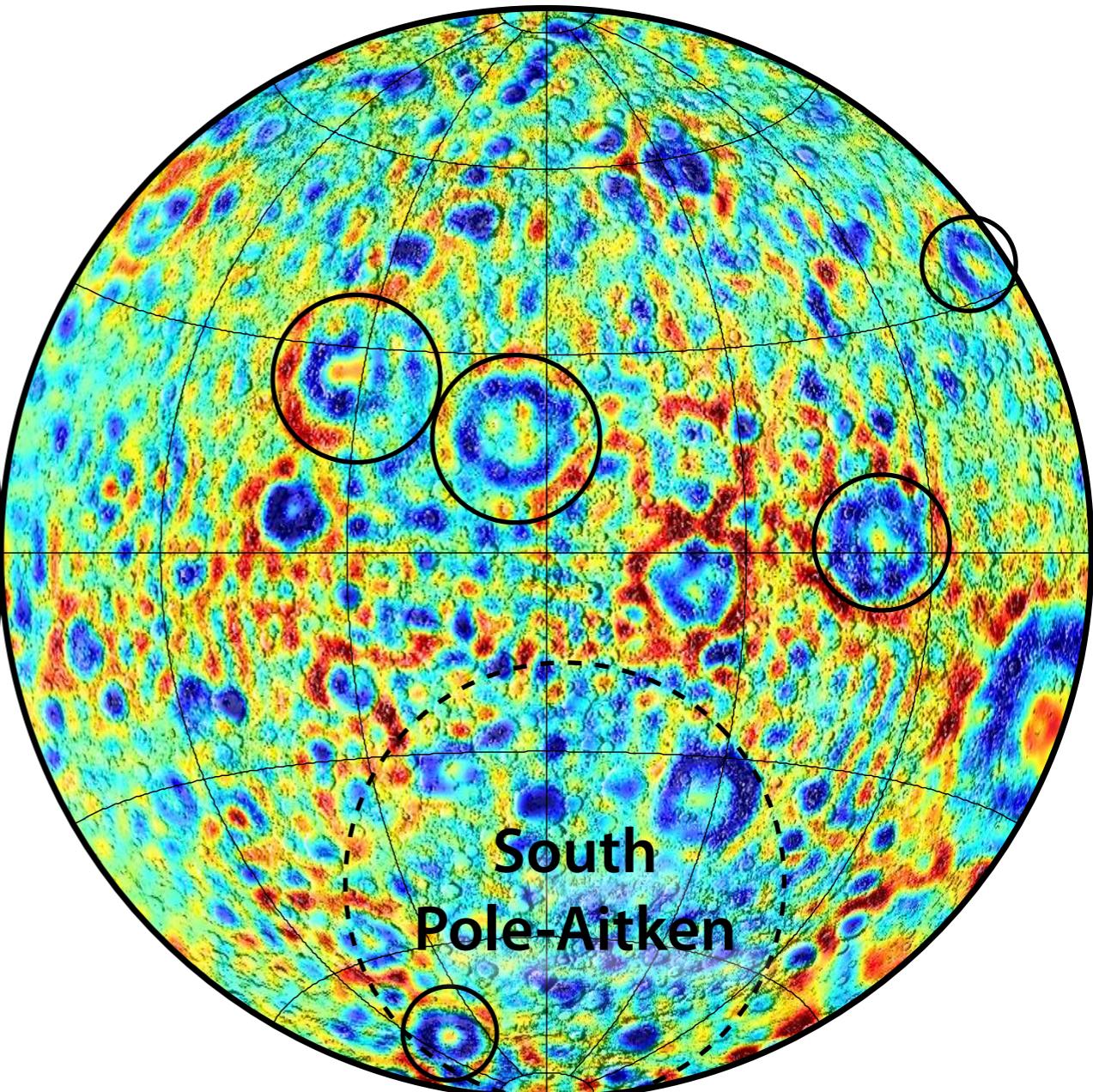


4-way tracking using two satellites has obtained data over the far-side hemisphere for the first time.

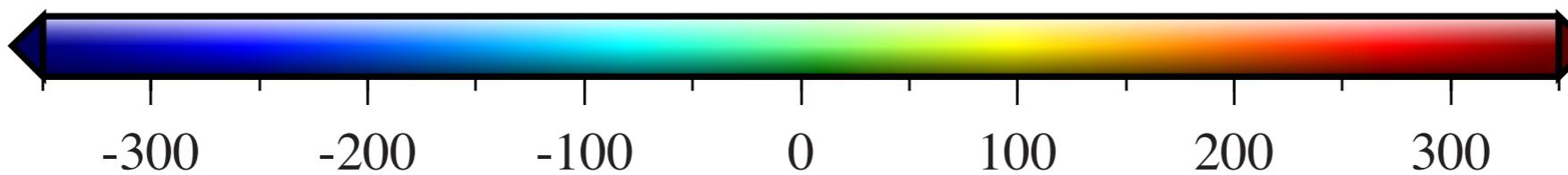
Near side



Far side



Namiki et al, 2009



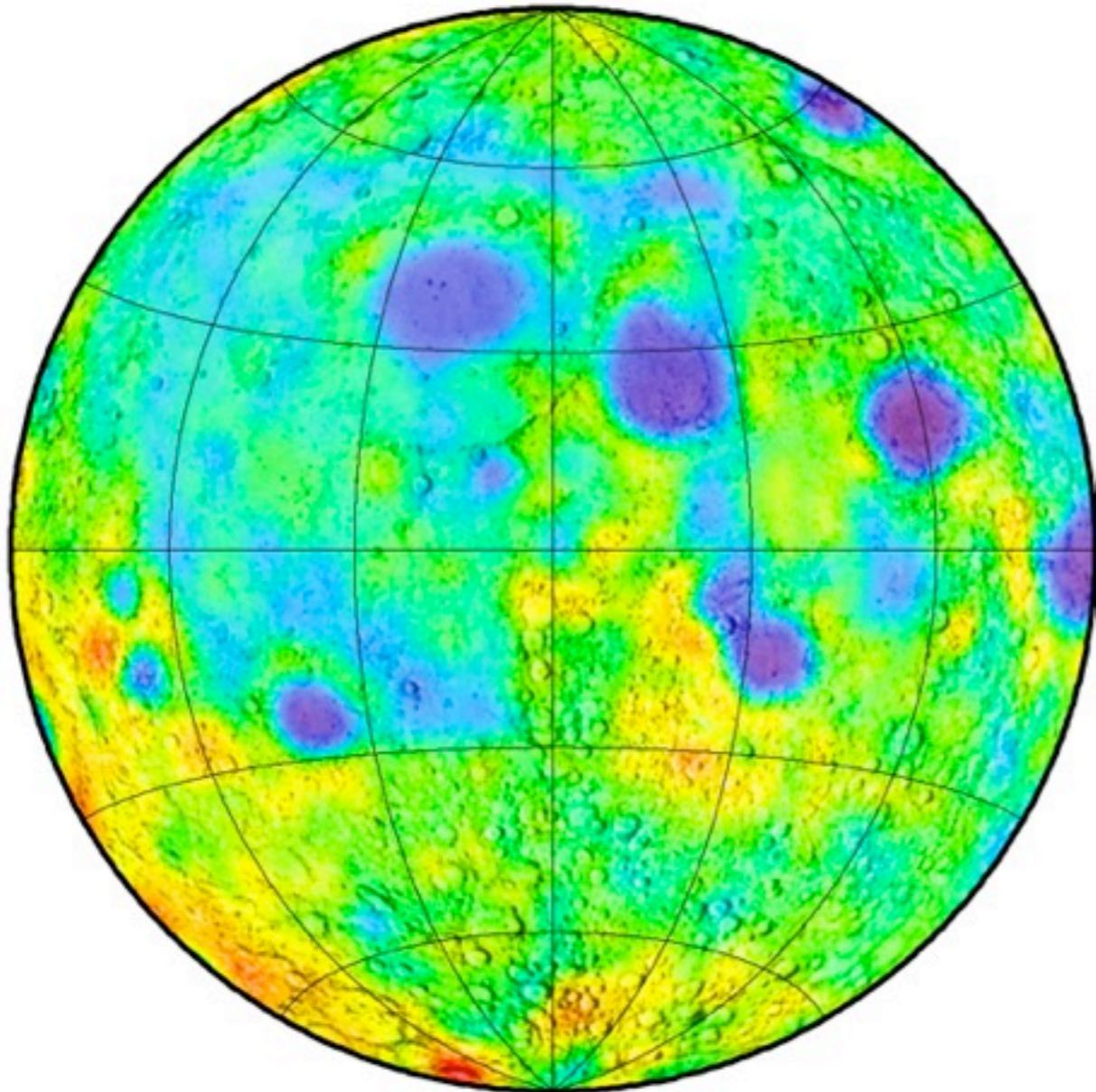
Radial Gravity Anomaly (mgals)

◆ Mascon with mare basalts

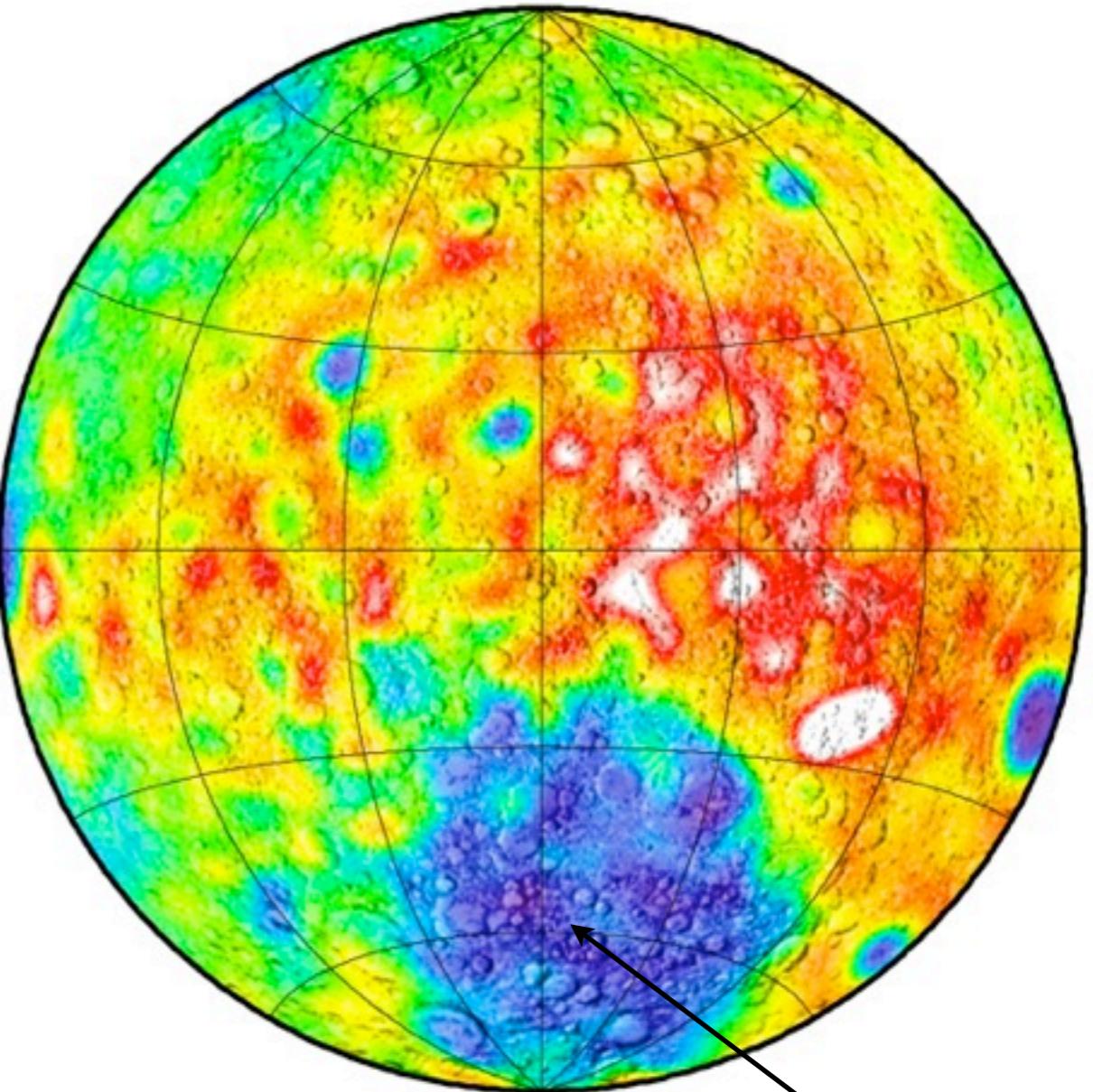
○ Mascon with no obvious mare

Crustal thickness modeling

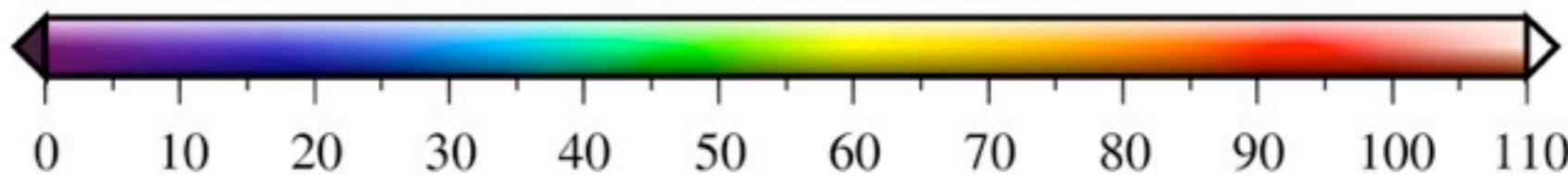
Near side



Far side



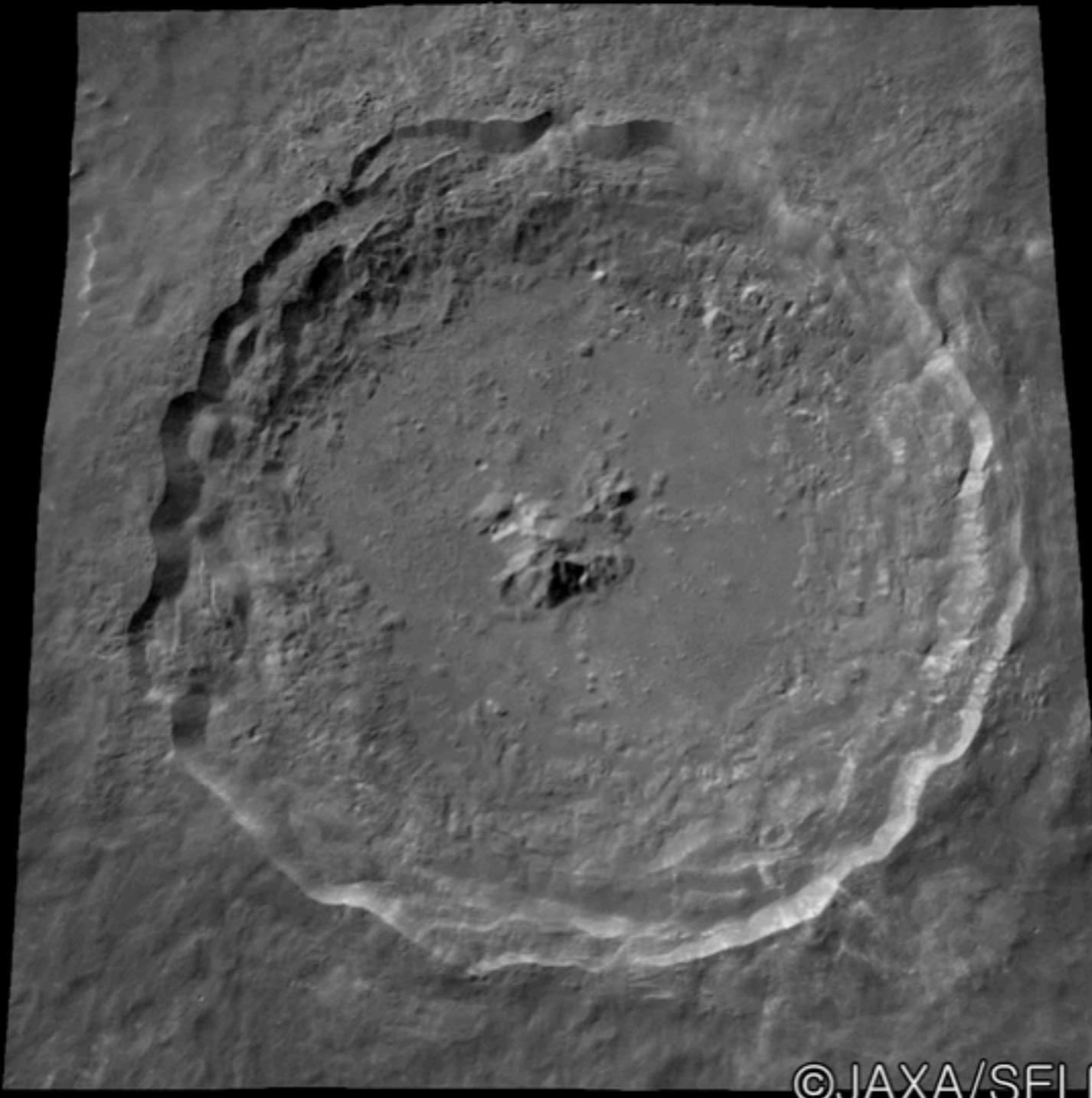
Ishihara et al, 2009



Crustal Thickness (km)

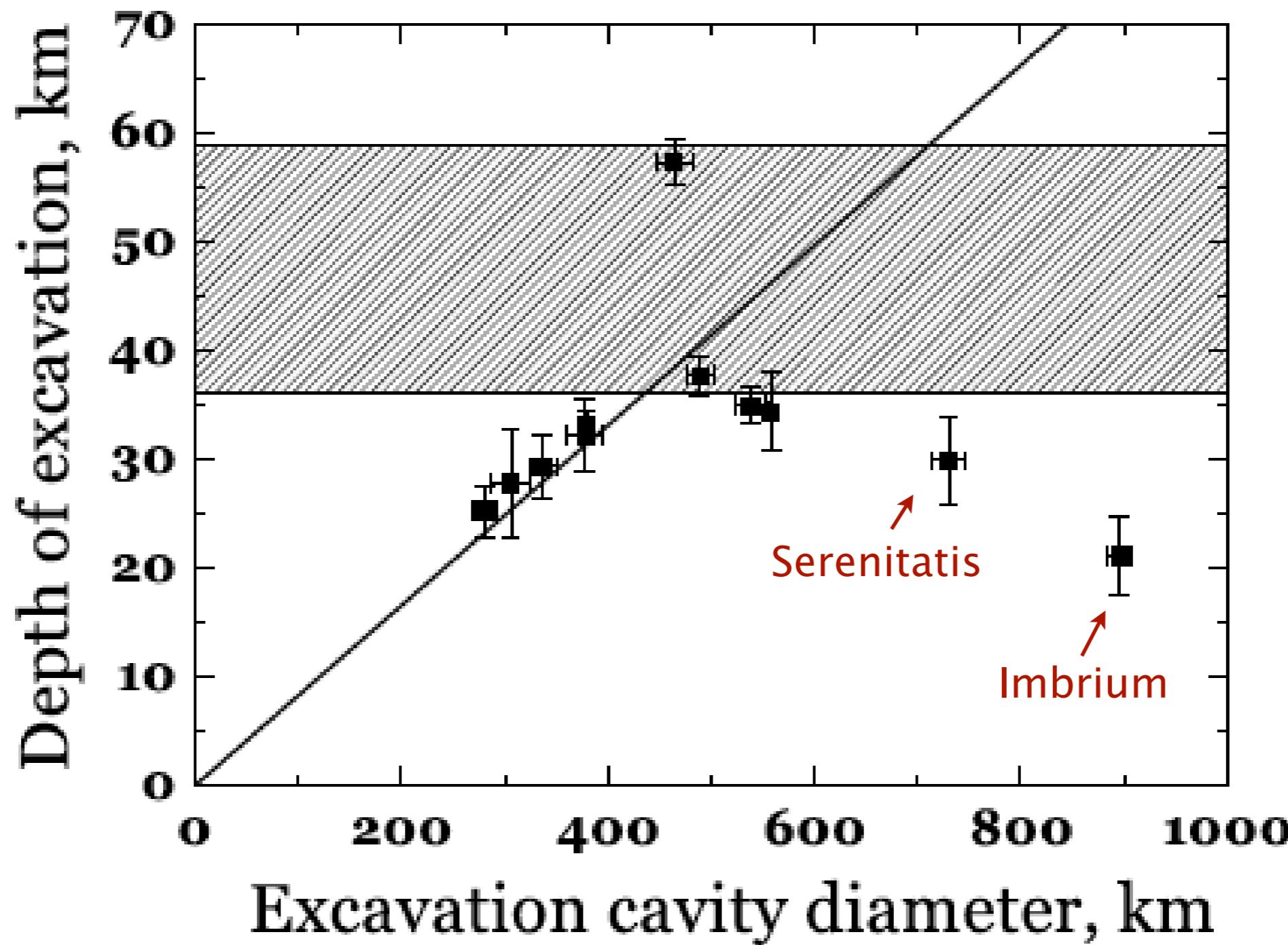
Large impact events excavated deep into the crust (and mantle?).

Tycho Crater: 85 km diameter

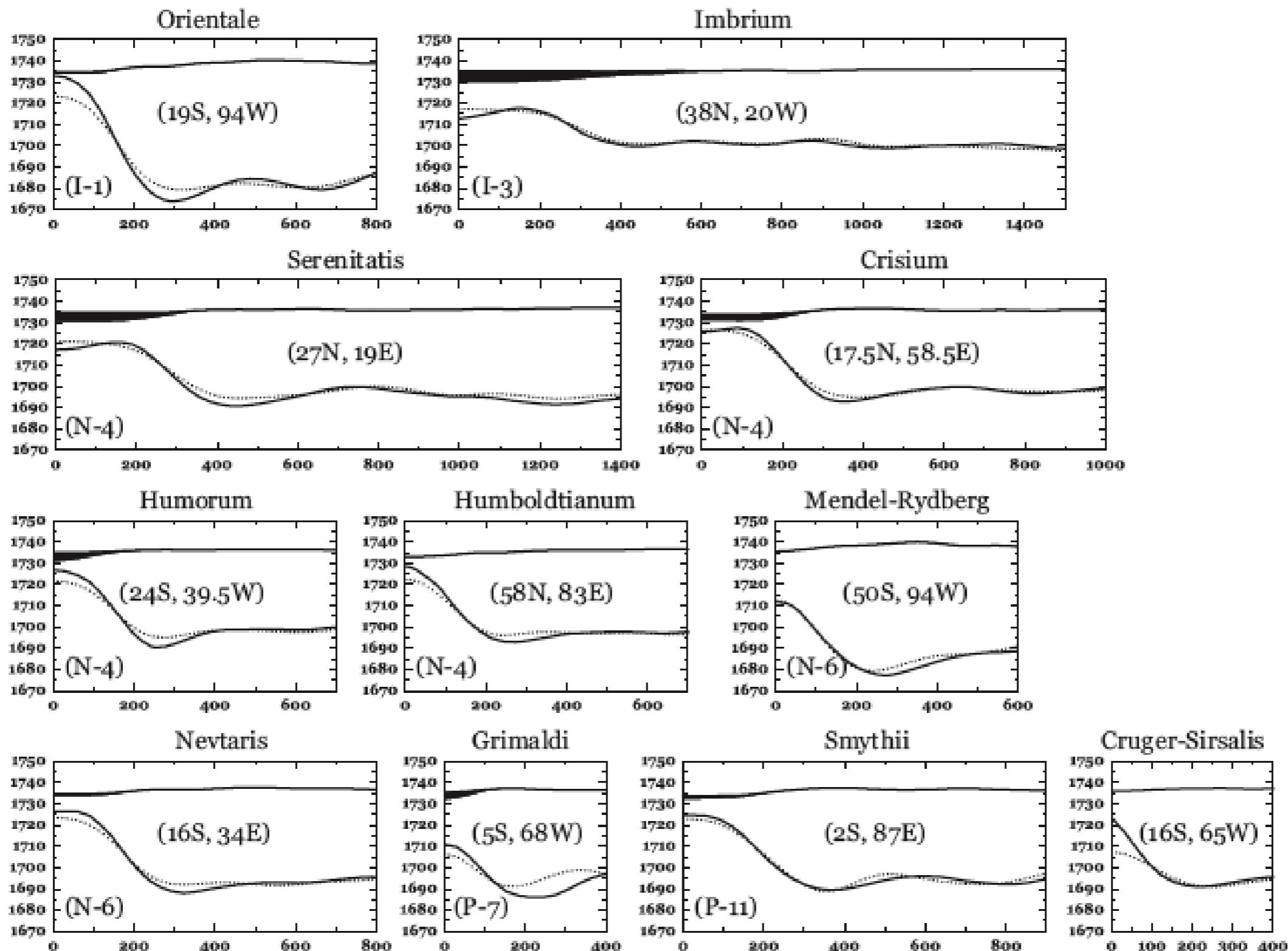


©JAXA/SELENE

The central peak could represent materials derived from about 10 km below the surface



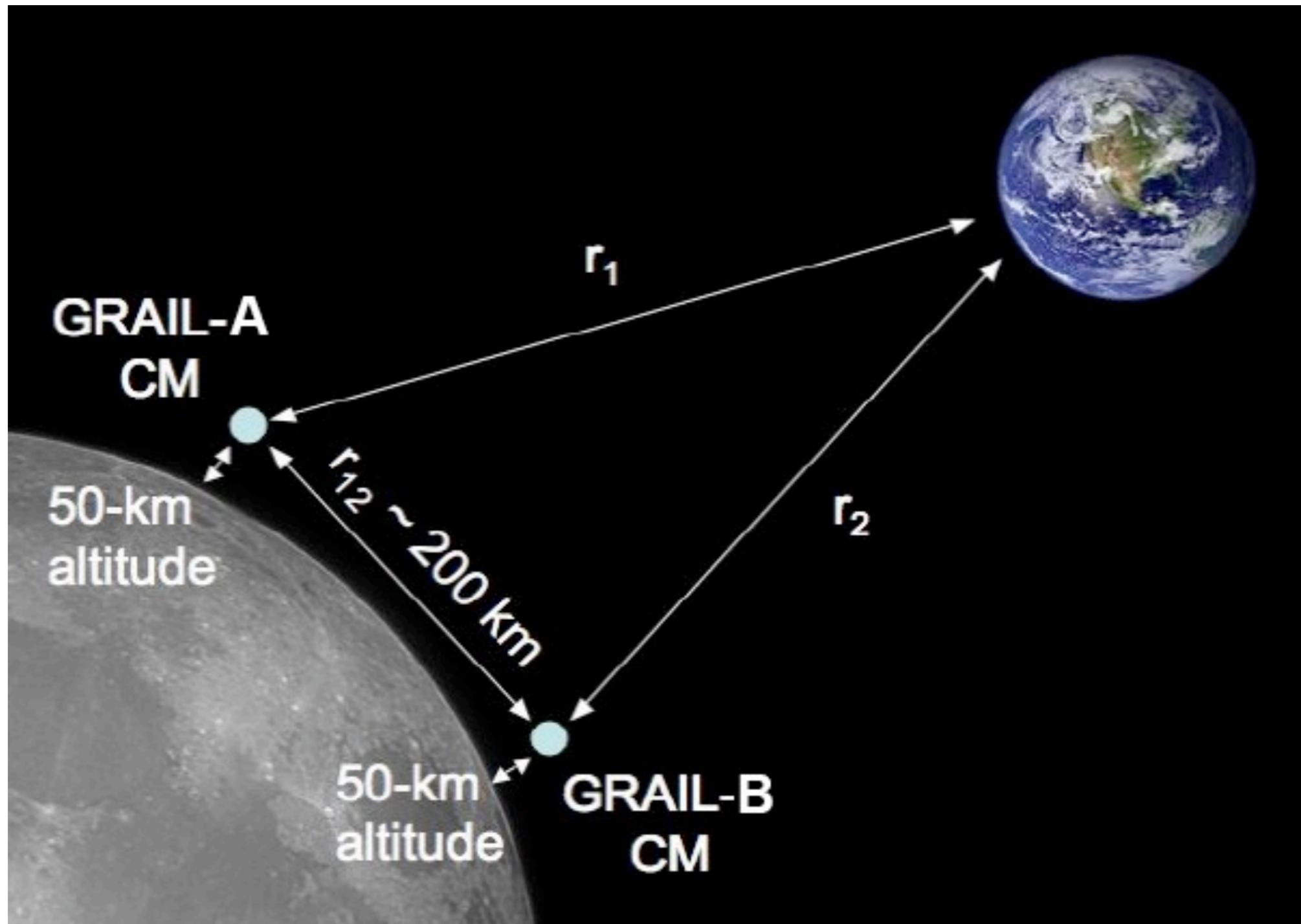
Structure of lunar impact basins



Hikida and Wieczorek (in press)

GRAIL (NASA)

Gravity Recovery and Interior Laboratory

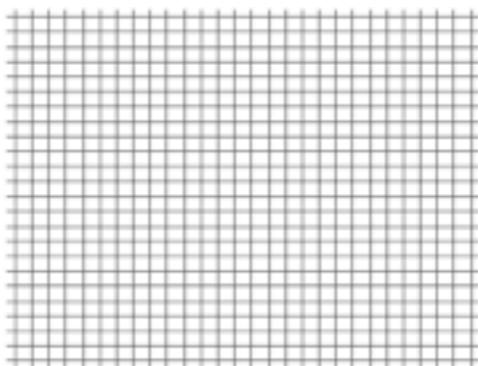
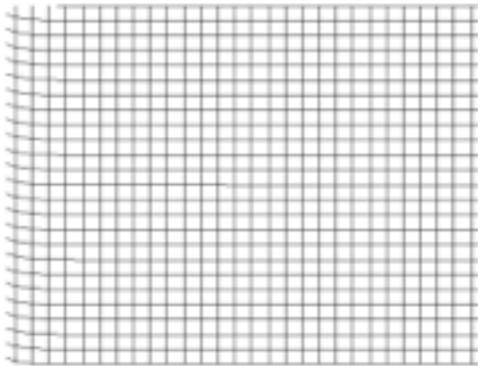


Tracking between two satellites will be obtained over the entire surface of the Moon, similar to the current Earth mission GRACE.

Seismology

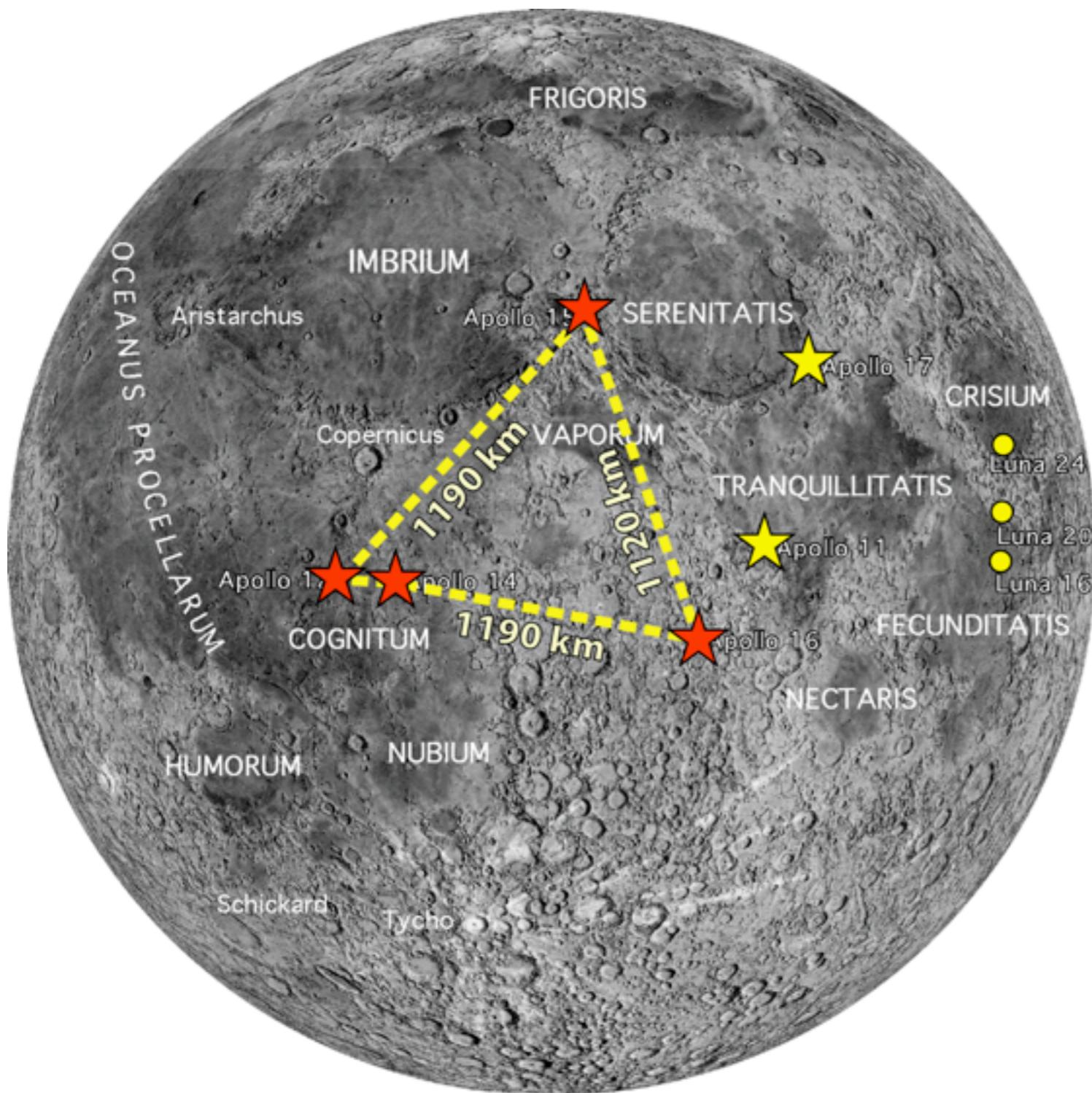
$$V_s = \sqrt{\frac{\mu}{\rho}}$$

$$V_p = \sqrt{\frac{K + \frac{4}{3}\mu}{\rho}}$$



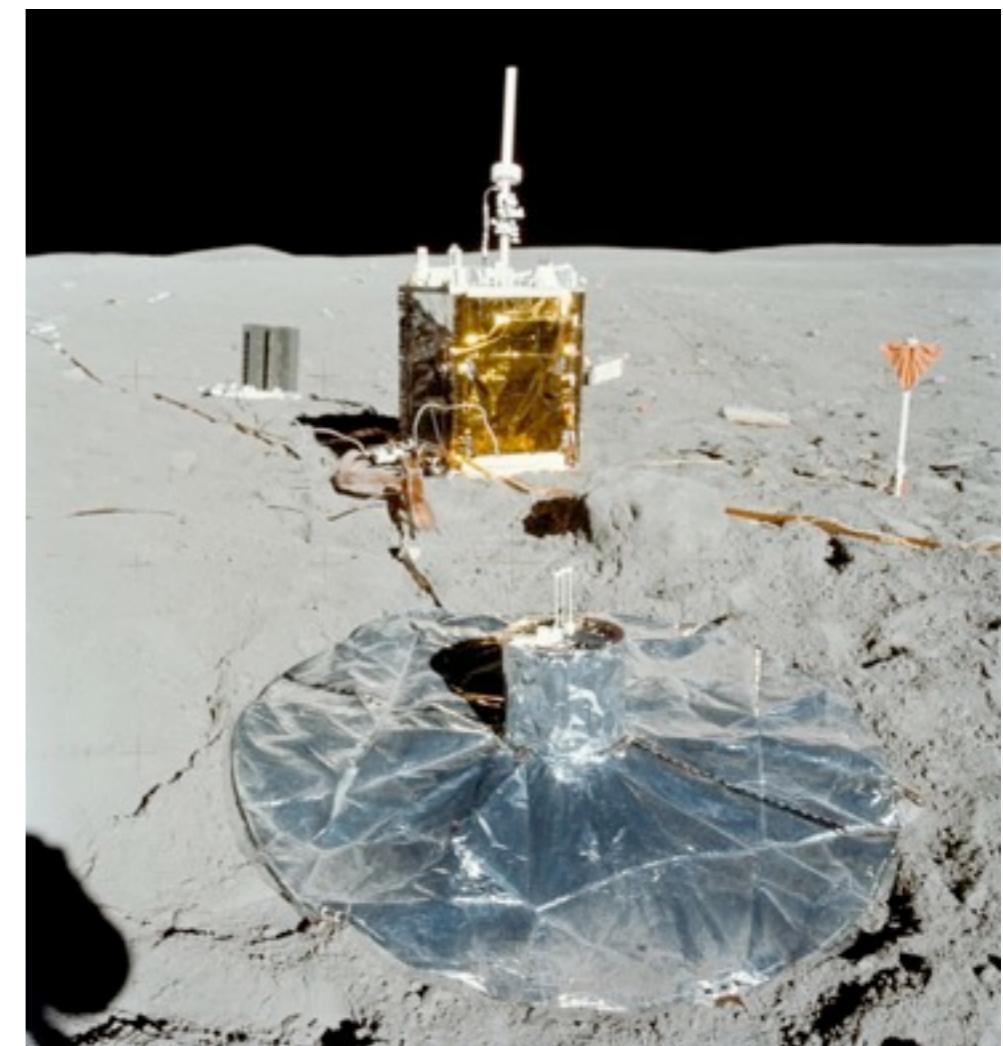
Seismic velocity depends upon both composition and temperature.

The ALSEP Network



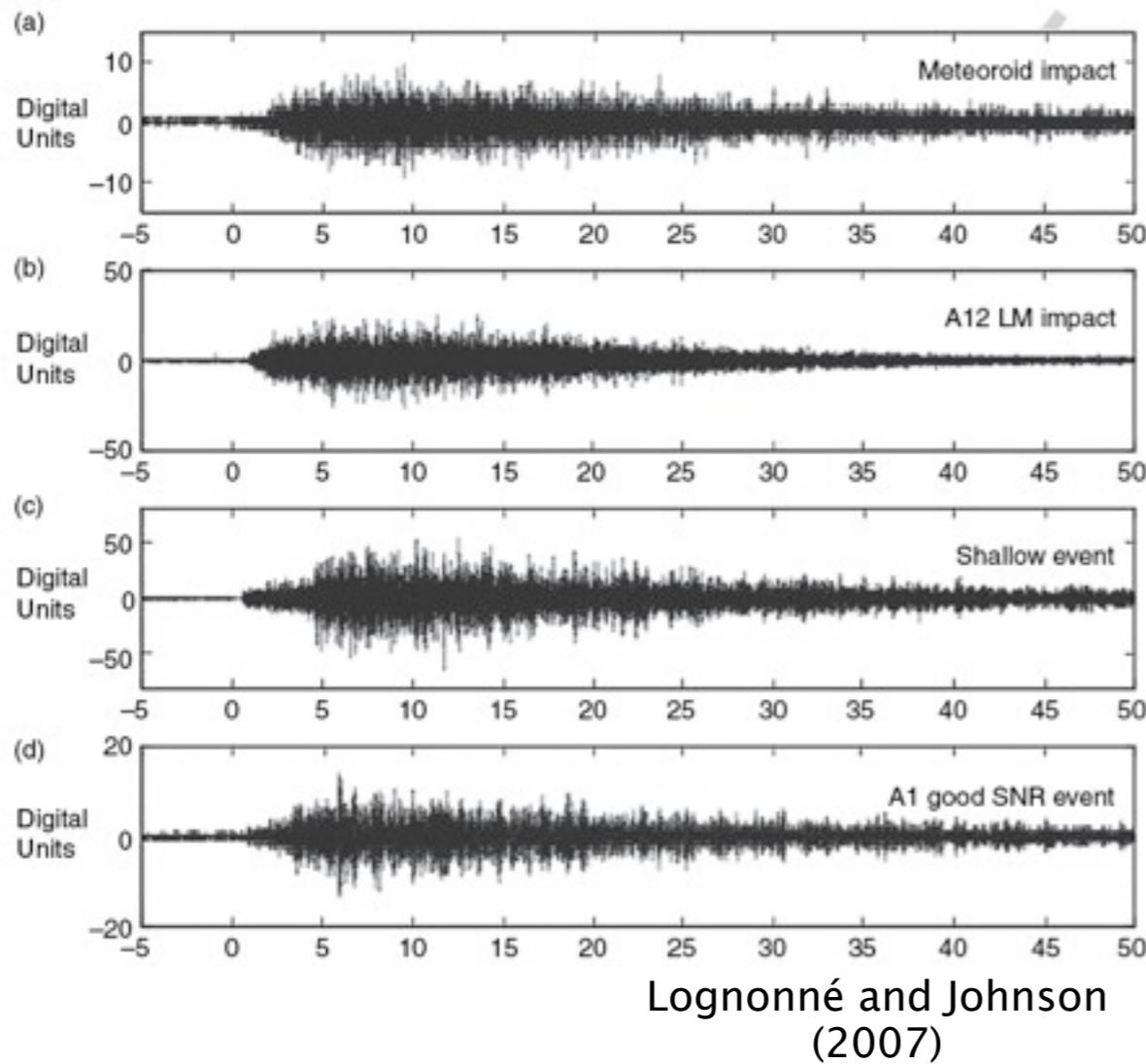
The ALSEP seismic network covered only a small portion of the near-side hemisphere.

Apollo 16 seismometer



The Apollo Lunar Surface Experiment Packages (ALSEP) operated concurrently from ~1972 to mid-1977.

Characteristics of moonquakes

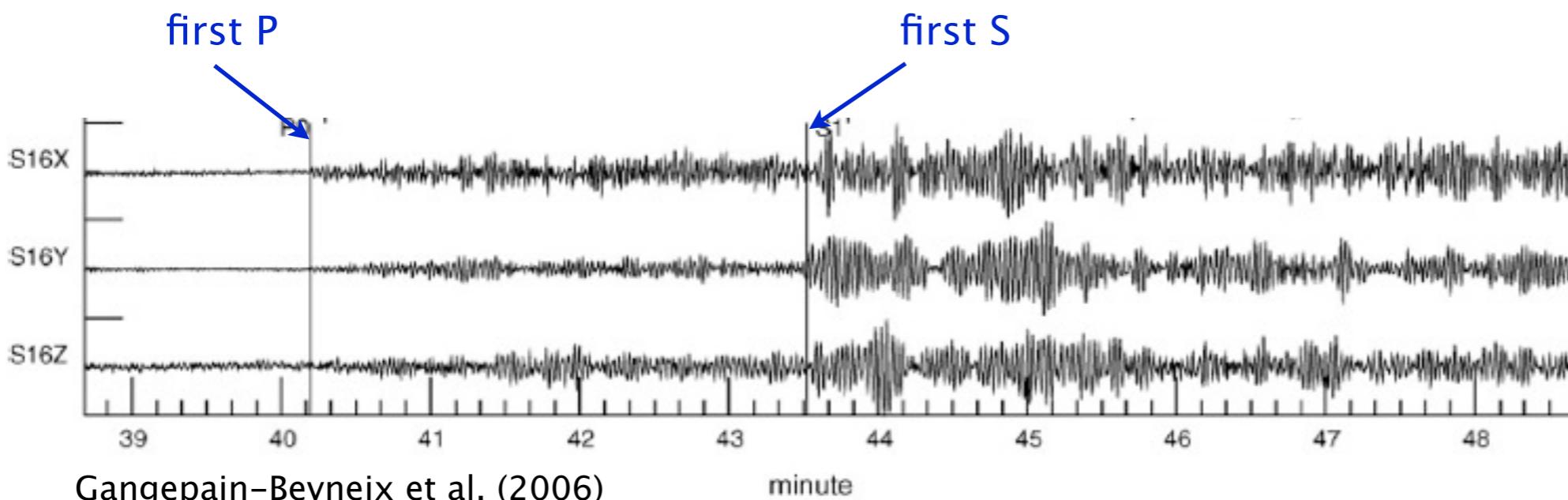


~1700 meteoroid impacts.

9 artificial impacts.

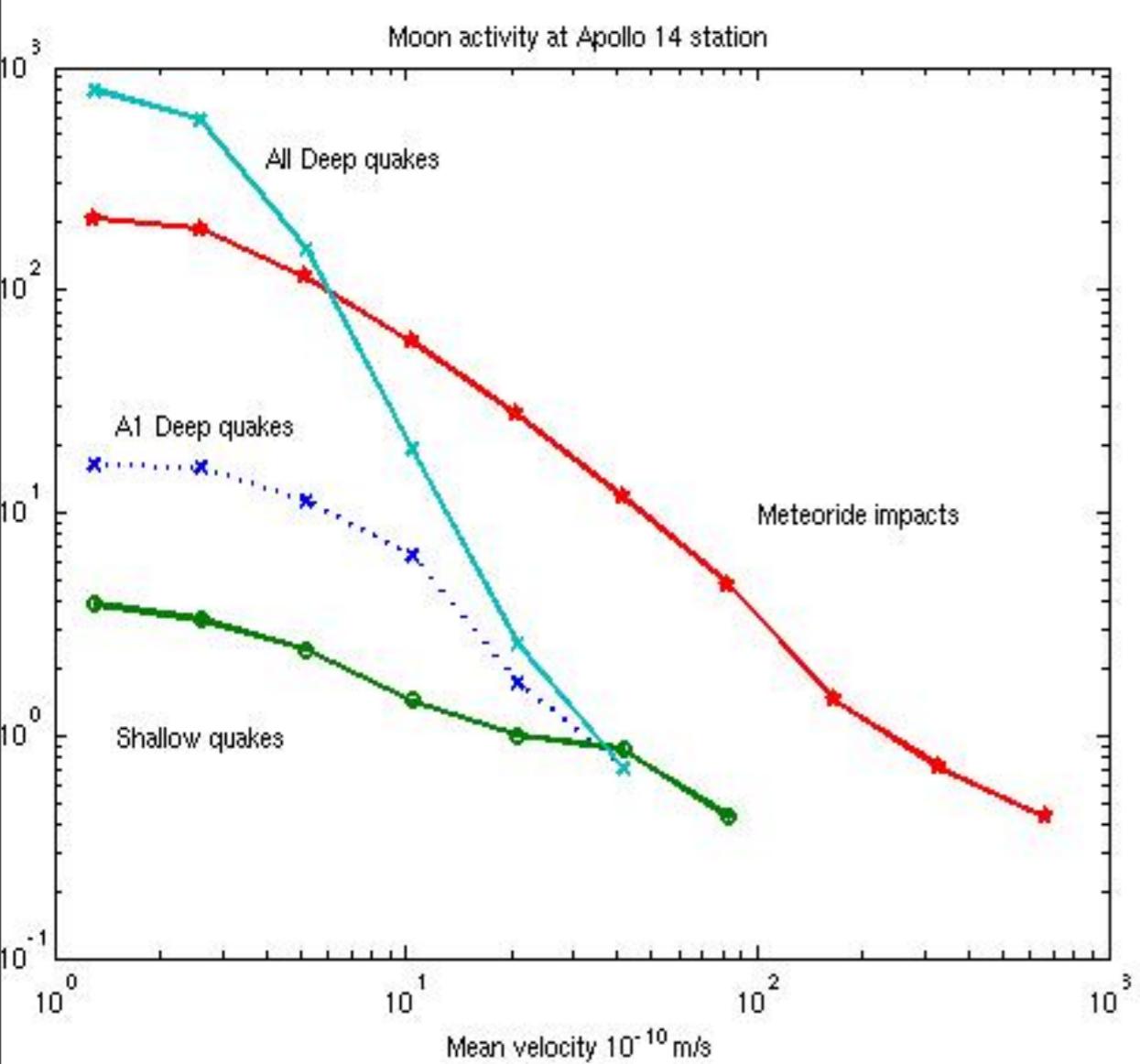
28 shallow “tectonic” moonquakes. (Most energetic, having magnitudes up to 5).

~7000 deep moonquakes originating from about 300 distinct source regions that are correlated with the tides.

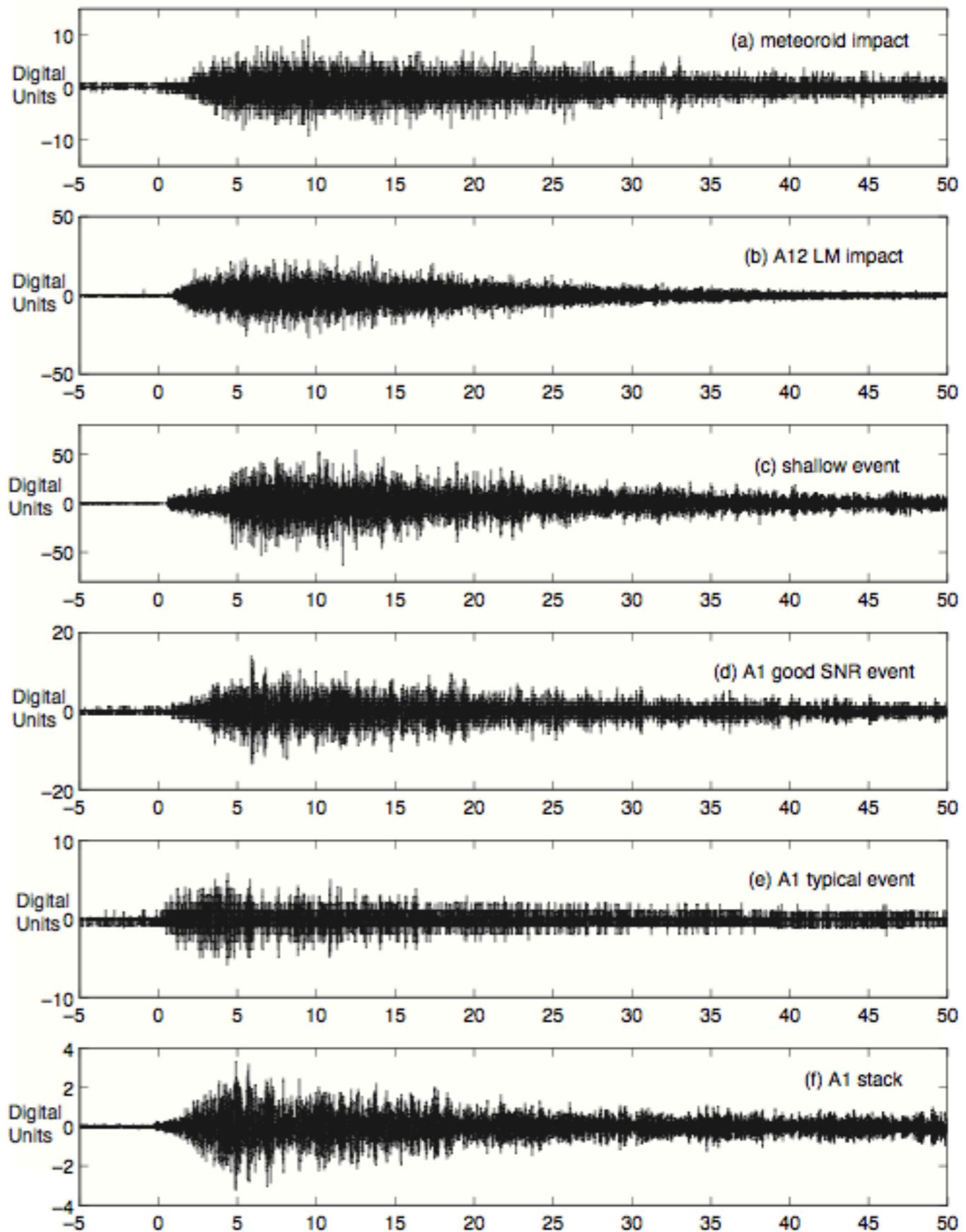


Picking P and S first-arrival times is subjective; uncertainties can be up to 10 seconds.

But very small amplitudes....



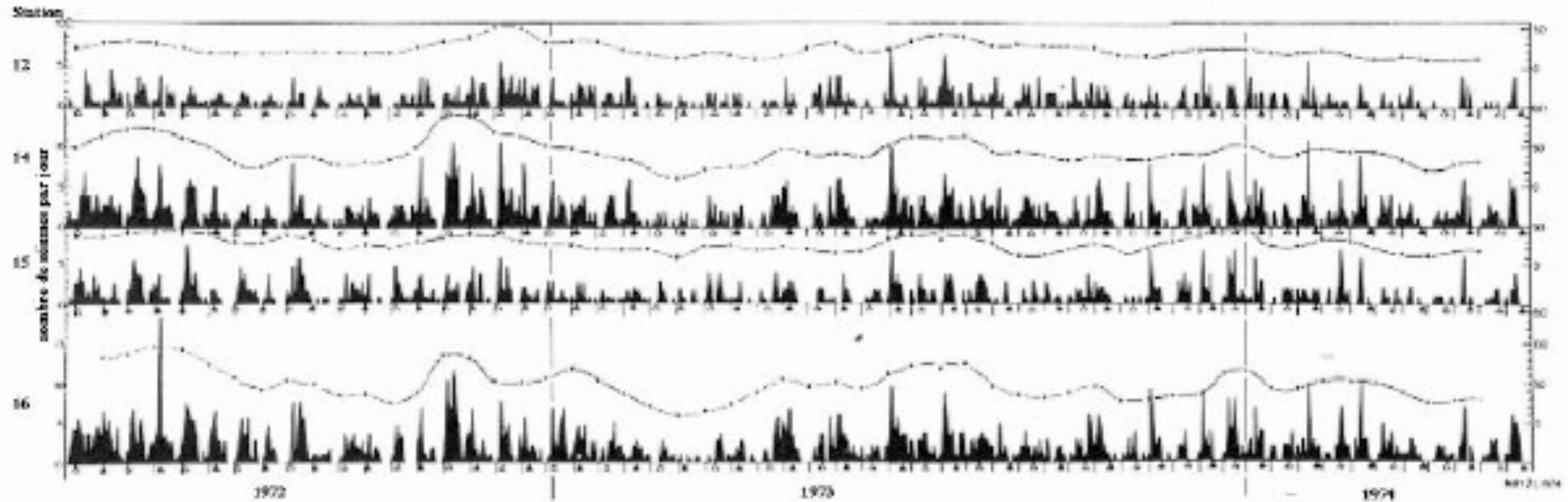
Lognonné and Johnson, 2007



Lunar specific seismic events

- Deep Moon quakes (Quakes occurring at the same locations)
- Impacts (on the Earth, most of the impacting meteorites are burned in the atmosphere)

Deep moonquakes



- Number and amplitude of quakes is related to the amplitude of tide
- About 50 active faults detected
- Quakes occur at the same fault regularly but with very low amplitudes, with ground displacement of a few Angströms at 2 sec ($0.5 \text{ } 10^{-9} \text{ ms}^{-2}$ of ground acceleration)

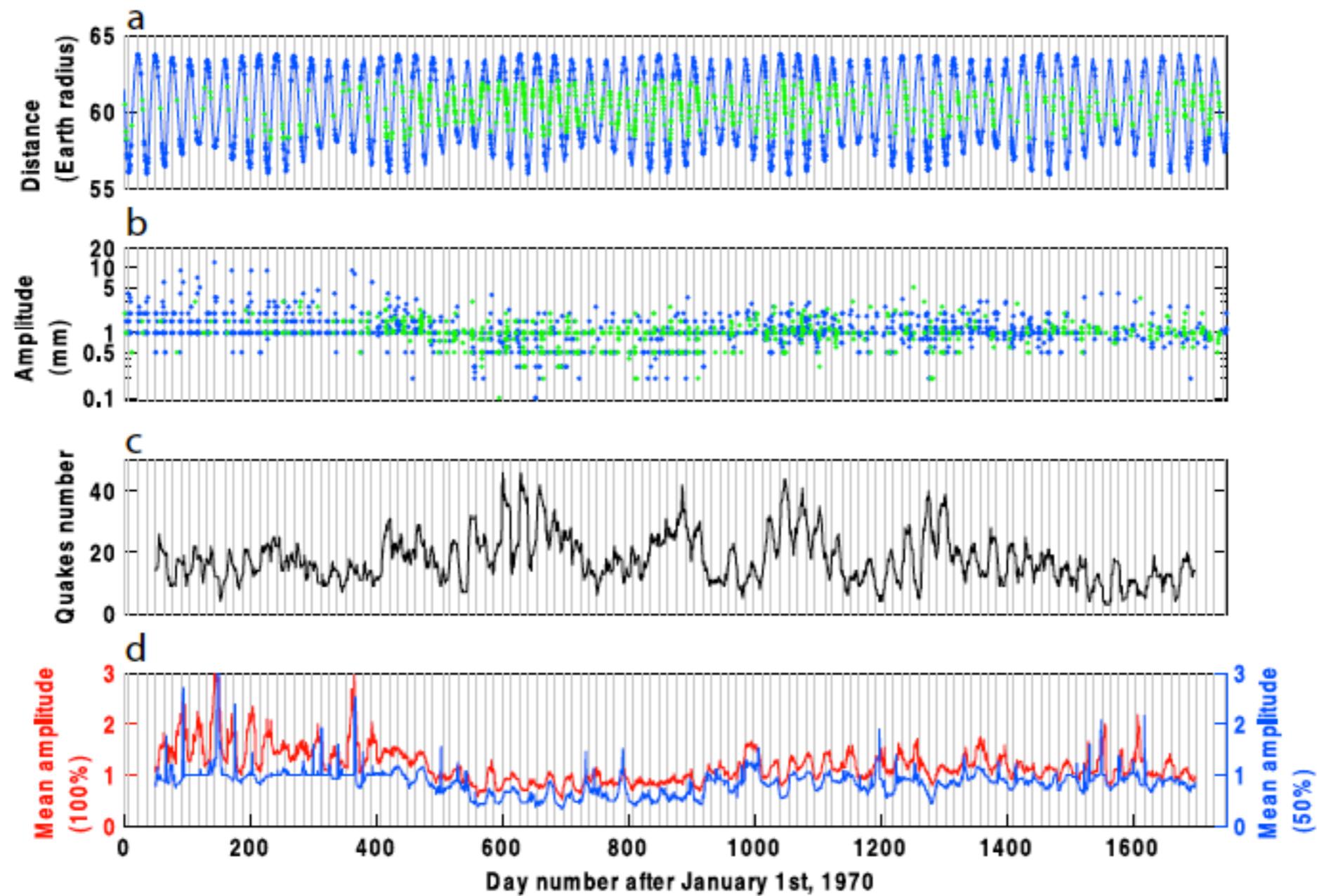
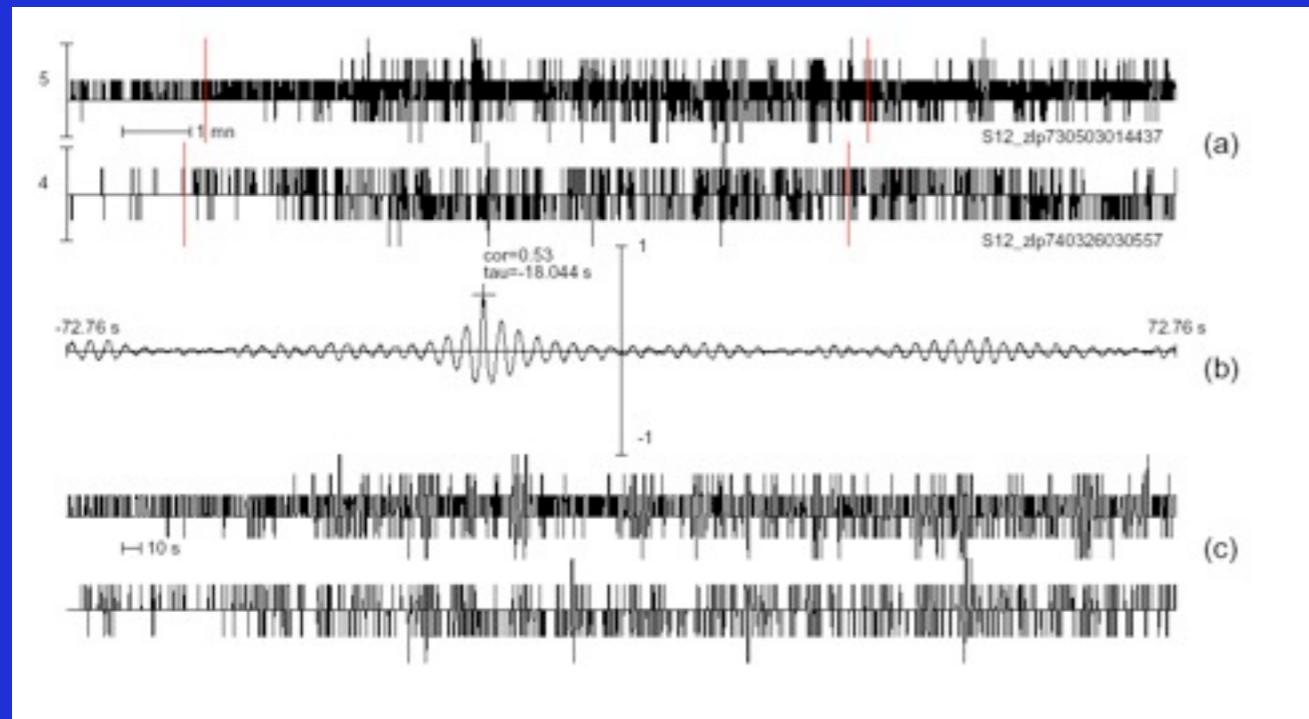
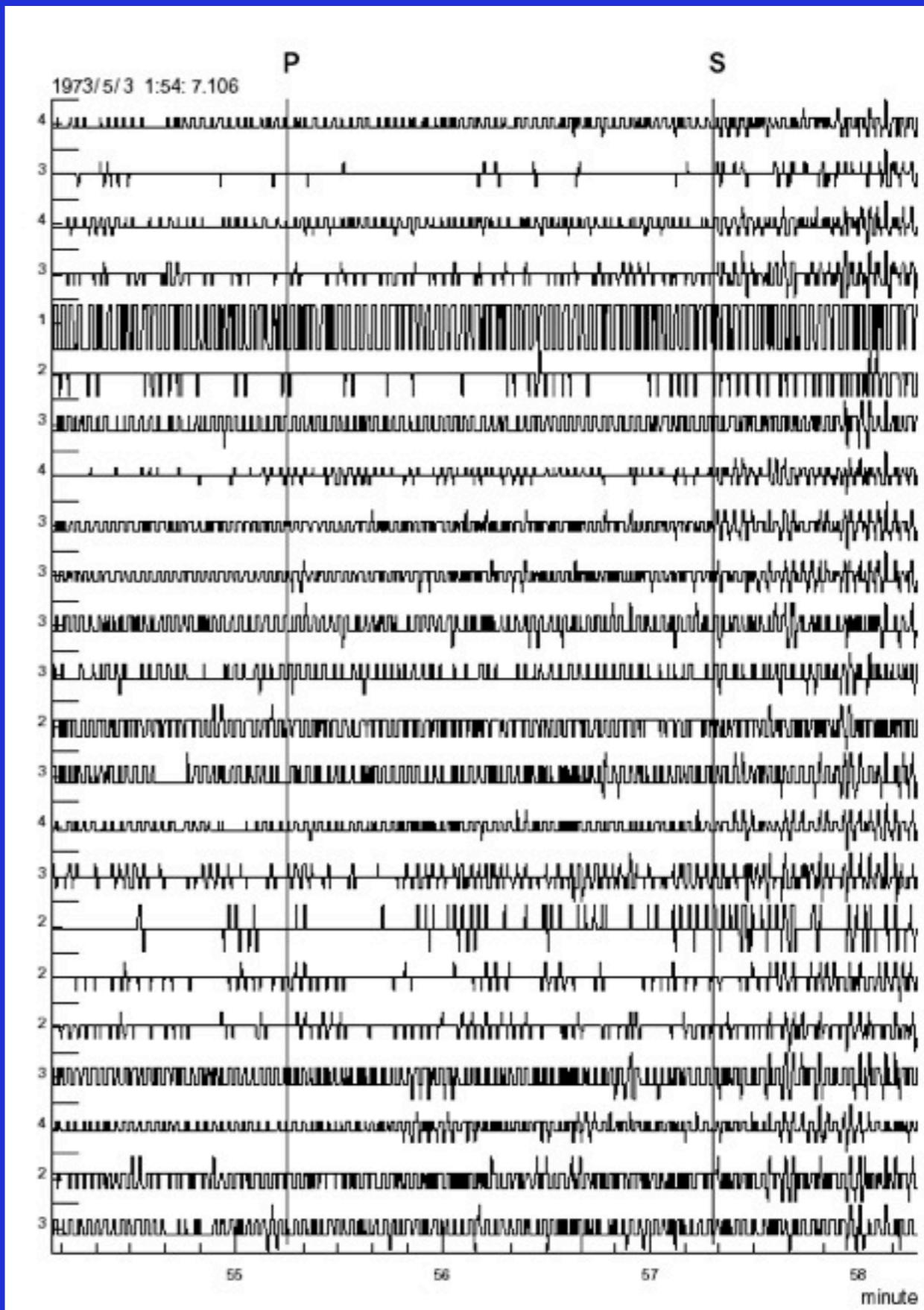


Figure 4. (a) Occurrence times of deep moonquakes plotted on the Earth-Moon distance curve. The green (blue) stars are used for events occurring when the Earth-Moon distance is smaller (greater) than 50% of its maximum excursion from the mean distance. (b) The corresponding amplitudes. (c) The number of moonquakes occurring in a 2 week period centered on any given day. (d) The mean amplitude of all events (red line) in this 2 week period, and the mean amplitude of the smallest 50% of events in the same period (blue line). We note variations in the latter between 0.5 to 1 mm.

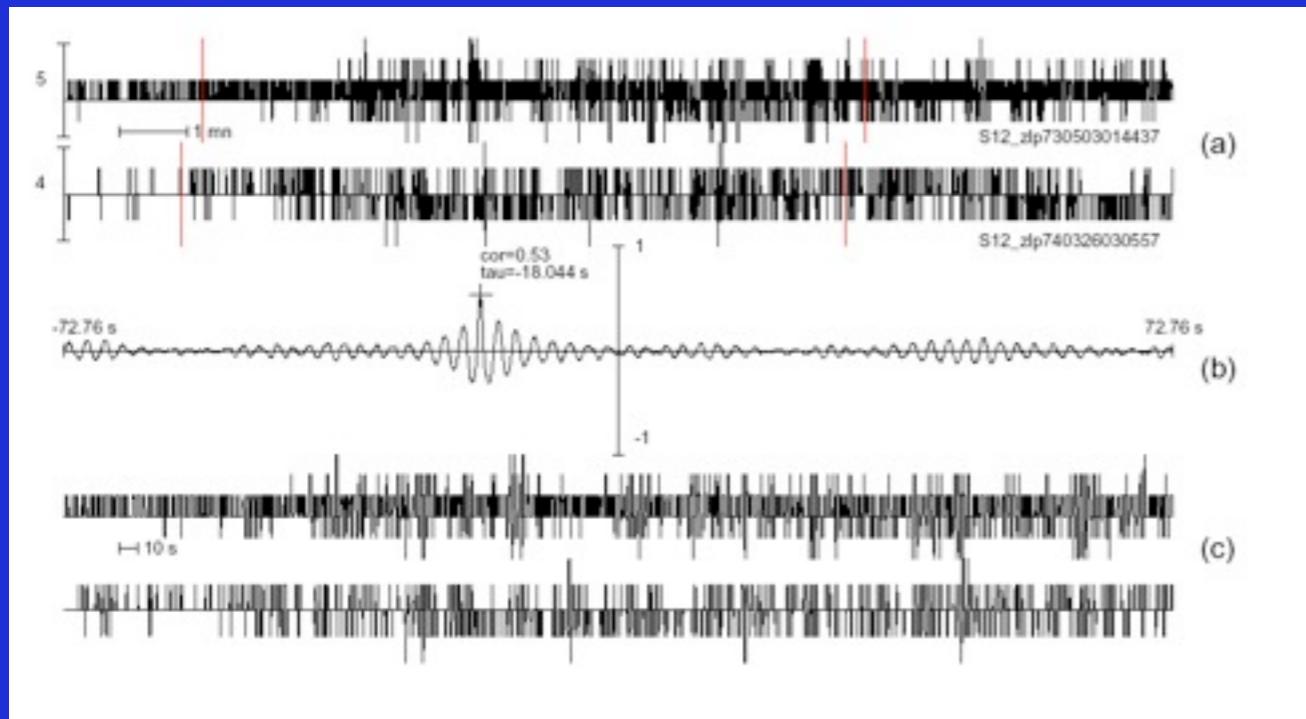
Deep Moonquake



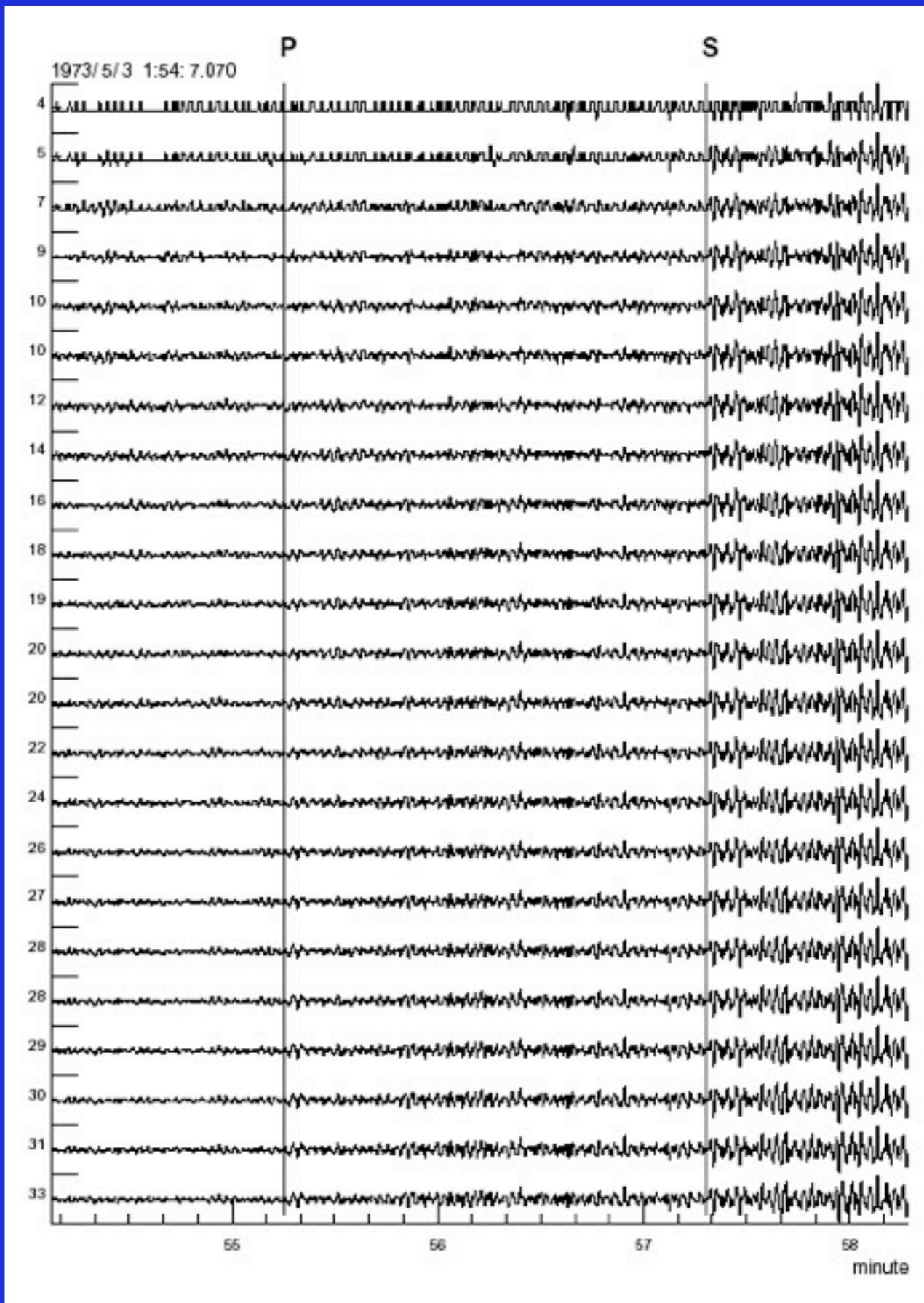
- example of two quakes (in 1973 and in 1974) from the same deep focus and their cross-correlation
- cross-correlation provides the time shift necessary to align the arrival times
- stacking can then be done



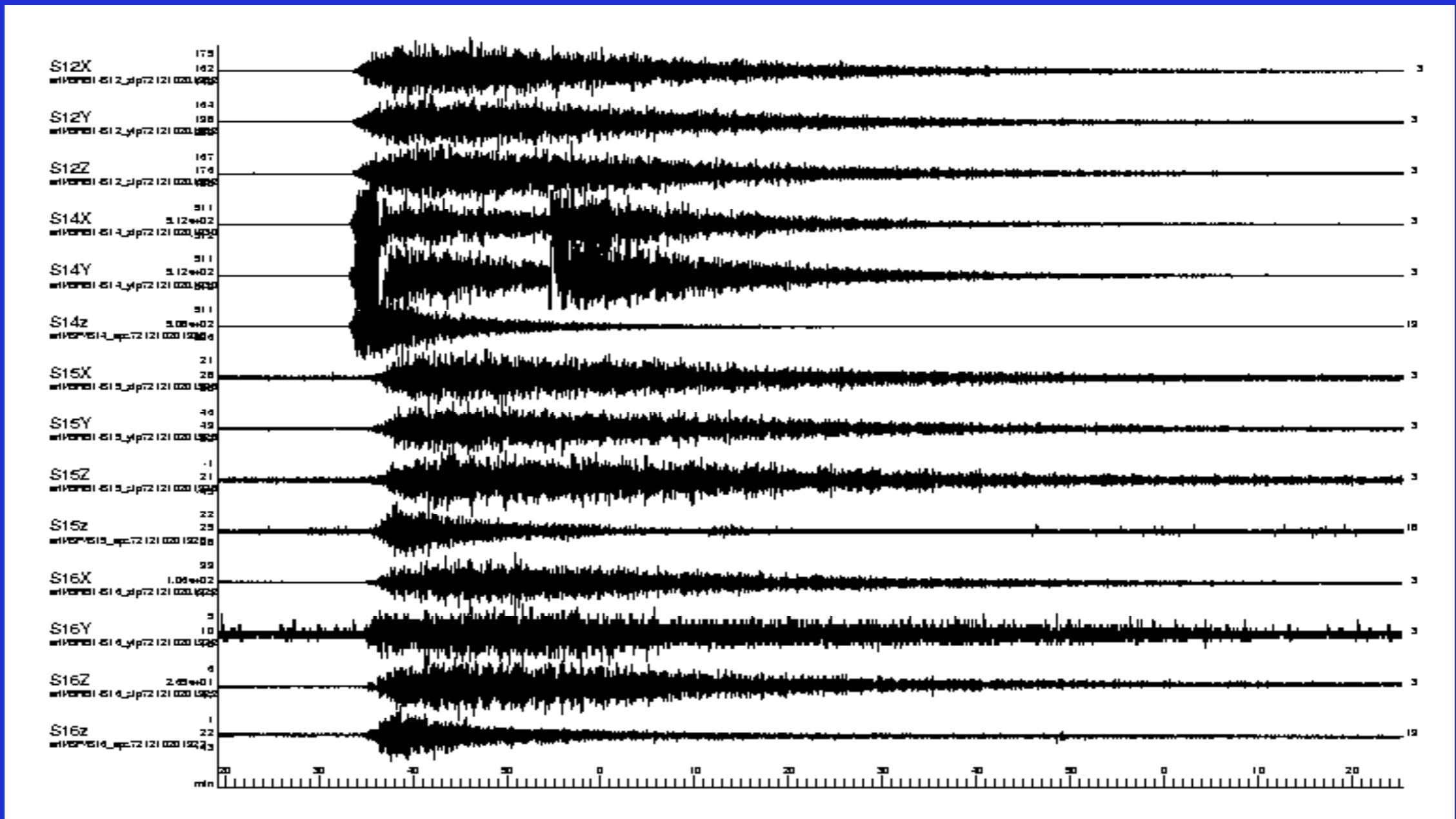
Deep Moonquake



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Active source: impacts

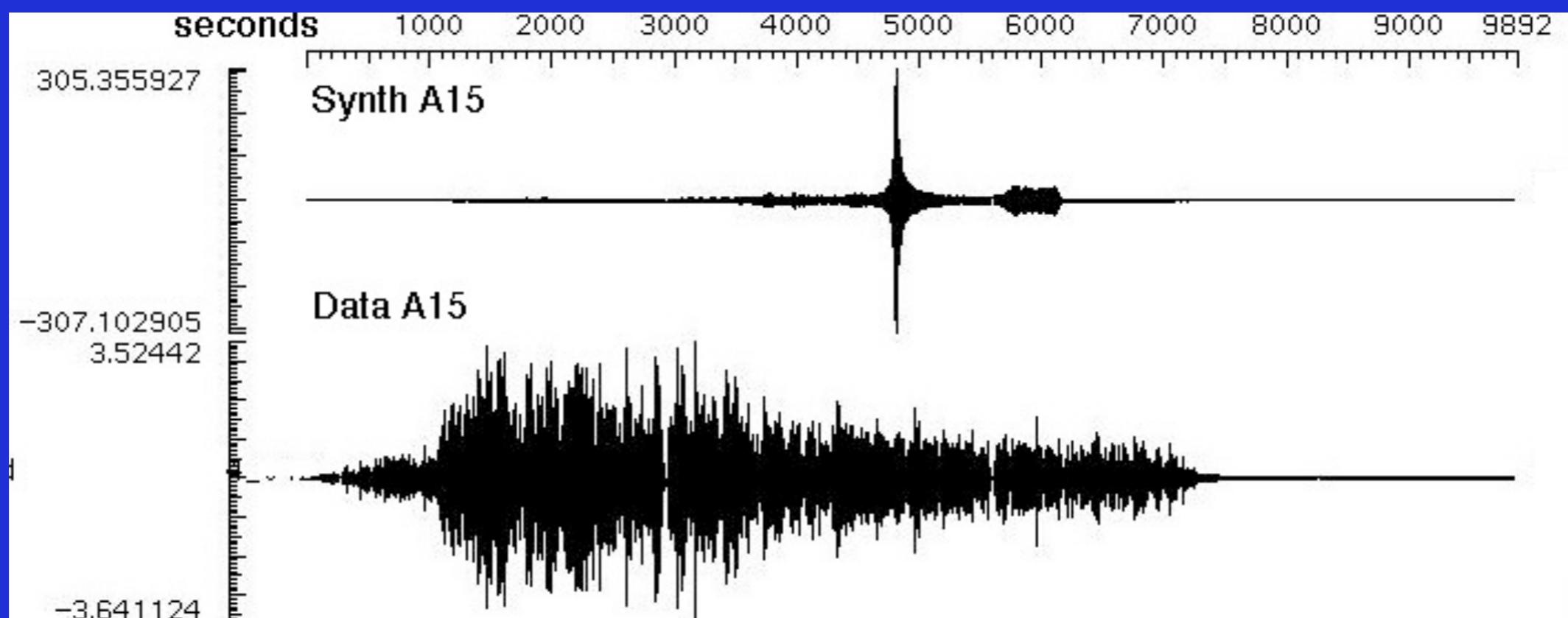


- Impact of the Apollo 17 Saturn V upper stage (Saturn IVB) on the Moon on 10 December 1972 at distances of 338, 157, 1032 and 850 km from the Apollo 12, 14, 15 and 16 stations, respectively. Amplitudes at Apollo 14 station, 157 km from impact, reach about 10^{-5} m s^{-2}
- Known time and location: all arrival times give information on the structure

Diffraction: the modelling challenge!

- The Moon subsurface is highly fracturated, as a results of non-resurfacing and of a long impacting history
- Propagation equation is not valid anymore for waves propagating in the crust and diffusion equation must be used
- Scattering destroy short period surface waves and is able to transfer energy from P to S waves up to an equipartition given by $E_p = v_s^3 / v_p^3 E_s / 2$, where E_p , E_s are the energy of P and S waves, v_p , v_s are the velocities of P and S waves

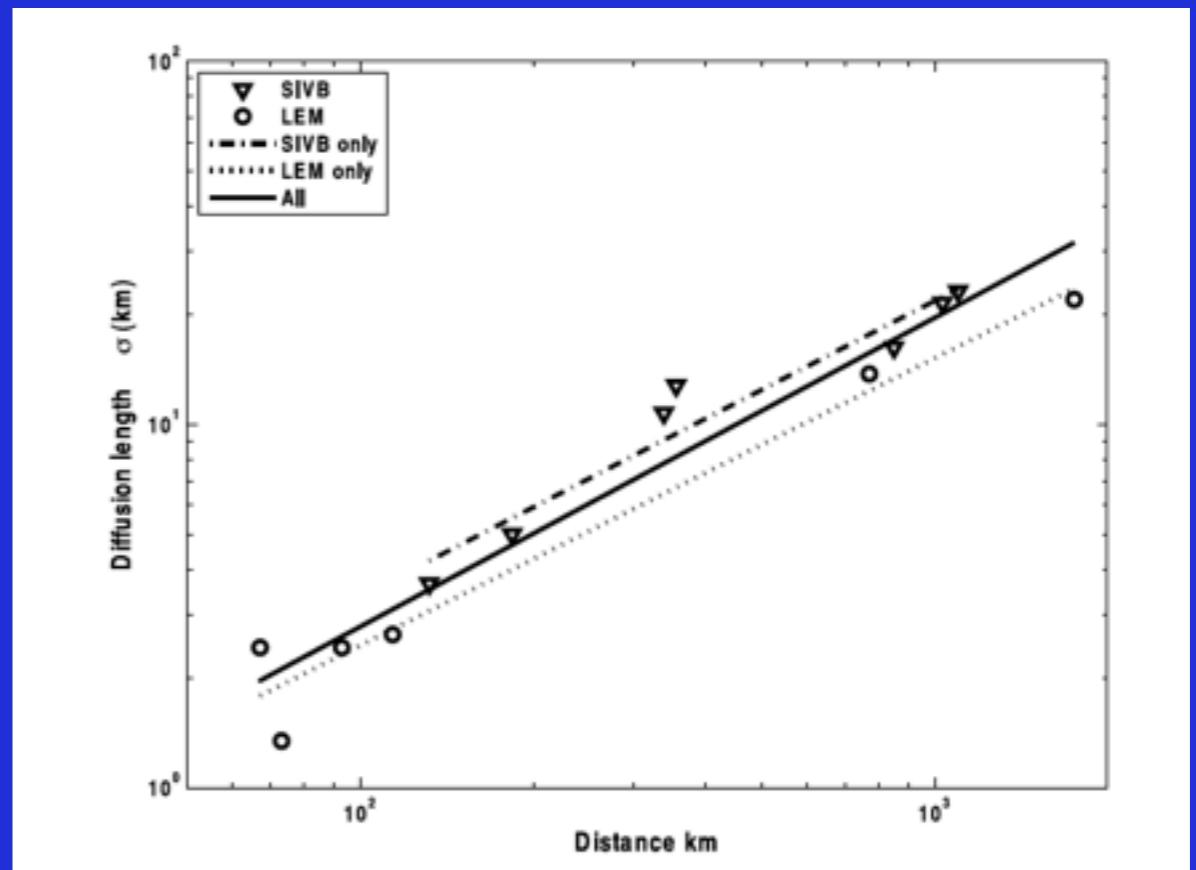
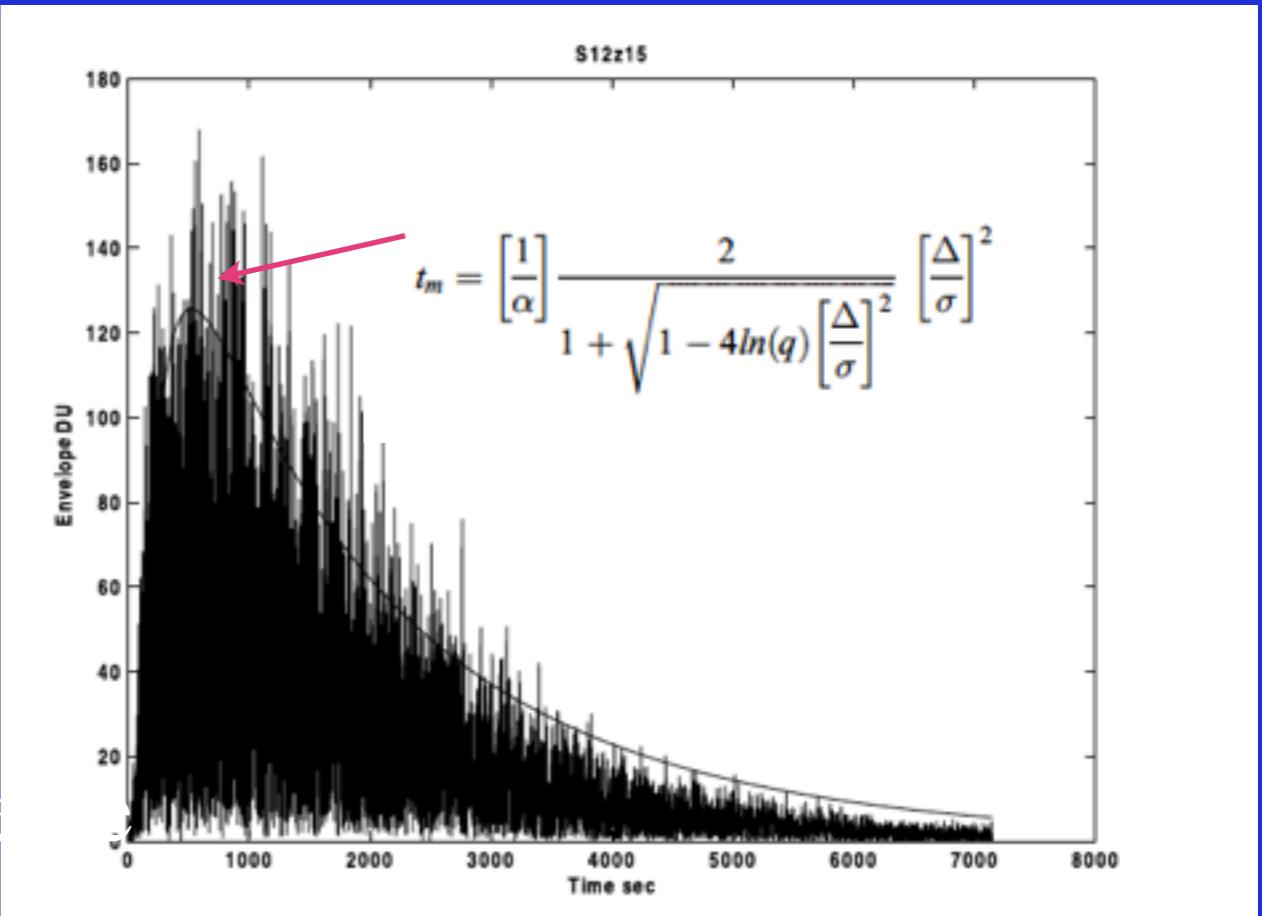
Example
a known
artifical
impact



$$e(t) = A^2 q^{at} \frac{1}{at} e^{-\frac{1\Delta^2}{at\sigma^2}}$$

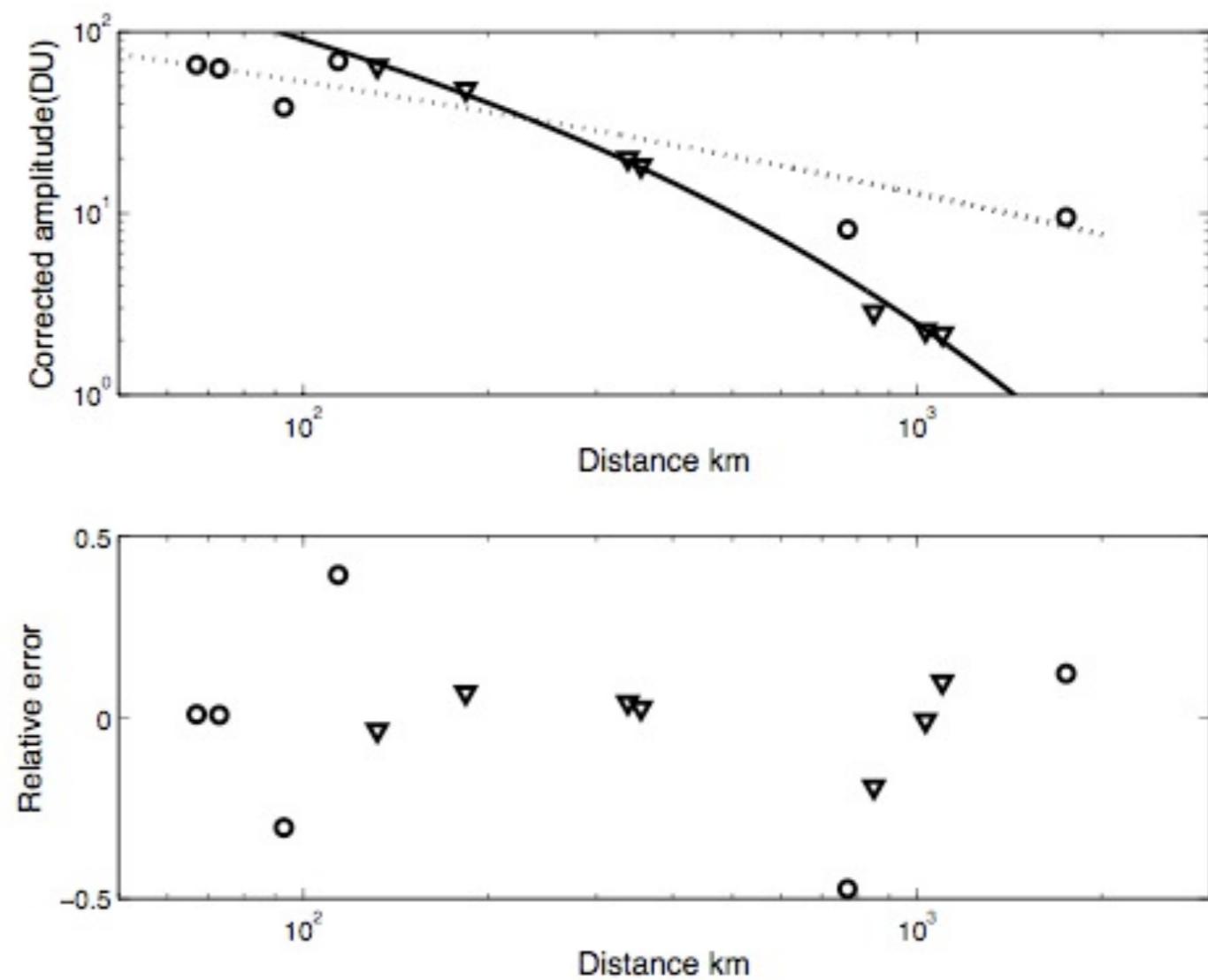
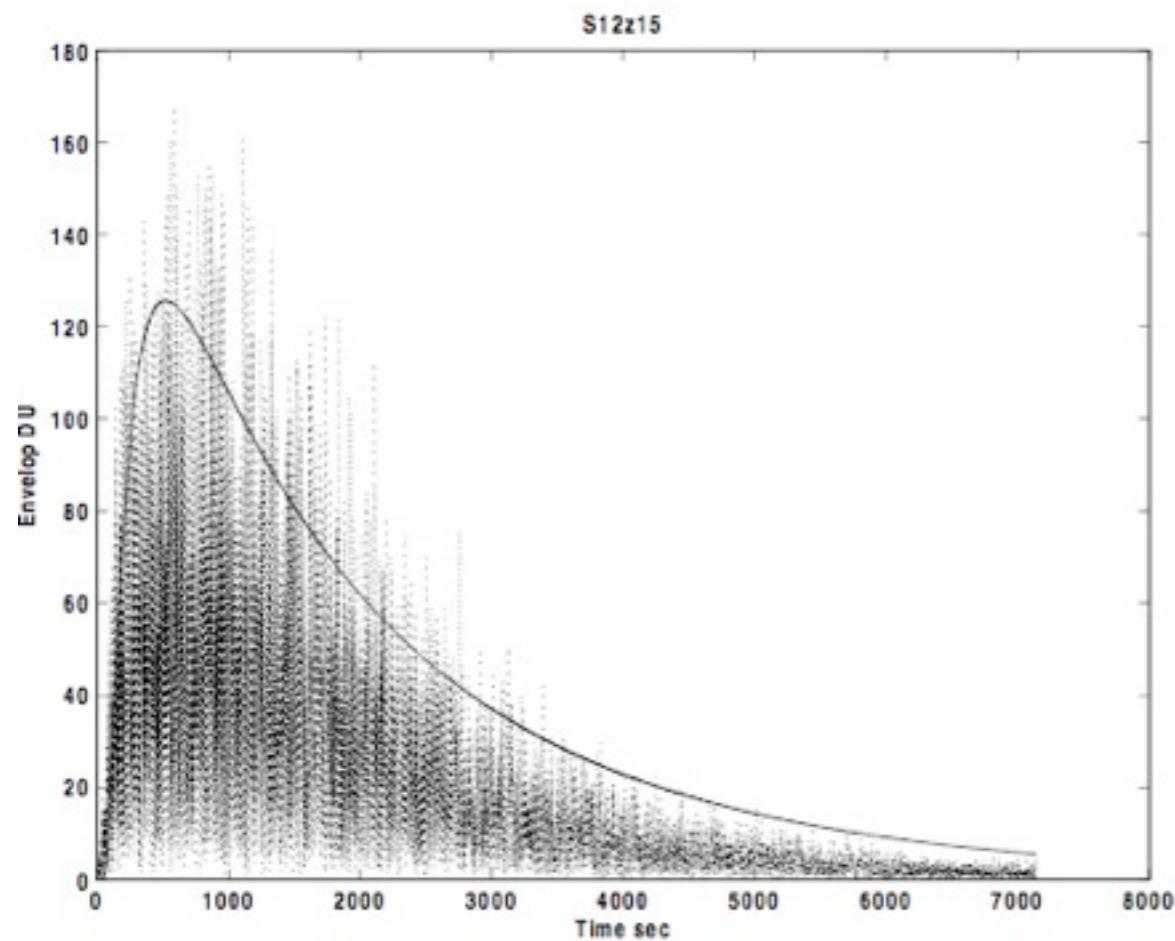
The envelope of the signal is given by:

- Simple Diffusion theory
(Strobach, 1970)



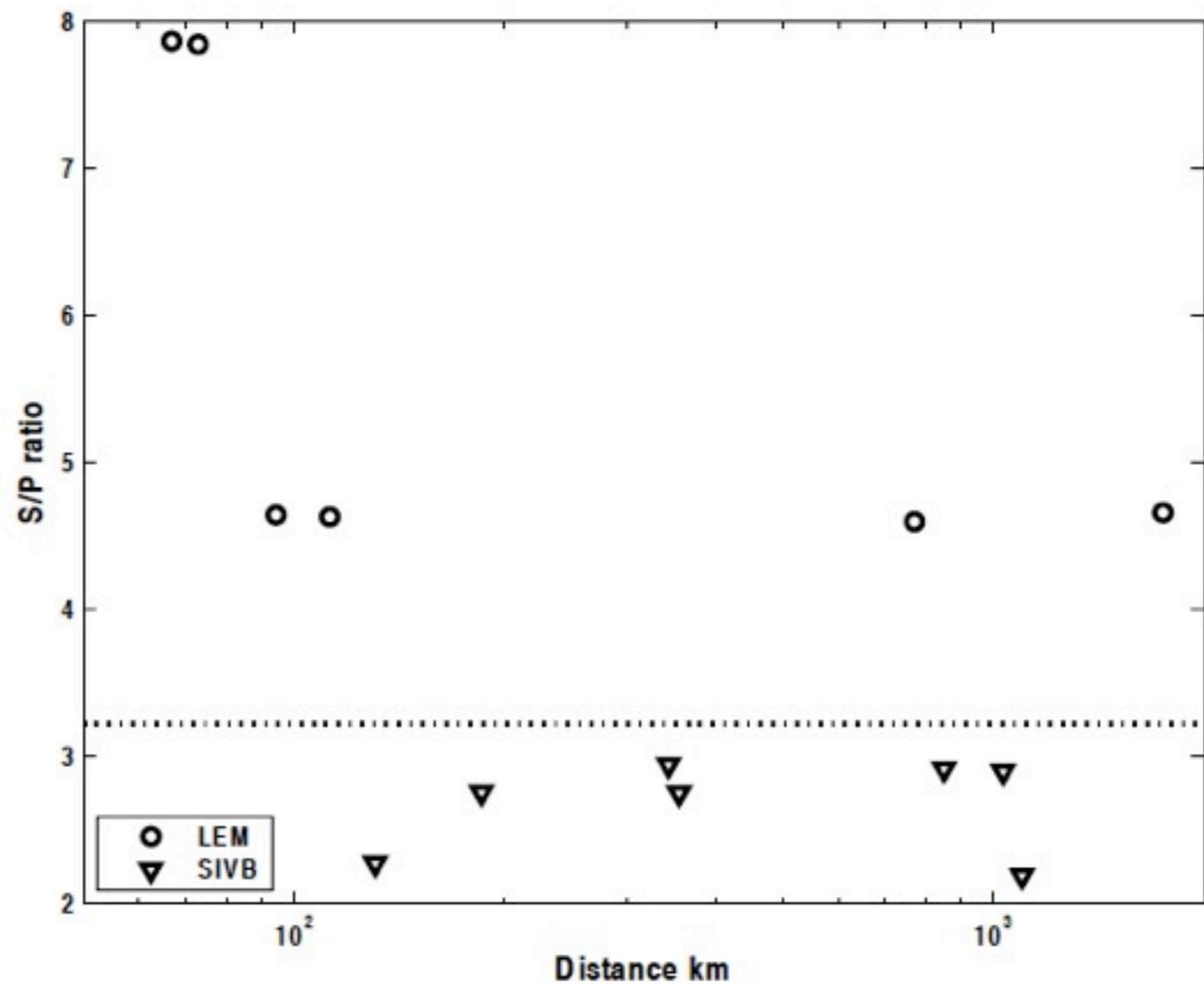


Excitation differences between the LEM and S4B impacts





A signature of a different diffusion regime?



Modeling without the diffracted surface waves

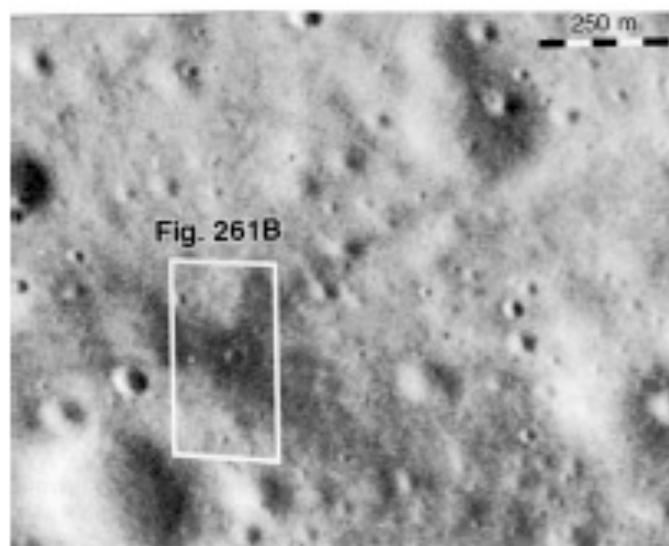
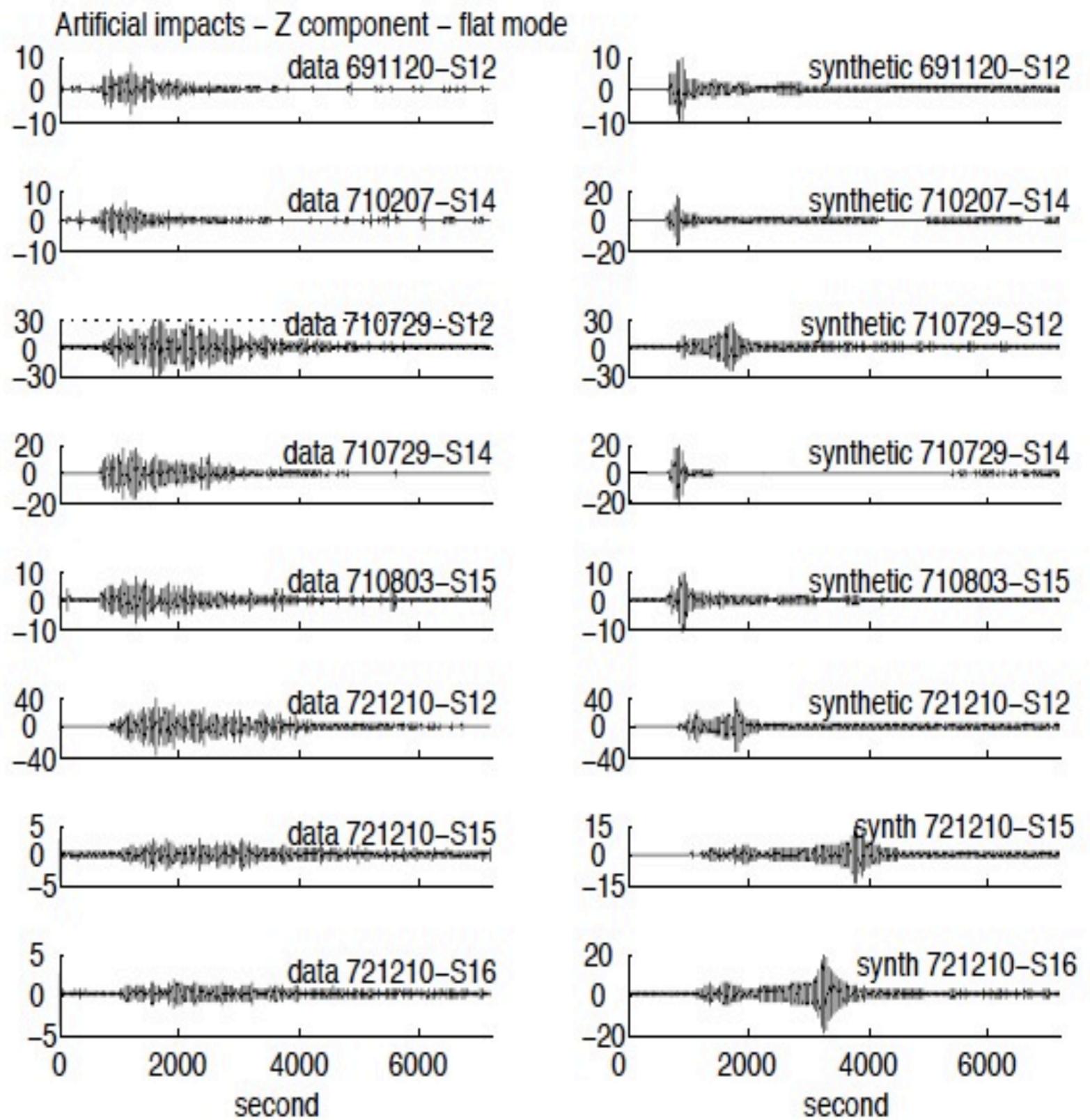
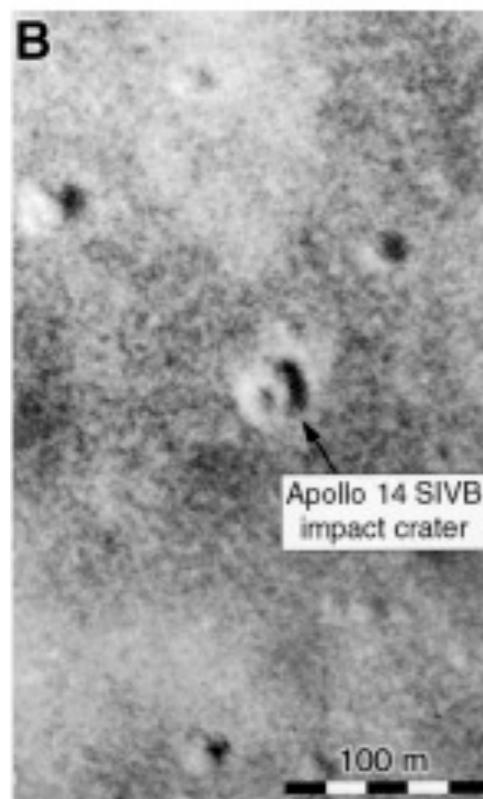
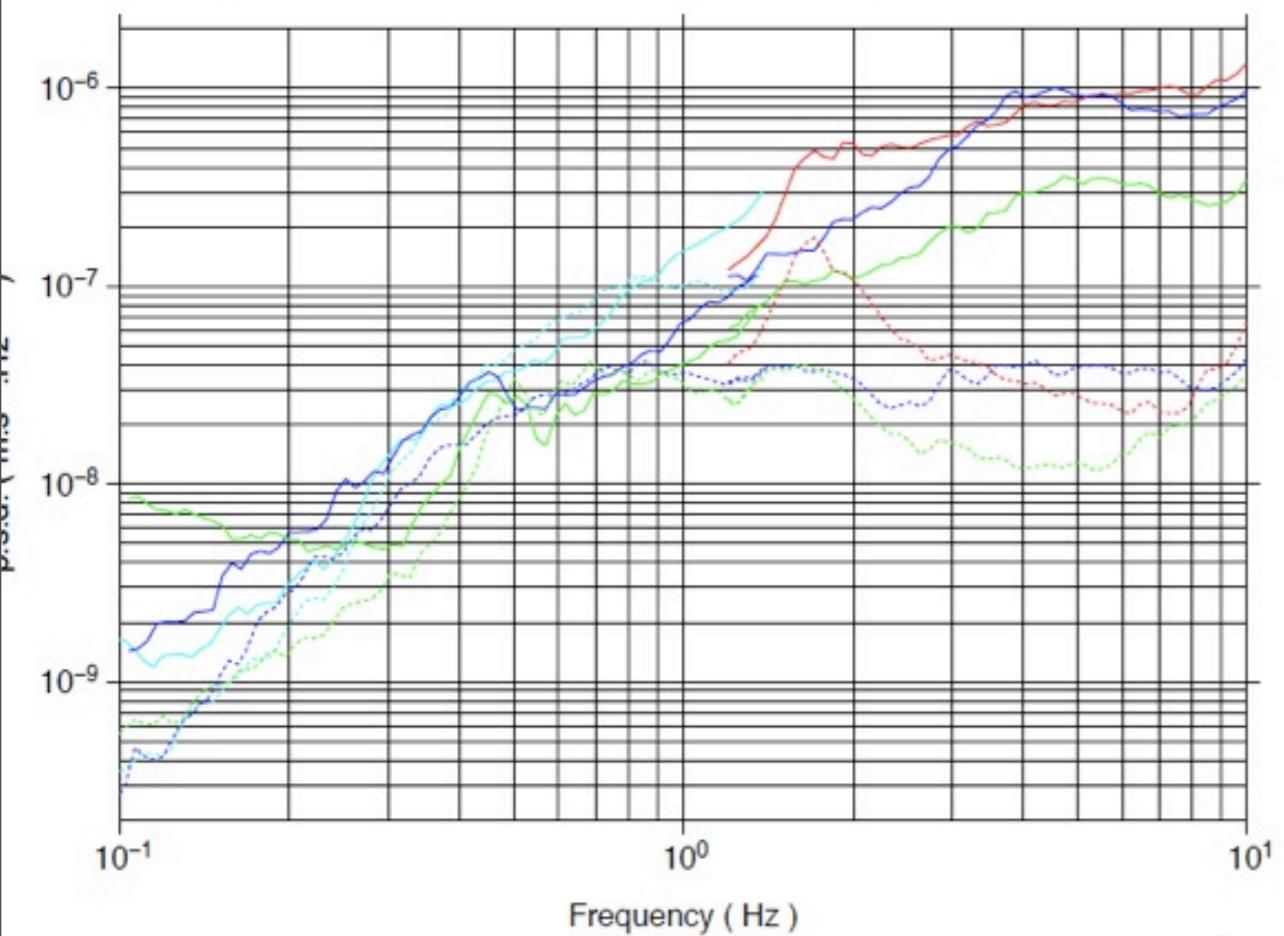


Fig. 1: Apollo 14 SIV/B impact site, images taken from [4]



Impacts

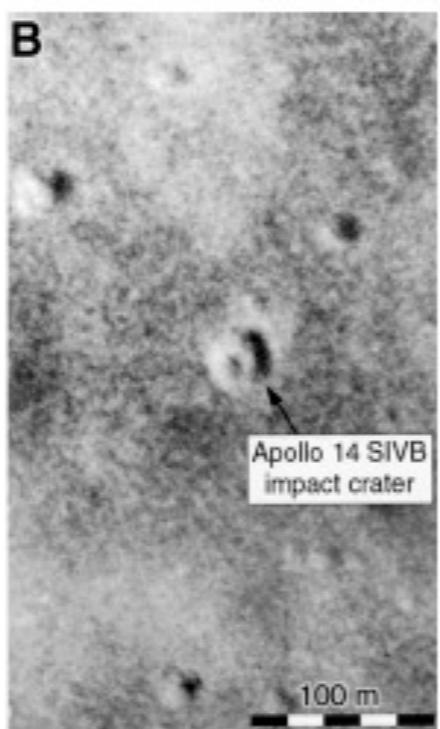


Meteorite Impact : 1976/11/14 23:13

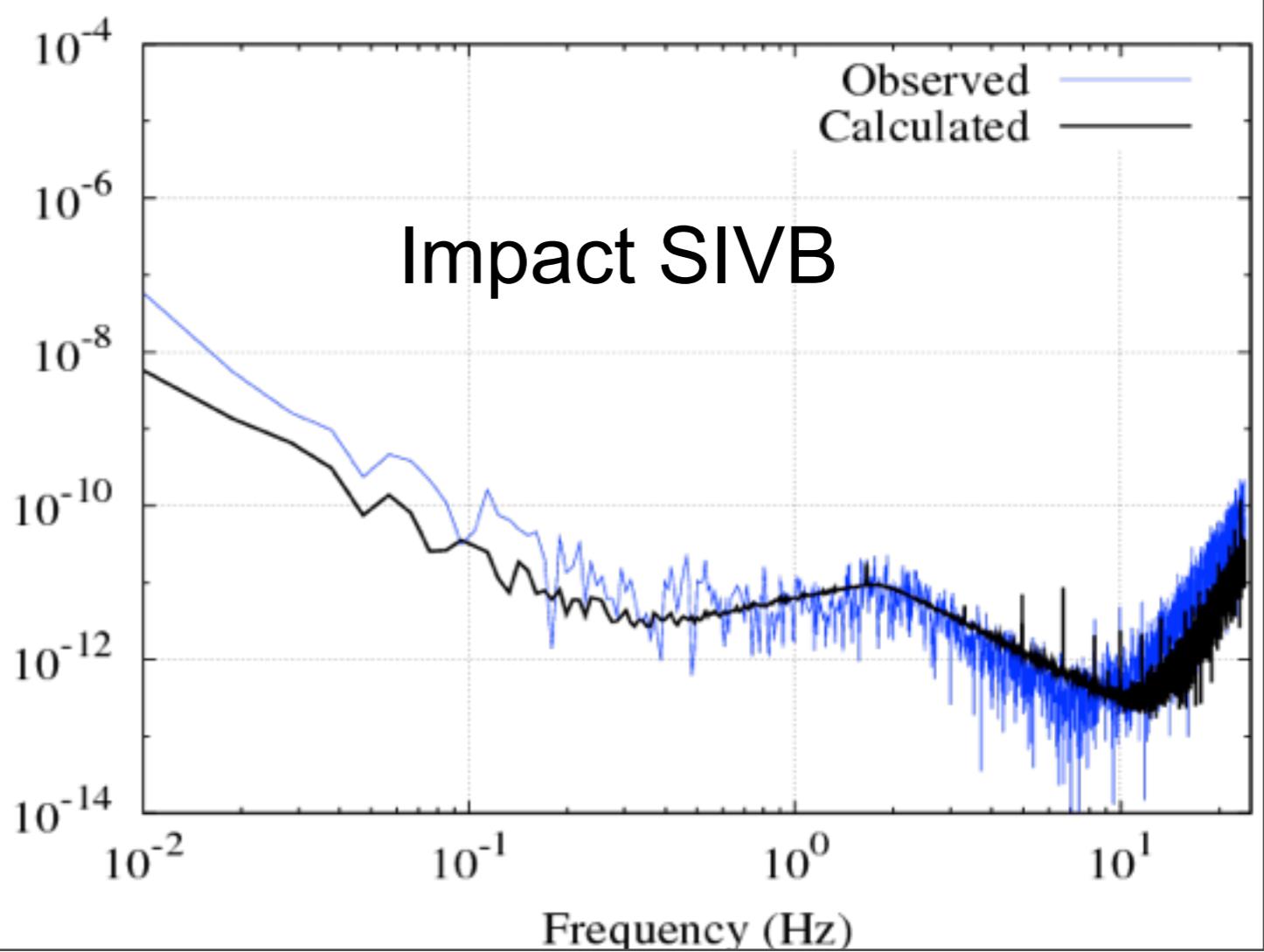
- S16z - 2300 km
- S16Z - 2300 km
- S15z - 2400 km
- S15Z - 2400 km
- S14z - 1850 km
- S12Z - 1700 km

Shallow Event : 1975/01/03 01:41

- S16z - 3300 km
- S16Z - 3300 km
- S15z - 2500 km
- S15Z - 2500 km
- S14z - 2350 km
- S12Z - 2200 km

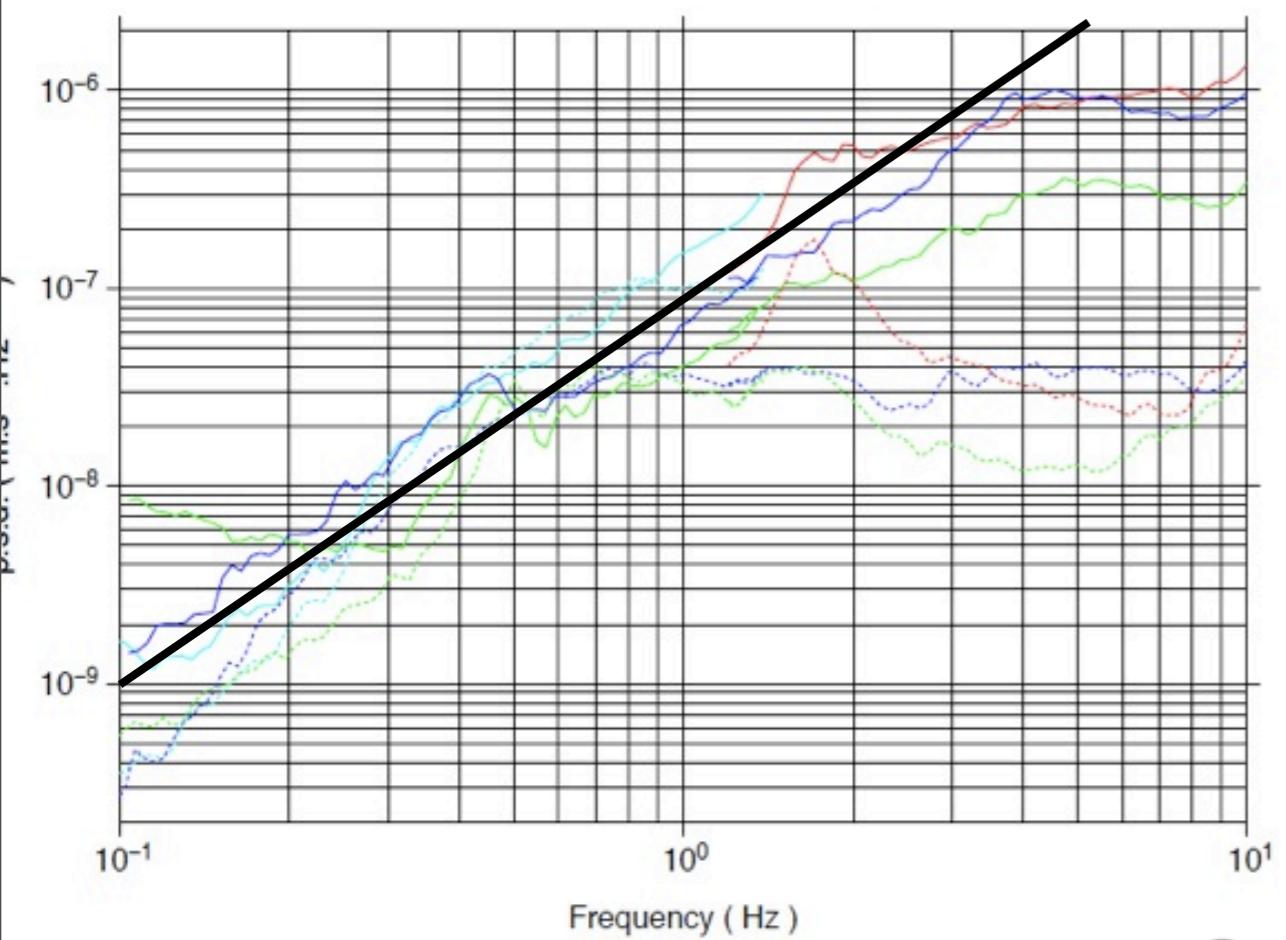


Power Spectrum ($\text{m}/\sqrt{\text{Hz}}$)



Impacts DO not generate high seismic frequencies!

Quake

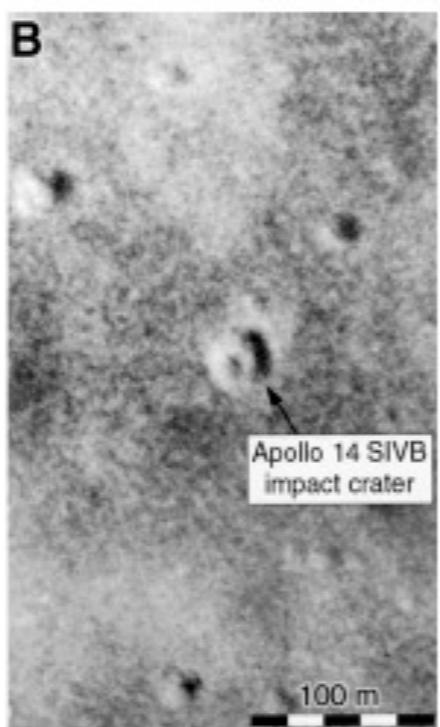


Meteorite Impact : 1976/11/14 23:13

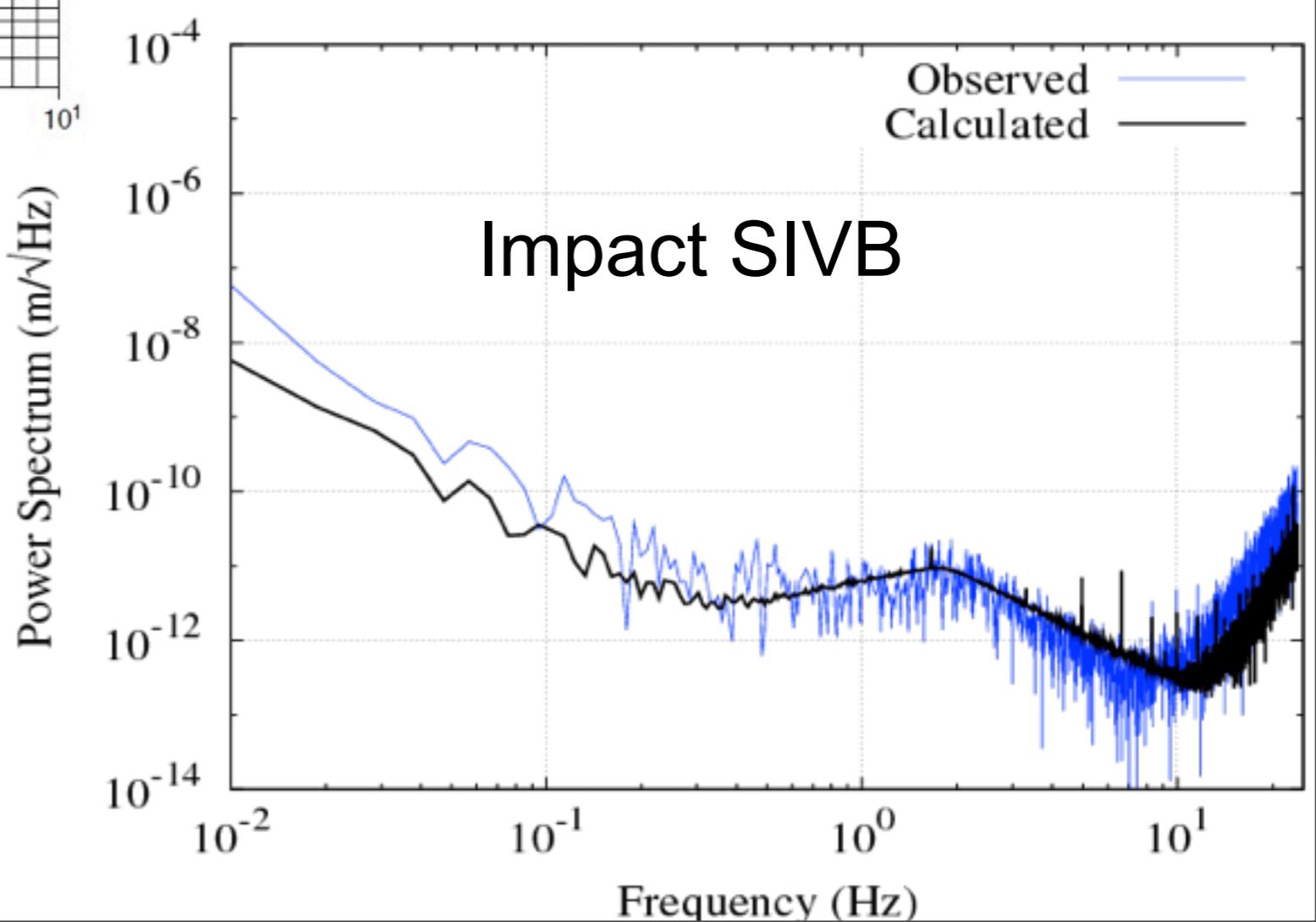
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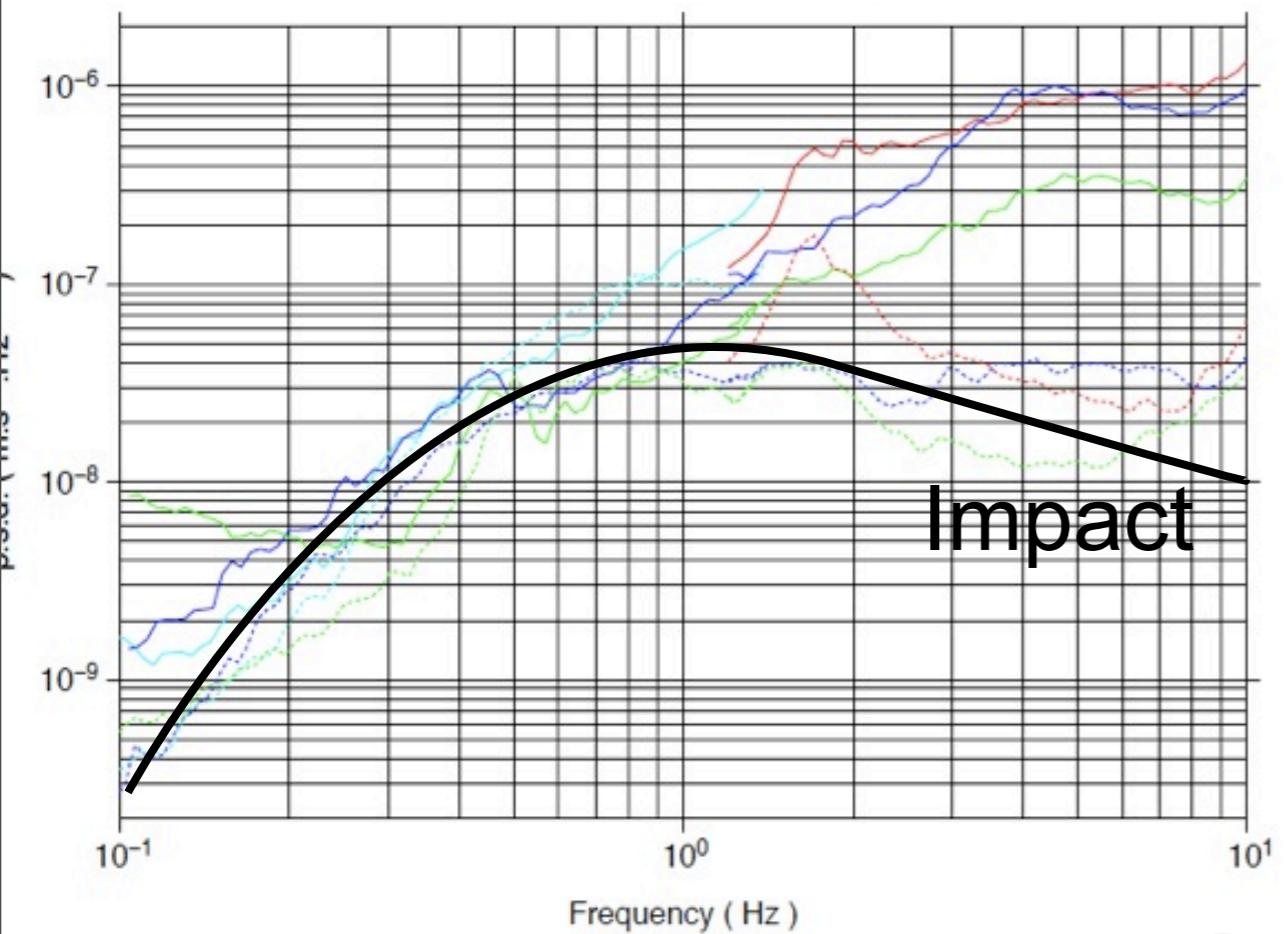


Impacts DO not generate high seismic frequencies!



Impact SIVB

Impacts

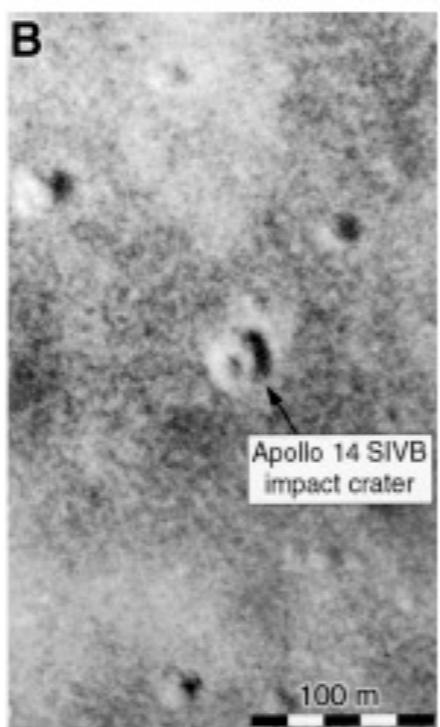


Meteorite Impact : 1976/11/14 23:13

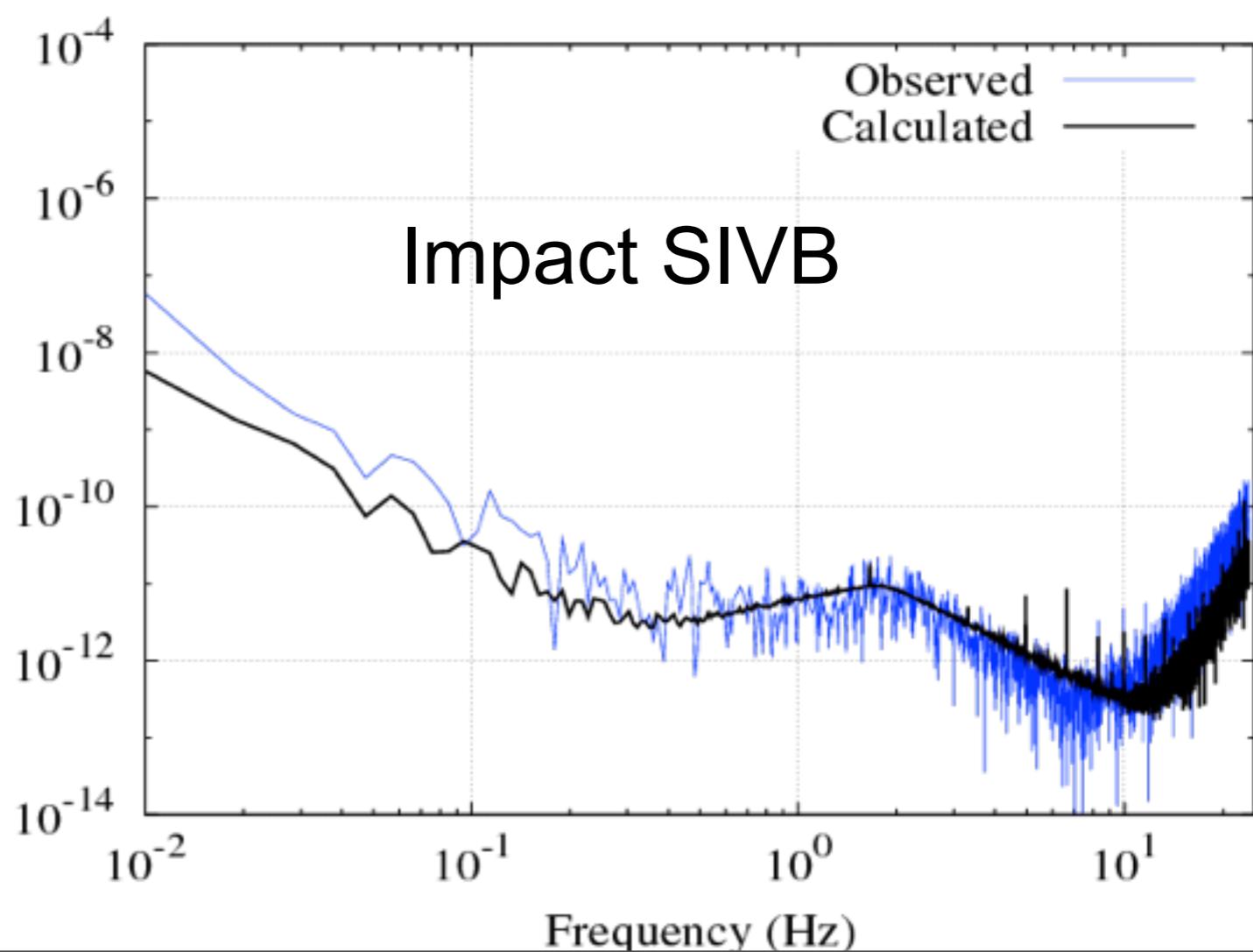
- S16z - 2300 km
- S16Z - 2300 km
- S15z - 2400 km
- S15Z - 2400 km
- S14z - 1850 km
- S12Z - 1700 km

Shallow Event : 1975/01/03 01:41

- S16z - 3300 km
- S16Z - 3300 km
- S15z - 2500 km
- S15Z - 2500 km
- S14z - 2350 km
- S12Z - 2200 km



Power Spectrum ($\text{m}/\sqrt{\text{Hz}}$)

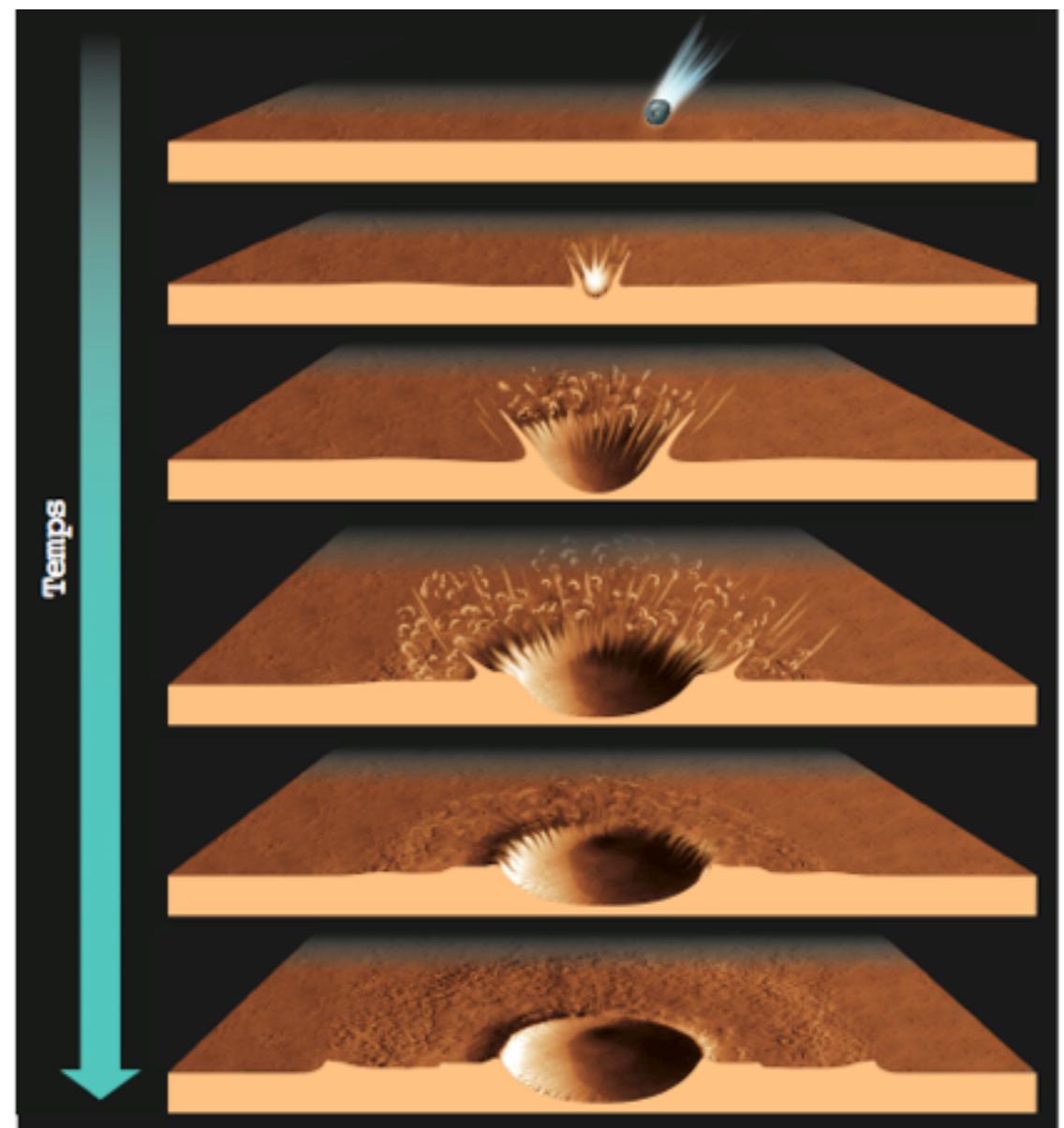


Impacts DO not generate high seismic frequencies!
Why?



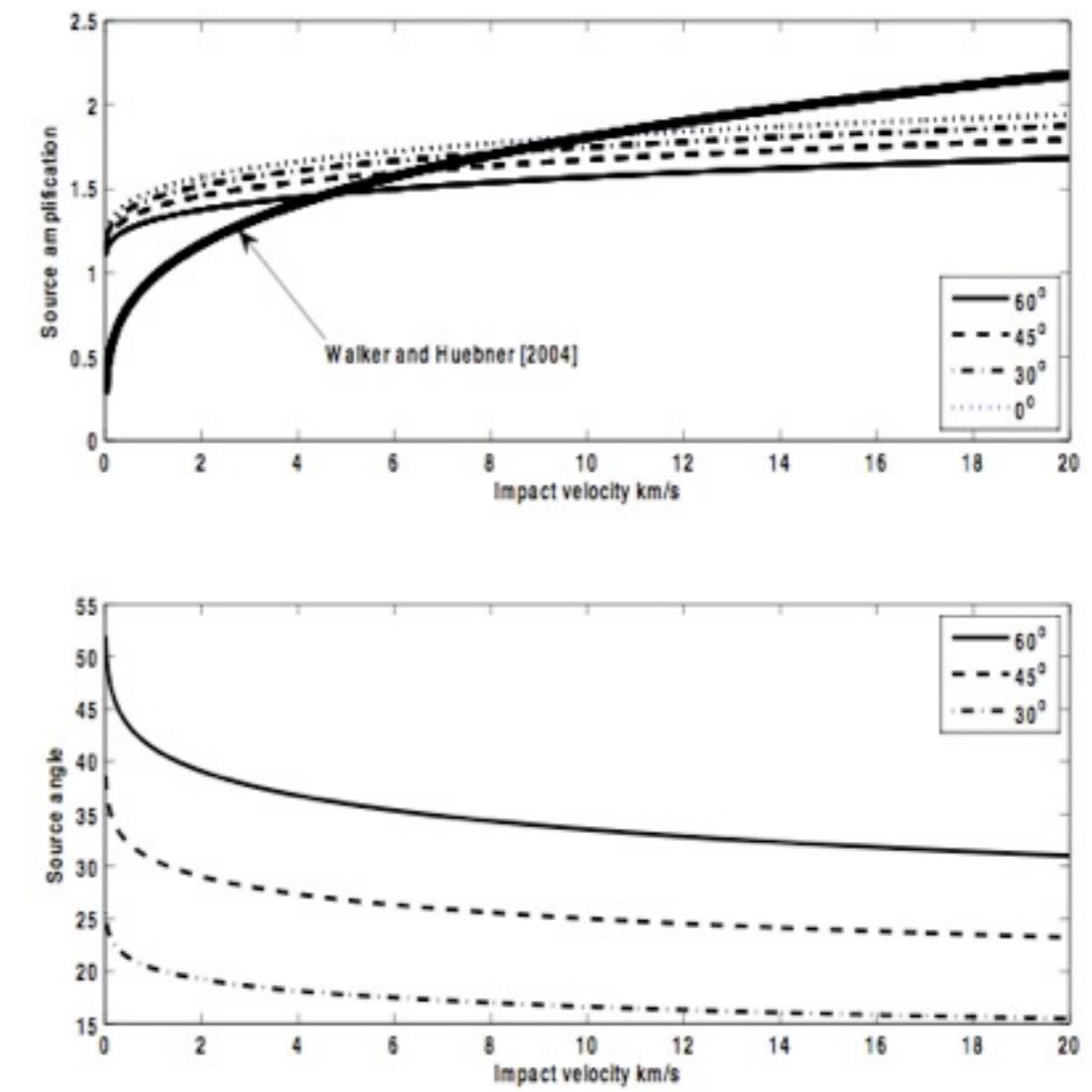
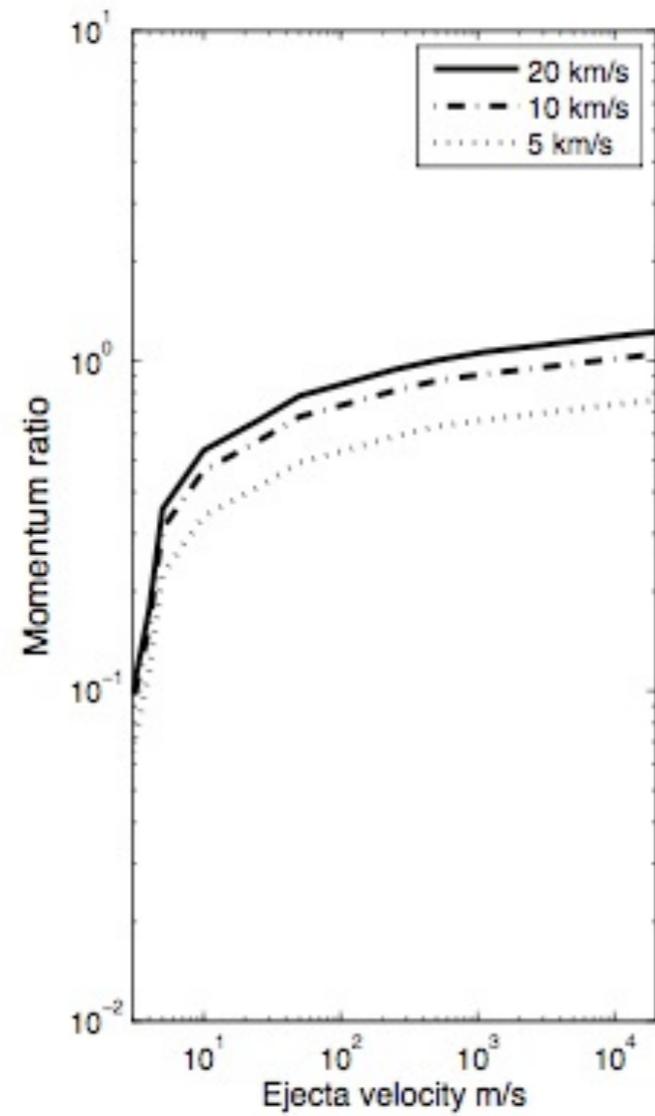
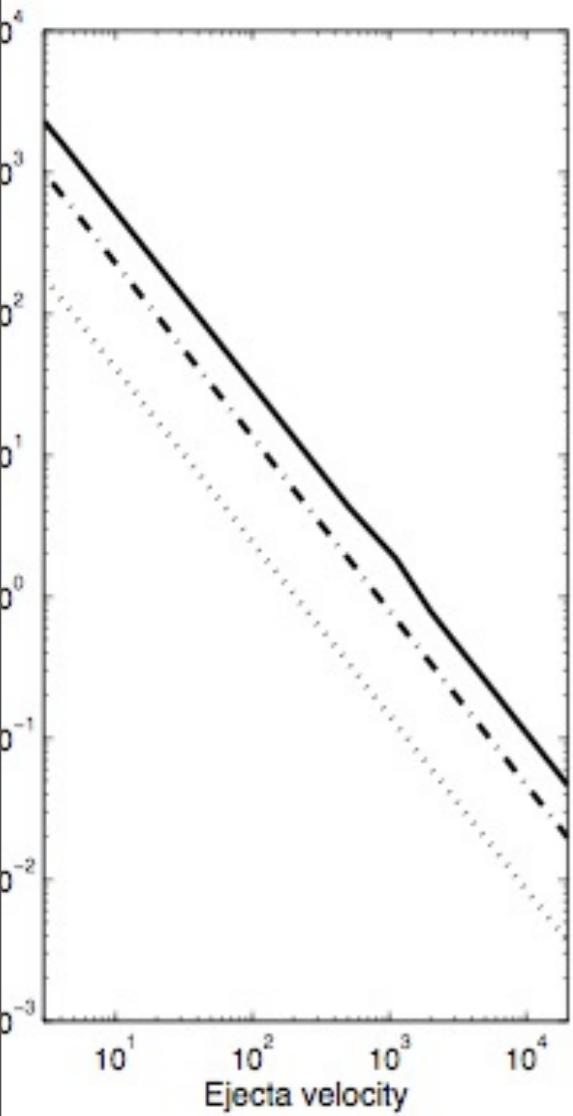
- Seismic source must take into account both the ejecta and the formation time of the crater
 - Ejecta mass are much larger than impactor mass
 - Momentum of the ejecta is significant and increase the force
 - Formation time leads to cutoff in the 1Hz-10hz range

$$\dot{f}_0(t) = \frac{\mathbf{r}}{r} (\mathbf{v} - \mathbf{p}_{eject}) \delta(t)$$
$$f(t) = f_0(t) * g(t)$$



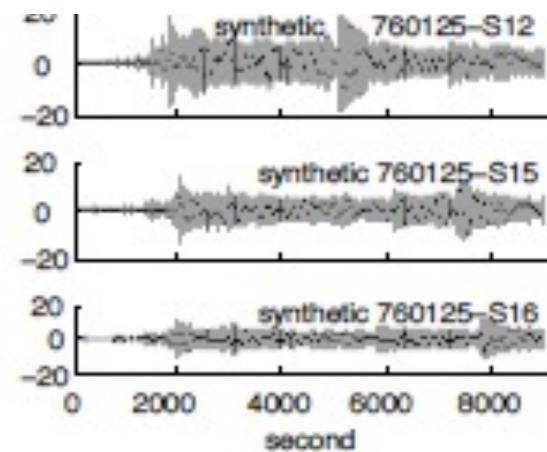
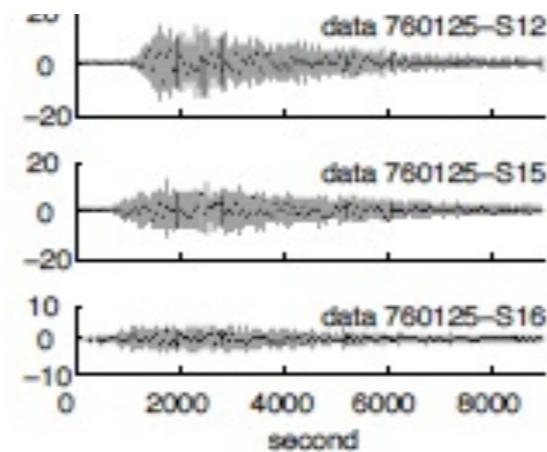
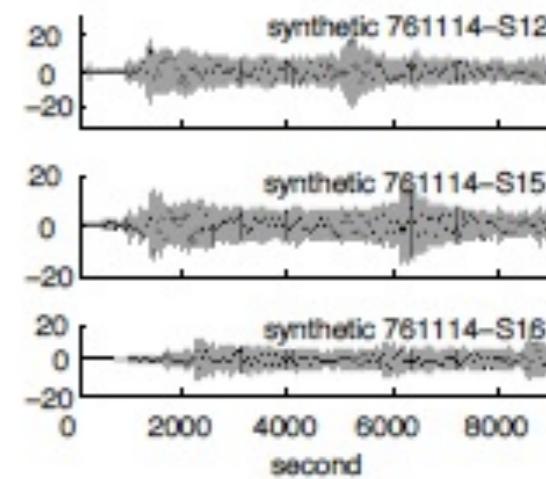
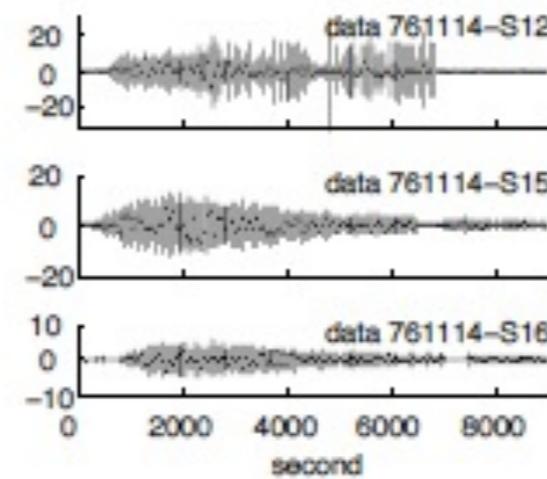
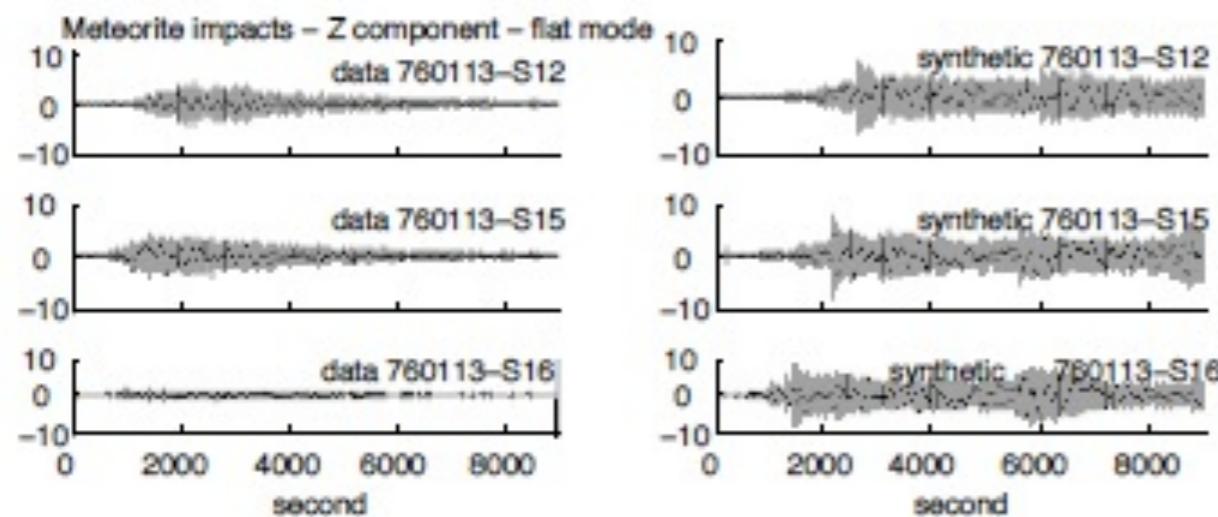


Ejecta amplification



Ejecta mass and momentum

Ejecta seismic amplification



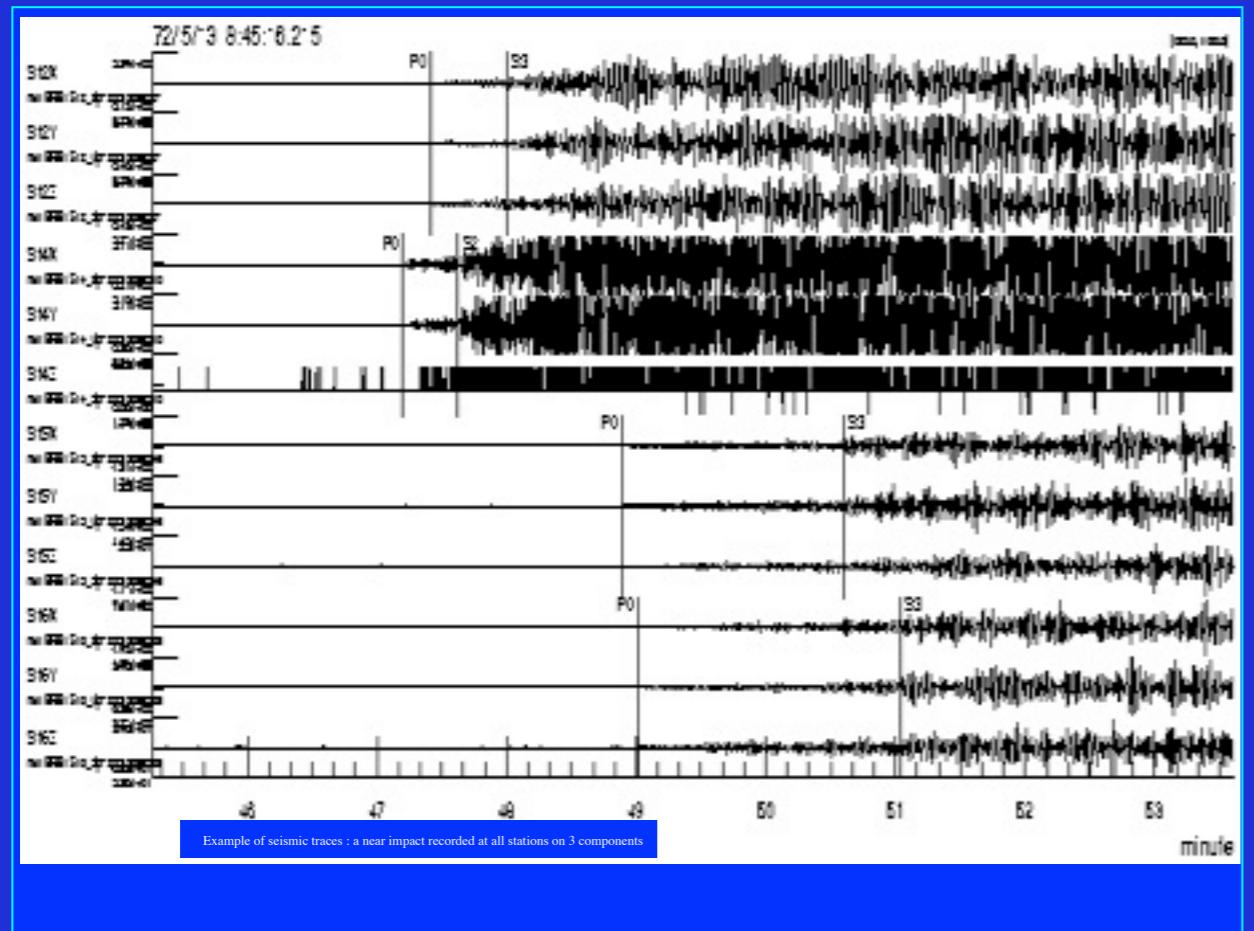
3 large impact

Date	I (kg m/s)	m_{VM} (kg m/s)	Mass (10^3 kg)	Diameter of meteoroids (m)	Crater diameter (m)	Crater depth (m)	Crater formation time (s)
13 Jan 1976	5×10^8	$(2.9-3.6) \times 10^8$	15-18	2.1-2.3	52-62	14-17	3.0-3.3
25 Jan 1976	8×10^8	$(4.7-5.7) \times 10^8$	24-29	2.5-2.6	60-70	16-19	3.2-3.5
14 Nov 1976	9×10^8	$(5.3-6.4) \times 10^8$	27-32	2.6-2.7	61-73	17-20	3.3-3.6

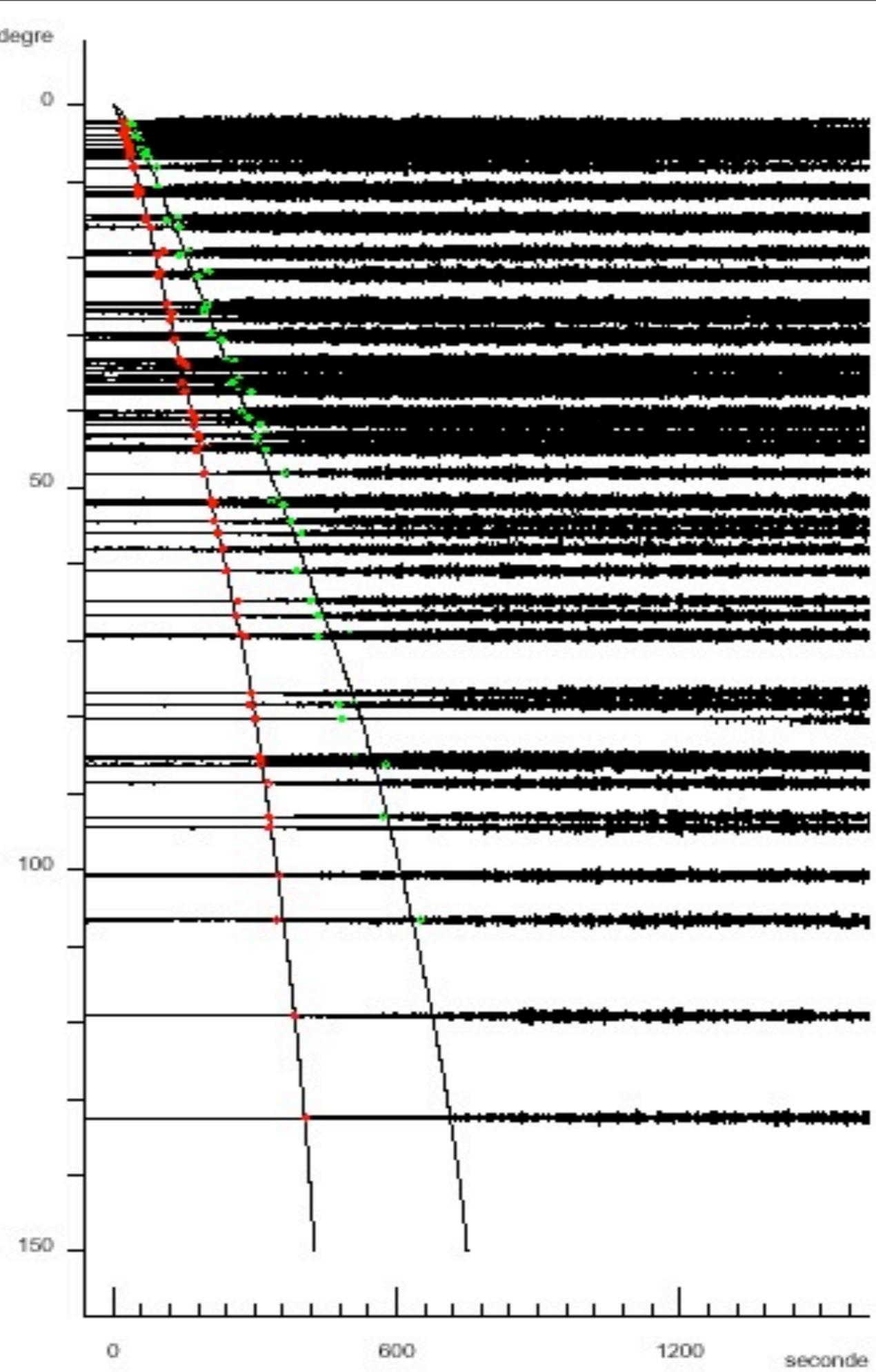
What can be done?

- Like on Earth?
- Interior models with travel times to invert
 - crust
 - mantle
 - core
 - 3D lateral variation, tomography....

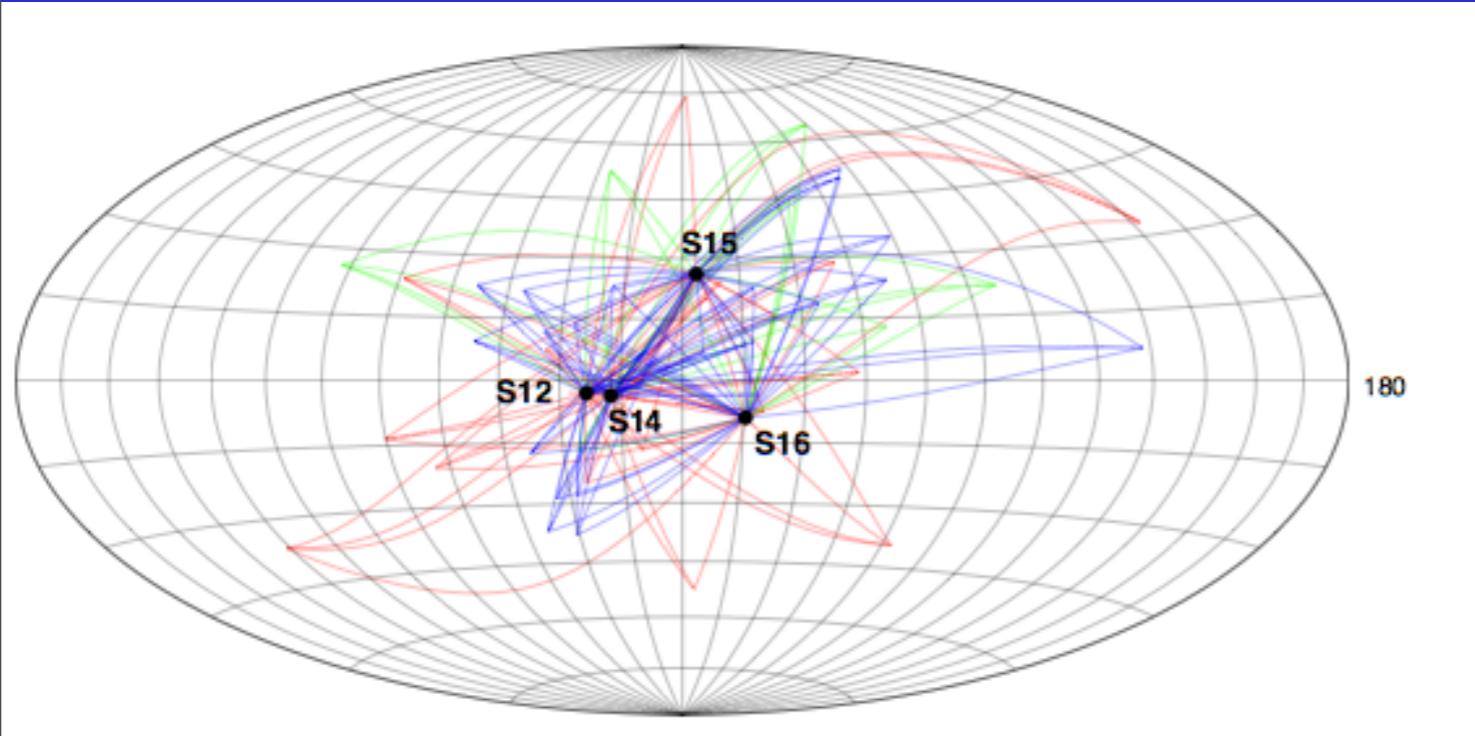
Example of arrival time determination



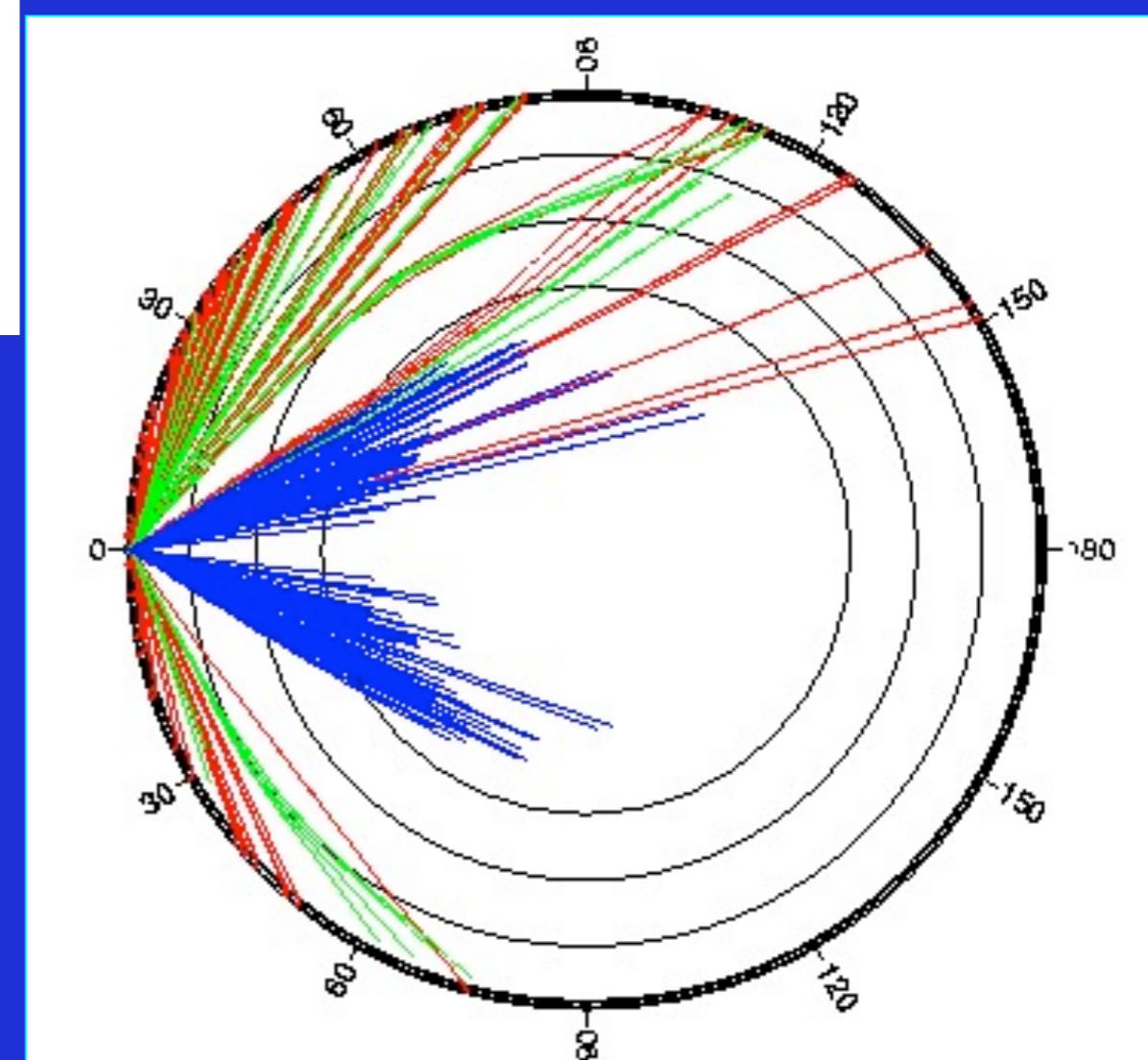
- In many cases, diffraction is making the determination of arrival times difficult, with error up to 10sec (mean error is about 2s)



Rays sampling



- recording events with different epicentral distances give access to the structure with depth
- the inverted model is however not a mean model of the planet, but a mean model of the area where the network is deployed



All ray paths available in the Moon. Blue is for deep events, red for impacts, green for superficial moonquakes.

Principle of the inversion

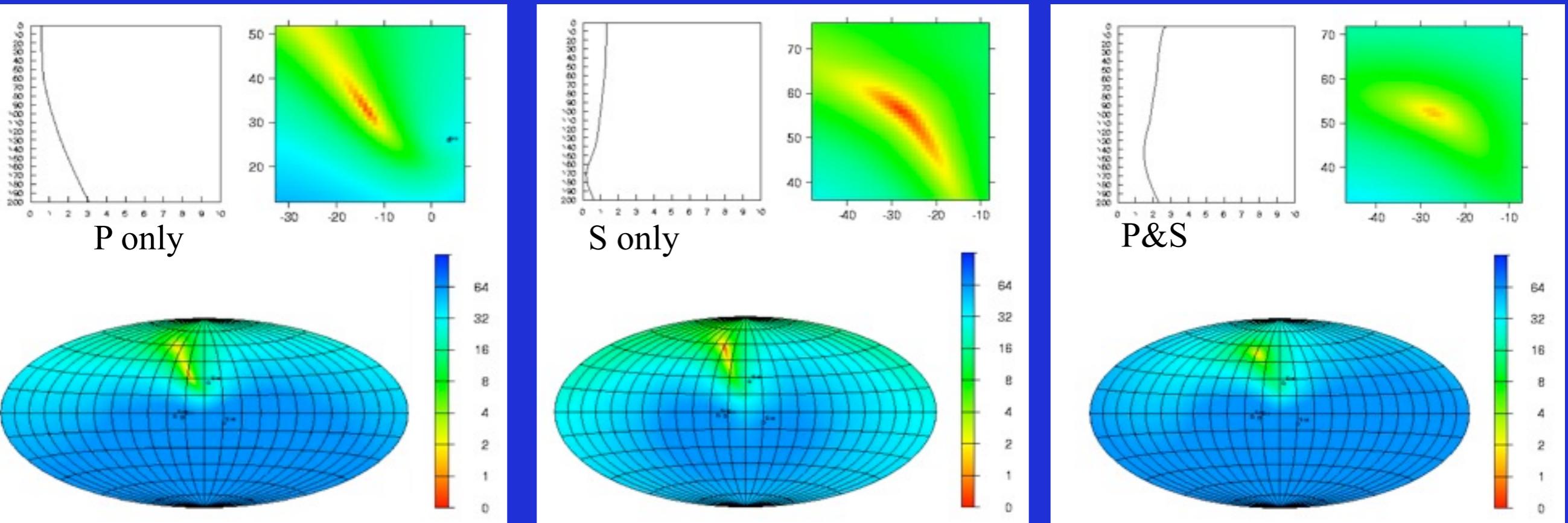
Seismic data,
i.e. arrival
times at the
stations

Source
parameters,
i.e. position
and times of
the quakes

Model
parameters,
i.e. P and S
seismic
velocities
with depth

Sources relocation

- Source localisation is done iteratively in the inversion: for each new structure new model, a new localisation of the sources is done and then used for next inversion of structure



Principle of the inversion

Seismic data,
i.e. arrival
times at the
stations

$N \times 6$

Source
parameters,
i.e. position
and times of
the quakes

$N \times 4$

Model
parameters,
i.e. P and S
seismic
velocities
with depth

$< 2N$

- N is the number of quakes
- The seismic model must
 - be limited to depth seen by the seismic rays
 - if errors are high, an oversampling is mandatory to reduce the impact of errors on the data
- Number of layers with V_p and V_s inverted is therefore $N_l \ll N$

Inversion in the Appolo case

Seismic data,
i.e. arrival
times at the
stations

Nx6

Source
parameters,
i.e. position
and times of
the quakes

Nx4

Model
parameters,
i.e. P and S
seismic
velocities
with depth

< 2N

- Practically, in total 319 P & S arrival time data where used to constrains 59 seismic sources, including 185 source parameters and 134 degree of freedom available for internal structure
- Mean error is 2 sec for arrival times

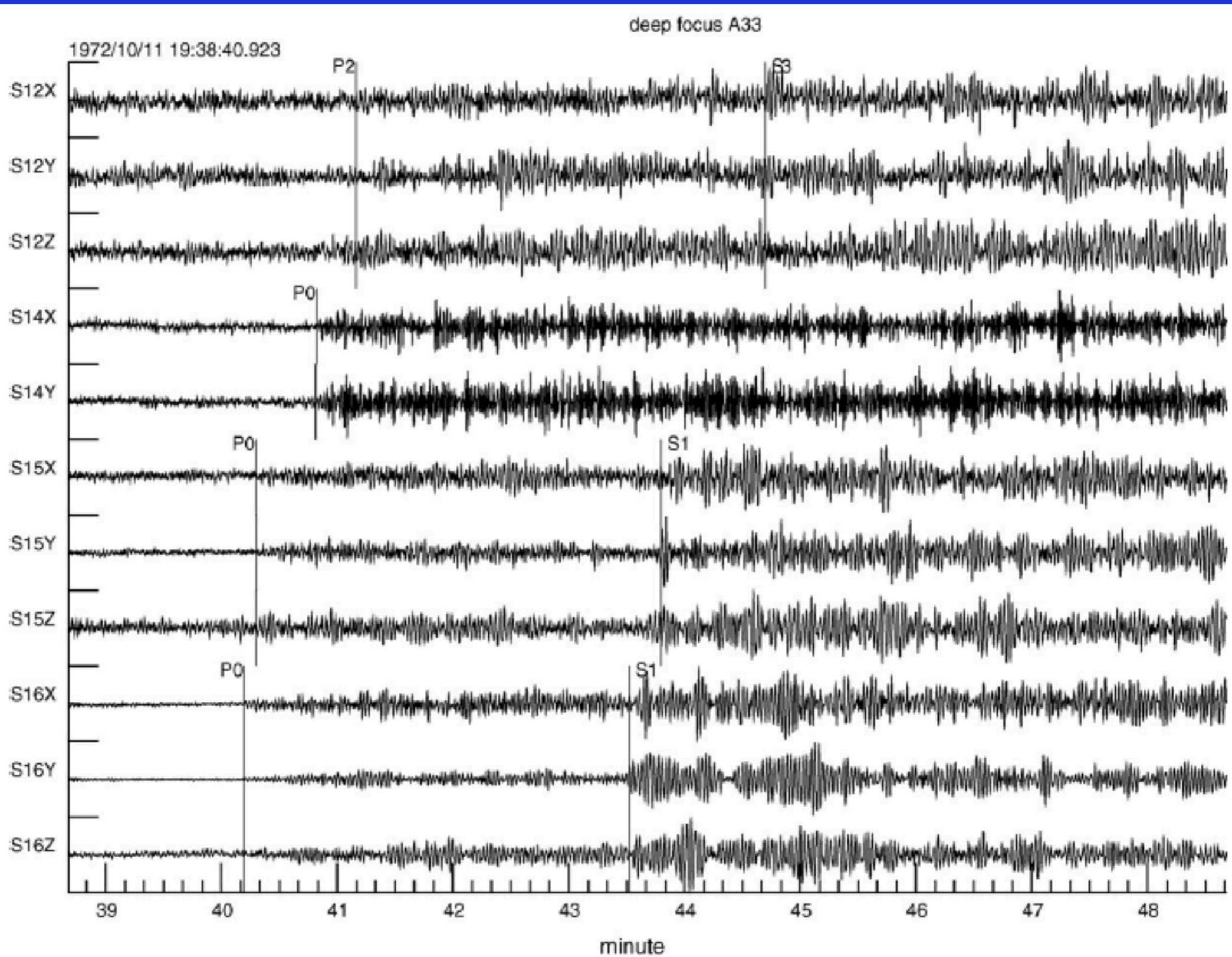
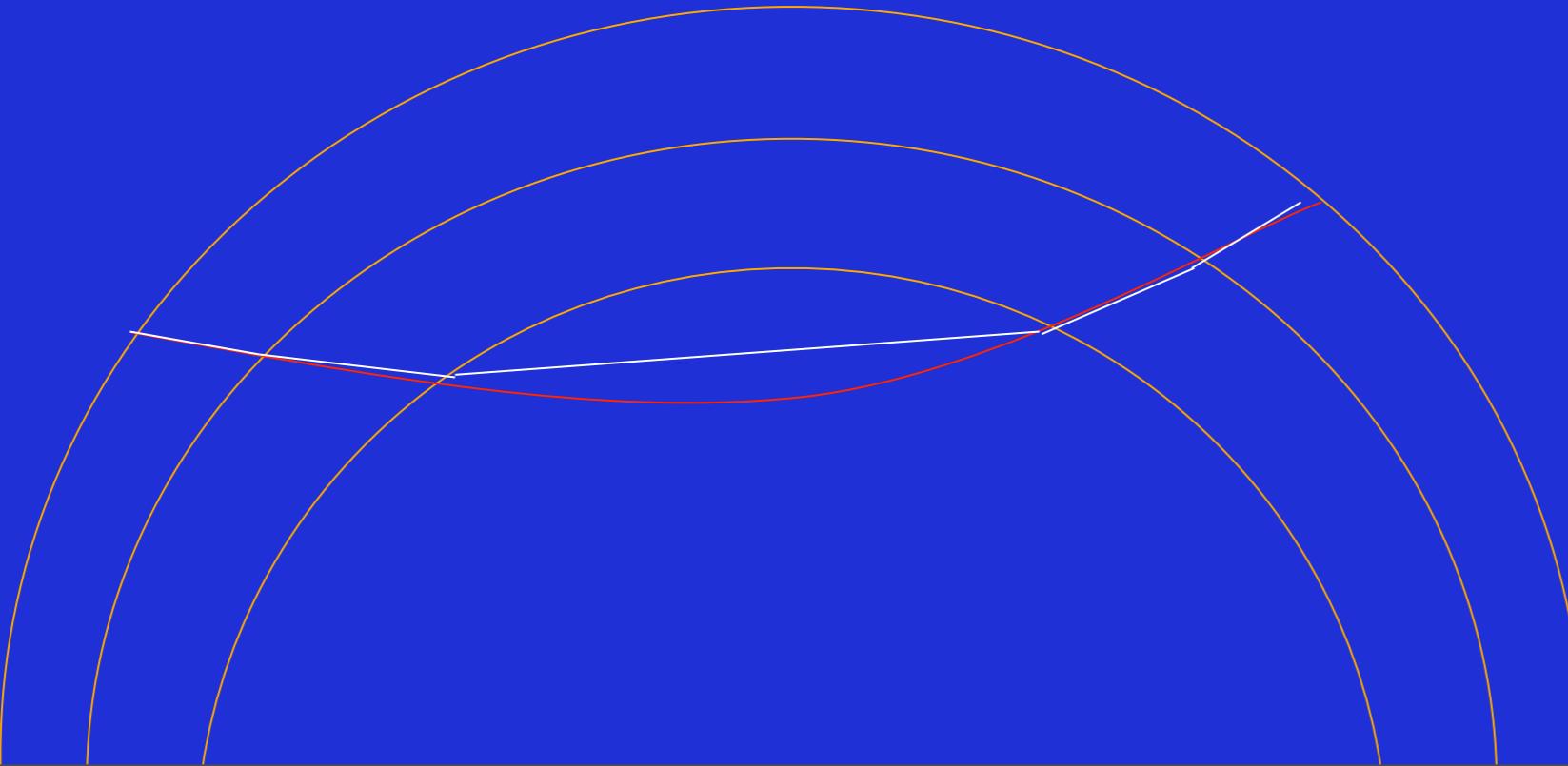
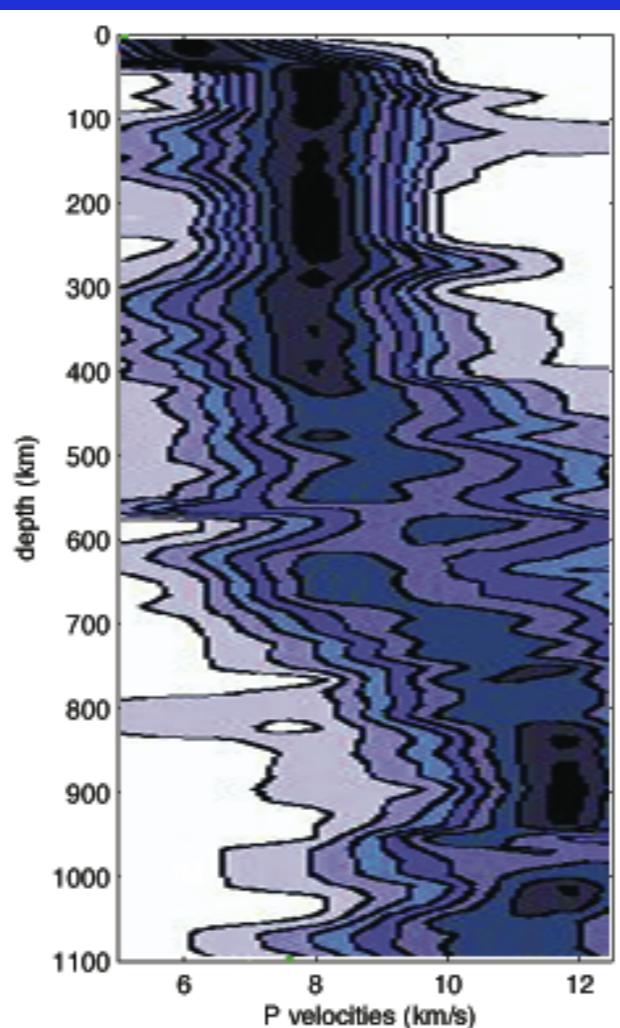
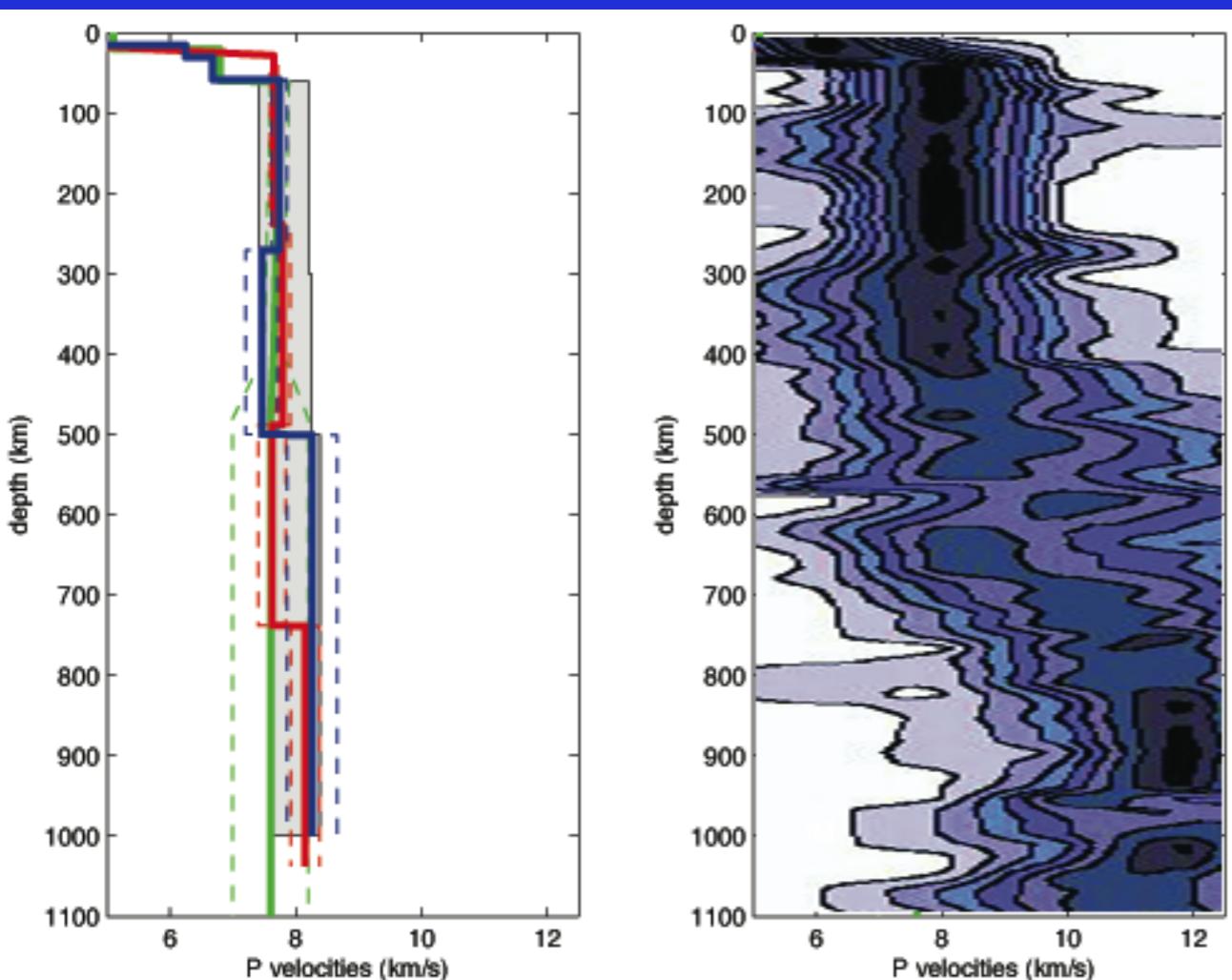


Fig. 3. Example of arrival time pickings for deep focus A33. The index 0, 1, 2 and 3 correspond respectively to uncertainty about 1, 3, 10, 30 s.

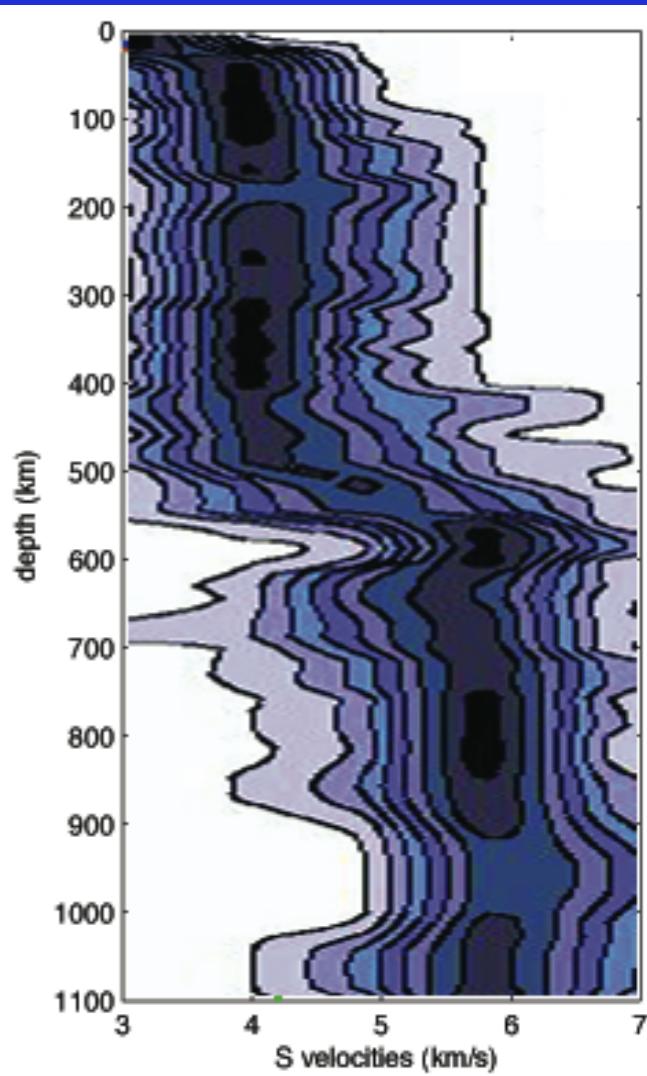
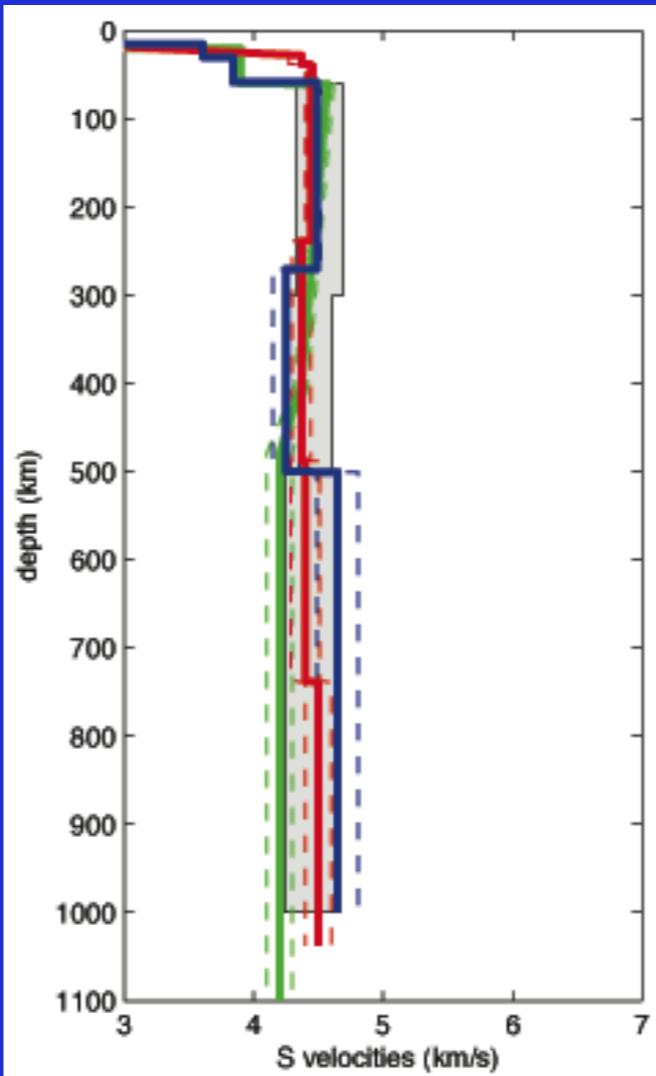
-
- 2 possible inversion strategy
 - Inversion with a limited number of layers (typically about 5-10)
 - Inverted parameters are not the true velocities but the mean velocities in a layer
 - Some error is done in the theory
 - When $s_{\text{data}} > s_{\text{theory}}$, the error on the inverted models is improved
 - Inversion with a large number of layers (typically 50)
 - Inverted velocities have error directly related to the mean quality of data



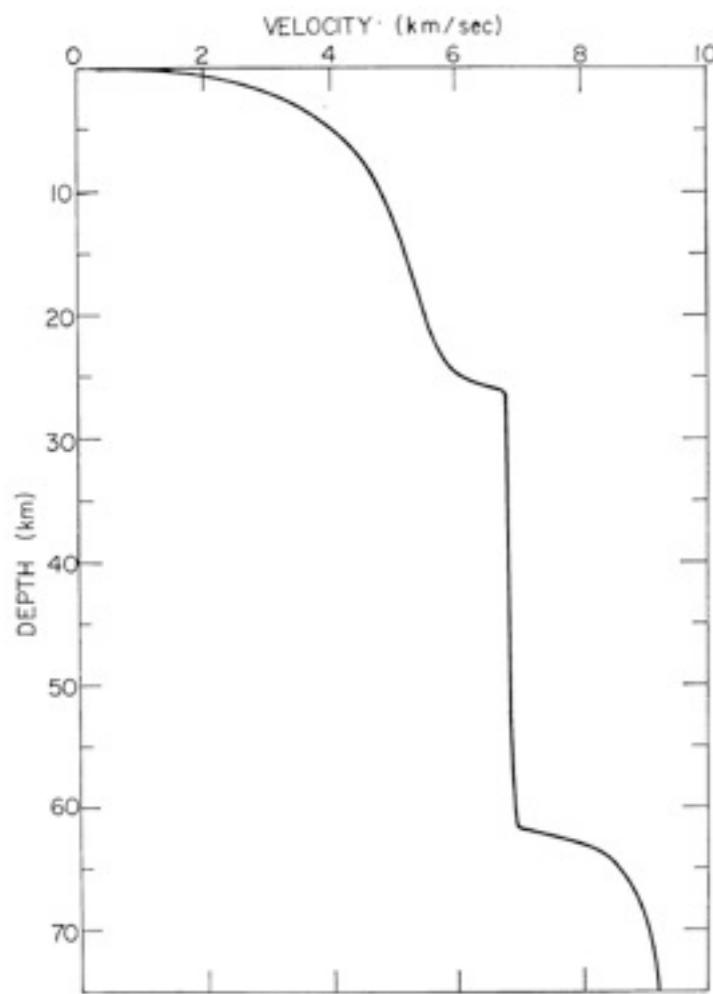
Inversion results



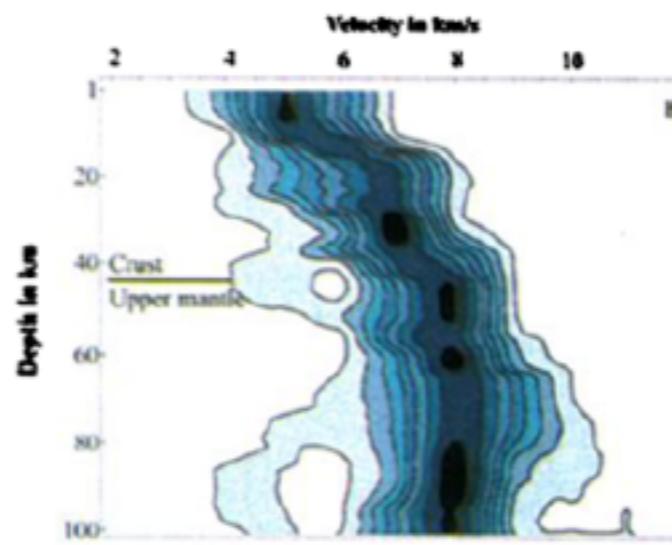
- right: highly layered model (Khan et al., 2000, 2002)
- left: weakly layered model (Lognonné et al., 2003)



Results: Thickness of the crust

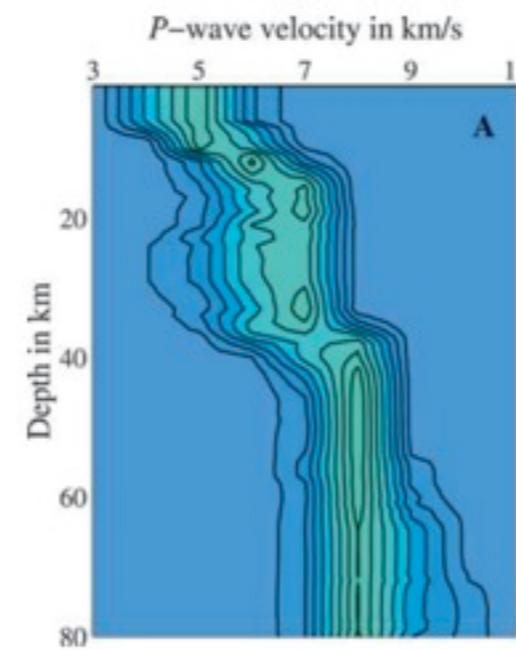


Toksöz et al. (1972)
~60 km



Khan et al (2000)

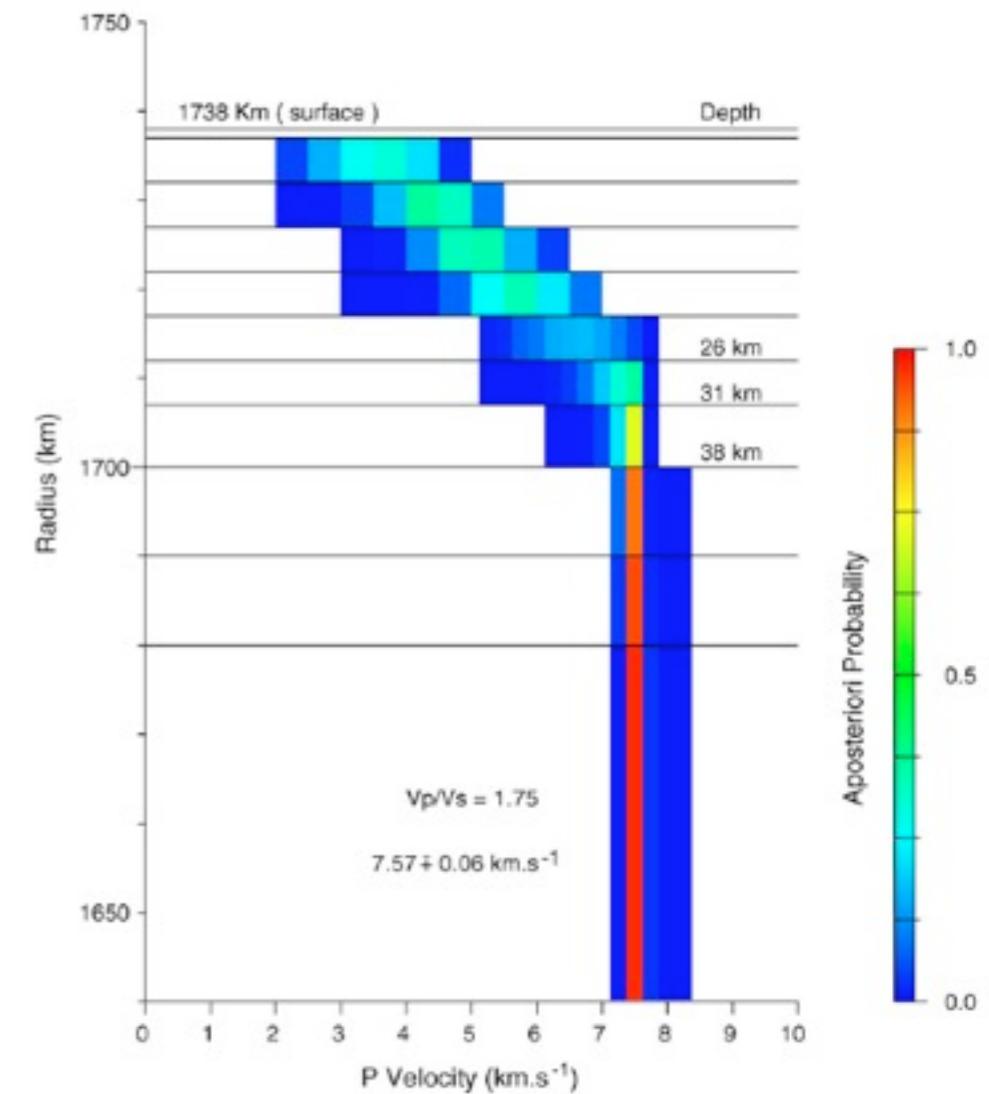
45 ± 5 km



Khan and Mosegaard
(2002)

38 ± 3 km

Each study used different seismic events, seismic arrival times and analysis techniques... and thickness do not always fit the gravity one

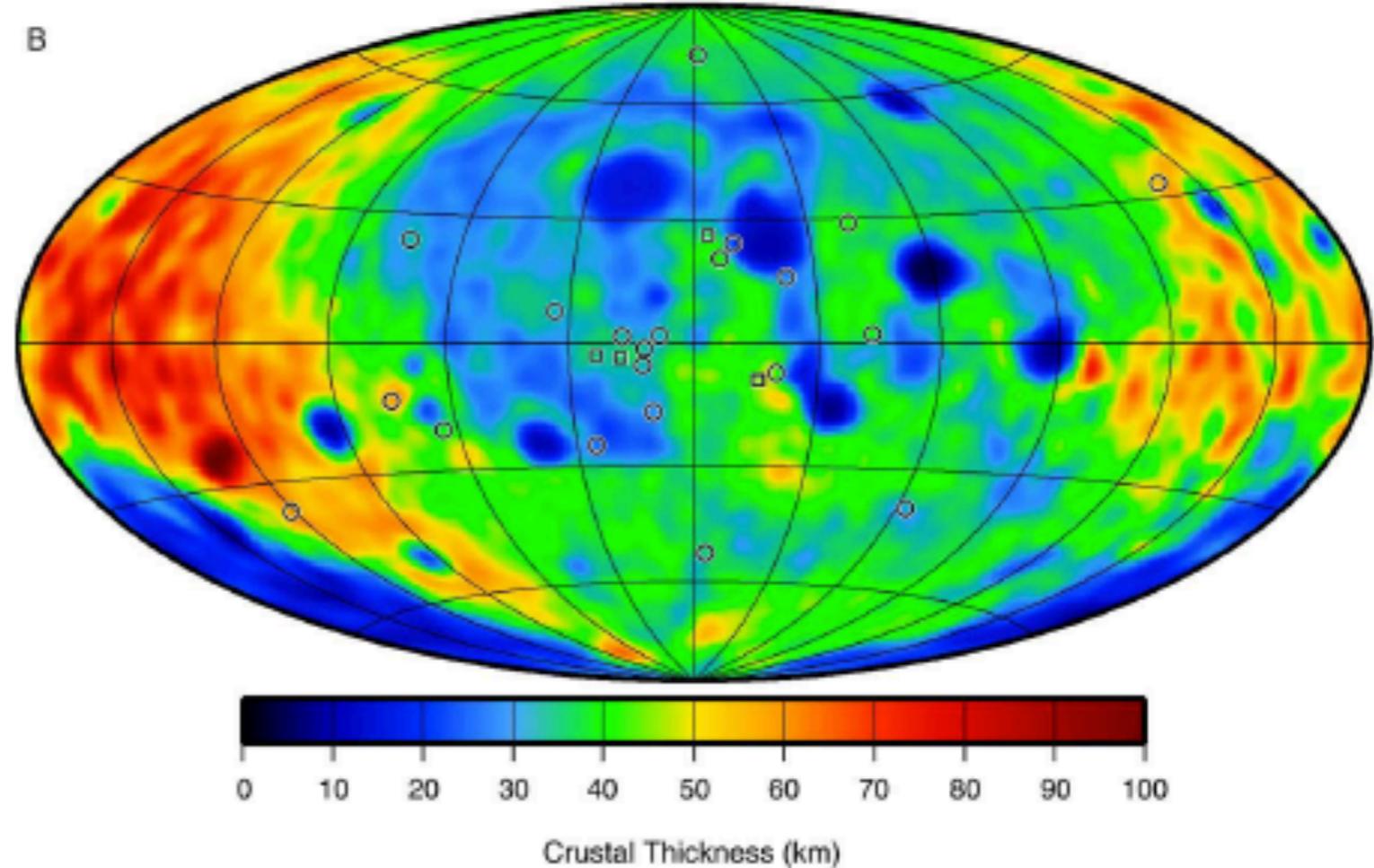
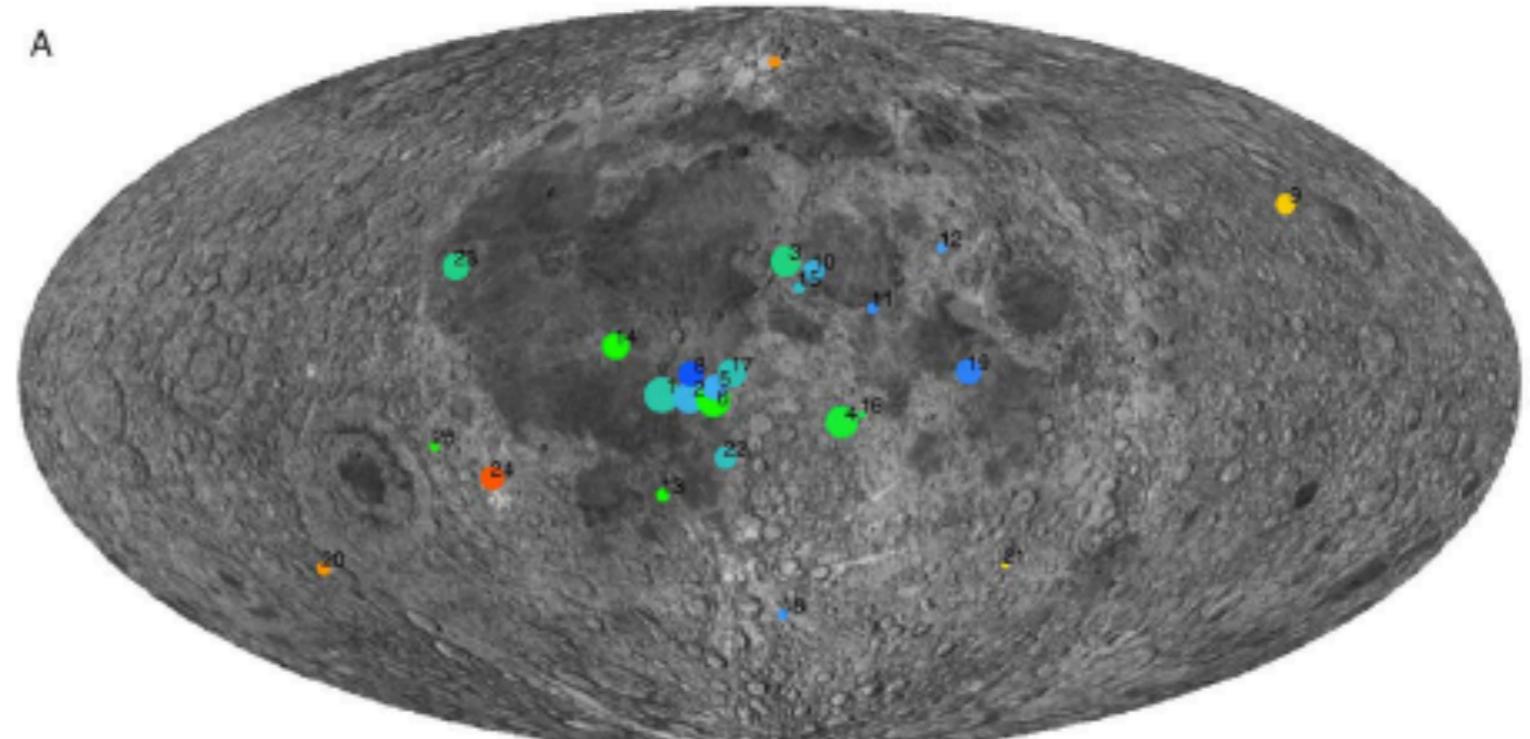
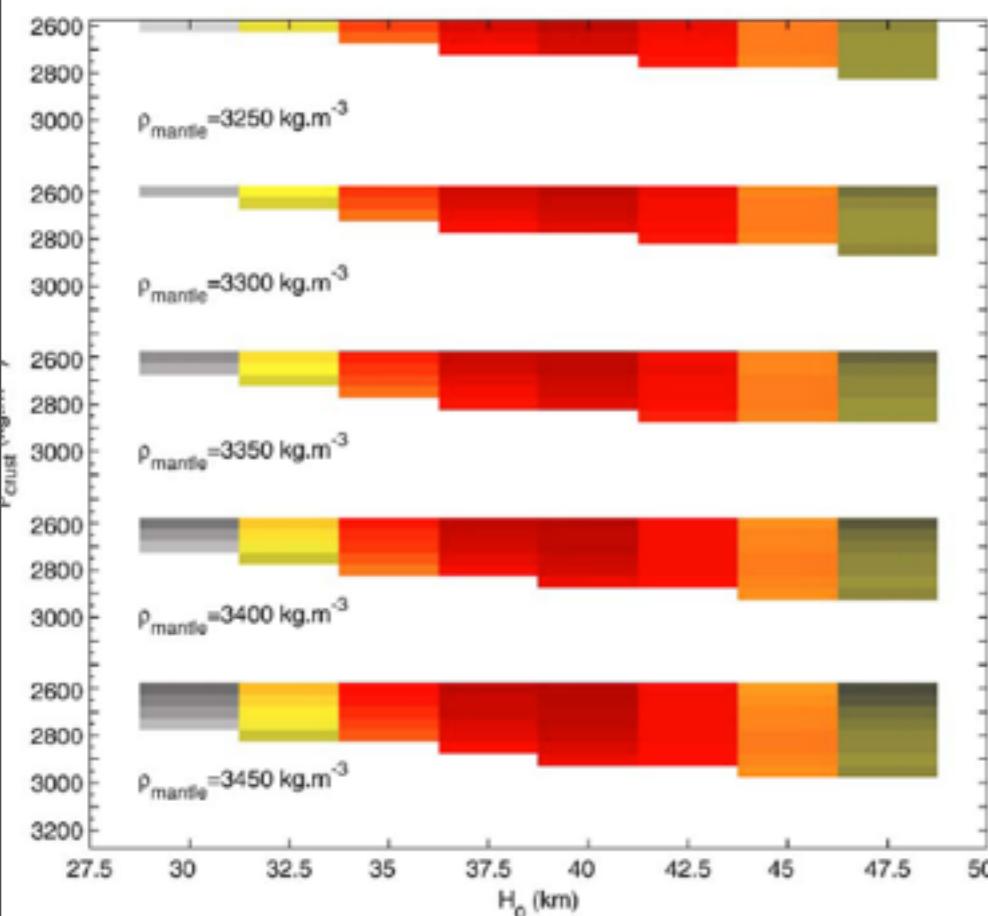


Lognonné et al. (2003)
 30 ± 3 km

Joint crustal inversion: gravity plus seismic

Chenet et al (2006)

$40 \pm 5 \text{ km}$



Why so much differences?

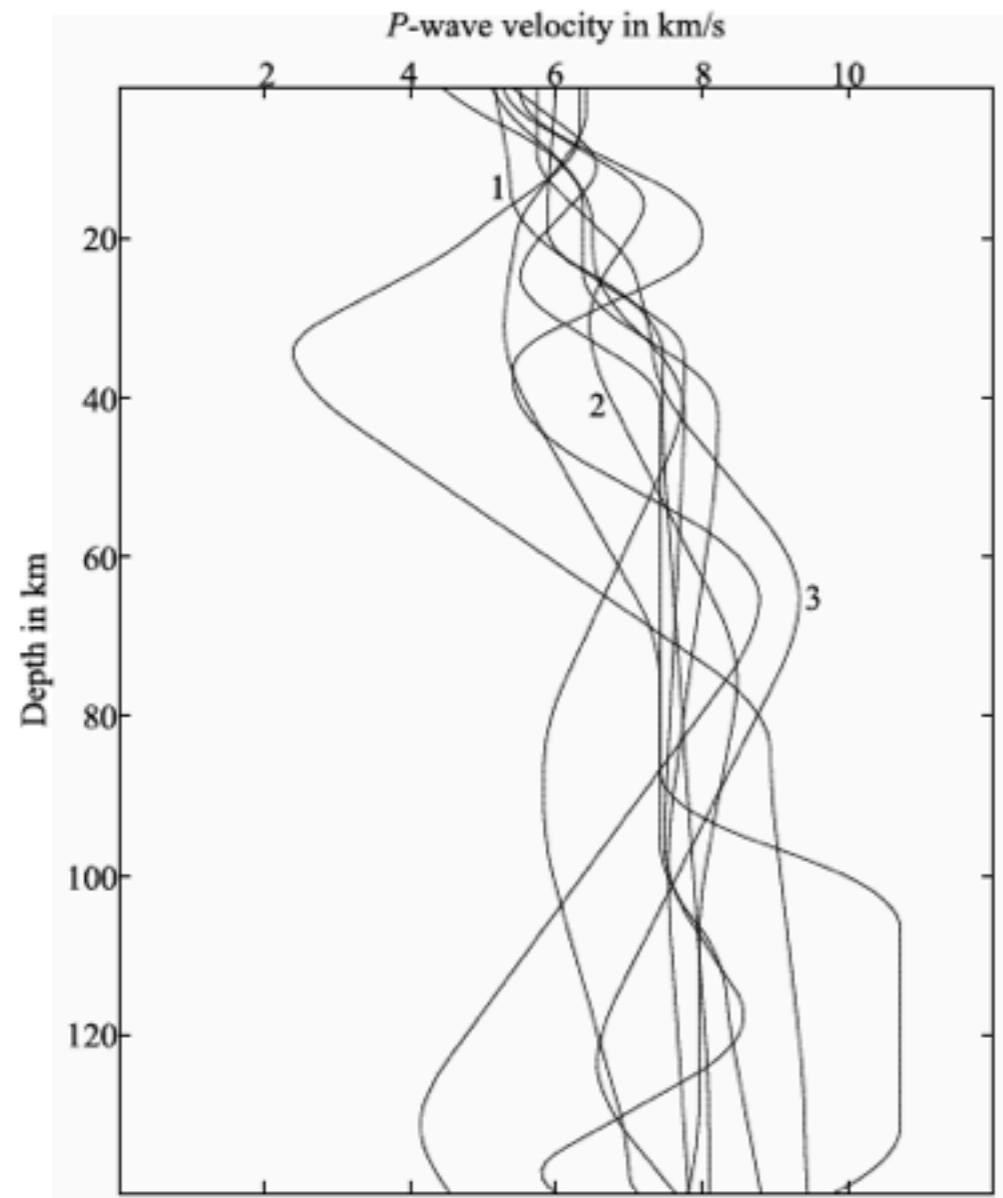


Figure 5. A smoothed version of 10 samples from the posterior distribution, each one obtained by sampling a different extremum in the model space. The models shown here emphasize only the crustal and upper mantle part. The three models numbered 1–3 have been taken as examples of models which individually highlight seemingly different structures but nonetheless are models that all produce a fairly large likelihood value, that is, produce a good fit to the observed data (see Table 1).

- seismology is mainly sensitive to the travel times, which means integration of the slowness along ray
- gravity does not constrain the mean crustal thickness if the mass of the mantle is not known
- gravity lateral variation is to first order sensitive to the surface density

Khan et al, 2002

Real differences?

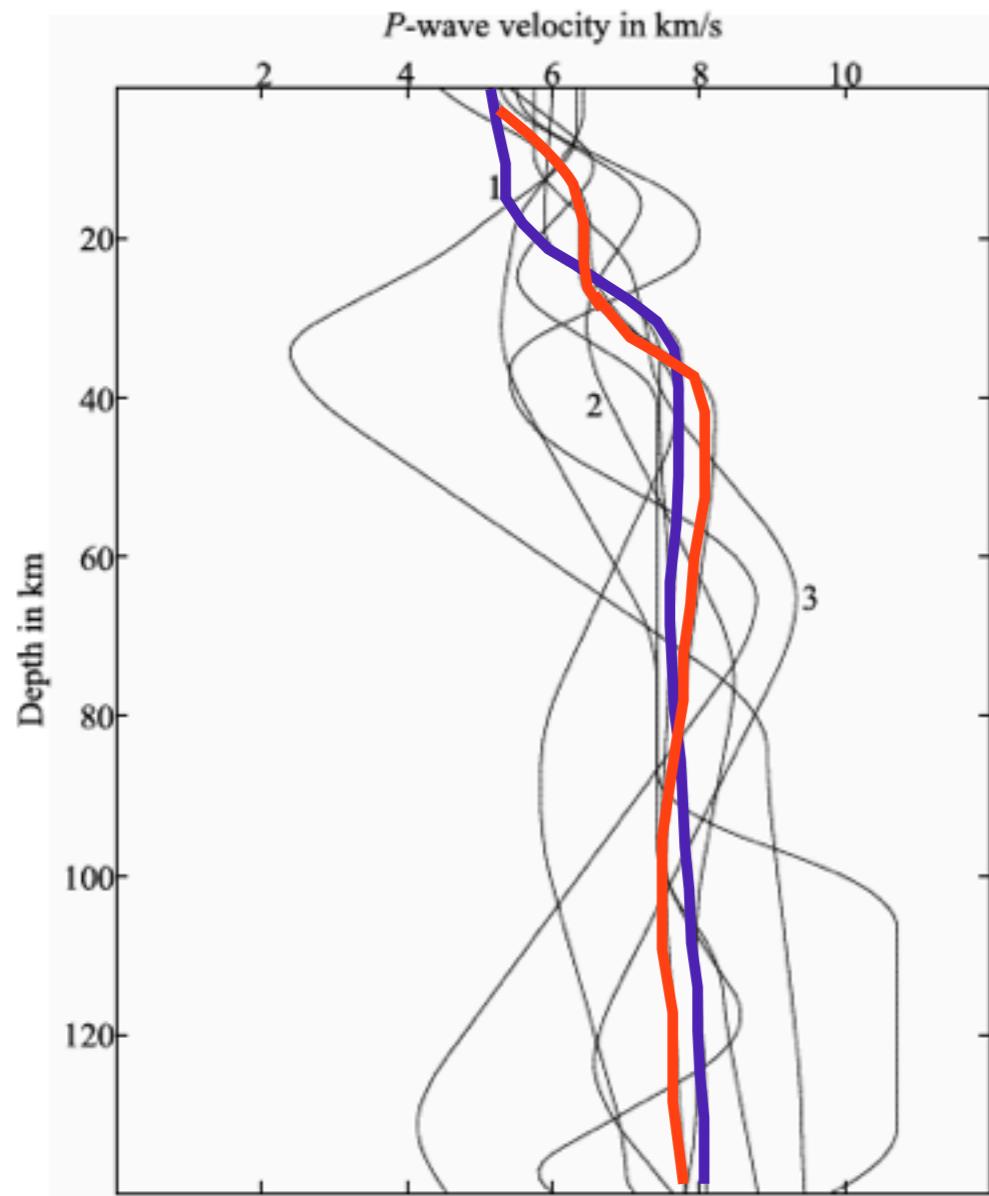
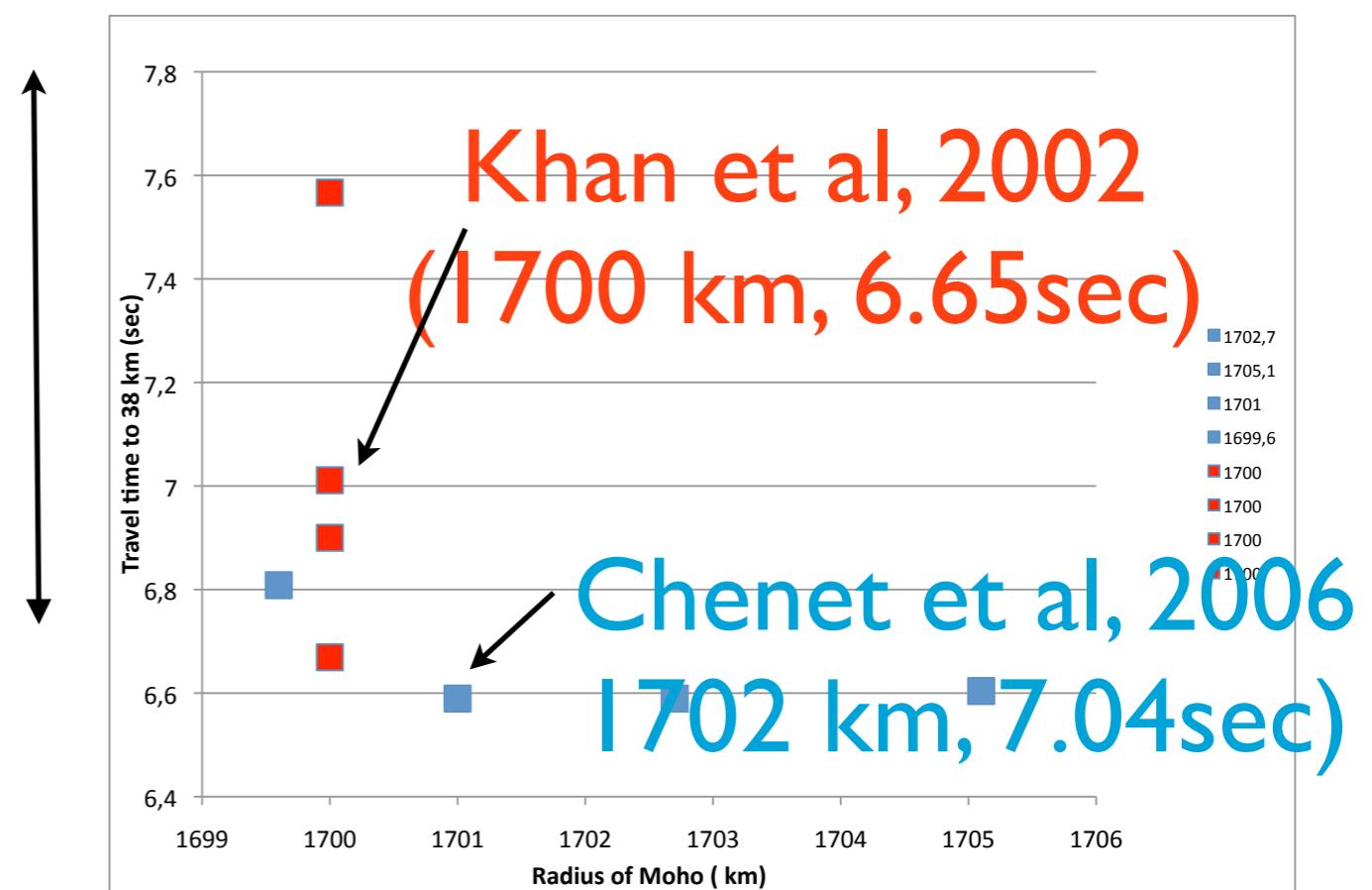


Figure 5. A smoothed version of 10 samples from the posterior distribution, each one obtained by sampling a different extremum in the model space. The models shown here emphasize only the crustal and upper mantle part. The three models numbered 1–3 have been taken as examples of models which individually highlight seemingly different structures but nonetheless are models that all produce a fairly large likelihood value, that is, produce a good fit to the observed data (see Table 1).

Khan et al, 2002

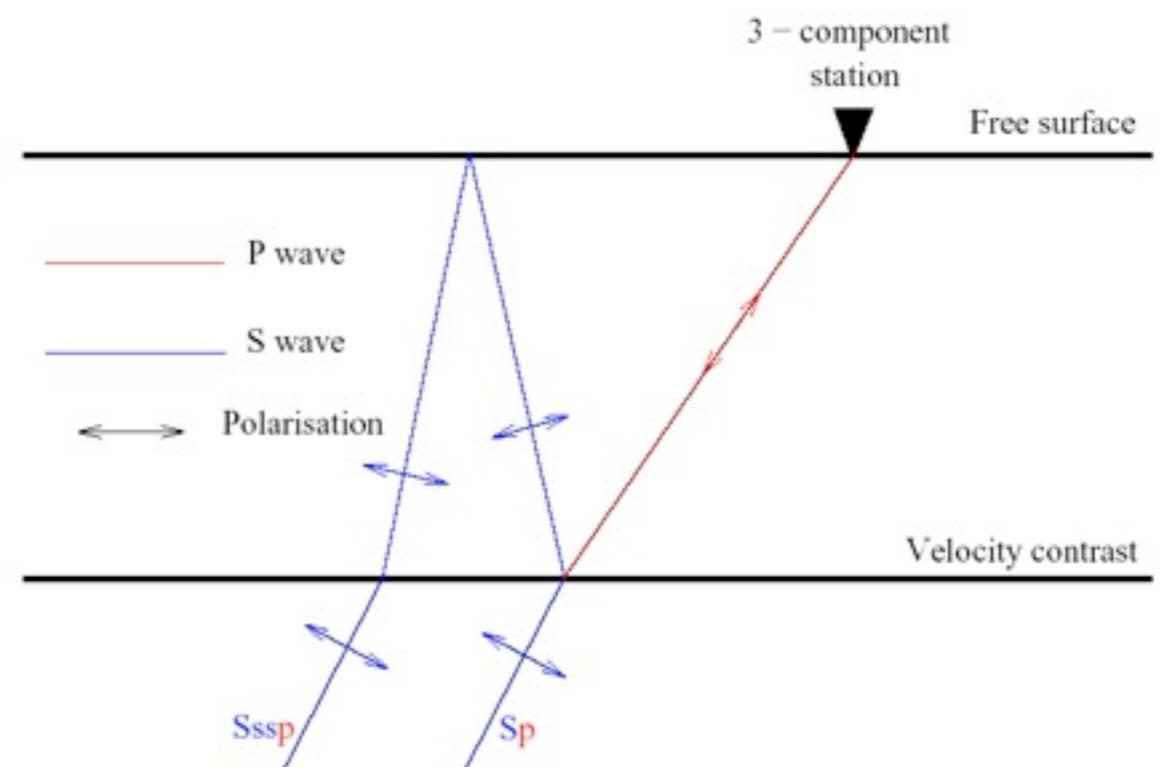
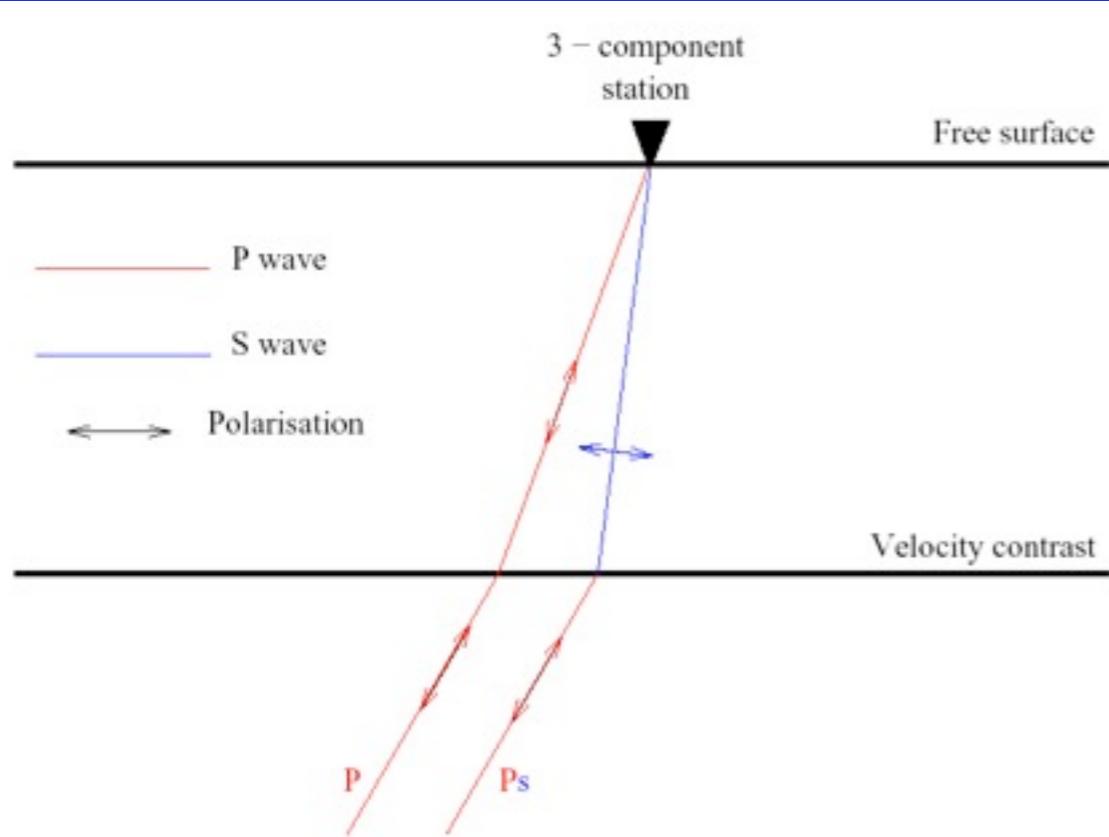
- seismology is mainly sensitive to the travel times, which means integration of the slowness along ray



- typical error $\pm 5\text{km}$, $\pm 1\text{sec}$

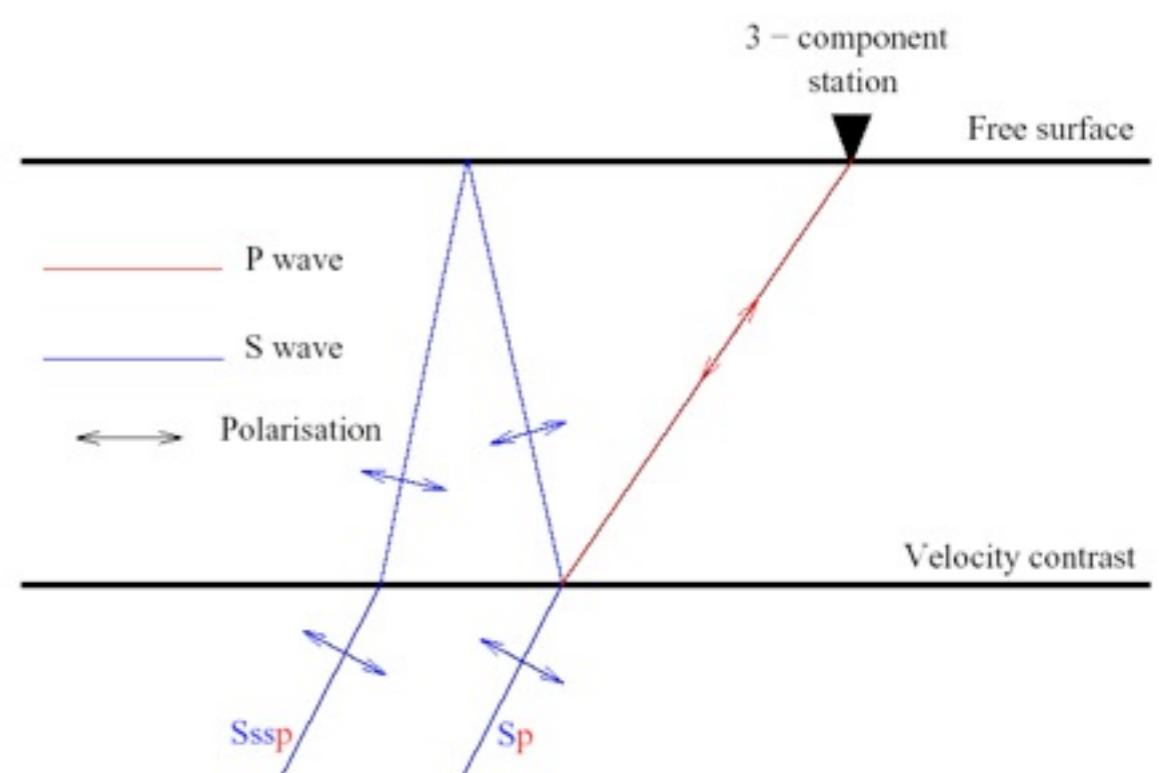
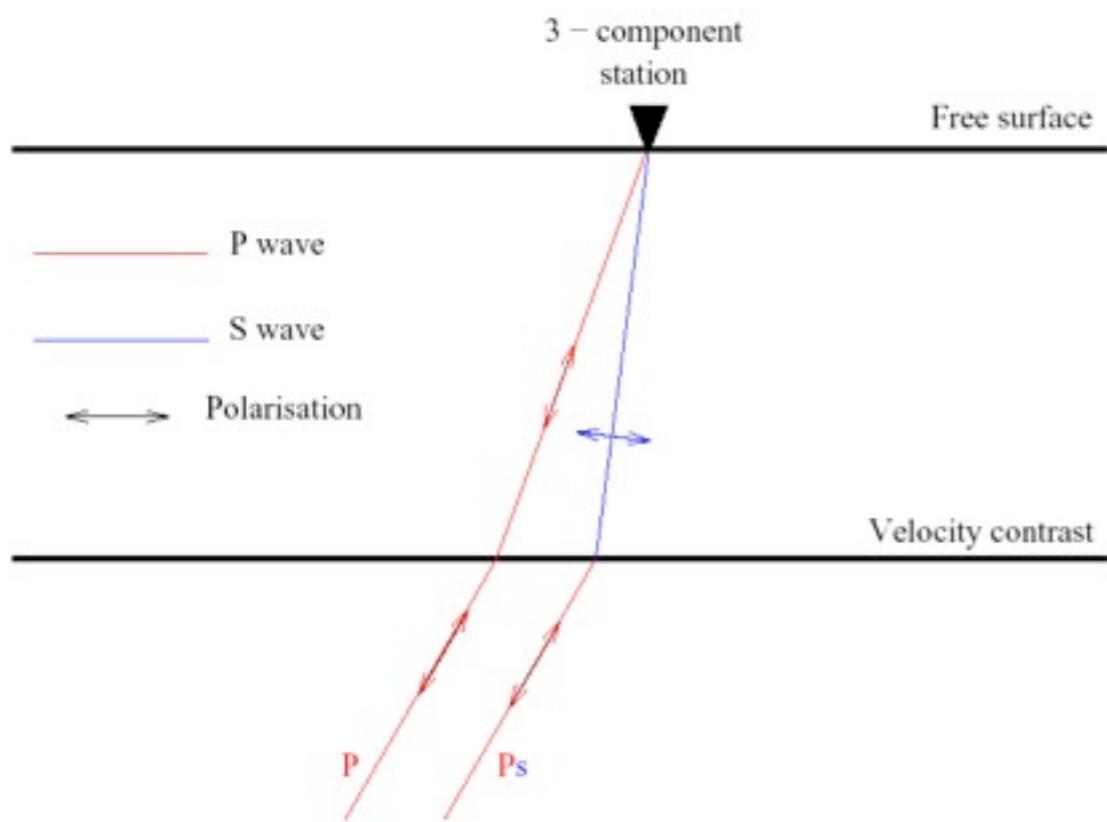
Inversion with some 3D effects: crustal structure

- The crustal structure leads to conversion and reverberations
 - Primary wave arrival $\sim P(t-t_p) \times T$
 - $P(t)$ is the amplitude in of the P wave below the crust, depending on the mantle propagation and of the seismic source, T the transmission coefficient to the crust and t_p the transmission time through the crust
 - Converted wave $\sim P(t-t_c) c C$
 - C is the transmission coefficient of the crust from Primary wave to converted wave and t_c the transmission time through the crust

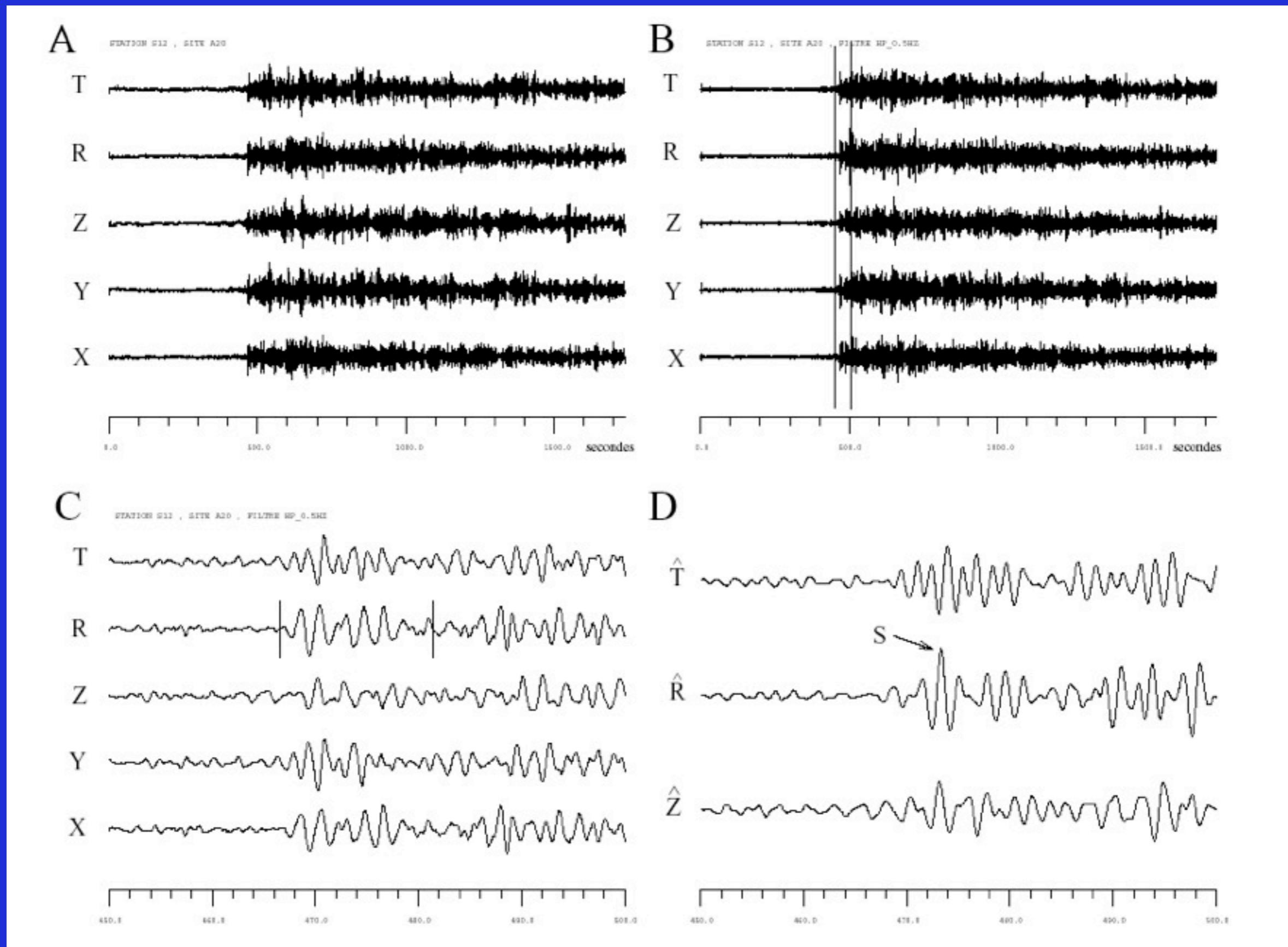


Receiver function method

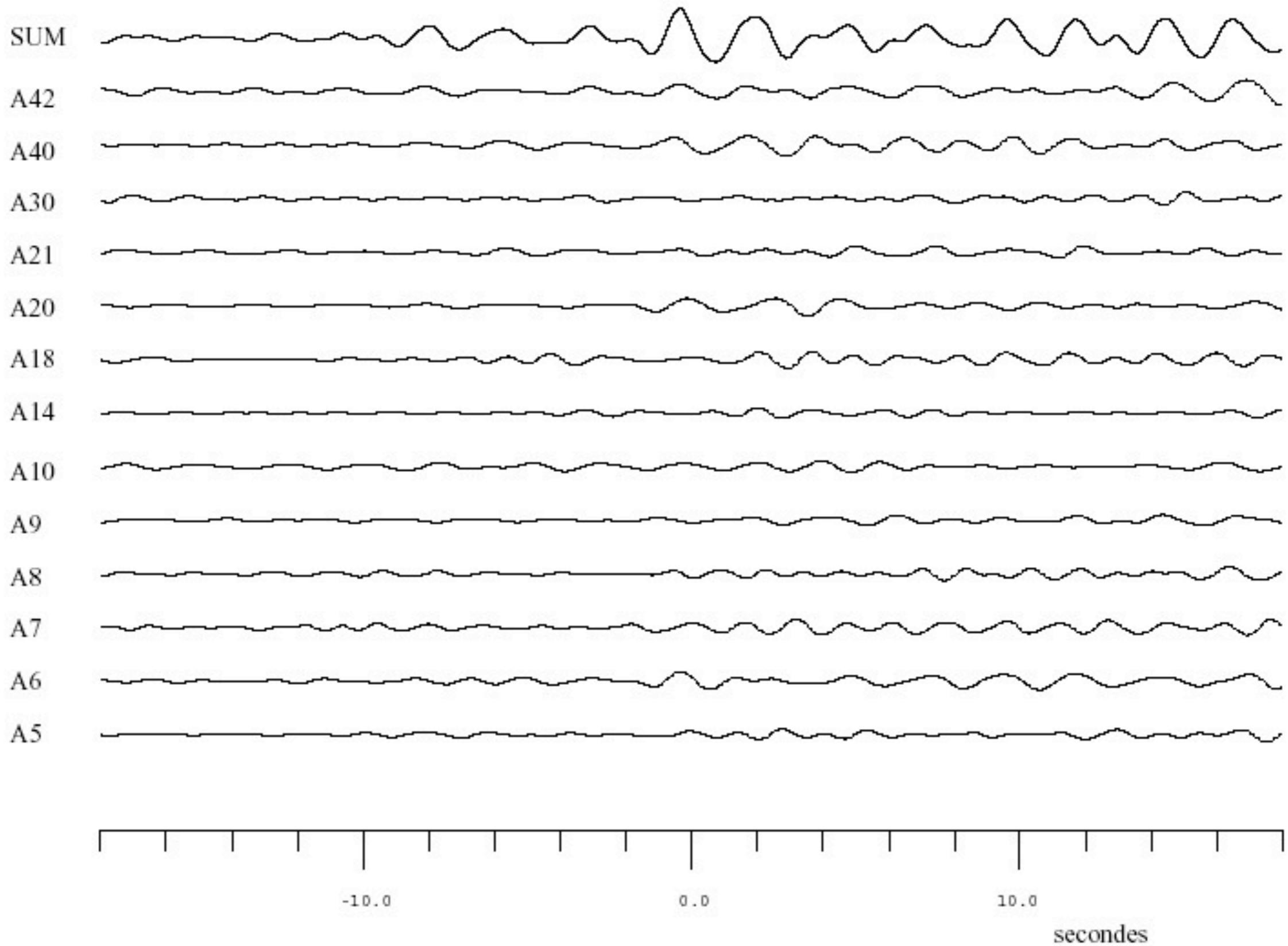
- 1st step : make the Fourier transformation of the arrivals
 - Primary wave arrival Fourier Transformation $\sim T P(\omega) \exp(i\omega t_p)$
 - Converted wave $\sim C P(\omega) \exp(i\omega t_x)$
- 2nd step: perform the deconvolution of the converted wave by the primary wave in frequency domain
 - $R(\omega) = [T P(\omega) \exp(i\omega t_p)] / [C P(\omega) \exp(i\omega t_x)] = T/C \exp(i\omega(t_p - t_x))$
- 3rd step: perform the inverse Fourier transformation
 - $R(t) = T/C \delta((t_p - t_x))$



Deconvolution process



Improving the signal to noise ratio with stack

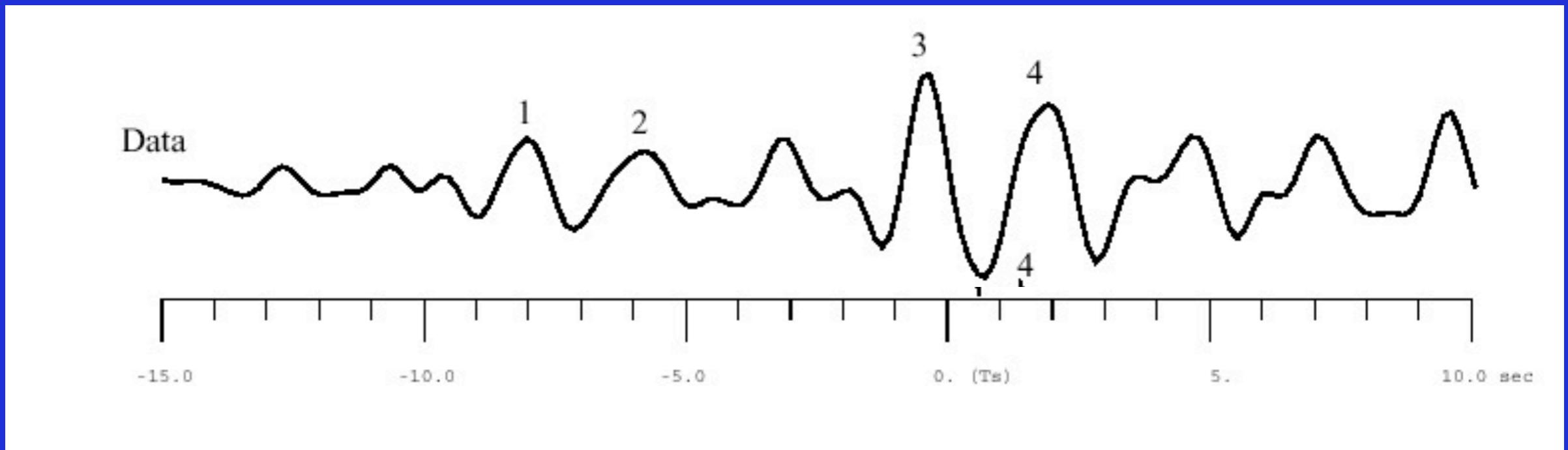


Moon receiver function (Apollo 12 site)

S->P conversion at the
Base of the crust

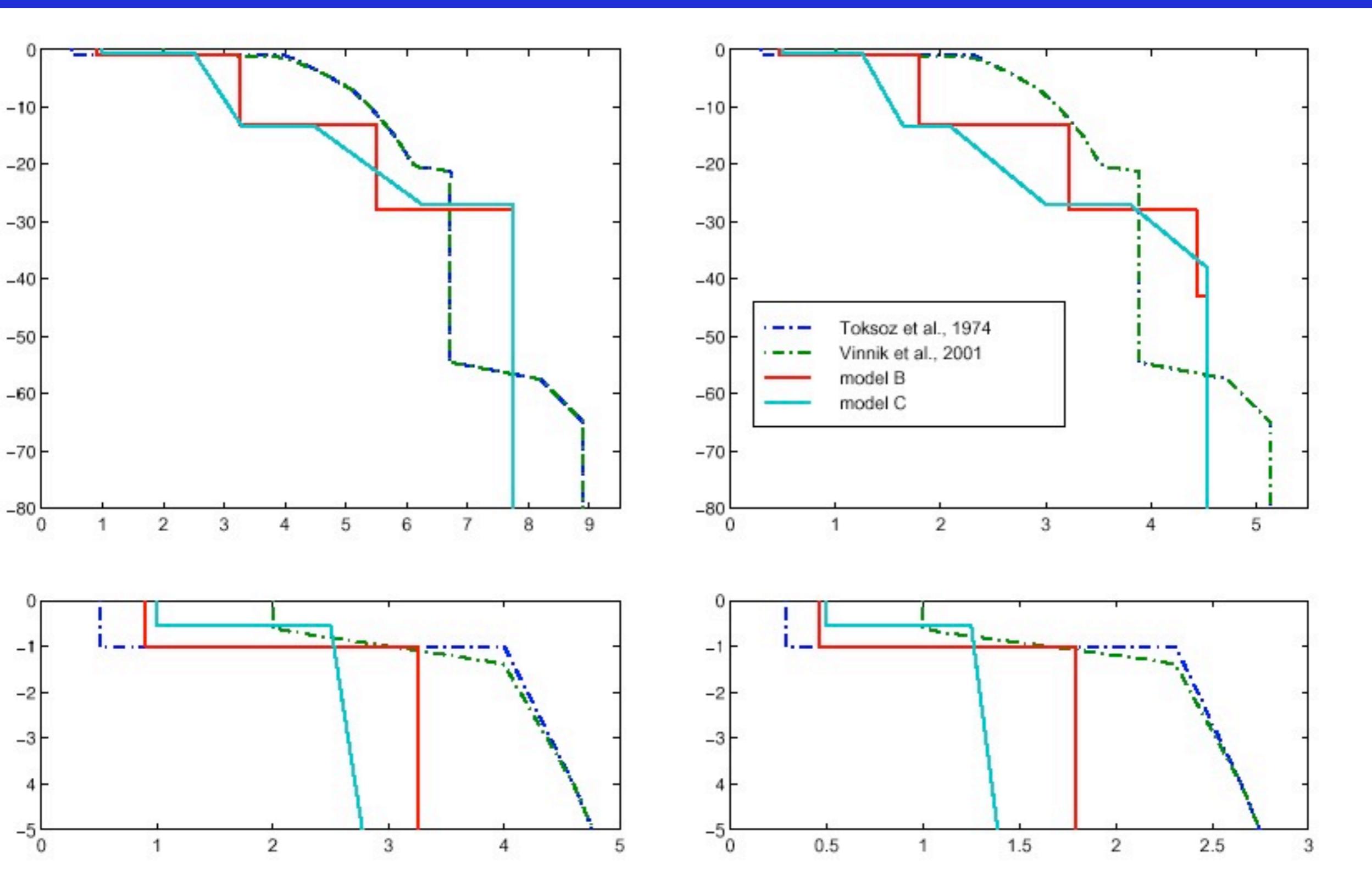


Subsurface/regolith
delay and reverberation

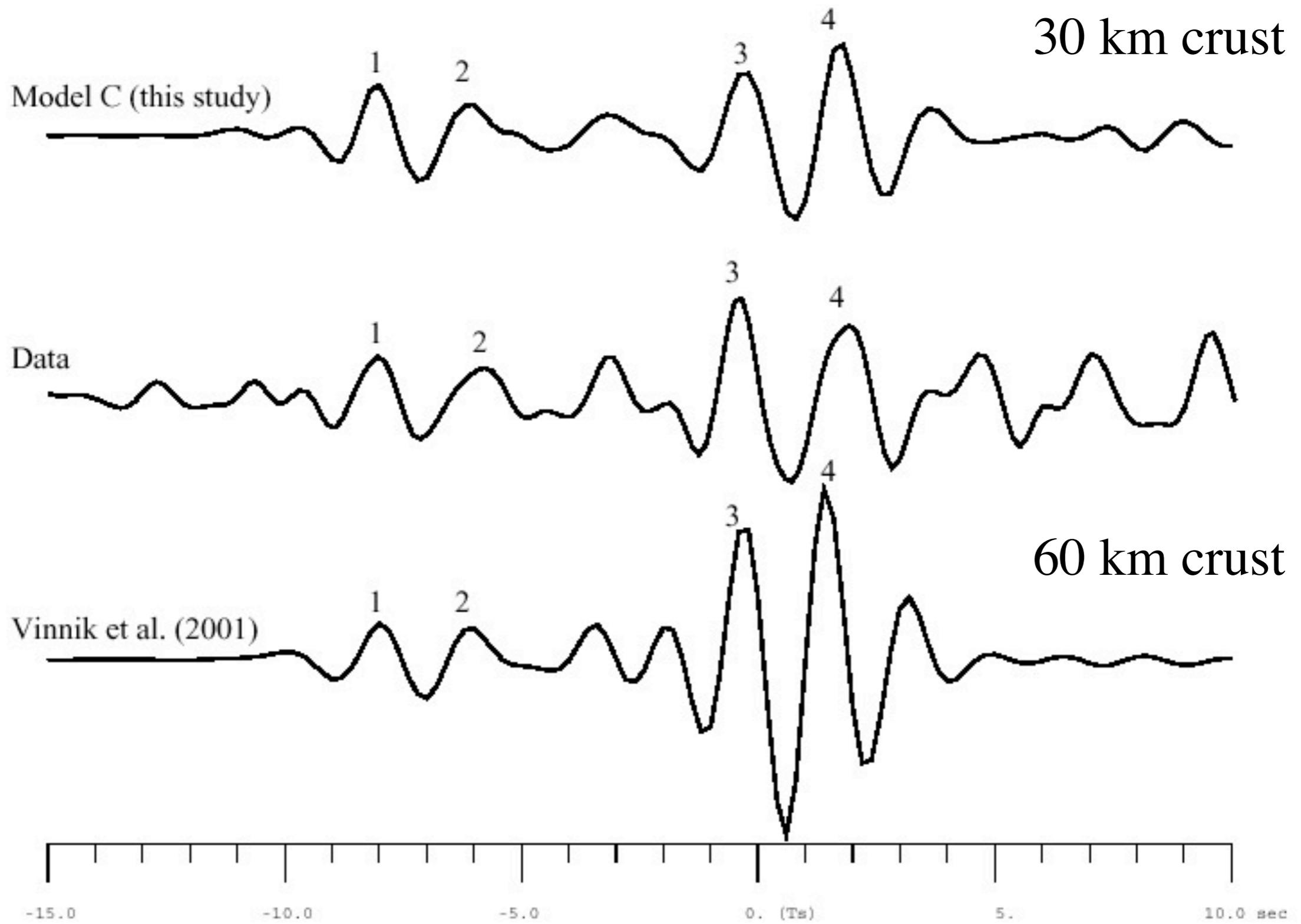


- S-P delay is equal to
And therefore does not give a unique solution
- other informations are needed (amplitude conversion coefficient)

$$\Delta t = t_s - t_p = D \left(\frac{1}{v_s} - \frac{1}{v_p} \right)$$



Moon receiver function (Apollo 12 site)

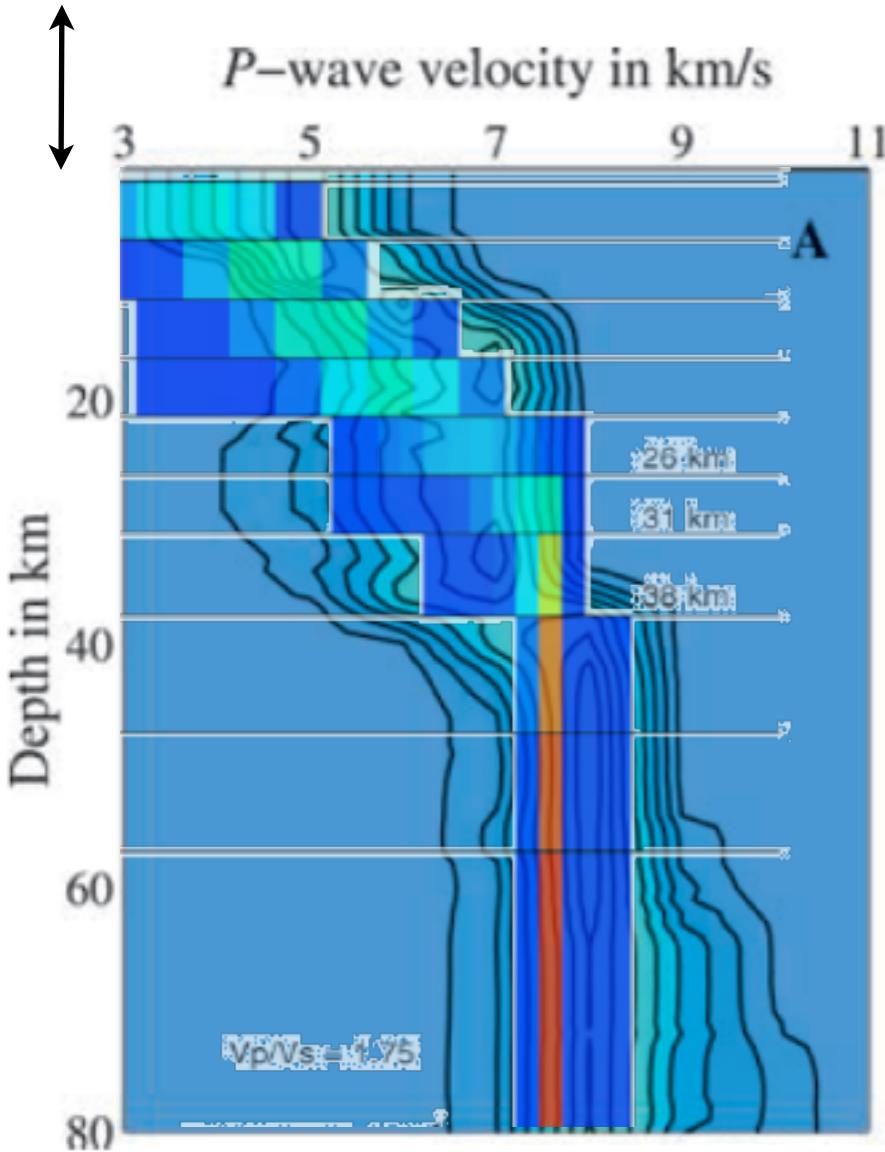


Surface fracturation ?

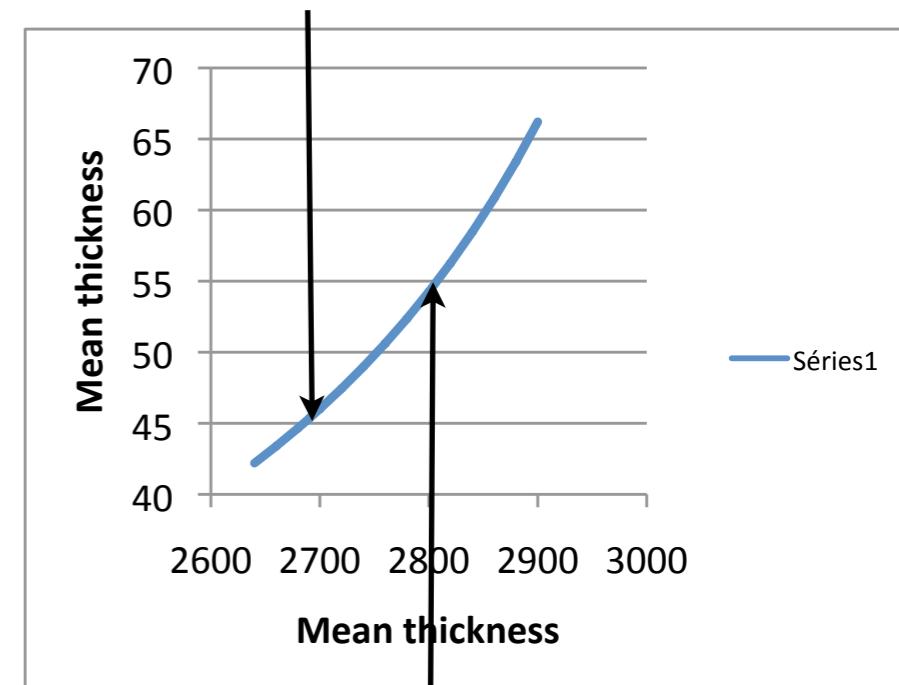
- Many recent evidence for higher porosity
- Possibly a key issue for more precise crustal estimation

Huang and Wieczorek, 2012

I km vp at least down to 3.3 km at
Apollo 17 , i.e. 2.4 km/s(Nakamura , 2011)

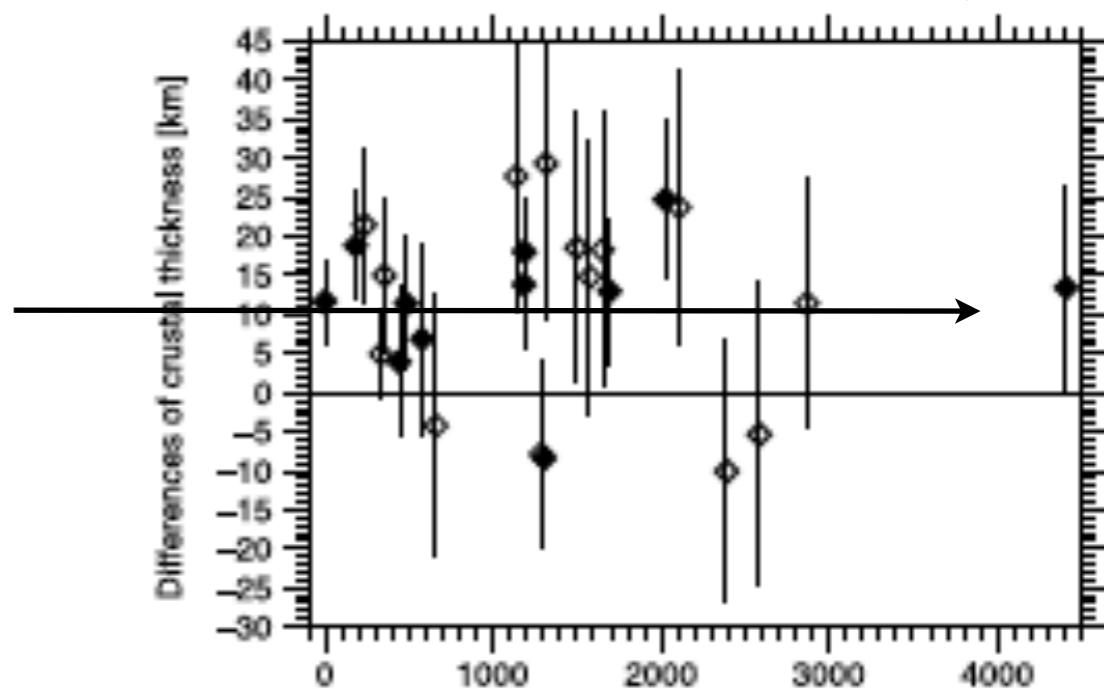


constant mass



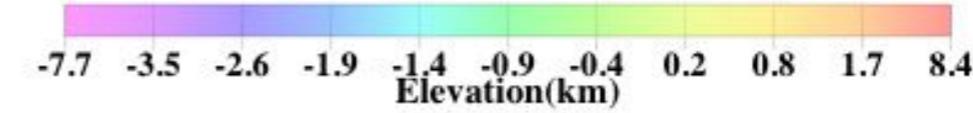
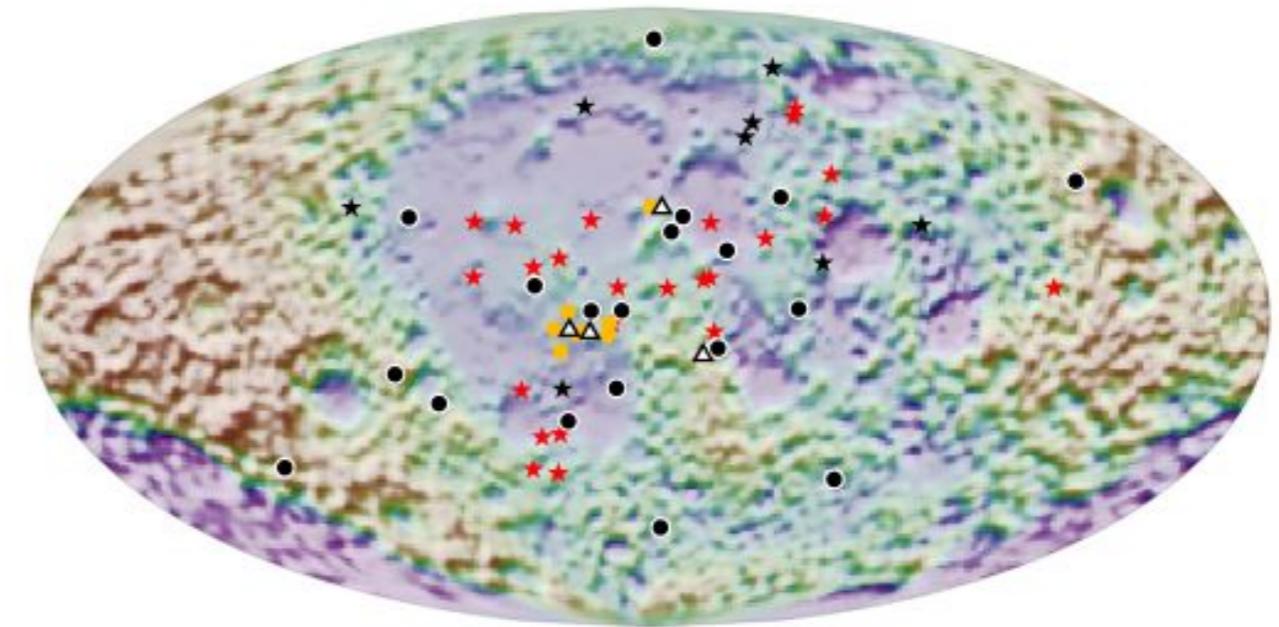
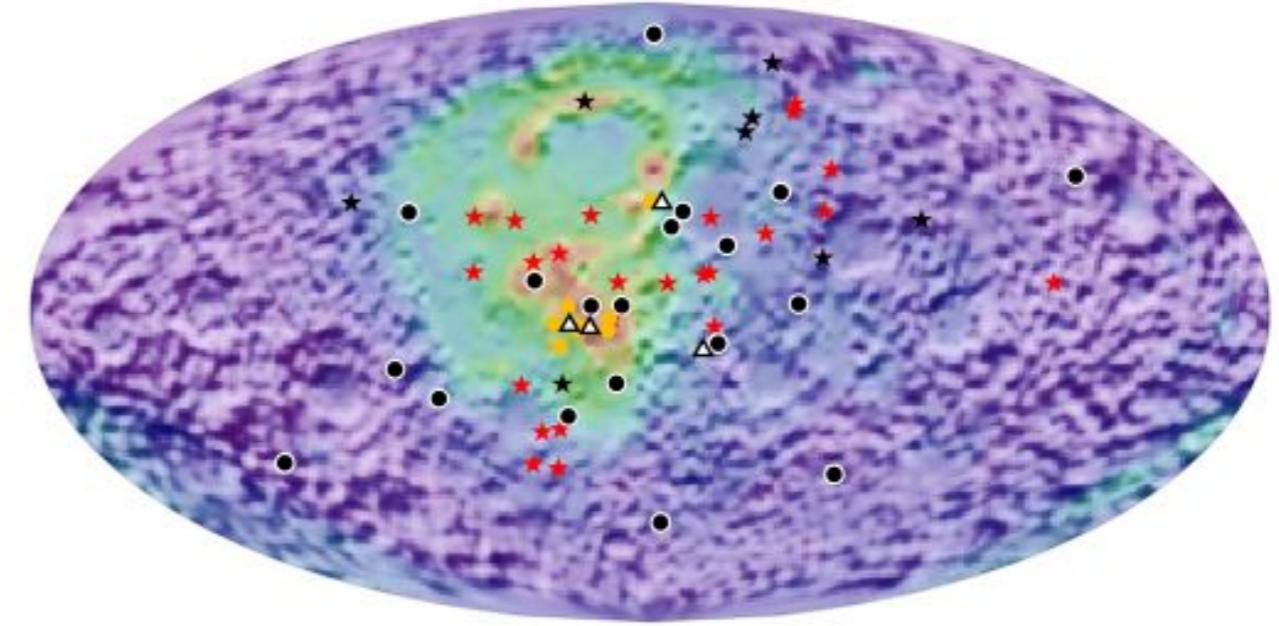
Ishihara et al, 2009

Porosity effect?

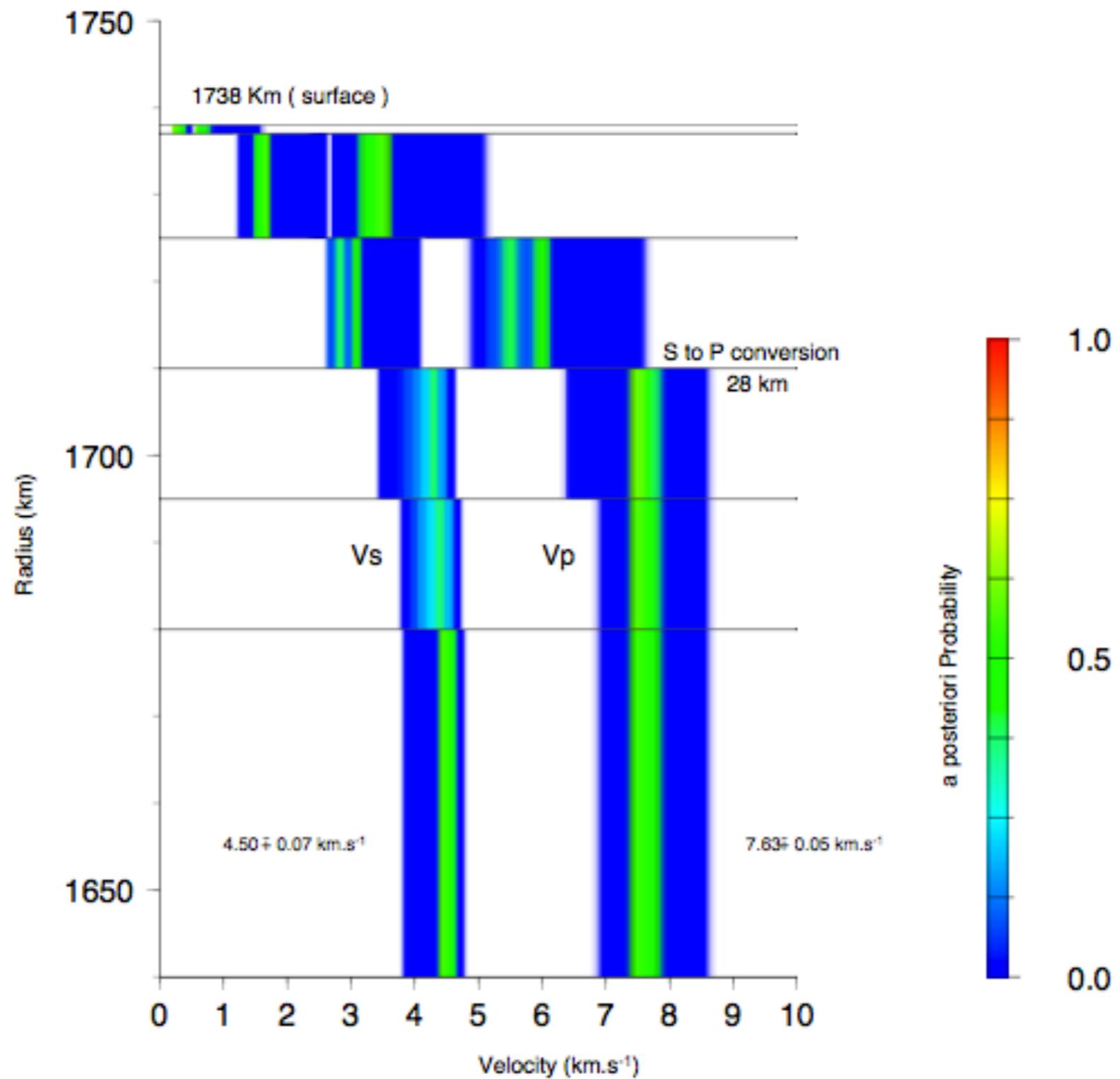


3D crustal structure

- The structure sampled by the Apollo seismic network is not providing a mean Moon model but a regional model associated to the Procellarum KREEP Terrane
 - Thinner crust
 - Probable High Th content

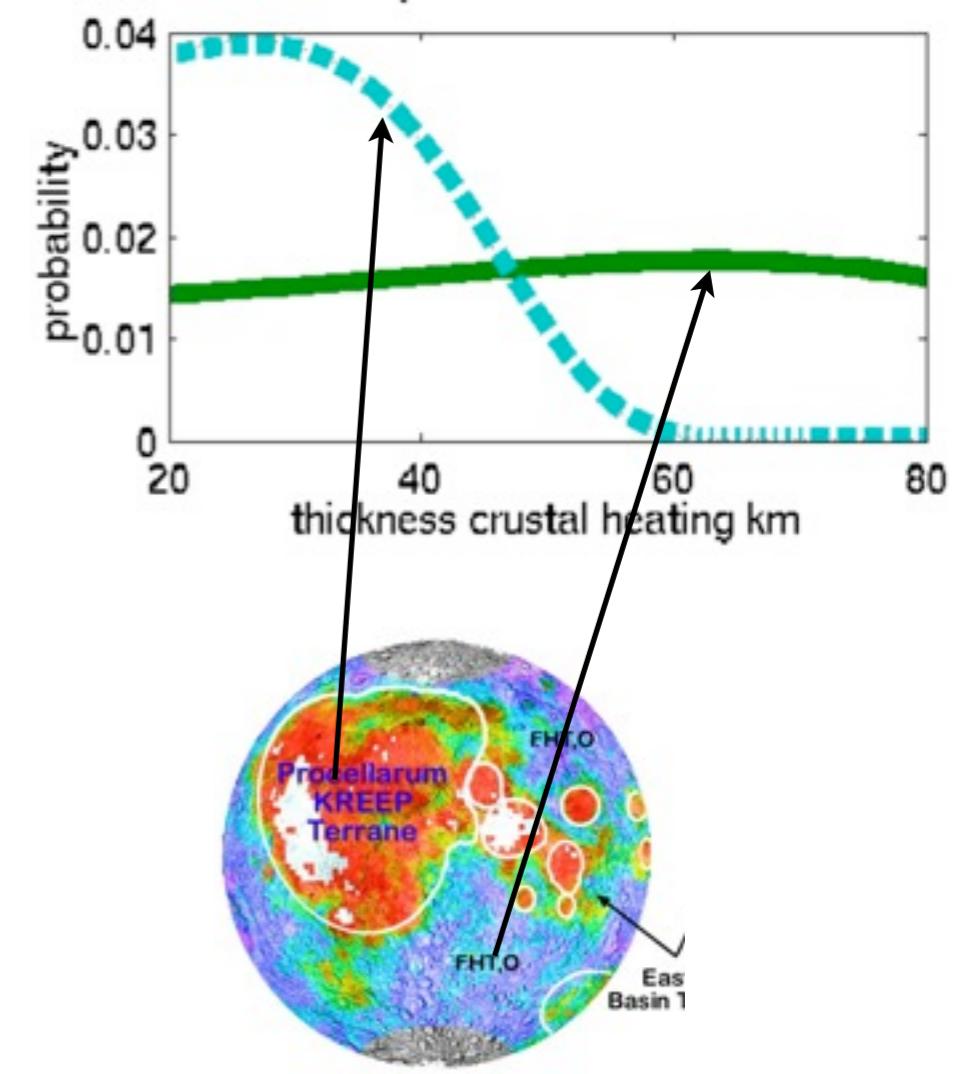
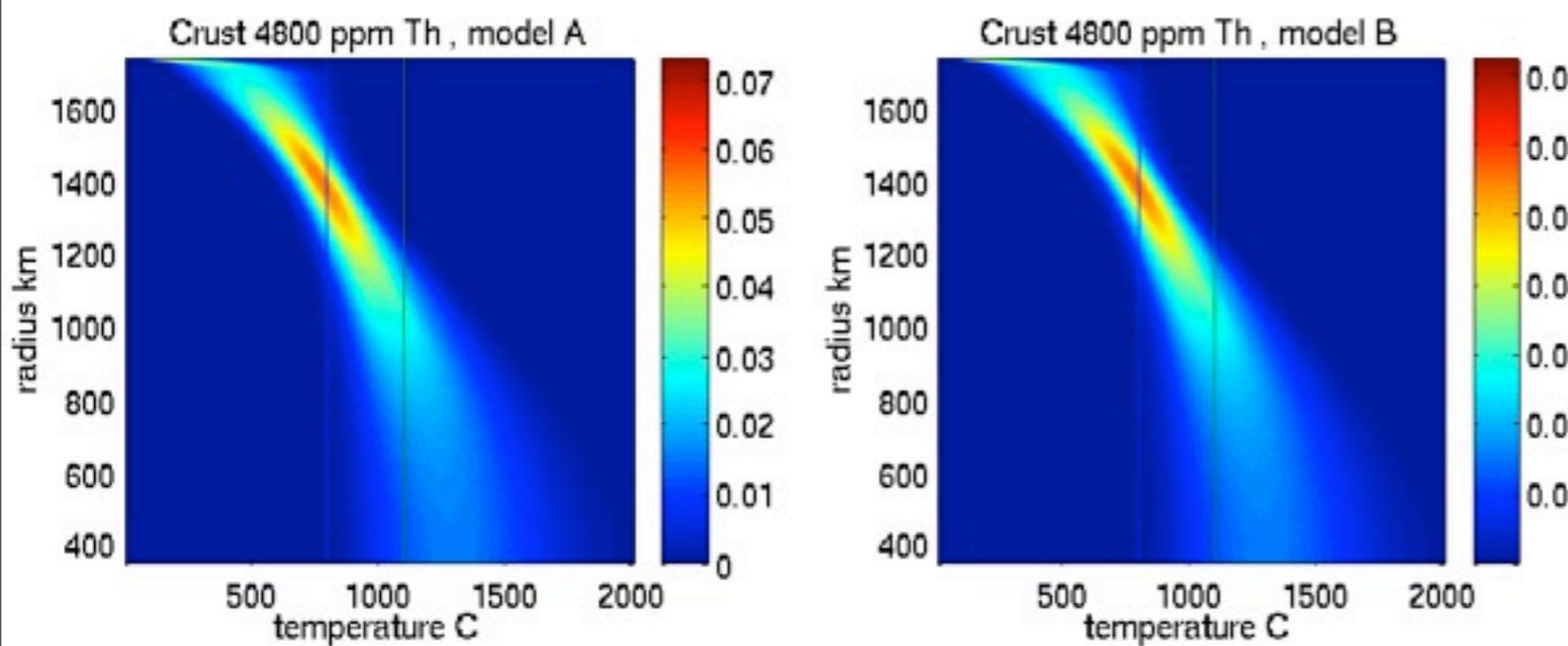


Down to Moho?



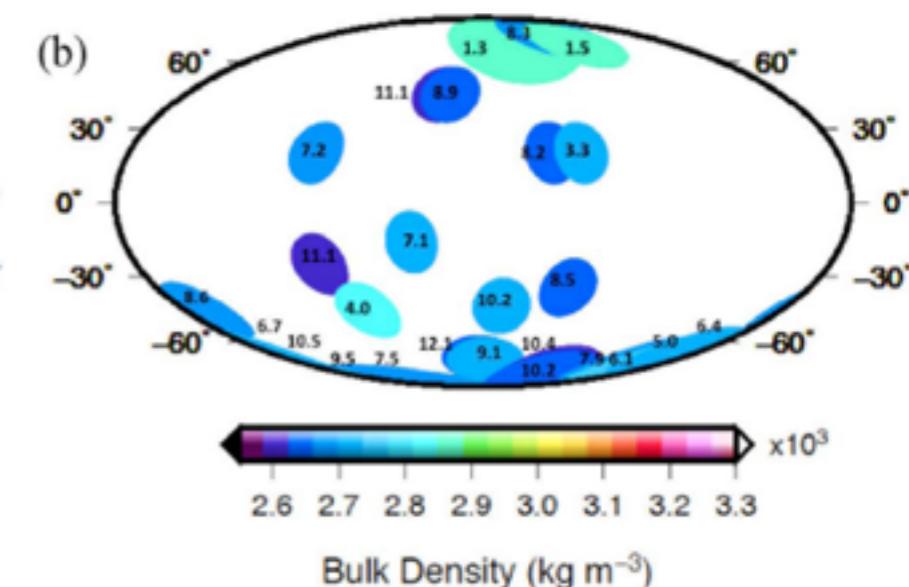
Joint crustal inversion: seismic plus mineralogy

- Use lunar samples to fix the mineralogy of the upper mantle
 - Use the upper mantle seismic velocity as «thermometer» to constrain the thickness of the radioactive heating crust



Further effects: Lateral density variations

- Typical lower crustal density is 2900-3040 kg/m³
- Typical upper mantle density is 3300-3400 kg/m³
- Difference is therefore ~12%
- 5 km of crustal thickness increase (negative mass) is therefore equivalent to crustal porosity increase by 6% in the upper 10 km



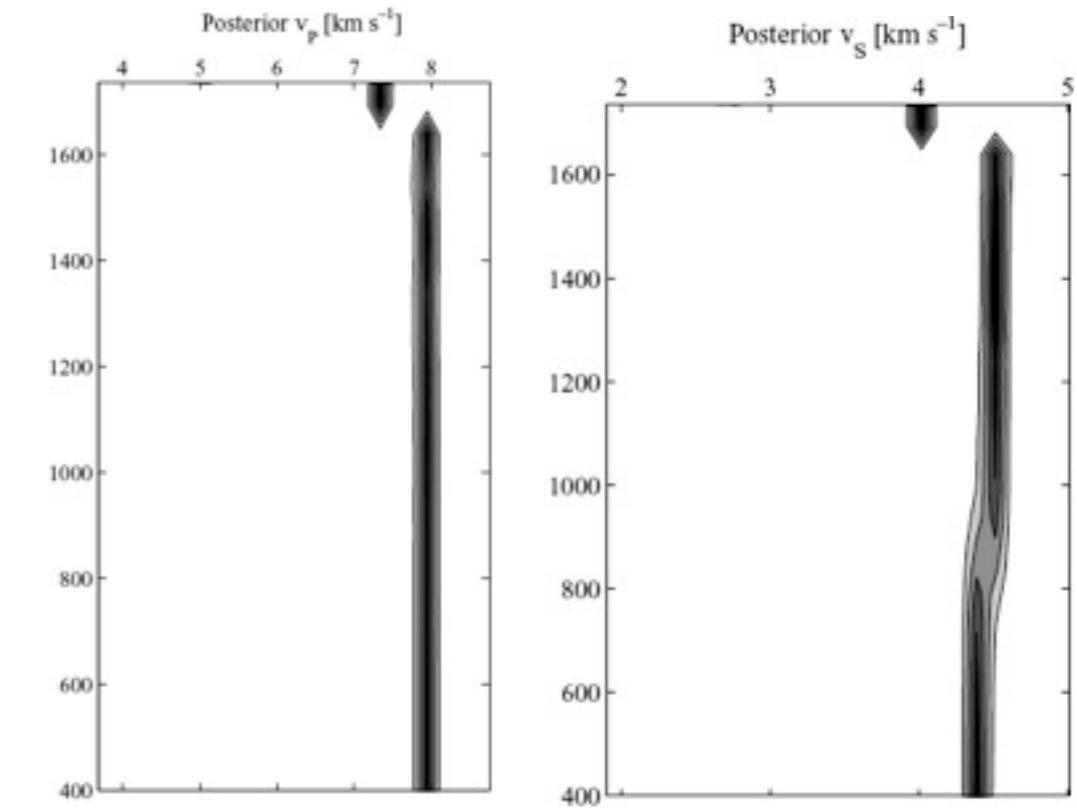
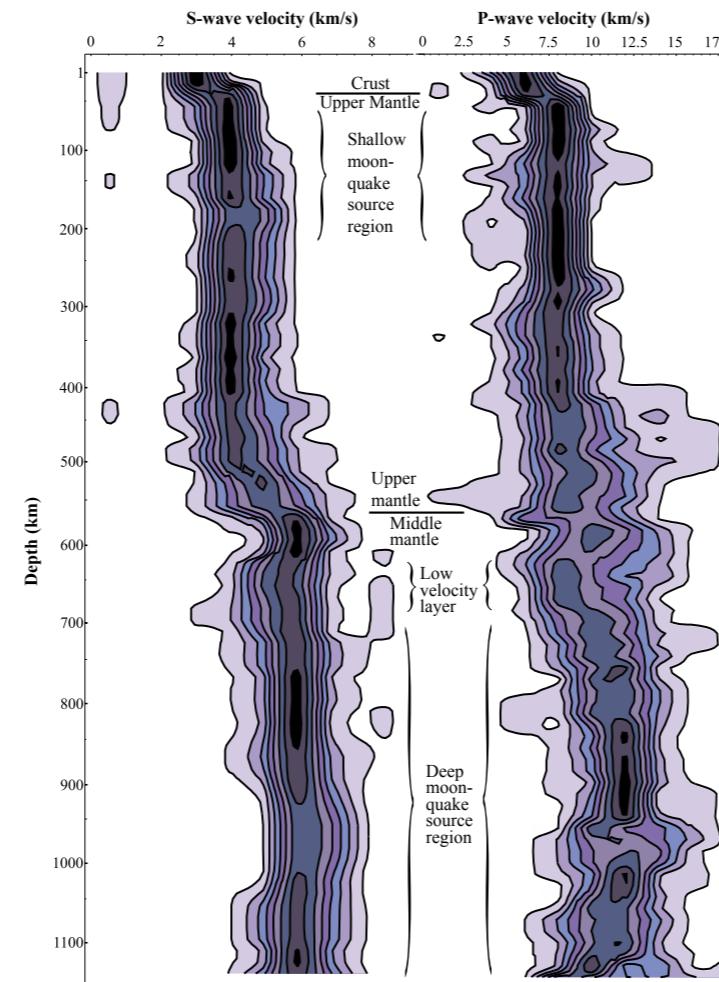
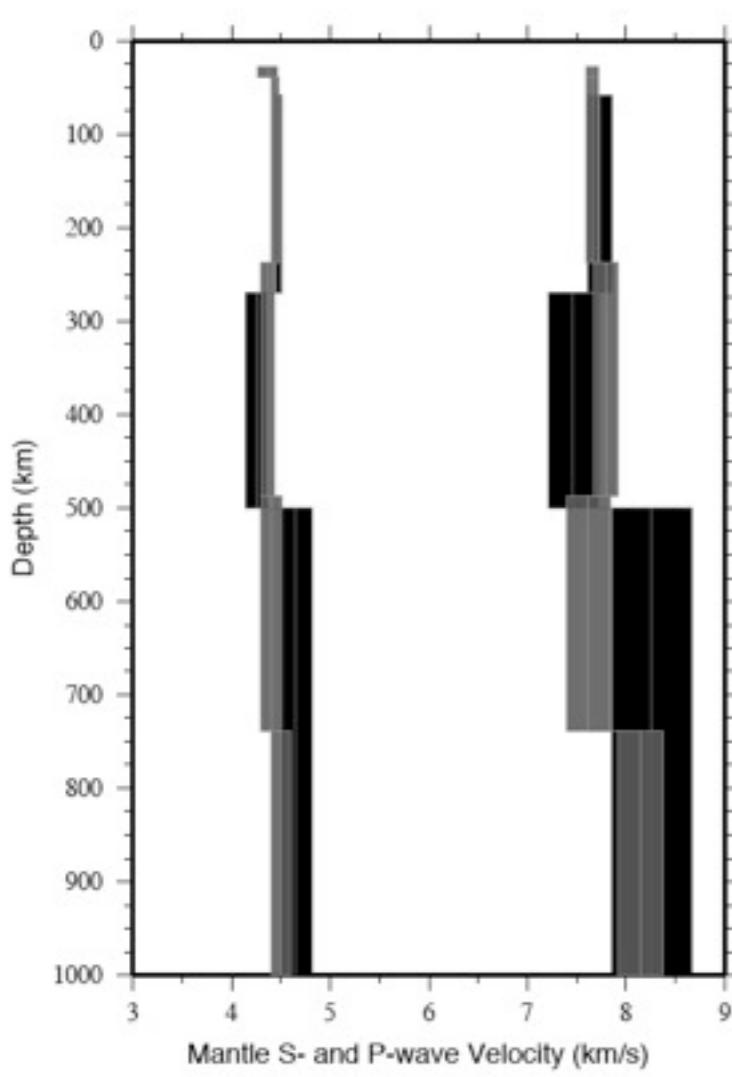
- Positive Thermal crustal-upper mantle feedback

- negative crustal mass
 - increased porosity (better isolation)
 - Larger thickness (more heating)



- negative mantle mass
 - hotter upper mantle

Is there a seismic discontinuity in the mantle?



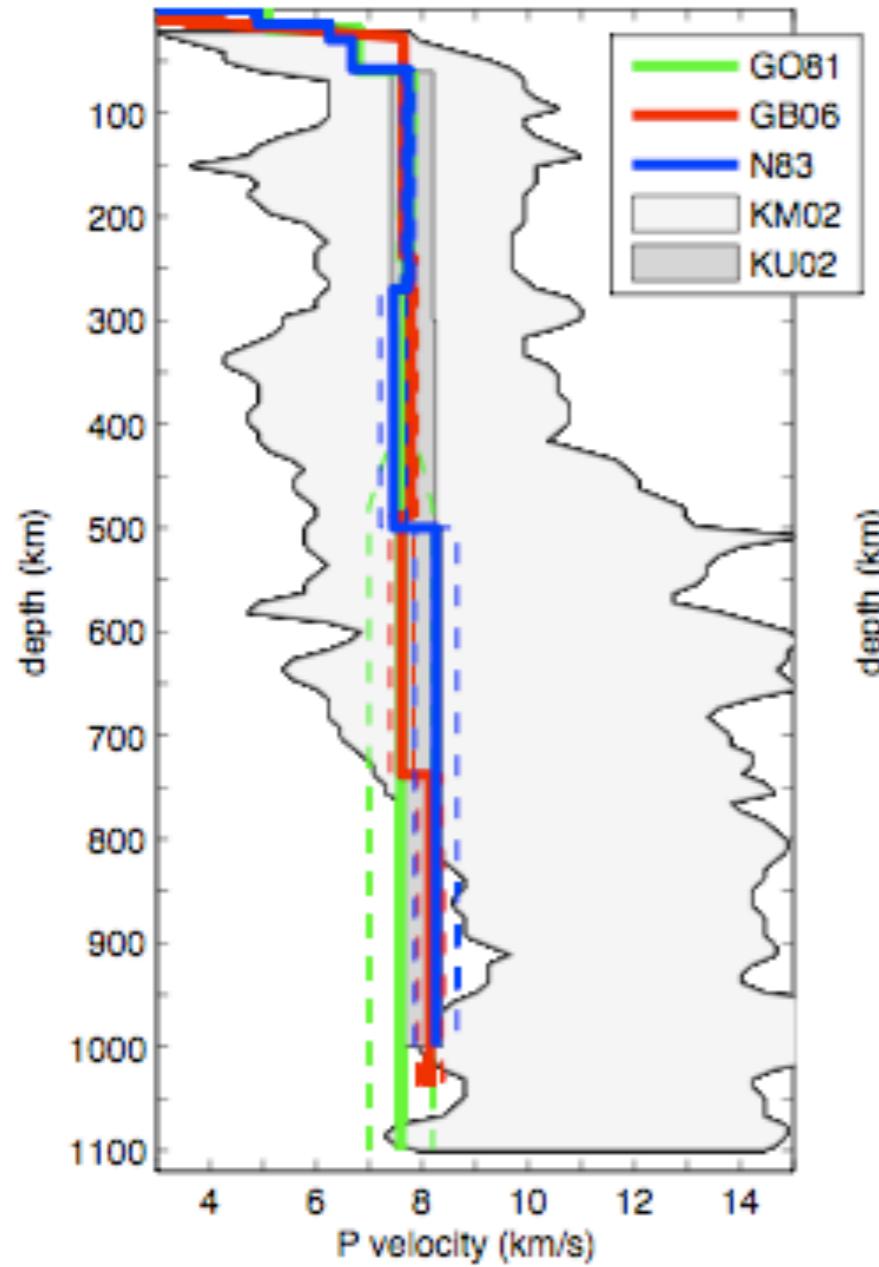
Nakamura et al. (1982),
Lognonné et al. (2003)
Maybe: ~500 km

Khan and Mosegaard
(2002)
Yes: 550 km depth

Khan et al. (2007)
NO? or 850 km depth?

Each study used different seismic events, seismic arrival times and analysis techniques...

Direct inversion of seismic velocities

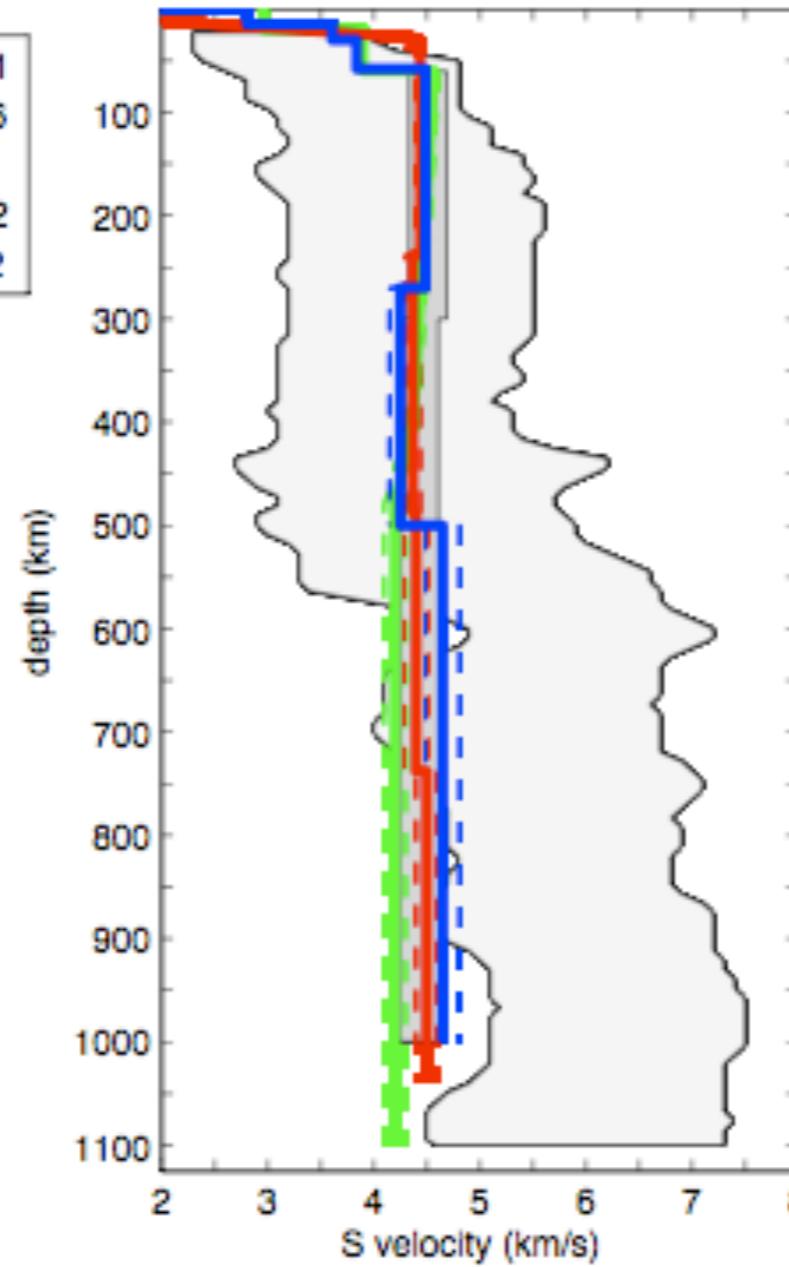


Nakamura, 1983

Goins, Dainty and N.Toksöz, 1981

Lognonné, 2003, Gagnepain-Beyneix 2006

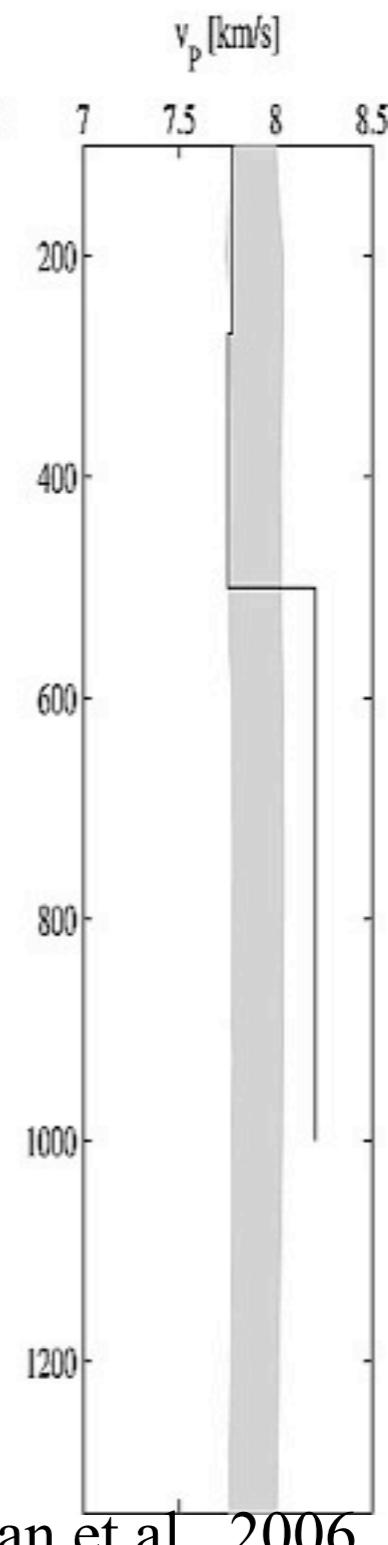
Kuskov et al, 2002



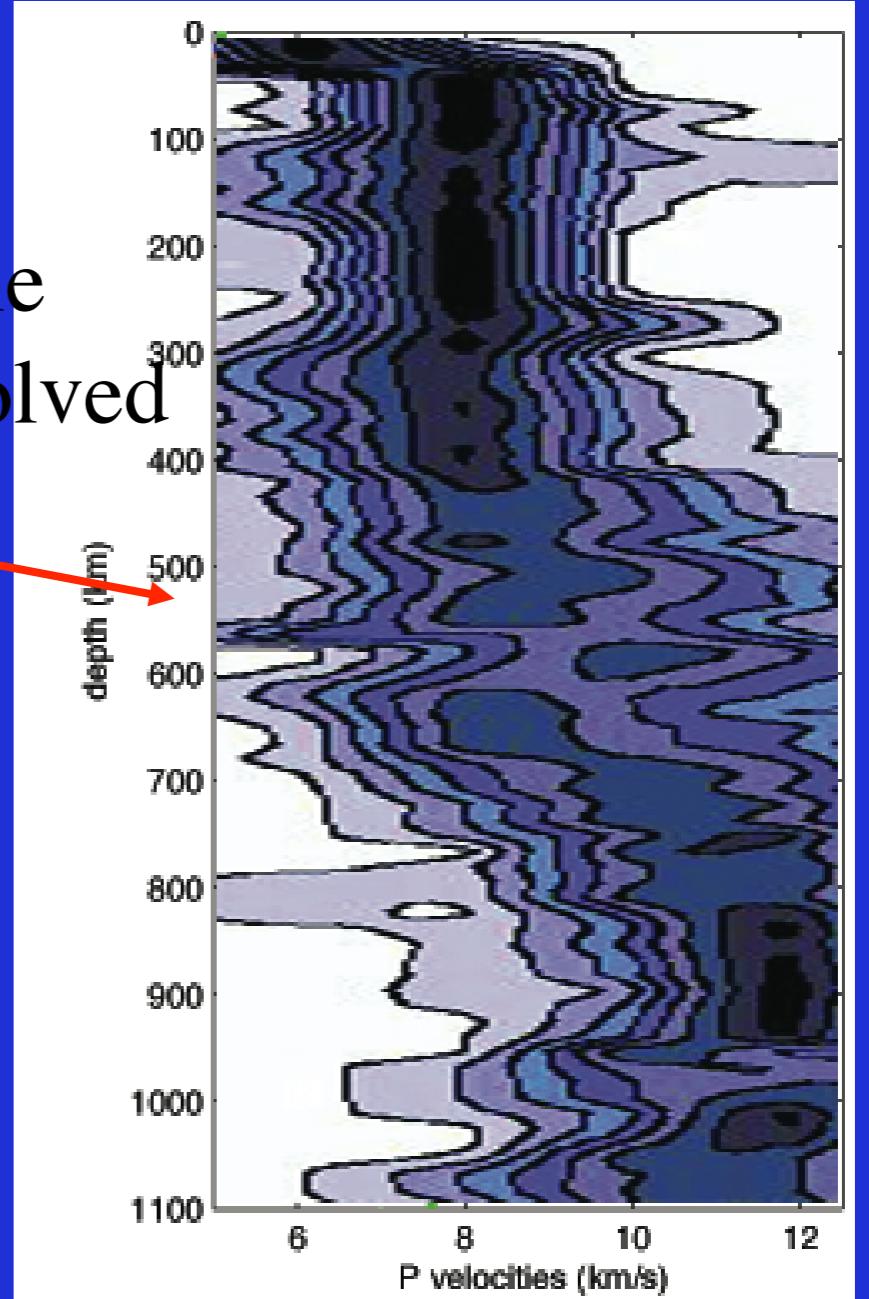
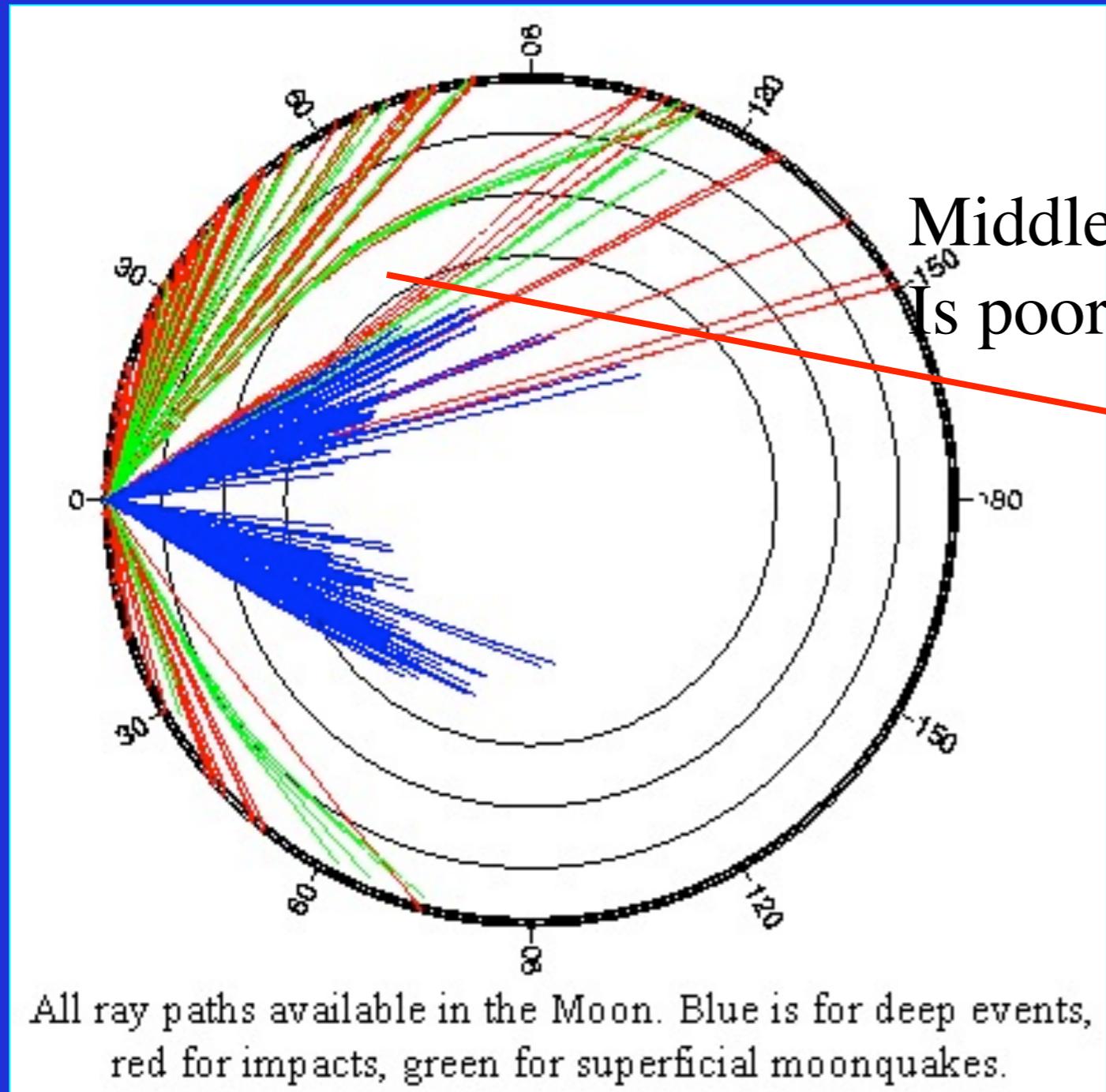
Khan et al, 2000

Khan and Mosegaard, 2002

Direct inversion of mineralogy



Khan et al., 2006





Sounding the Lunar core

- What we knew 2 years ago
 - Density and moment of inertia
 - Magnetic sounding
- What we know today

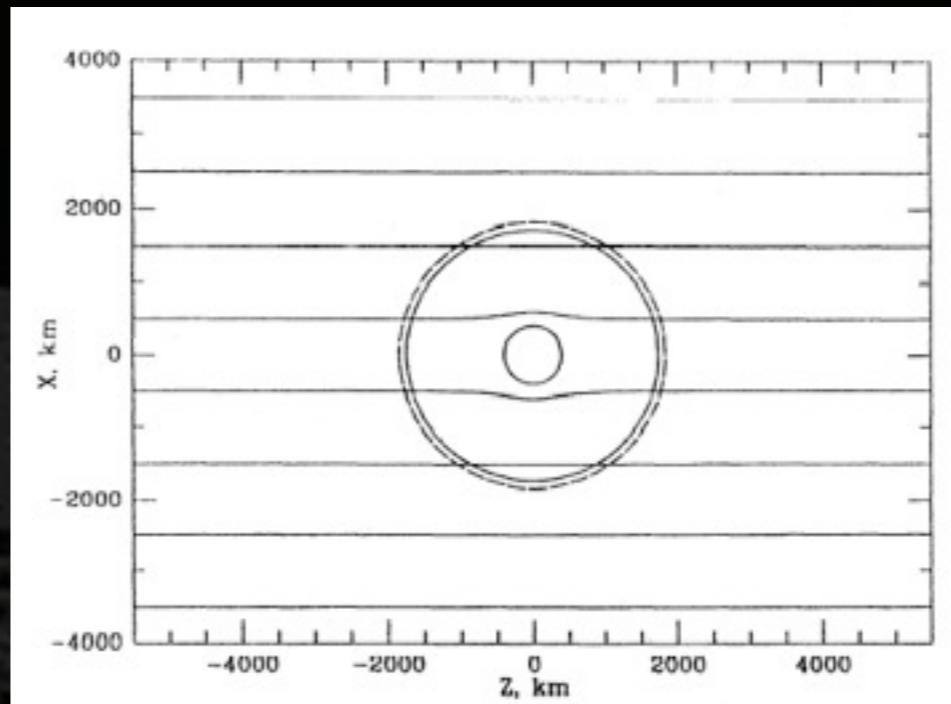
Coffee break



©JAXA/NHK

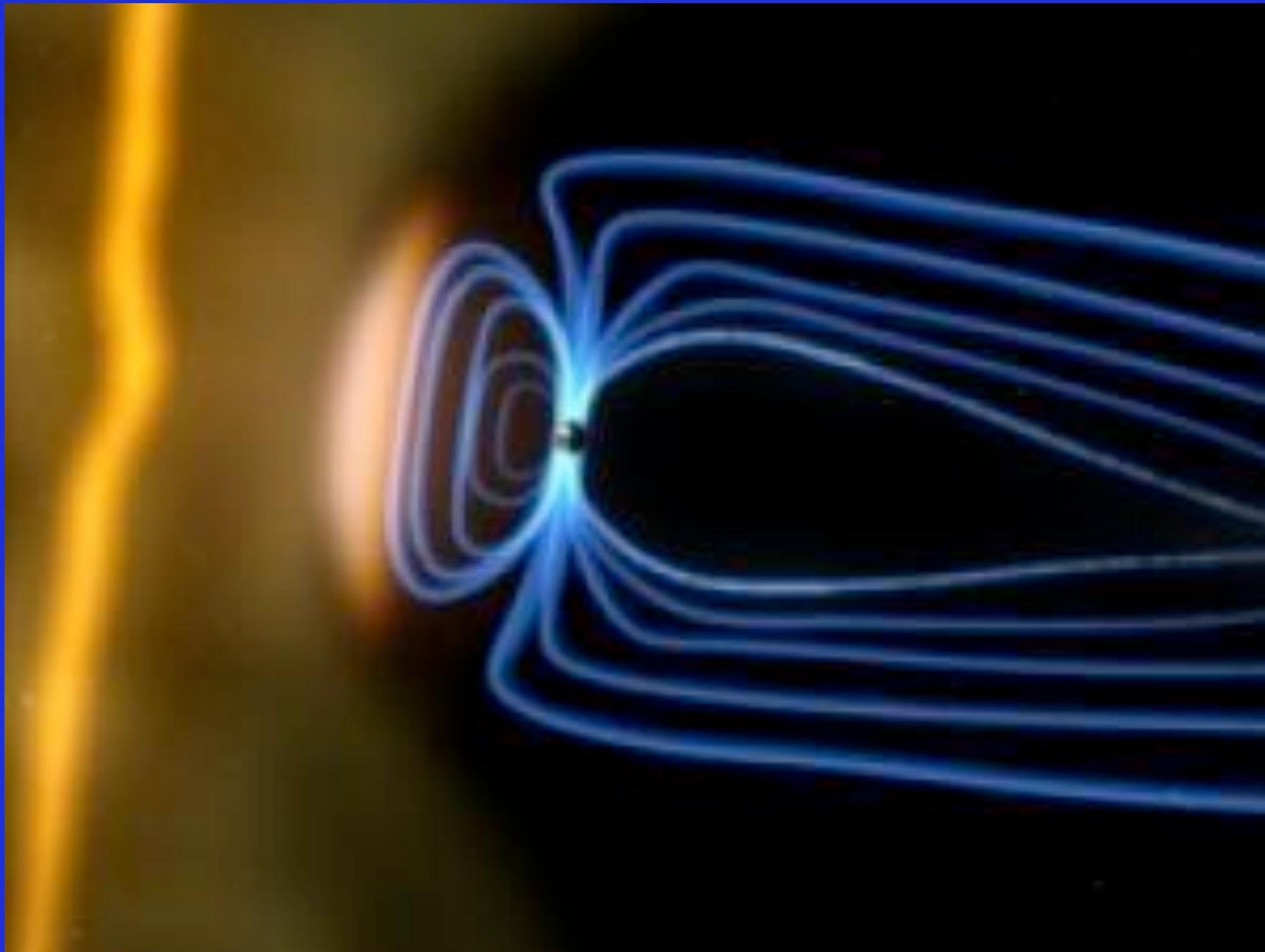
Magnetic Induction

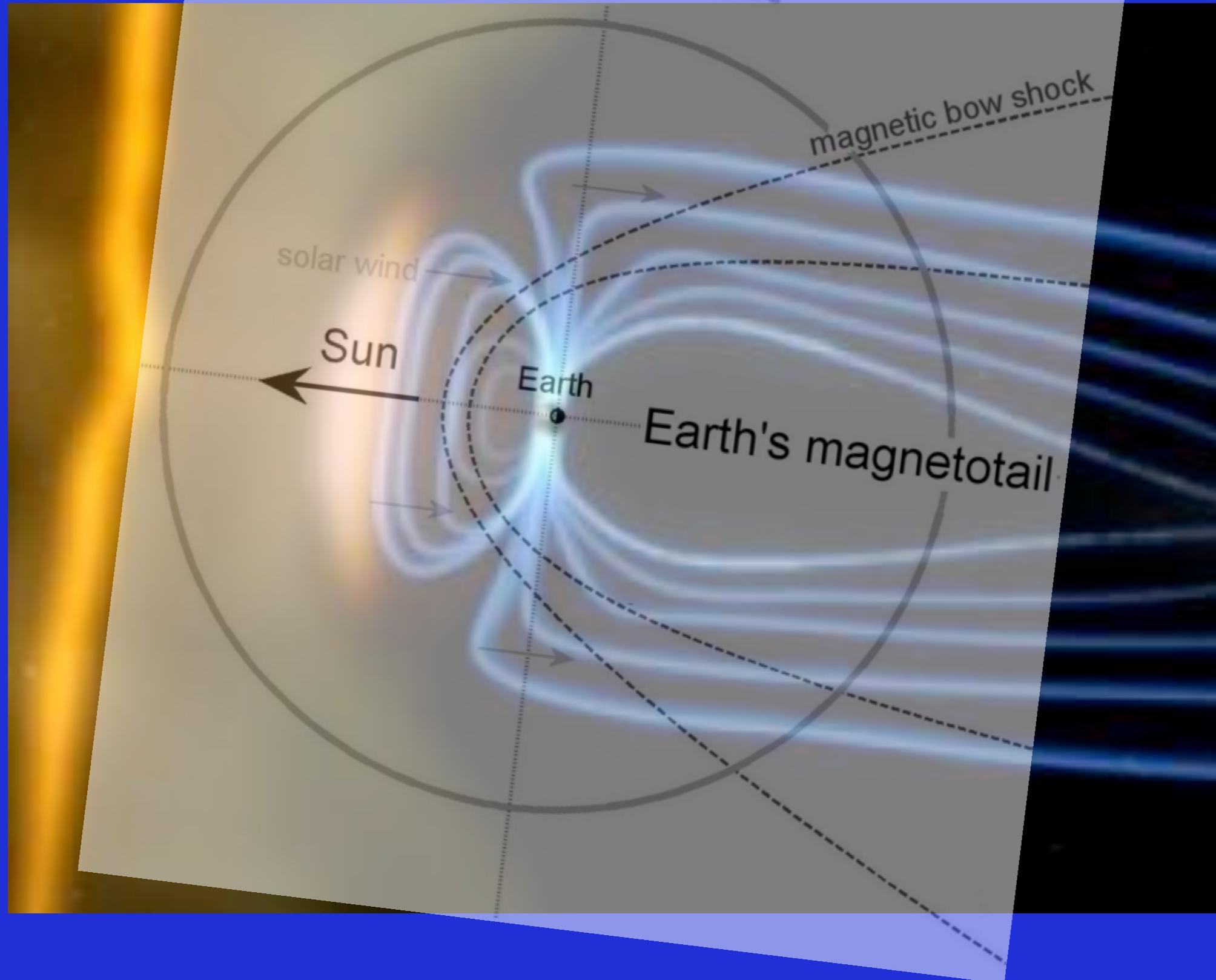
$$\nabla^2 \mathbf{B} = \mu\sigma \frac{\partial \mathbf{B}}{\partial t},$$



What is the (conductive) size of the Lunar Core?
What is the mantle conductivity ?

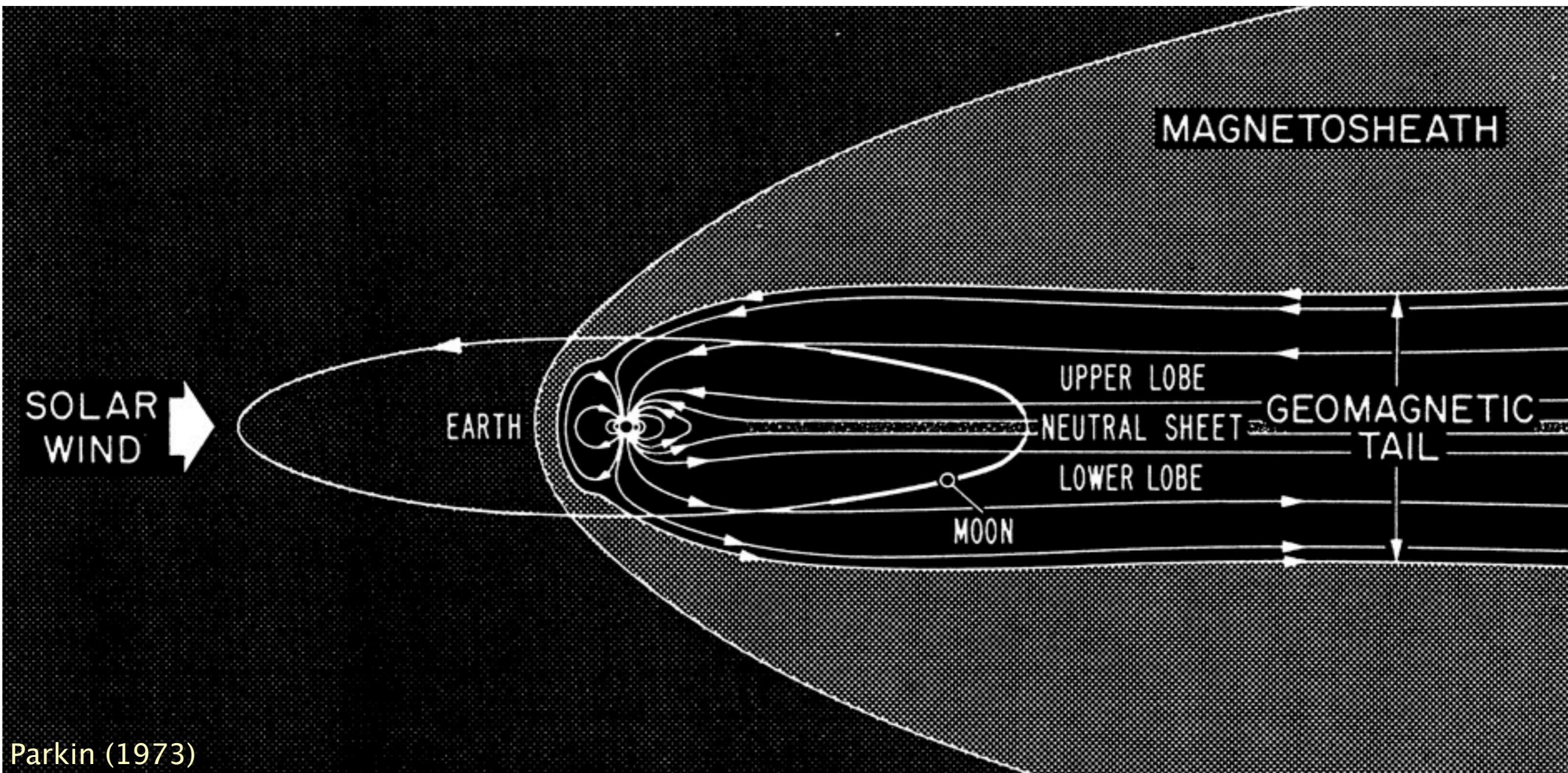
1997: Moon sounding with the Earth





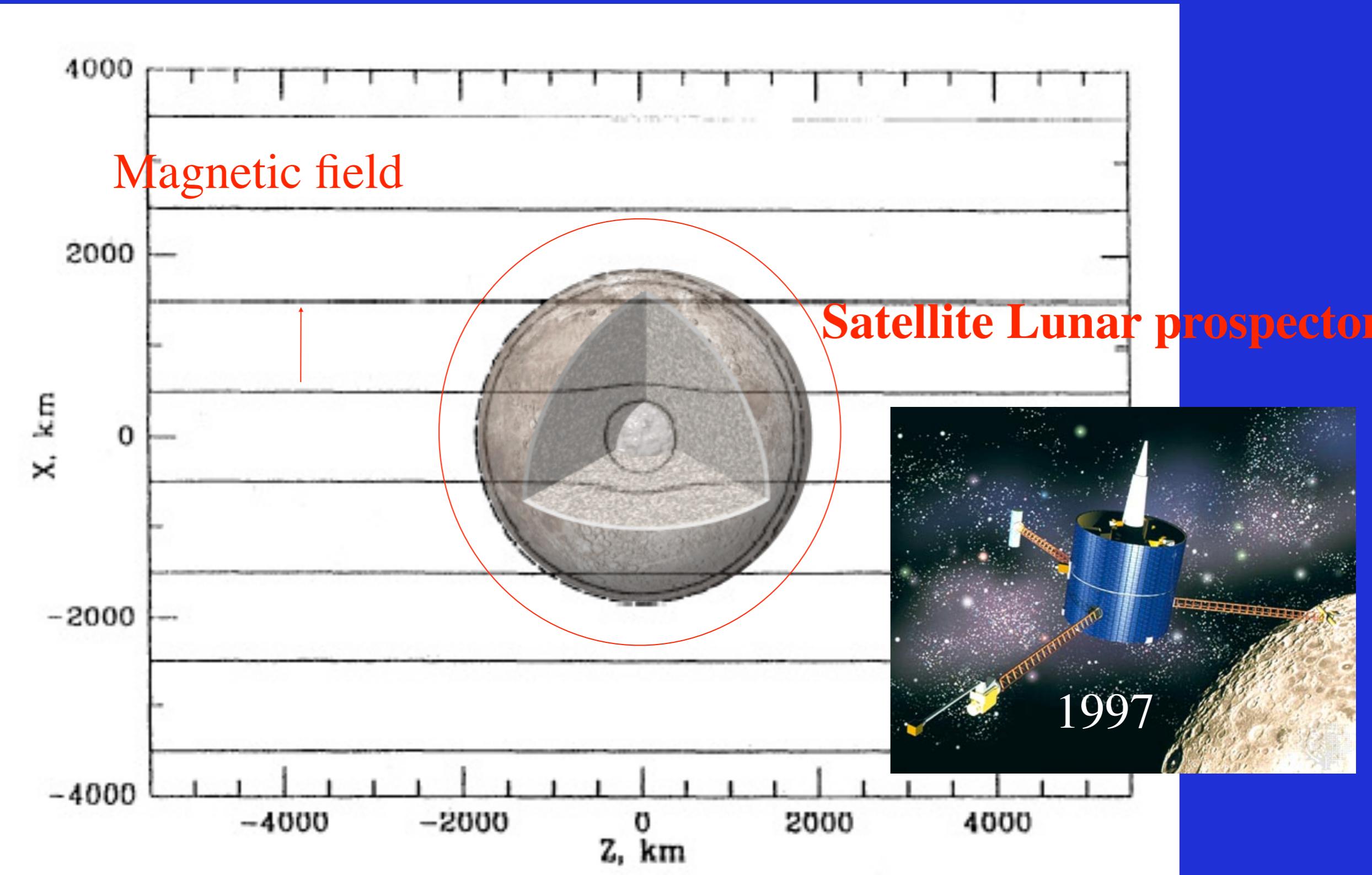
Moon's Orbit

The magnetic environment of the Moon



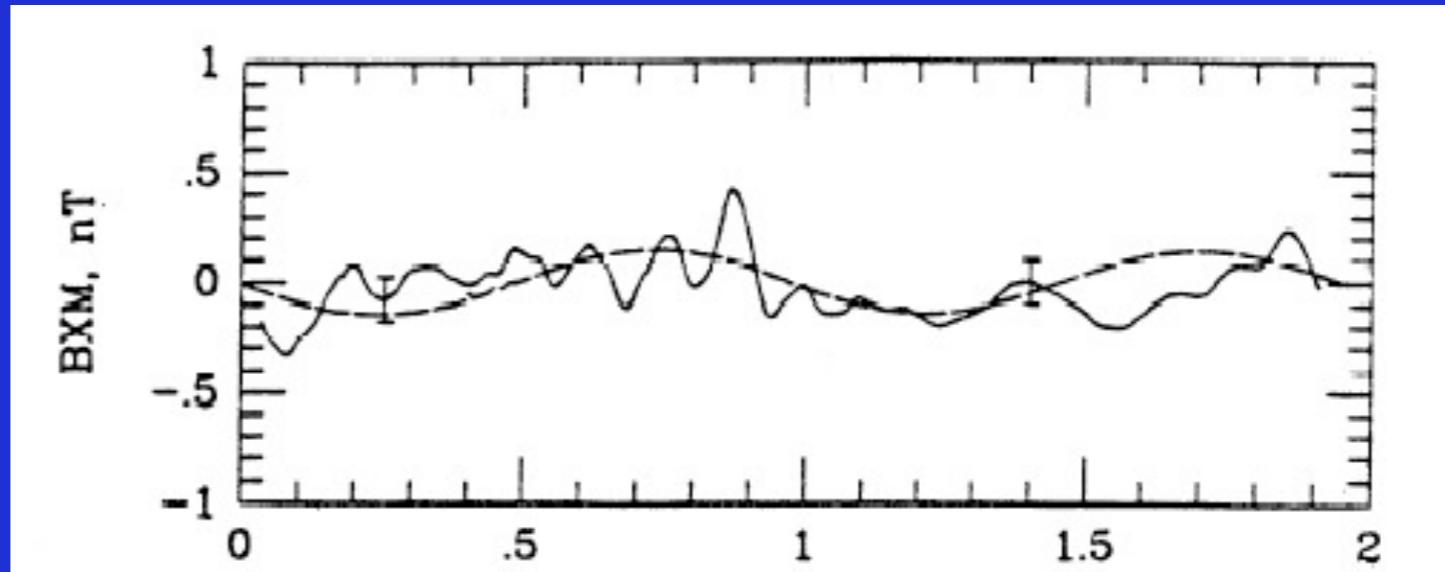
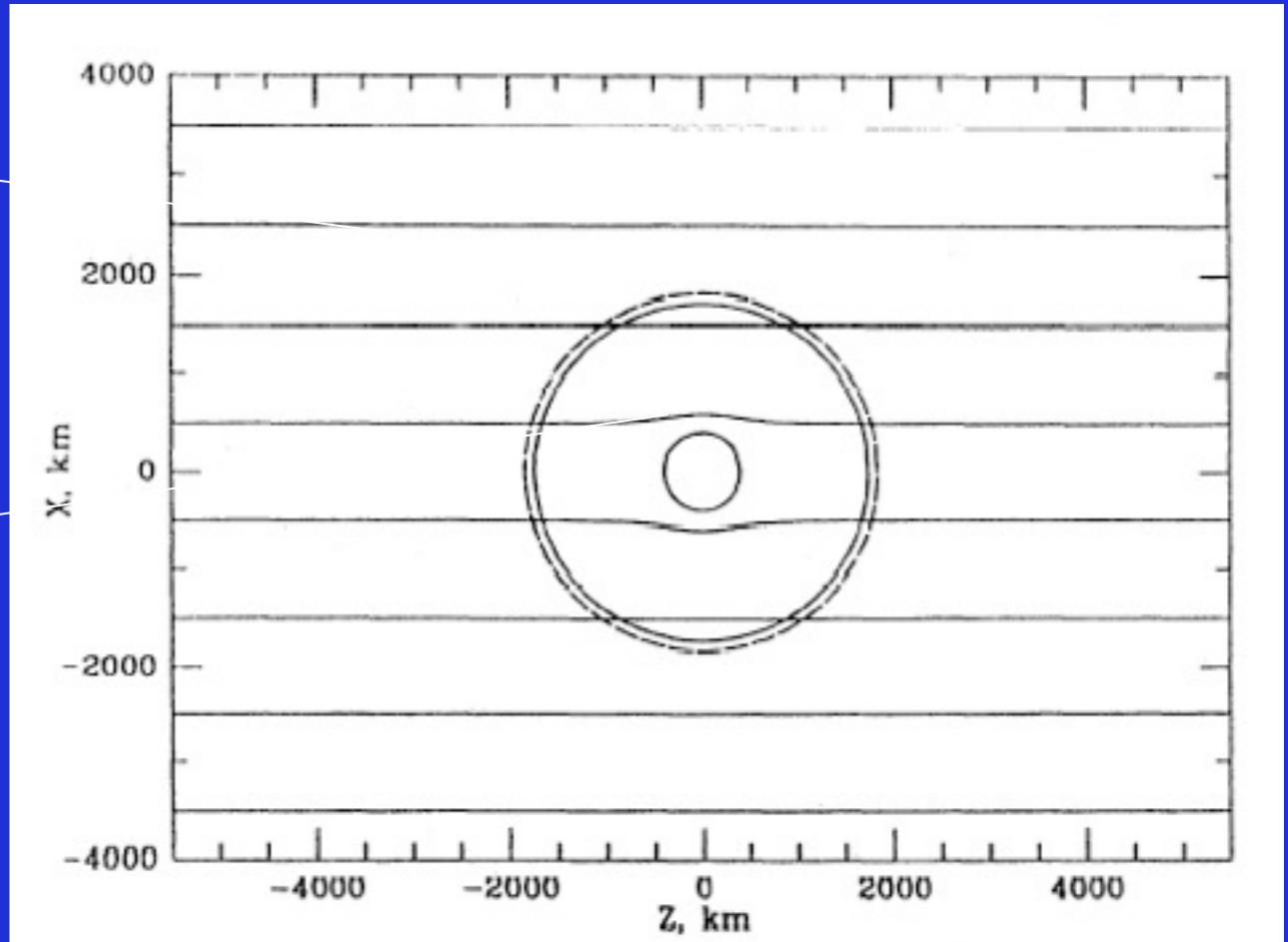
Parkin (1973)

The most precise measurements of the Moon's field are made on the hemisphere that is partially shielded against the solar wind, and for about 2 days per month when the Moon passes through the Earth's geomagnetic tail lobe.



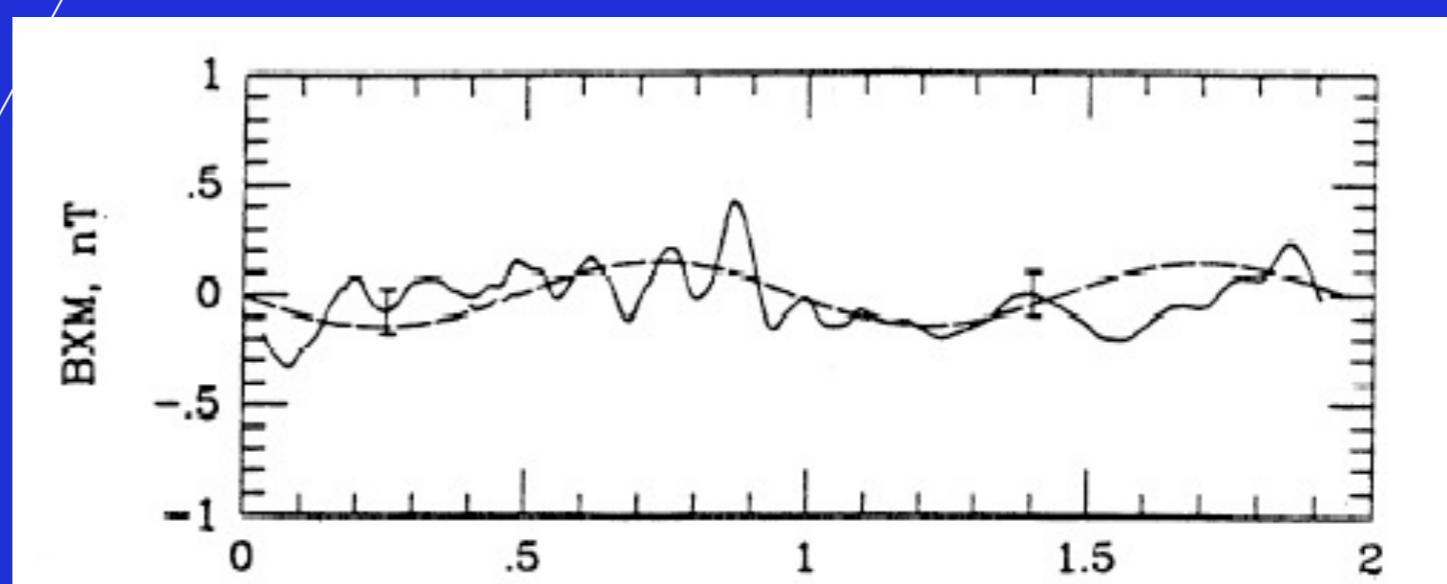
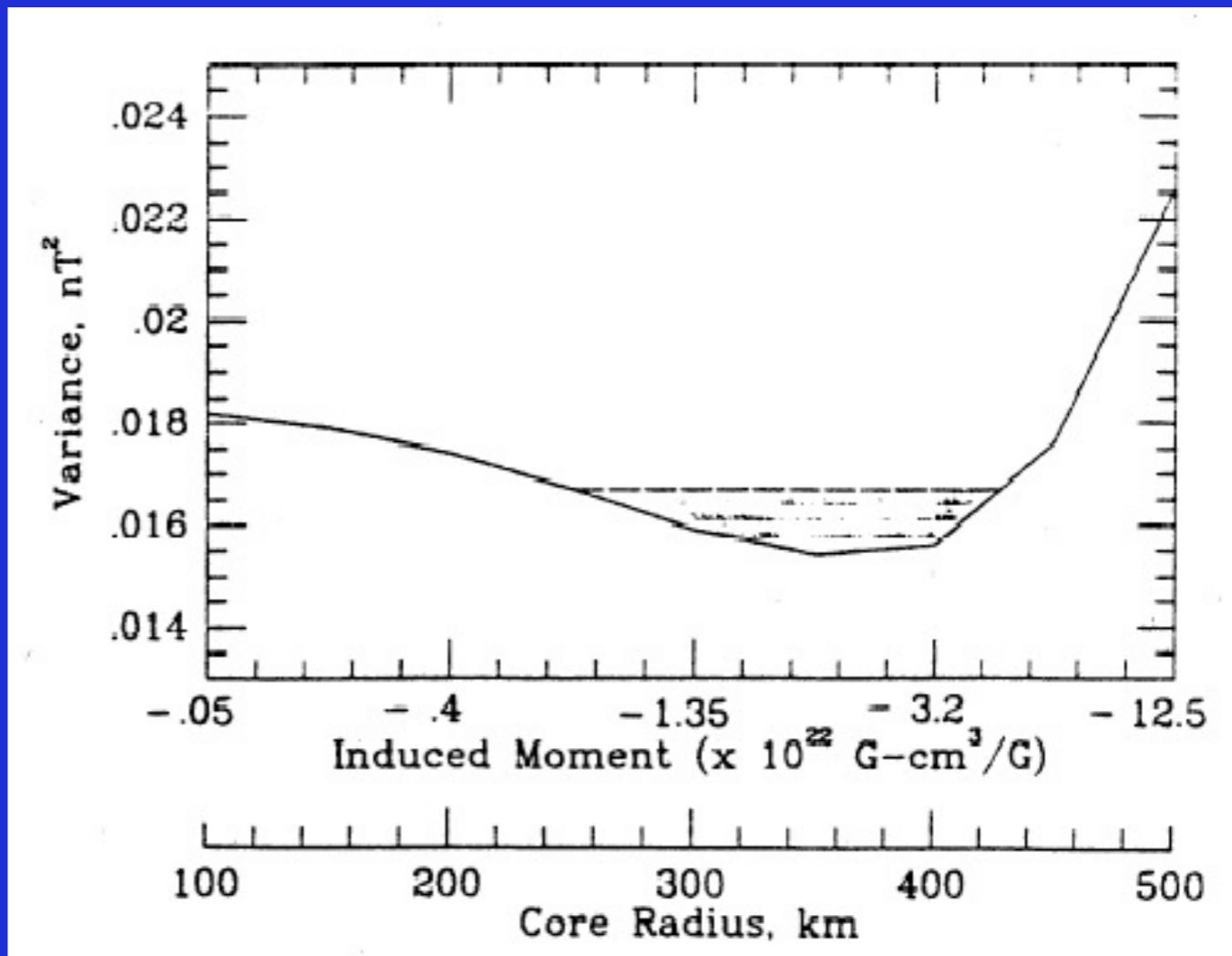
Lunar prospector magnetic sounding

- Primary magnetic field is the magnetic field of the geotail (12-16nT)
- Magnetic field is slightly expelled from the iron moon core
- A low altitude orbiting satellite with magnetometer (Lunar Prospector) measure the small (0.4 nT) perturbation
- Best fit is achieved with a metallic core of 400 km

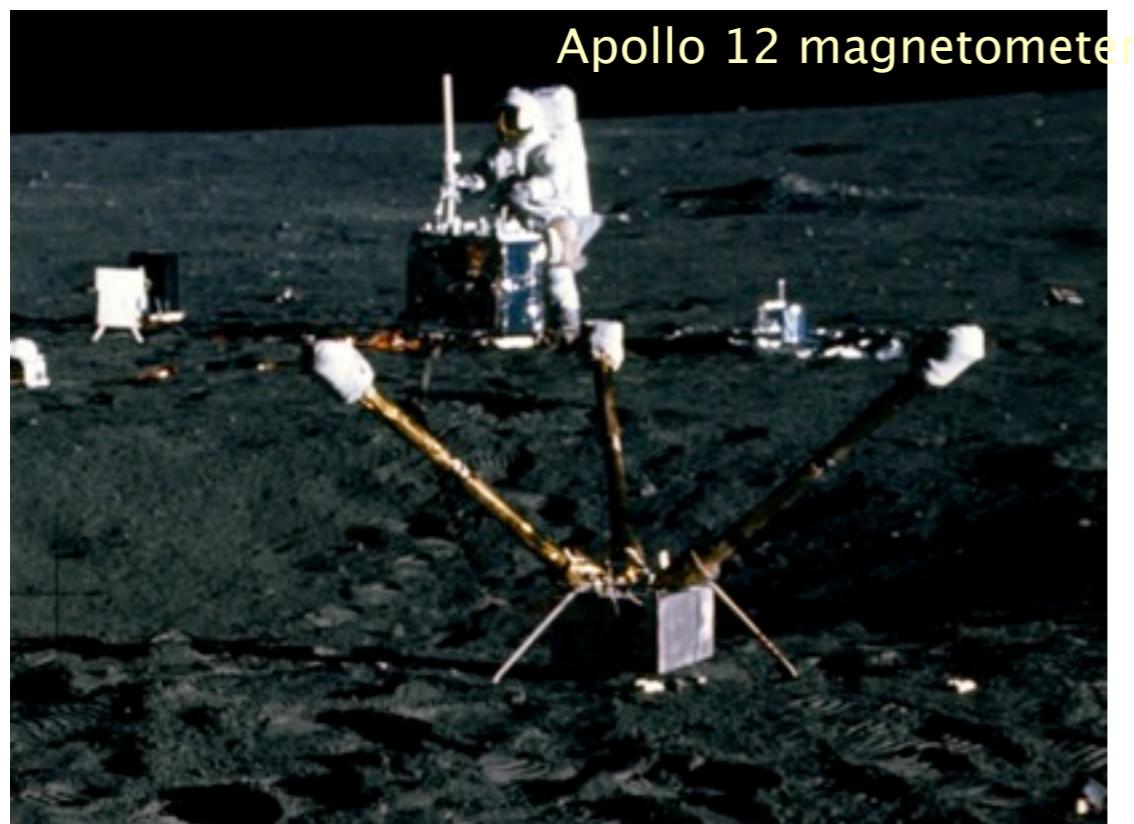


Lunar prospector magnetic sounding

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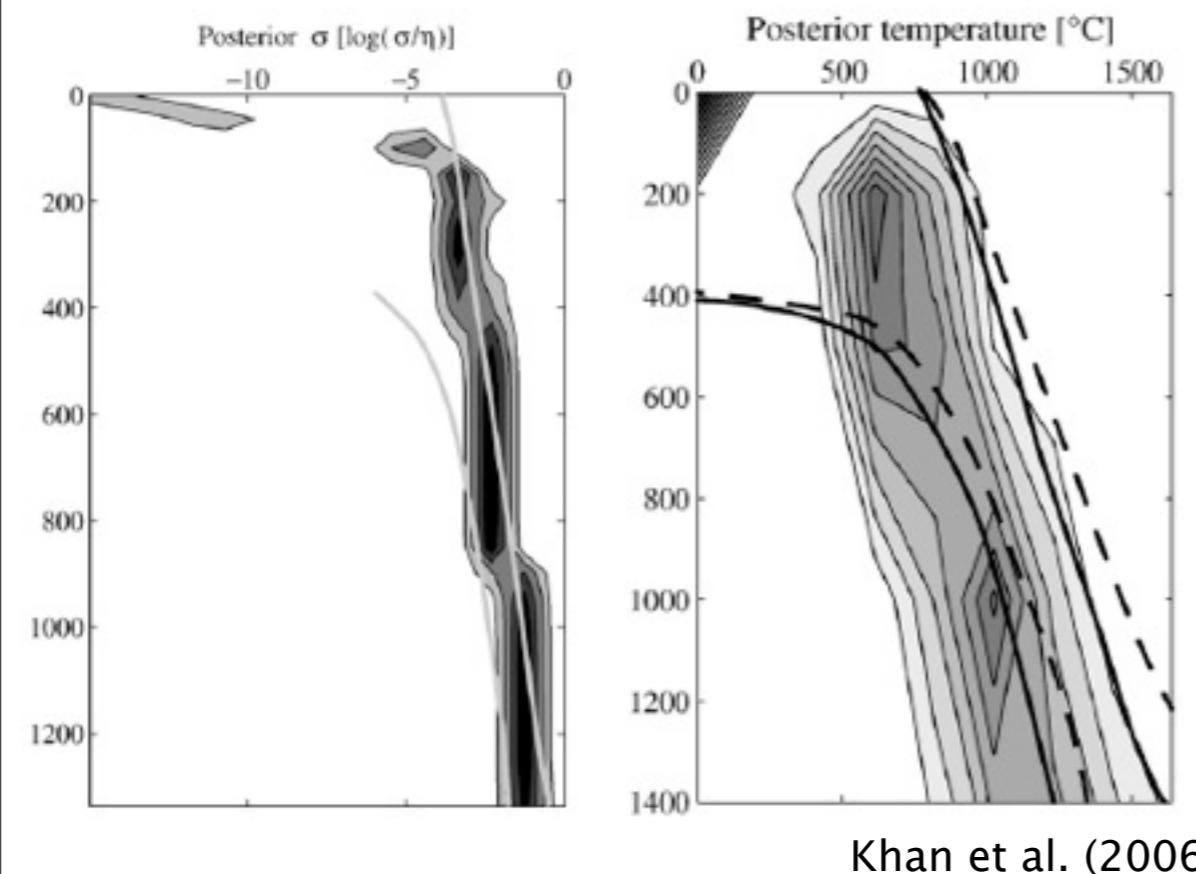


Time-variable magnetic induction signals

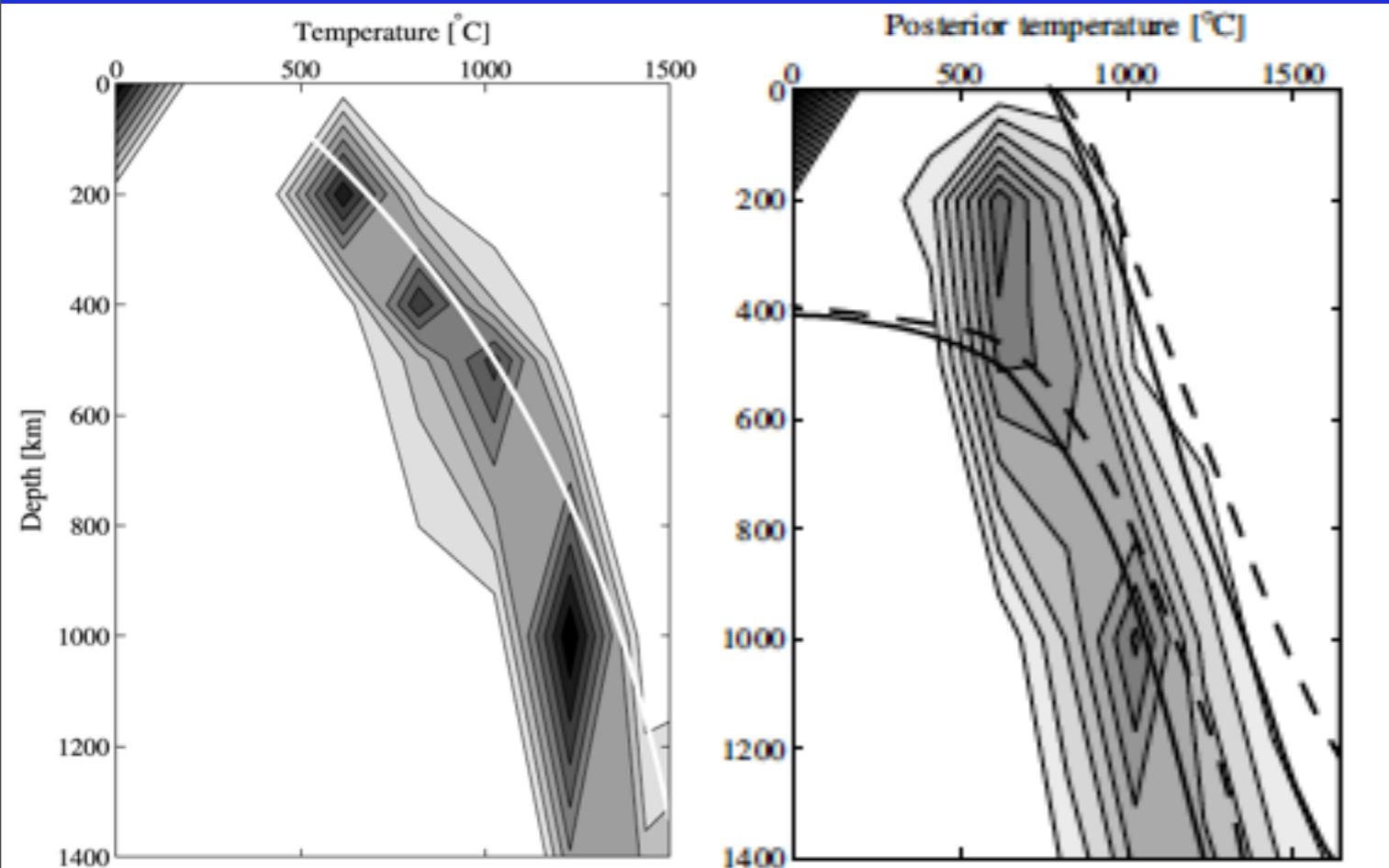


The electrical conductivity profile can be obtained by measuring the inducing field from orbit and the resulting magnetic field on the surface.

Inferred temperature profile depends upon a limited number of electrical conductivity measurements.

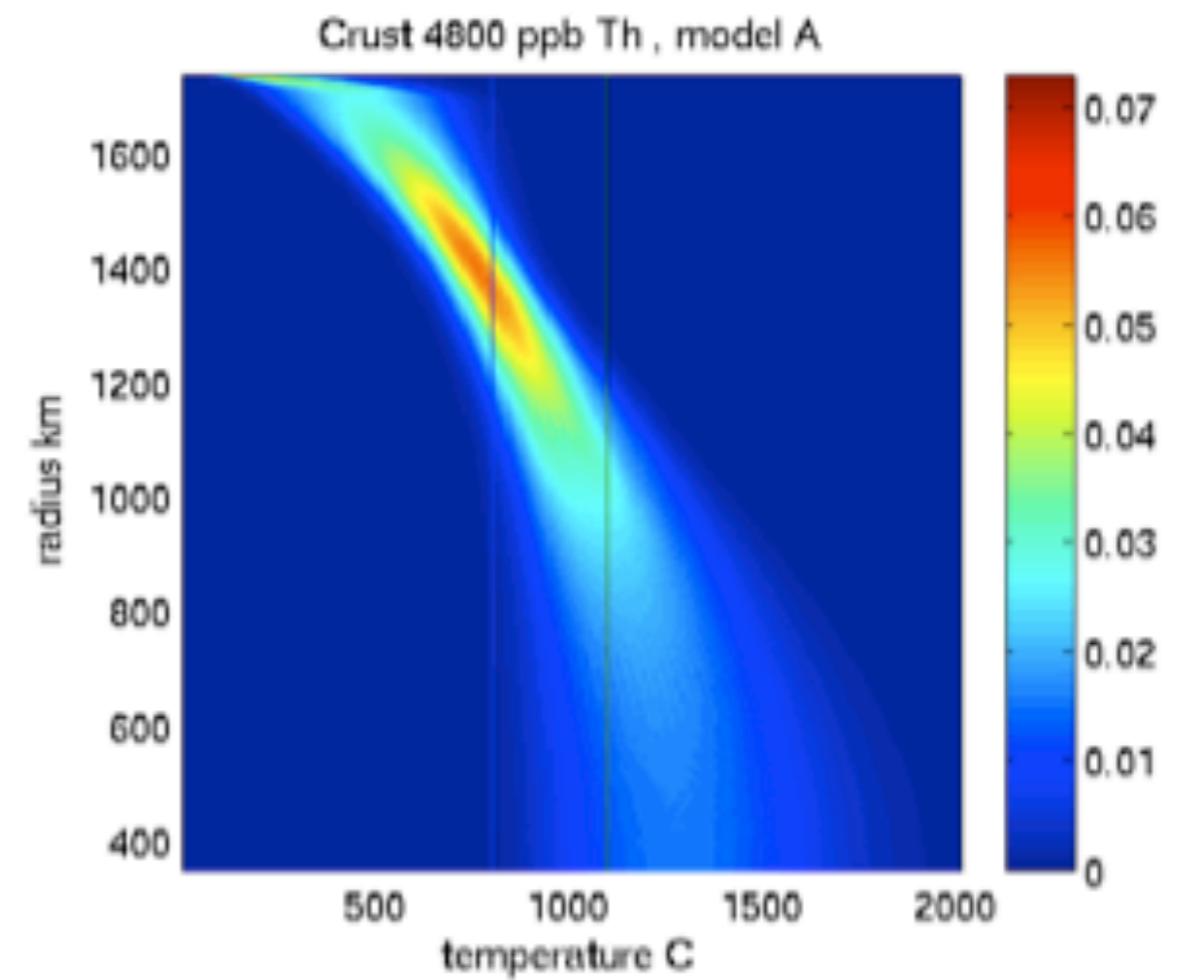


Other temperatures

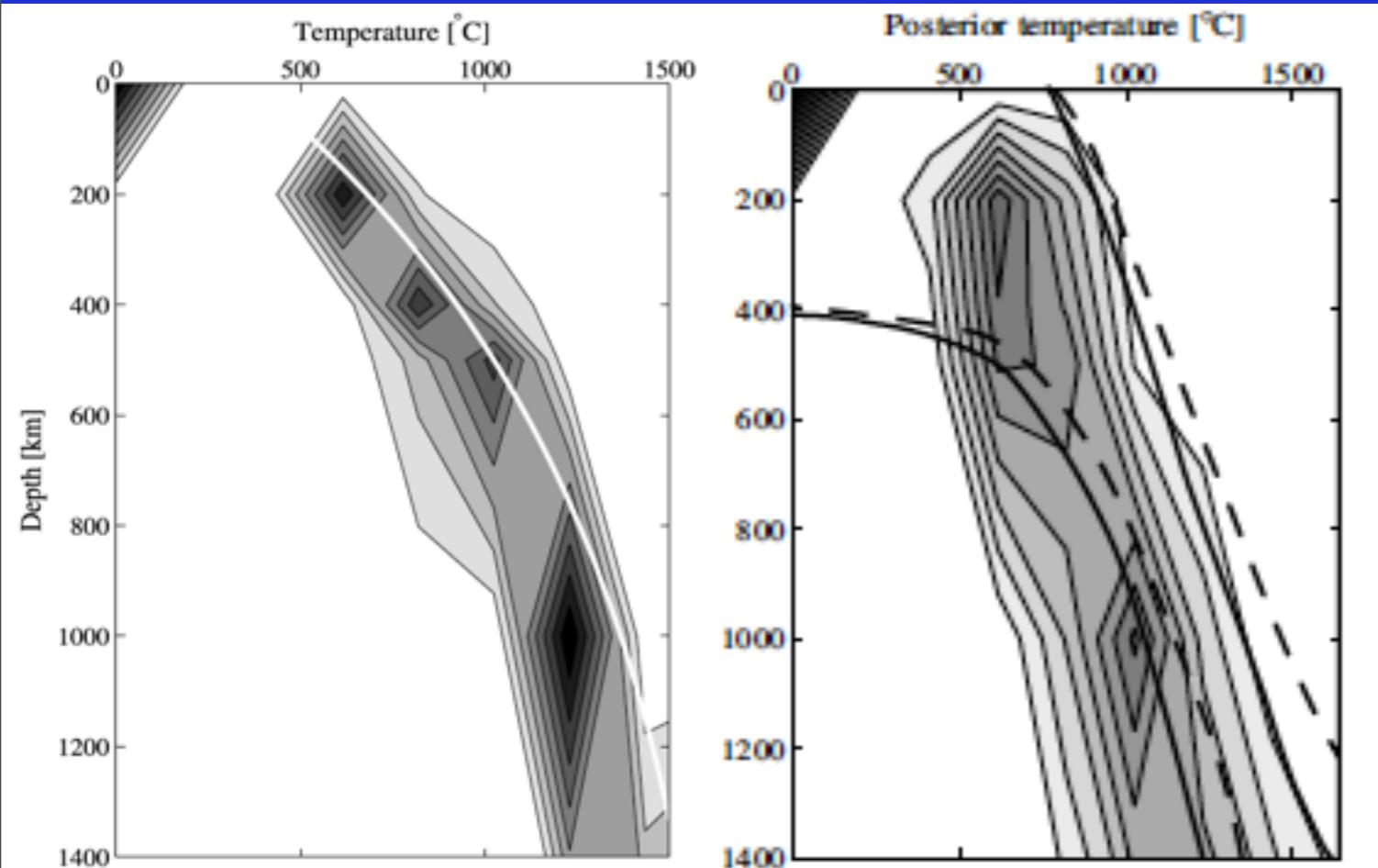


Khan et al, 2006
 (direct inversion
 of seismic data)

Khan et al, 2007
 (direct inversion
 of magnetic data)

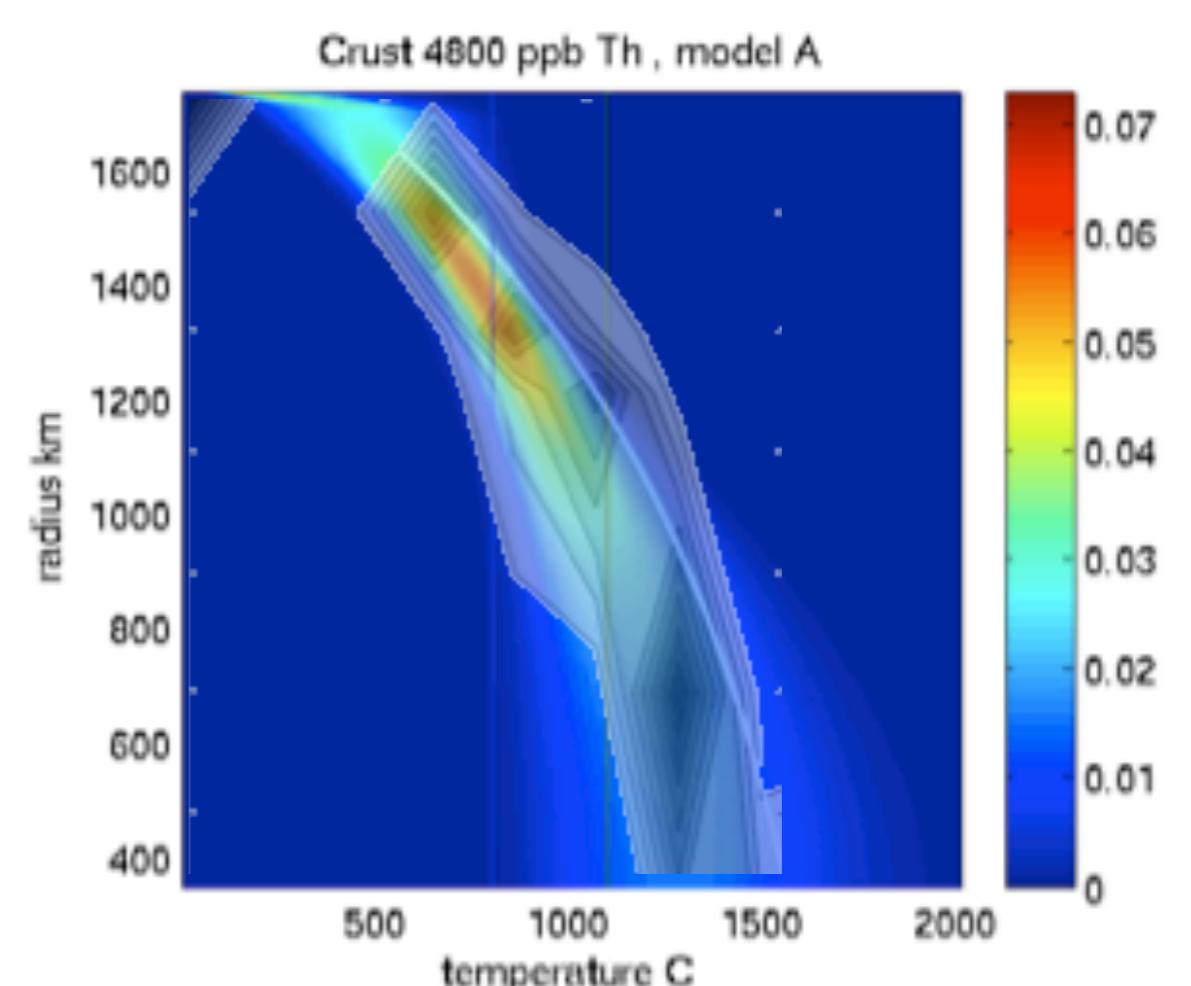


Other temperatures

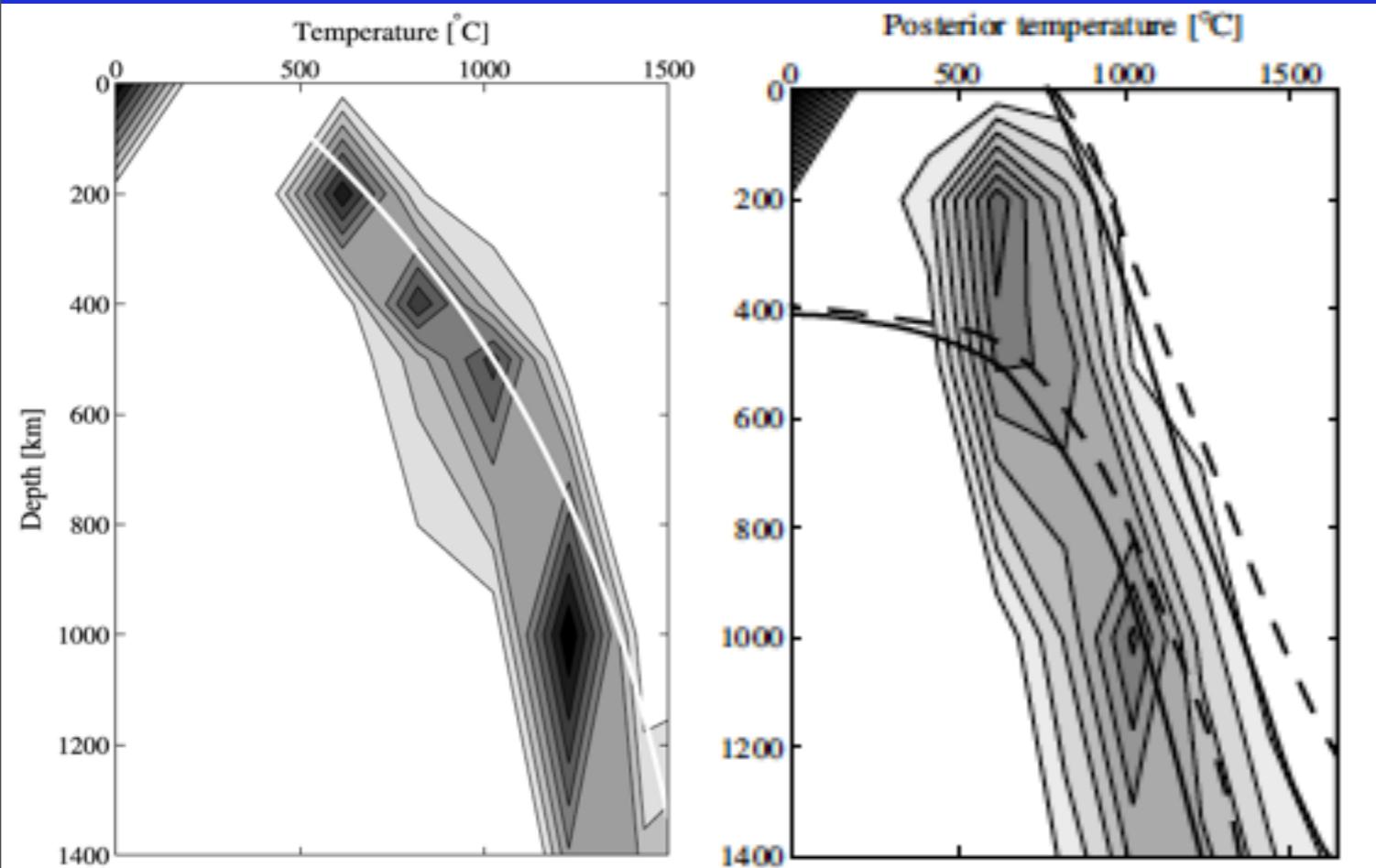


Khan et al, 2006
 (direct inversion
 of seismic data)

Khan et al, 2007
 (direct inversion
 of magnetic data)

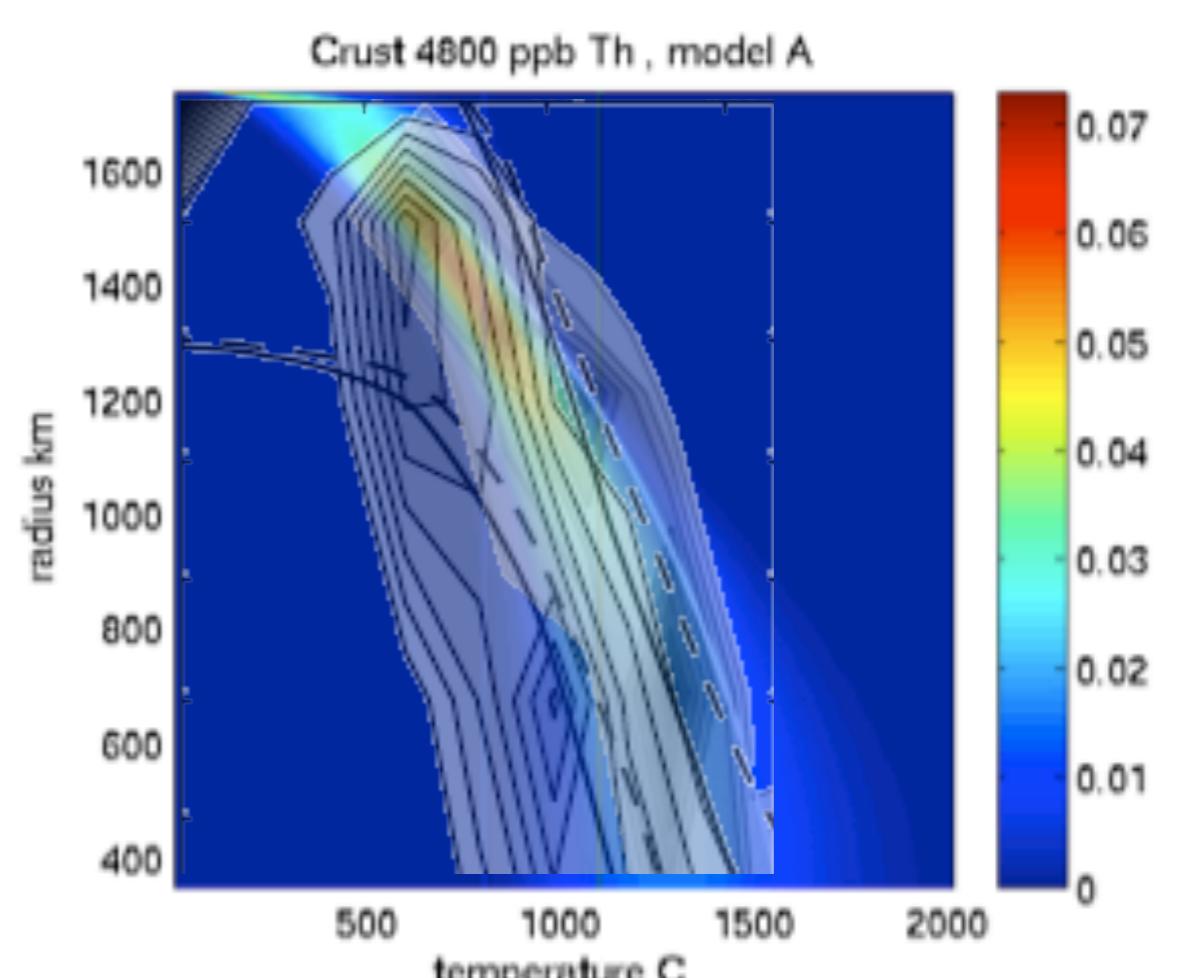


Other temperatures

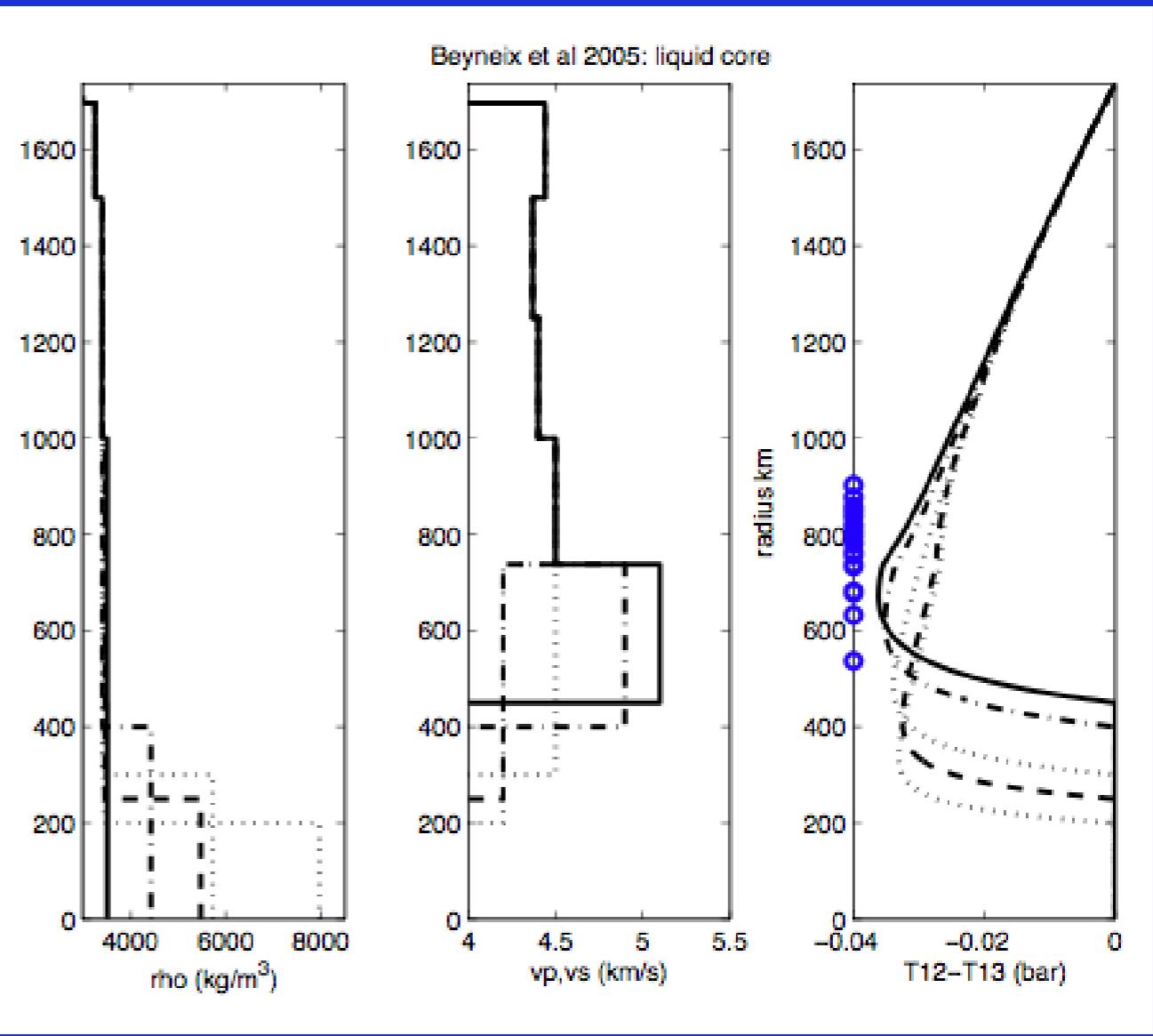
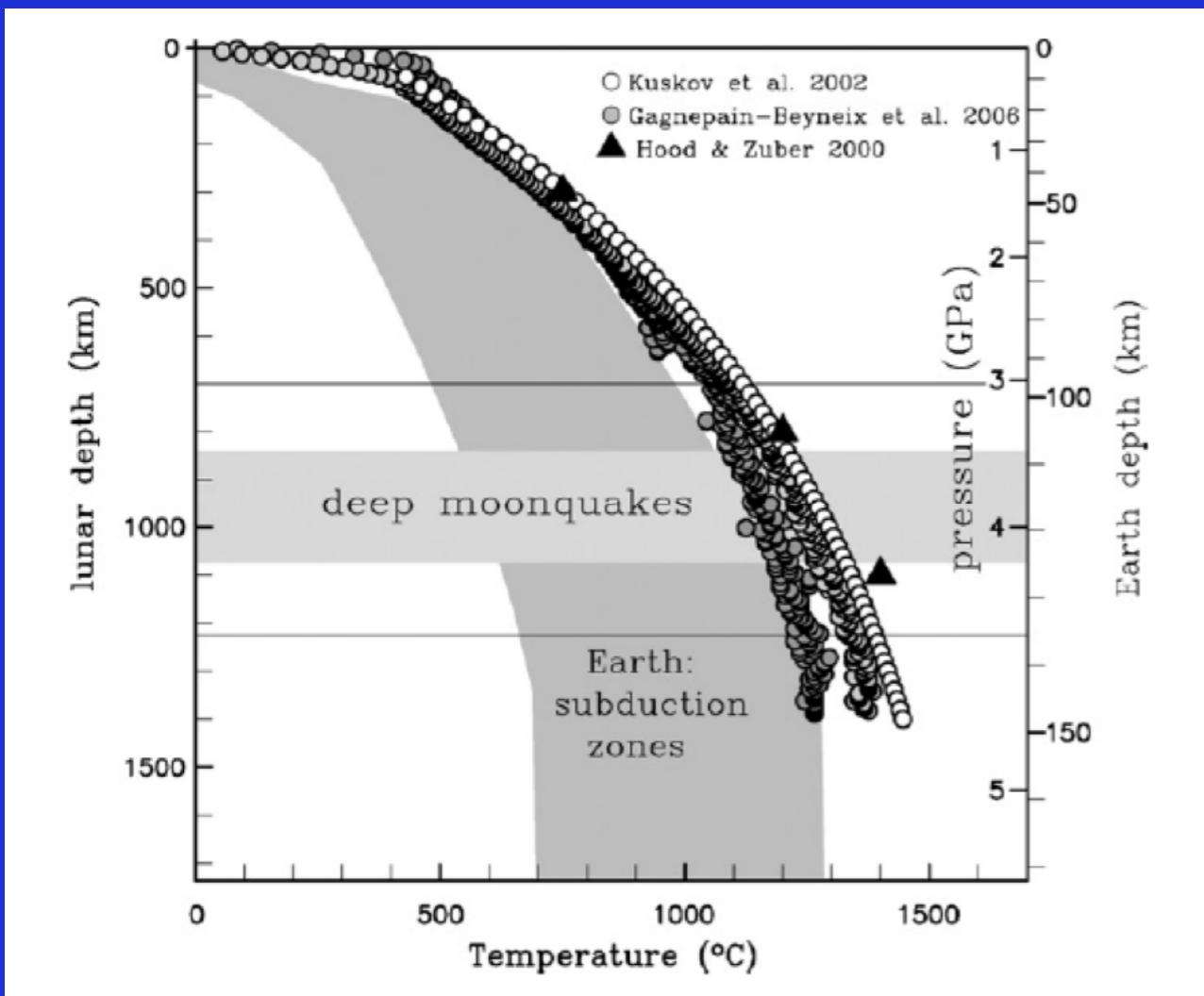


Khan et al, 2006
 (direct inversion
 of seismic data)

Khan et al, 2007
 (direct inversion
 of magnetic data)



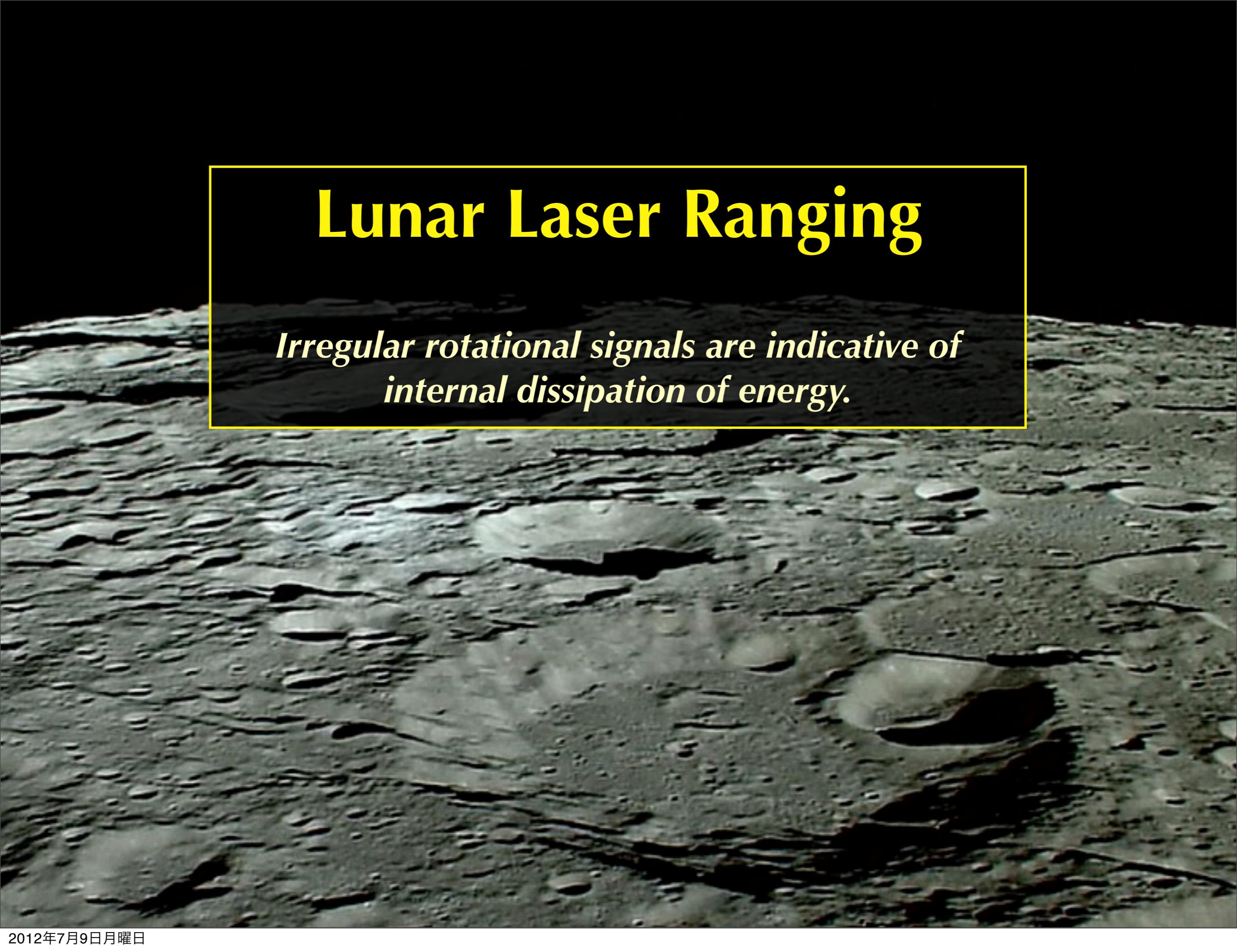
Tidal stresses and core size

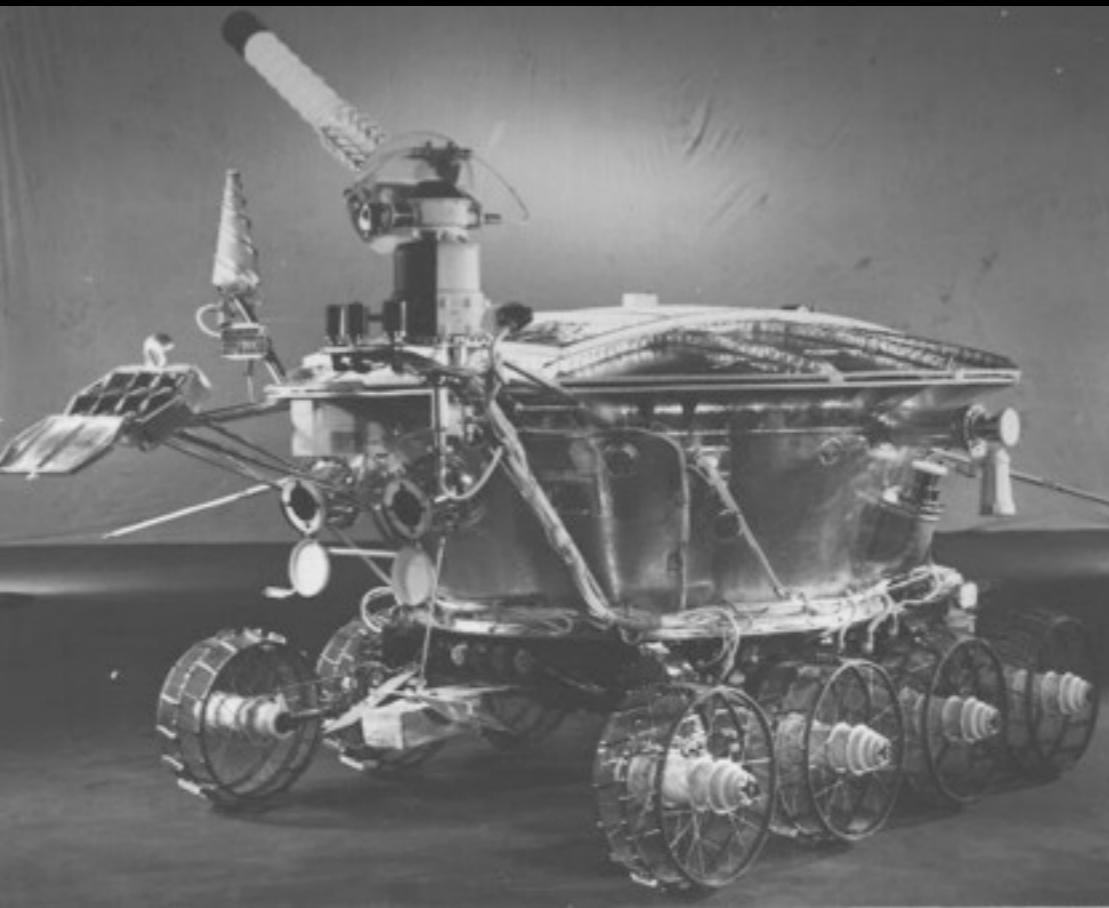
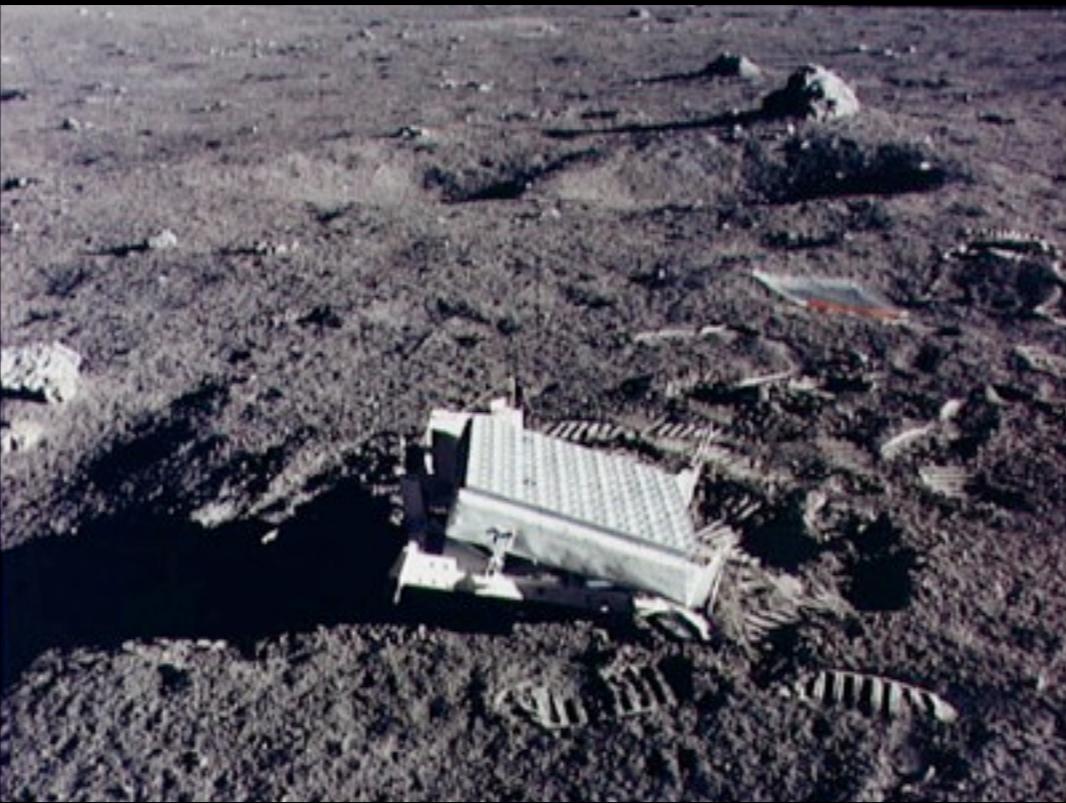


- Focal mechanism of the deep moonquakes remains to be better known but liquid core provide maximum stress at the deep moonquake depth
- Large core need a high (and maybe too high) Vs velocity in the lower mantle to match with the k_2 value
- Temperature are above the maximum temperature of subduction zone but in a possible dryer mantle than subduction zone or Earth upper mantle ($Q_s \sim 300$ on the deep Moon, $Q_s \sim 150$ on Earth)

Lunar Laser Ranging

Irregular rotational signals are indicative of internal dissipation of energy.





Lunar Laser Ranging can determine the Earth–Moon distance to an accuracy of ~2 cm.

By using ranges to several stations, it is possible to reconstruct the orientation of the Moon.

Rotational signals

Date: 2005 Sep 1 02:23:28 UT



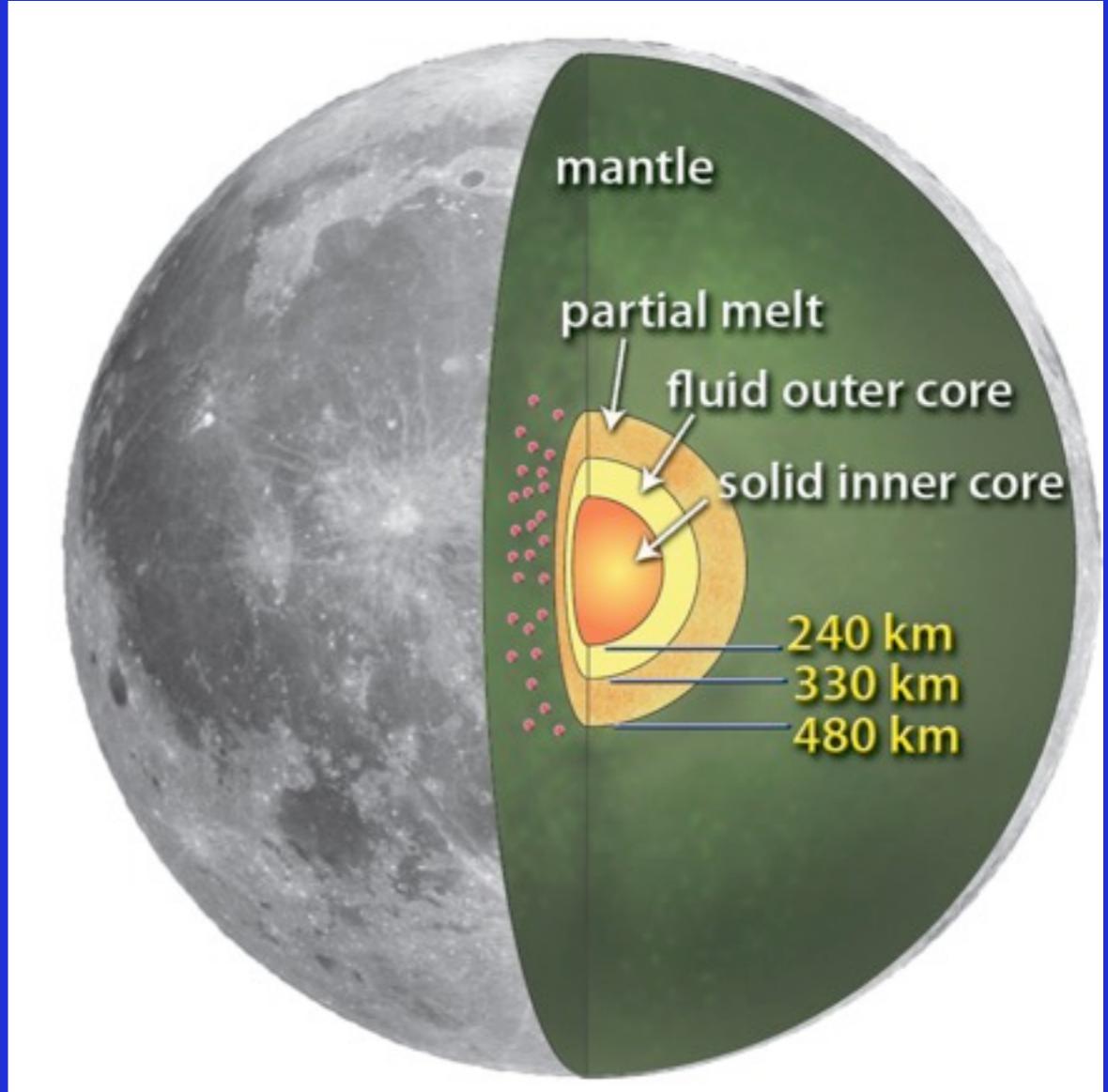
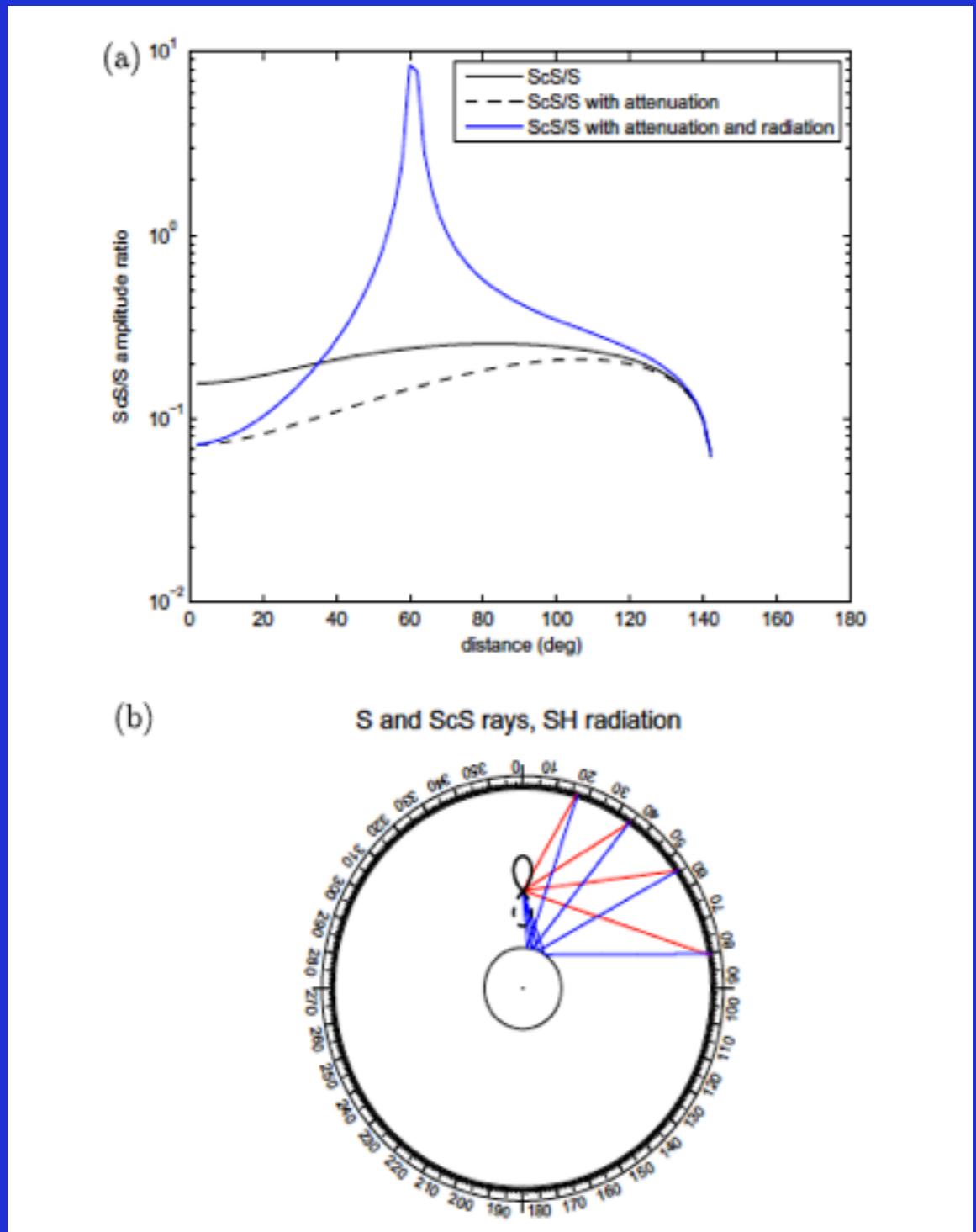
Tom Ruen

Optical librations are caused by the Moon's eccentric and inclined orbit.

Physical librations are caused by torques on the solid body of the Moon by Earth's gravity field. Velocity differences at the core-mantle boundary, as well as dissipation within the solid body, give rise to a distinctive rotational signatures.

The Moon possesses a molten core. Dissipation of energy is also occurring deep in the solid portion of the lunar mantle ($Q=37-60$). Is the deep mantle partially molten?

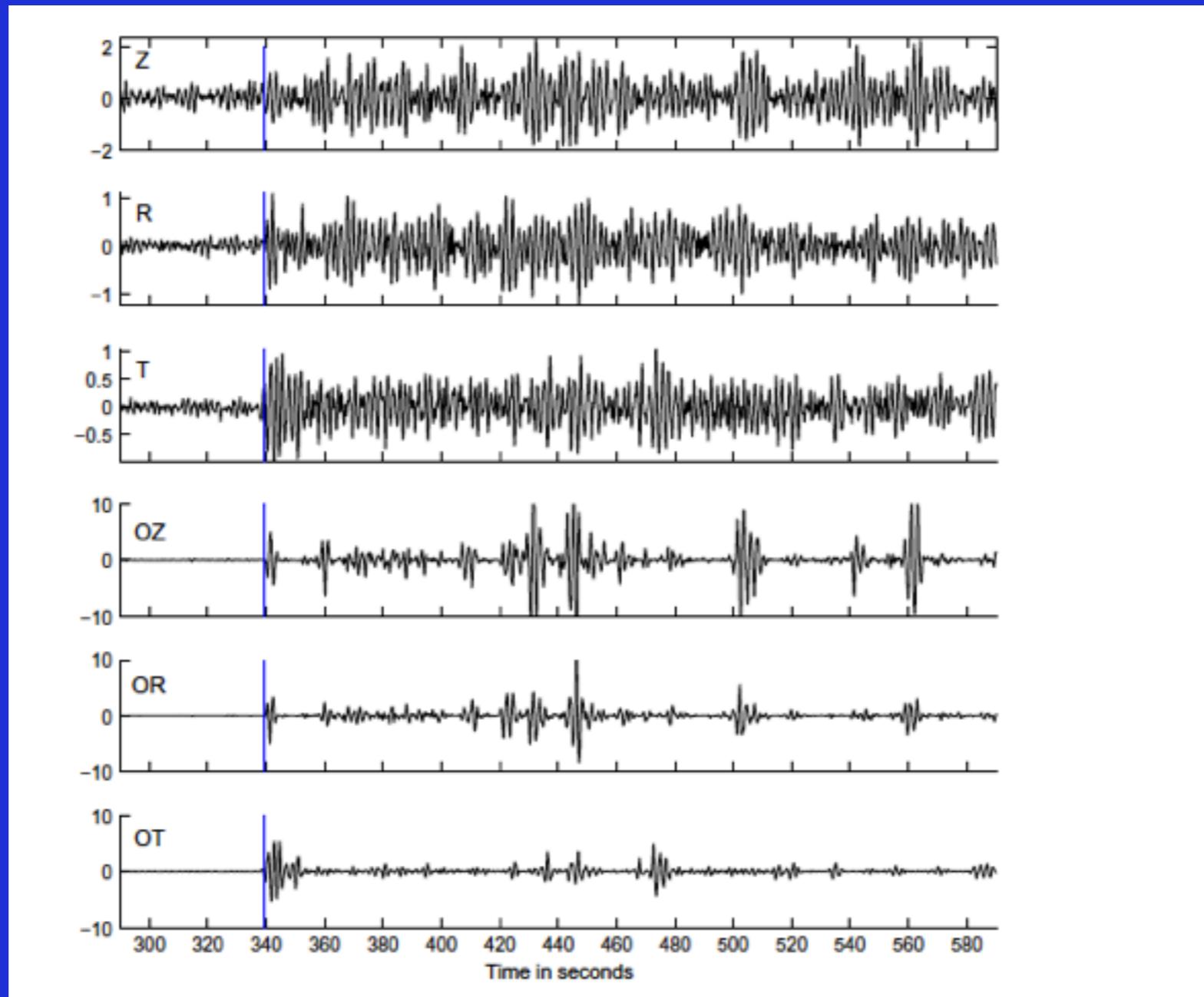
Core Seismic Phases



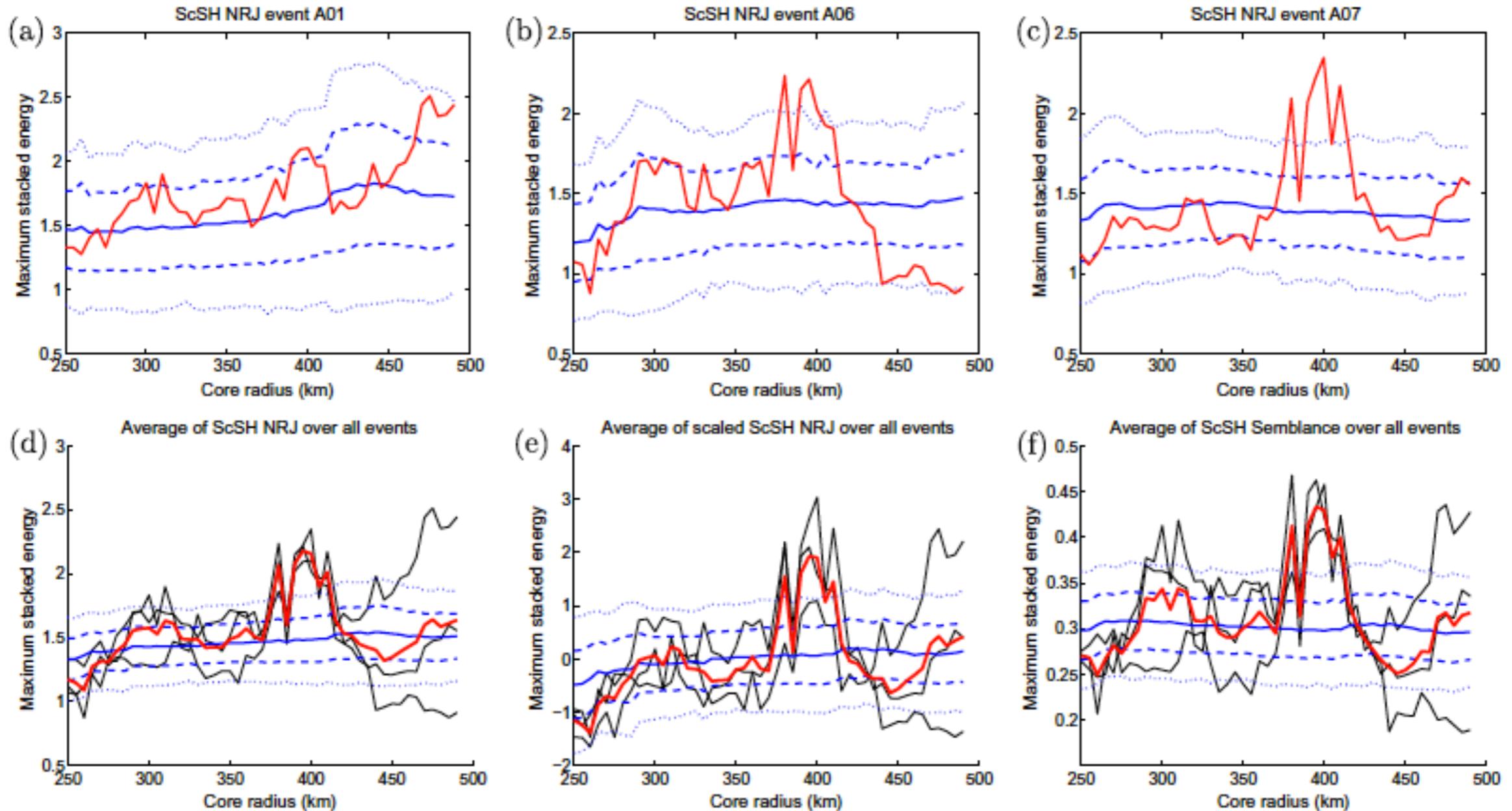
Weber et al, 2011
Garcia et al, 2011

Methodology

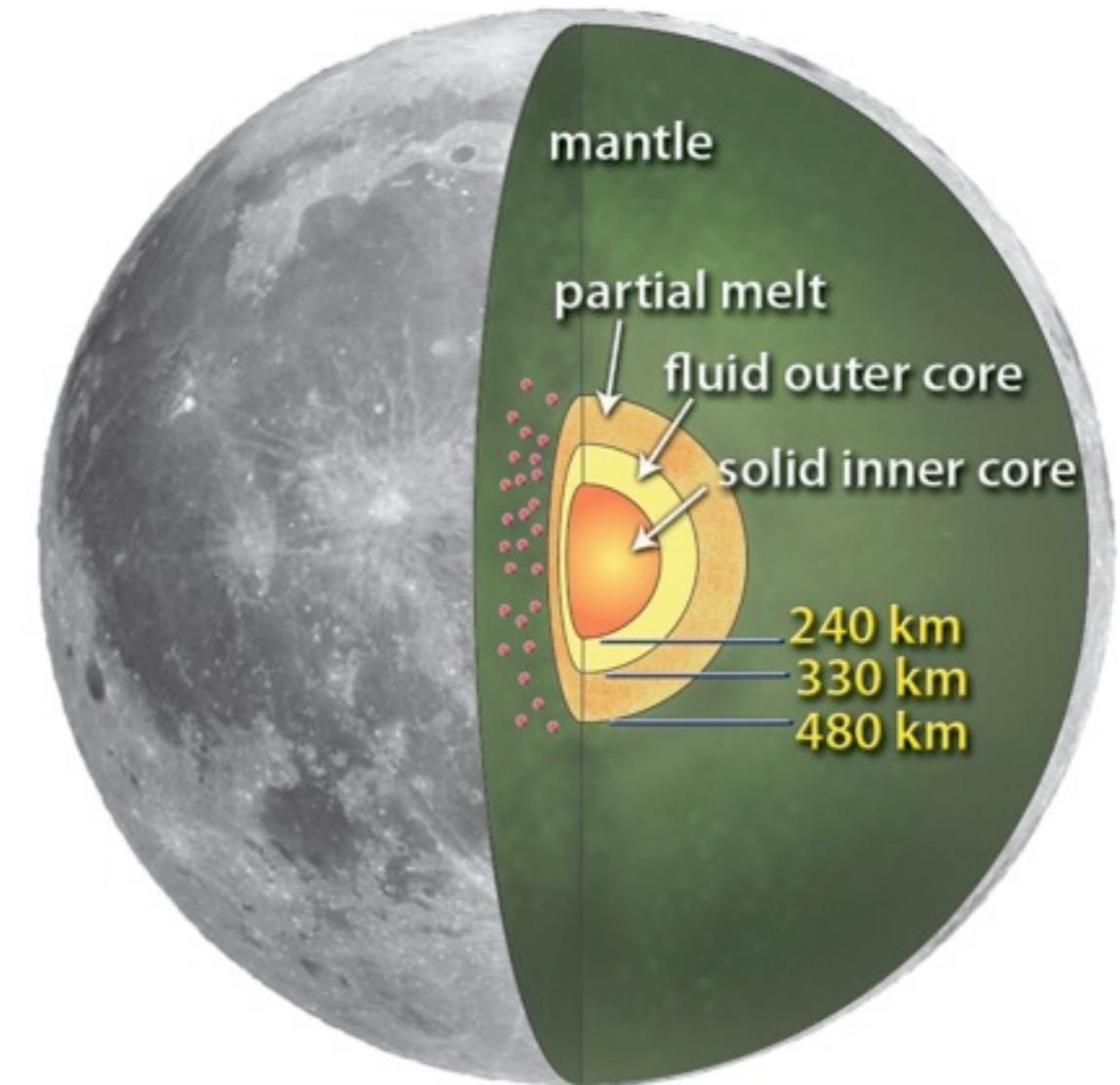
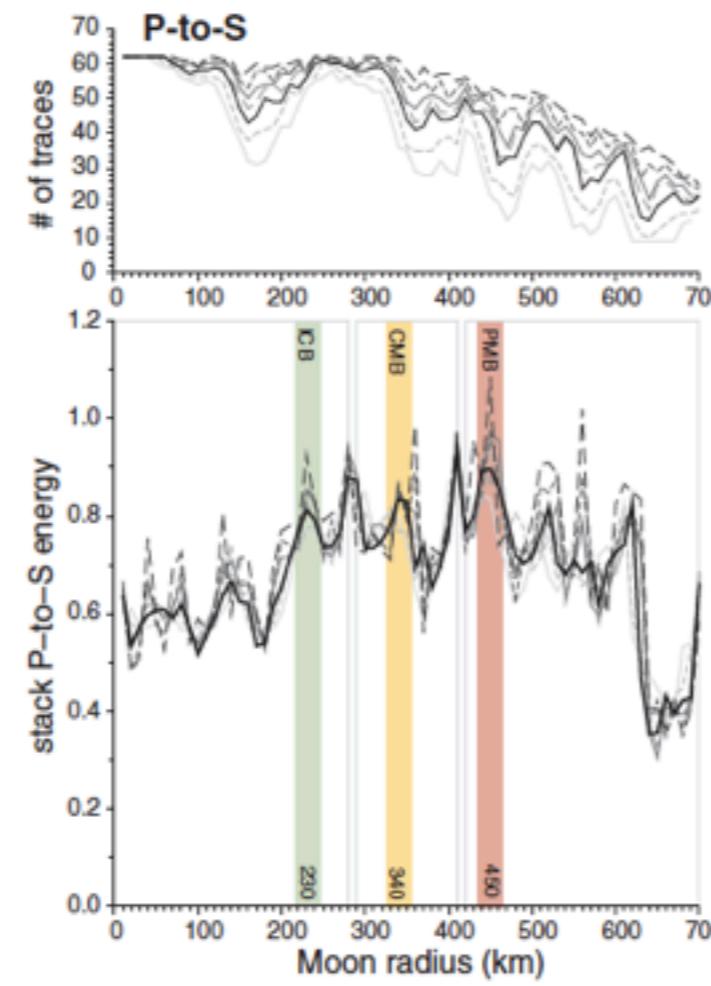
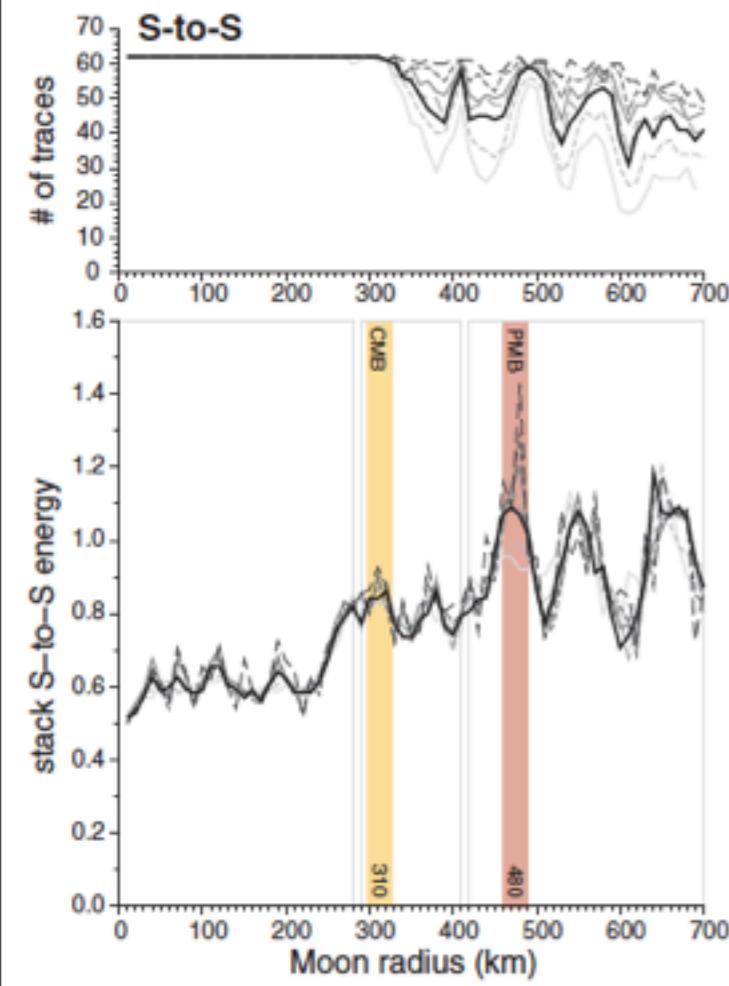
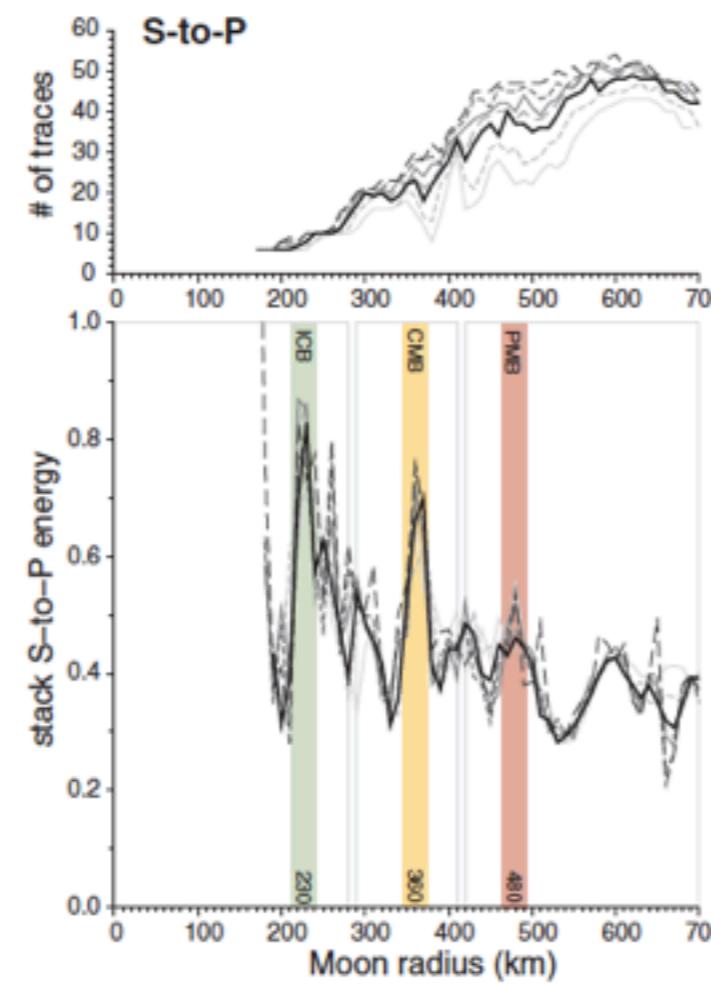
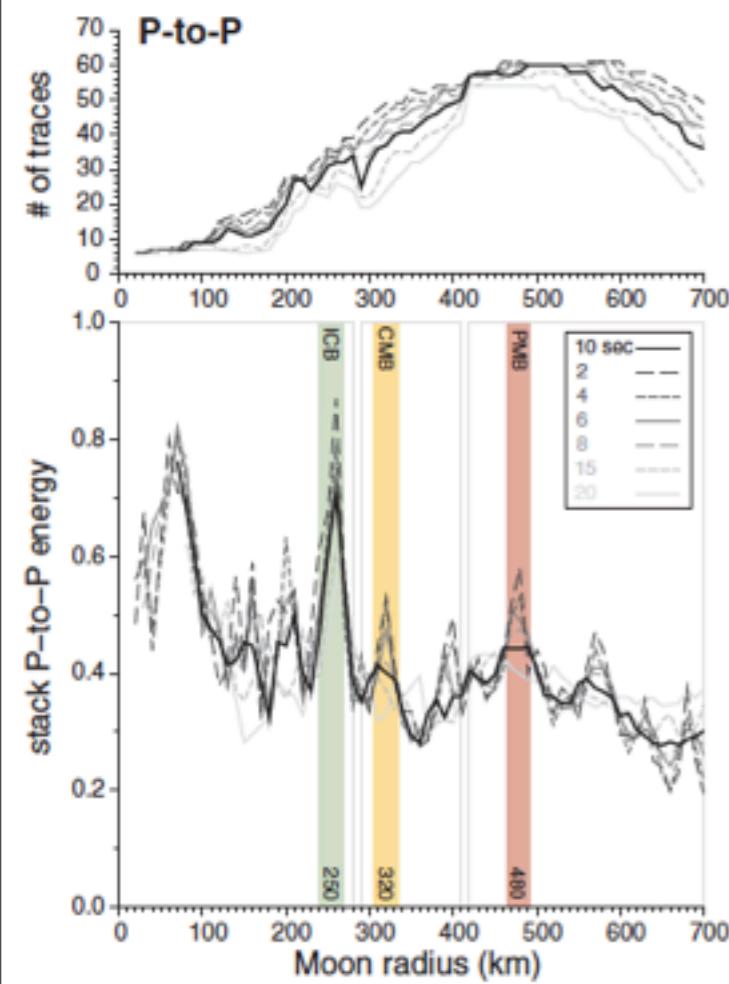
- Core phases are weak signals
 - DMQ stacking + All stations stacks
 - Use of Polarisation filters + Stations corrections



Results



- Clear identification of reflected energy from a 350-400 km radius reflector



Weber et al. 2011

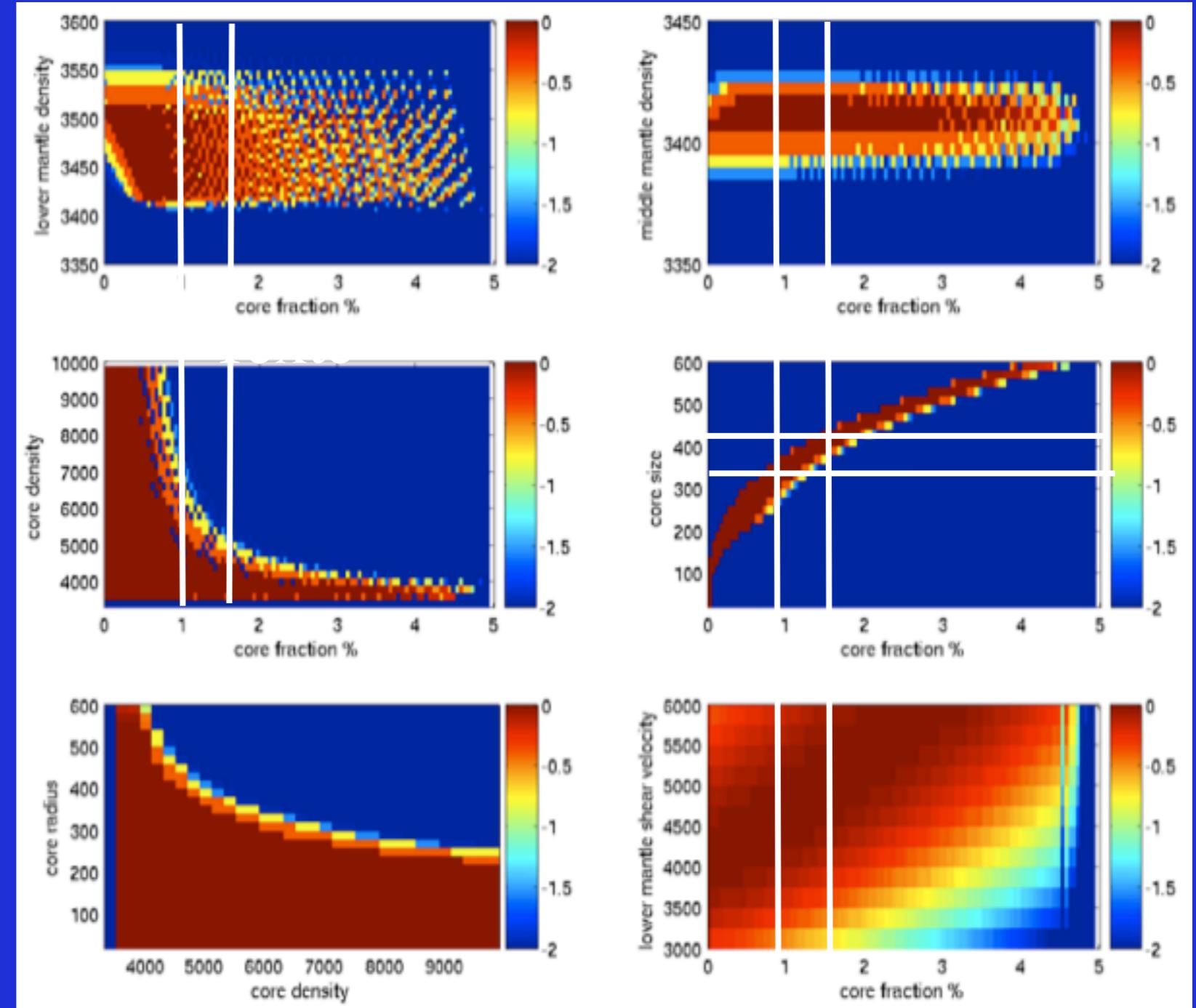
Deep interior and state of core

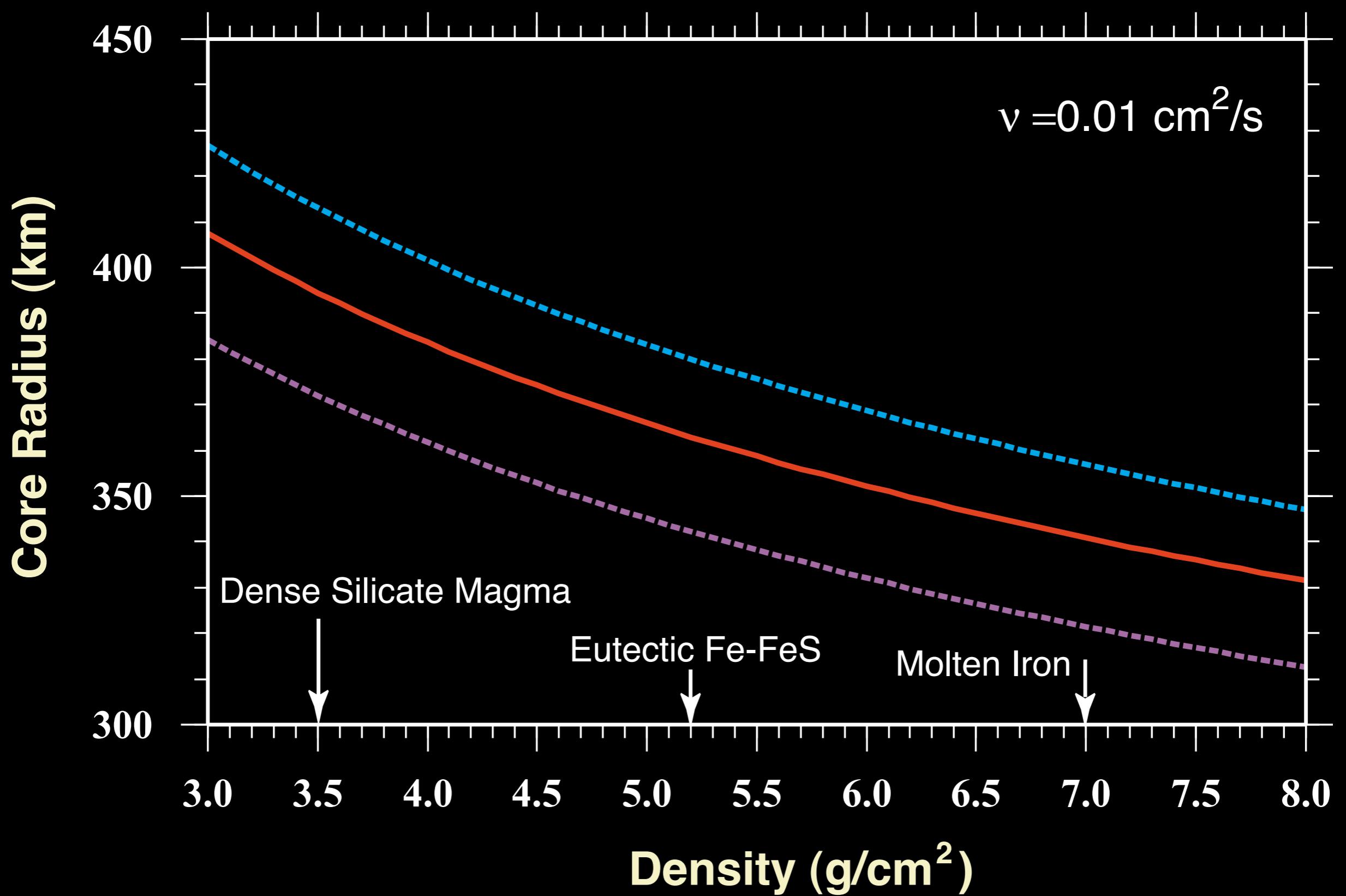
- Upper structure is constrained by seismic data
- Invert only for the structure not resolved by seismic data

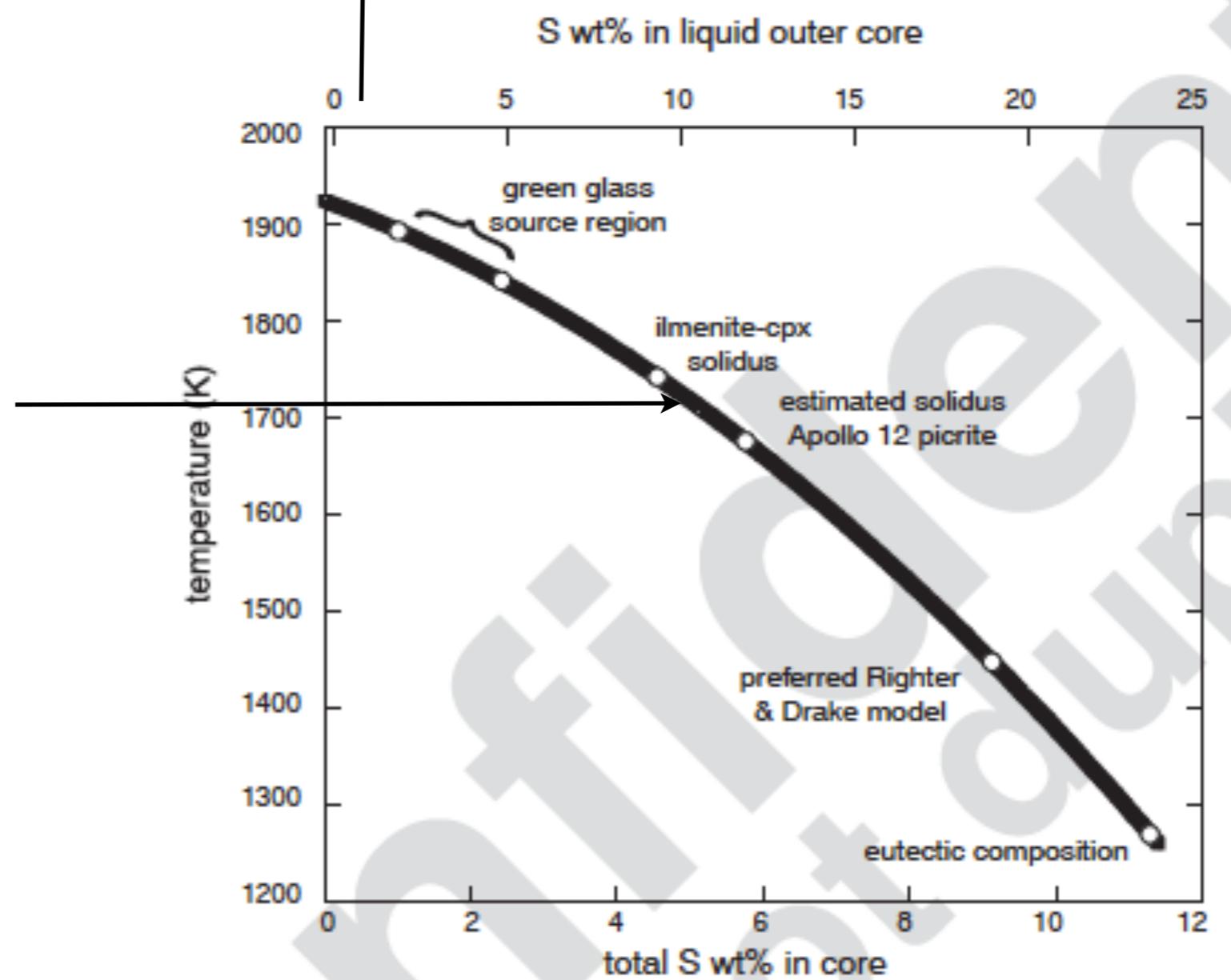
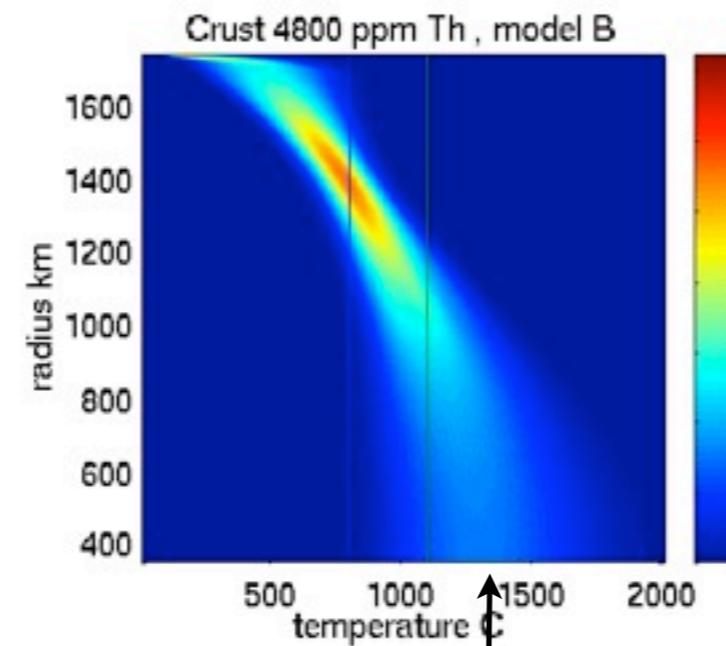
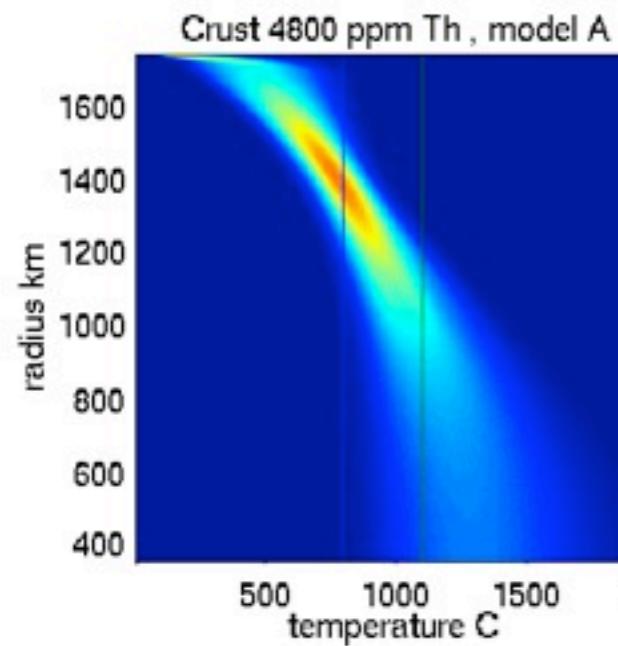
Garcia et al 2011:
 $380 \text{ km} \pm 40 \text{ km}$
 $5200 \pm 1000 \text{ kg/m}^3$

Weber et al 2011:
 $330 \text{ km} \pm 20 \text{ km}$
 $6200 \pm 1000 \text{ kg/m}^3$

Crust 40 km (Beyneix et al., 2005)





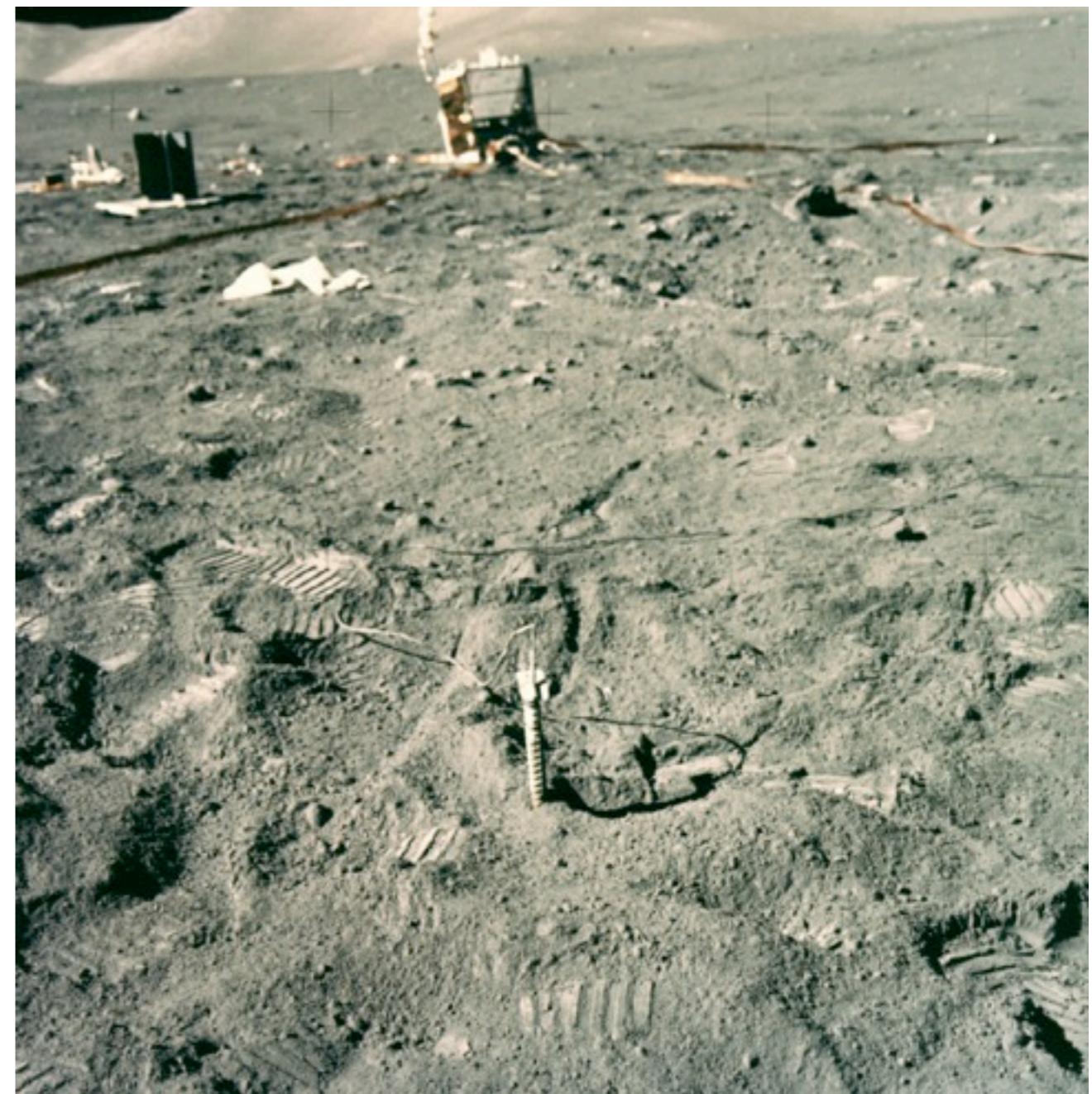


Heat Flow

$$q = k(T) \frac{dT}{dz}$$

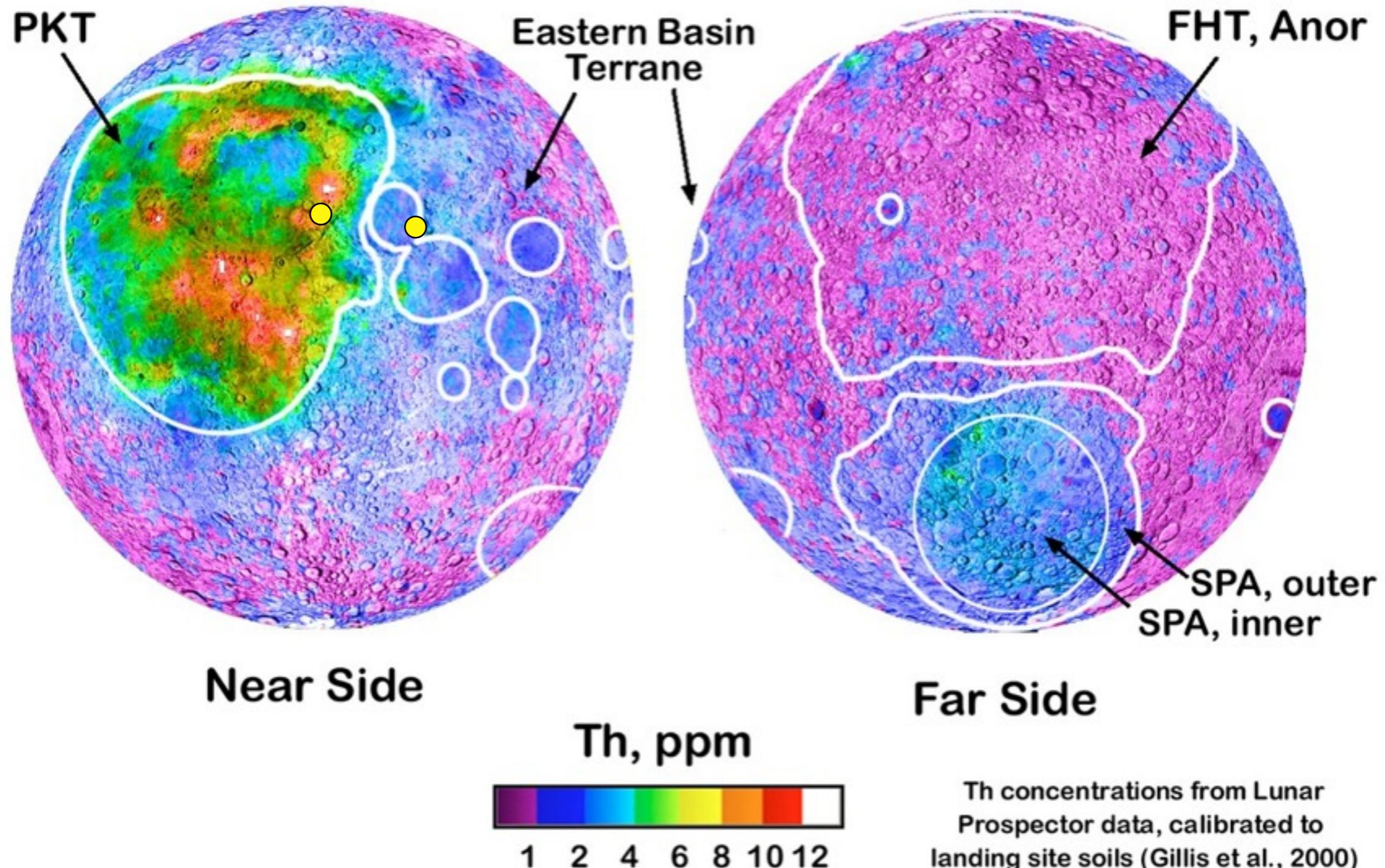
The heat flow depends upon the abundance of heat-producing elements and thermal evolution.

The heat flow was measured at two locations on the Moon: Apollo 15 and 17



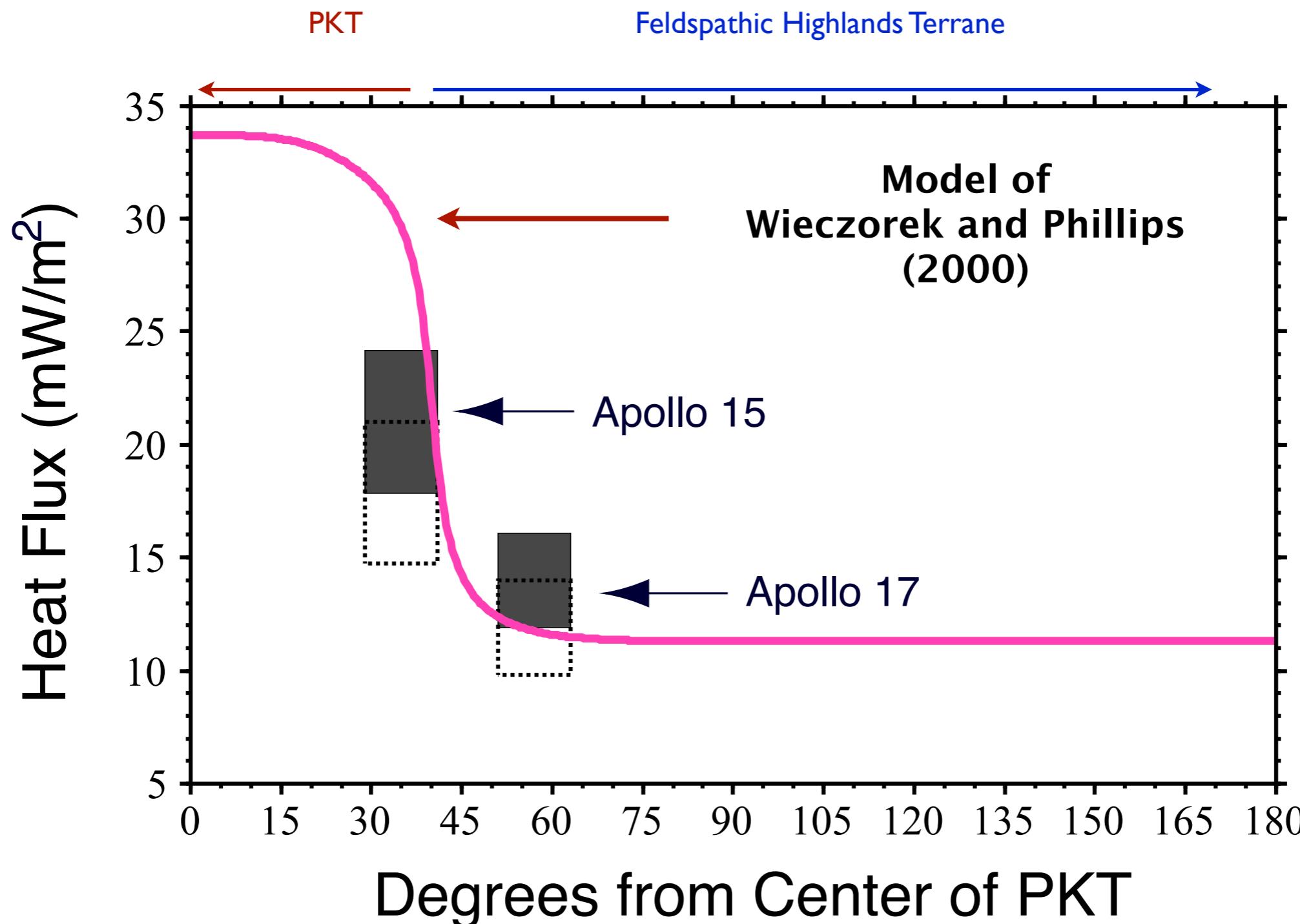
Final emplacement of the Apollo 15 heat flow probe

Geologic context of the heat flow measurements



Heat-producing elements are highly concentrated in a small near-side crustal province where the majority of mare basalts erupted.

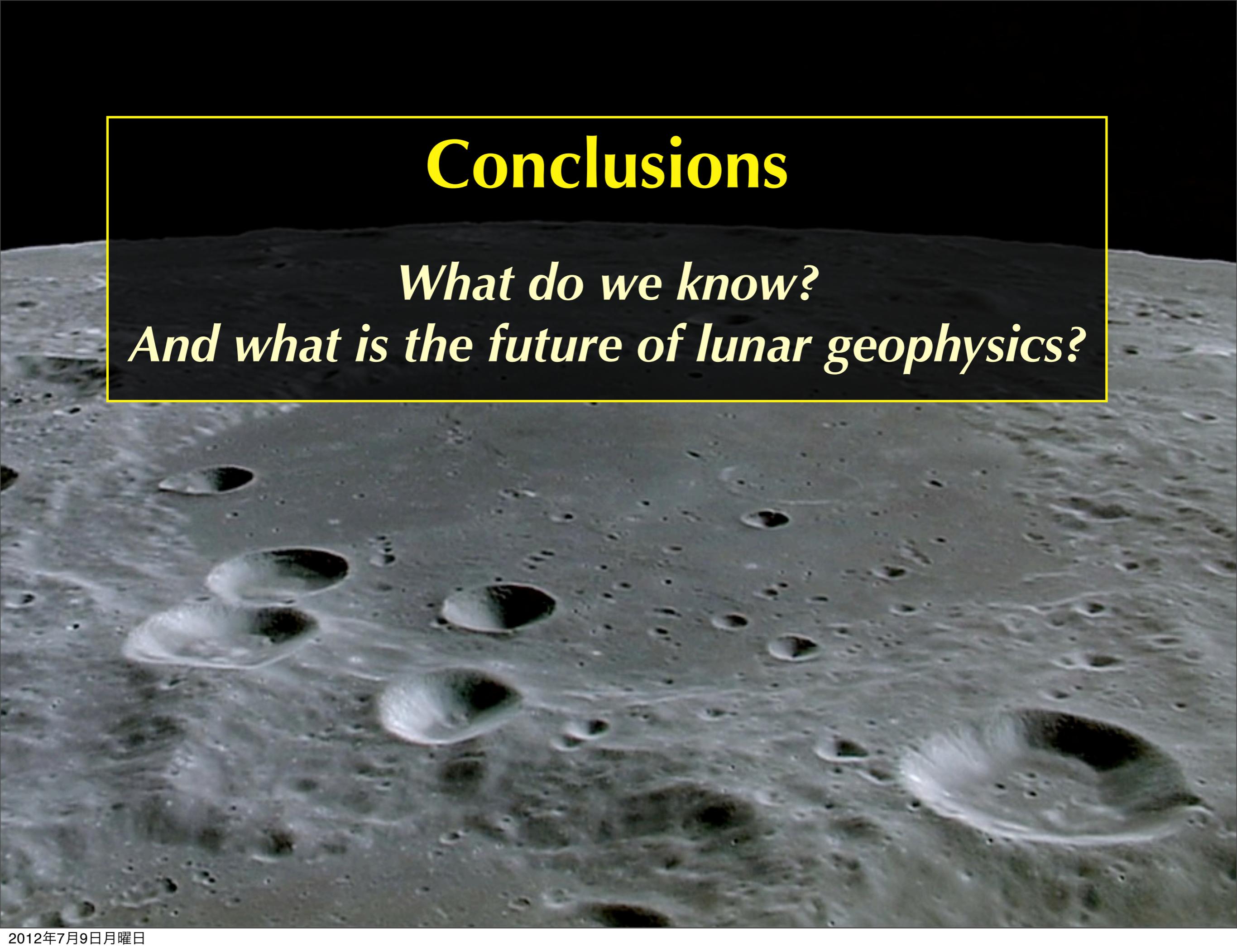
The measurements....



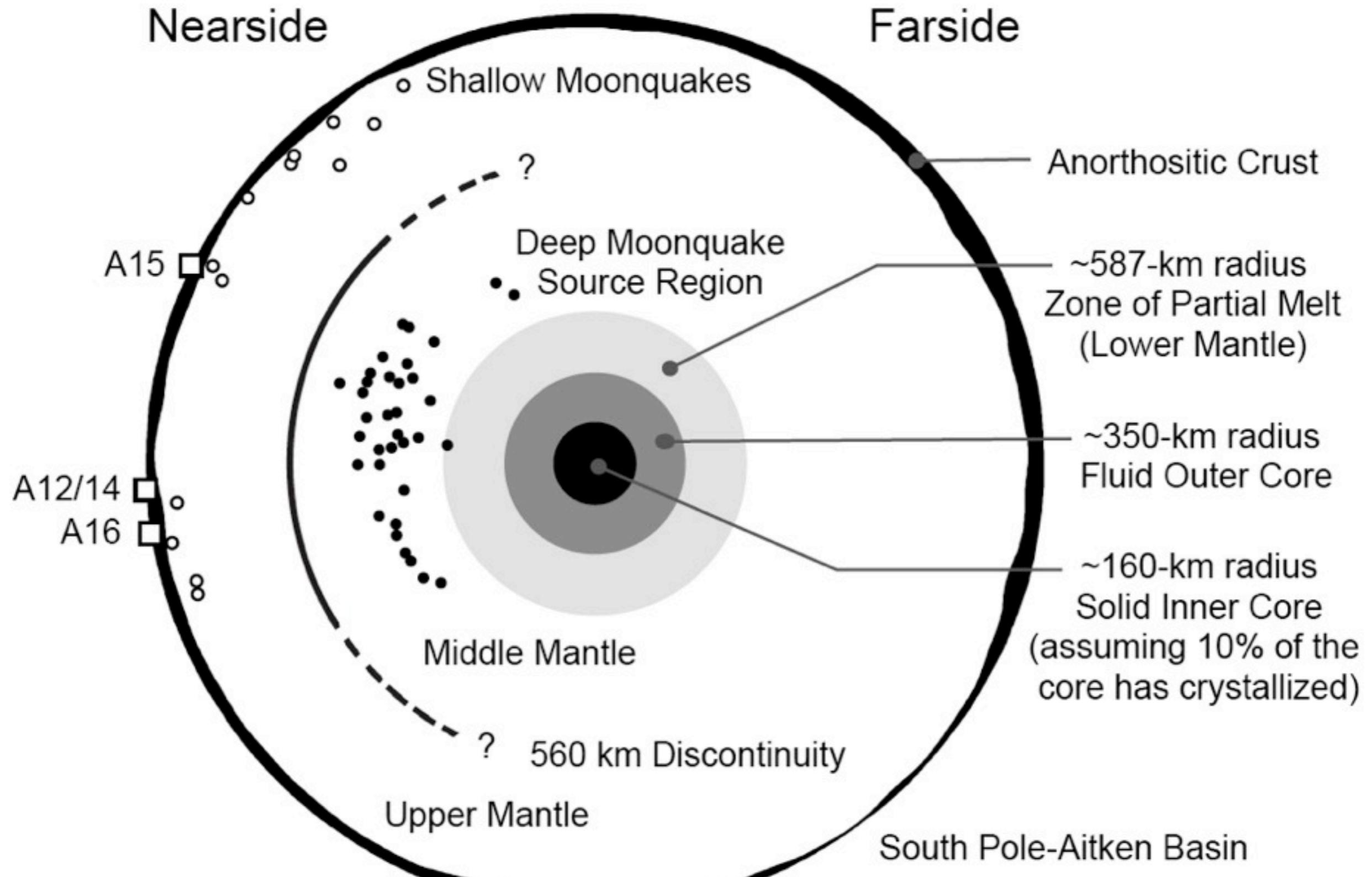
The heat flow is predicted to be about 3 times higher in the center of the Procellarum KREEP Terrane than in the Feldspathic Highlands Terrane.

Conclusions

*What do we know?
And what is the future of lunar geophysics?*

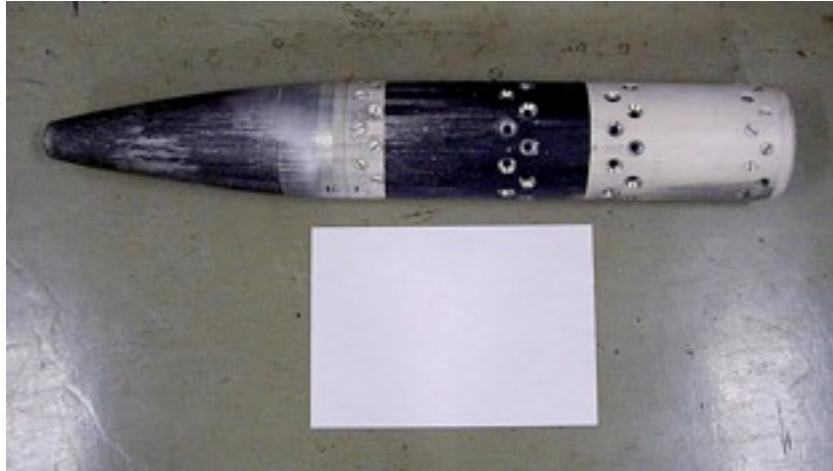


Our best guess



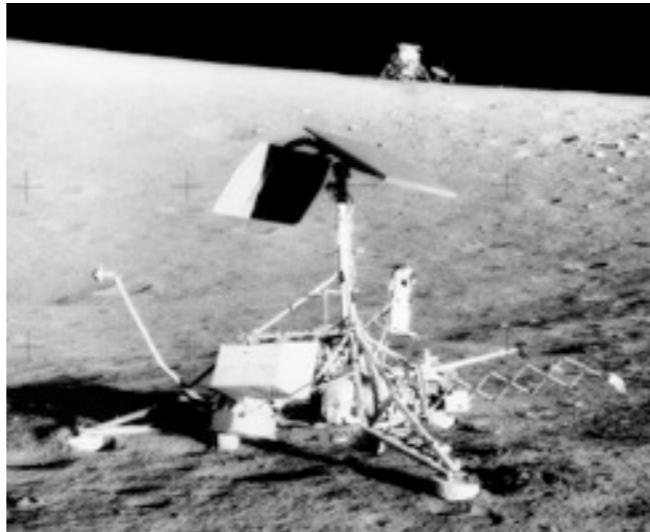
We need more data!

Several future seismic missions are being investigated.



Penetrators
(Japan, UK)

We need global coverage!
10+ stations on both the near- and far-side hemispheres.



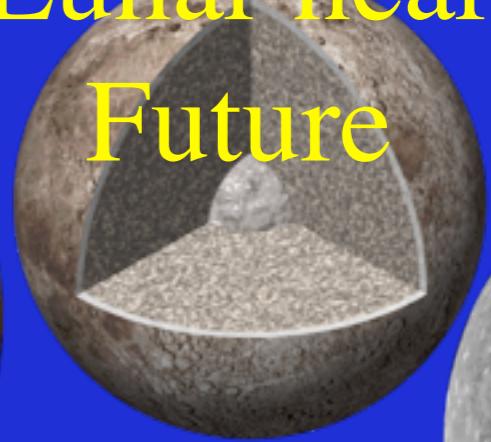
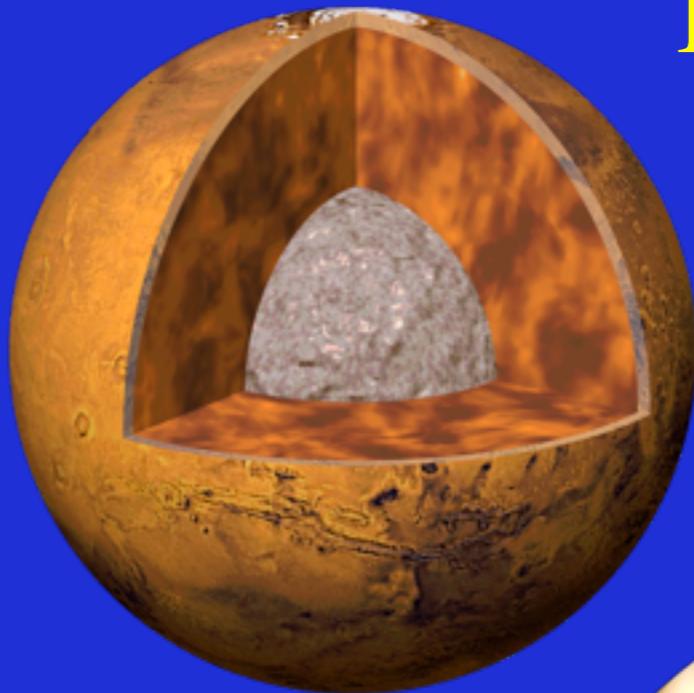
Landers
(Japan, Europe,
China, US)



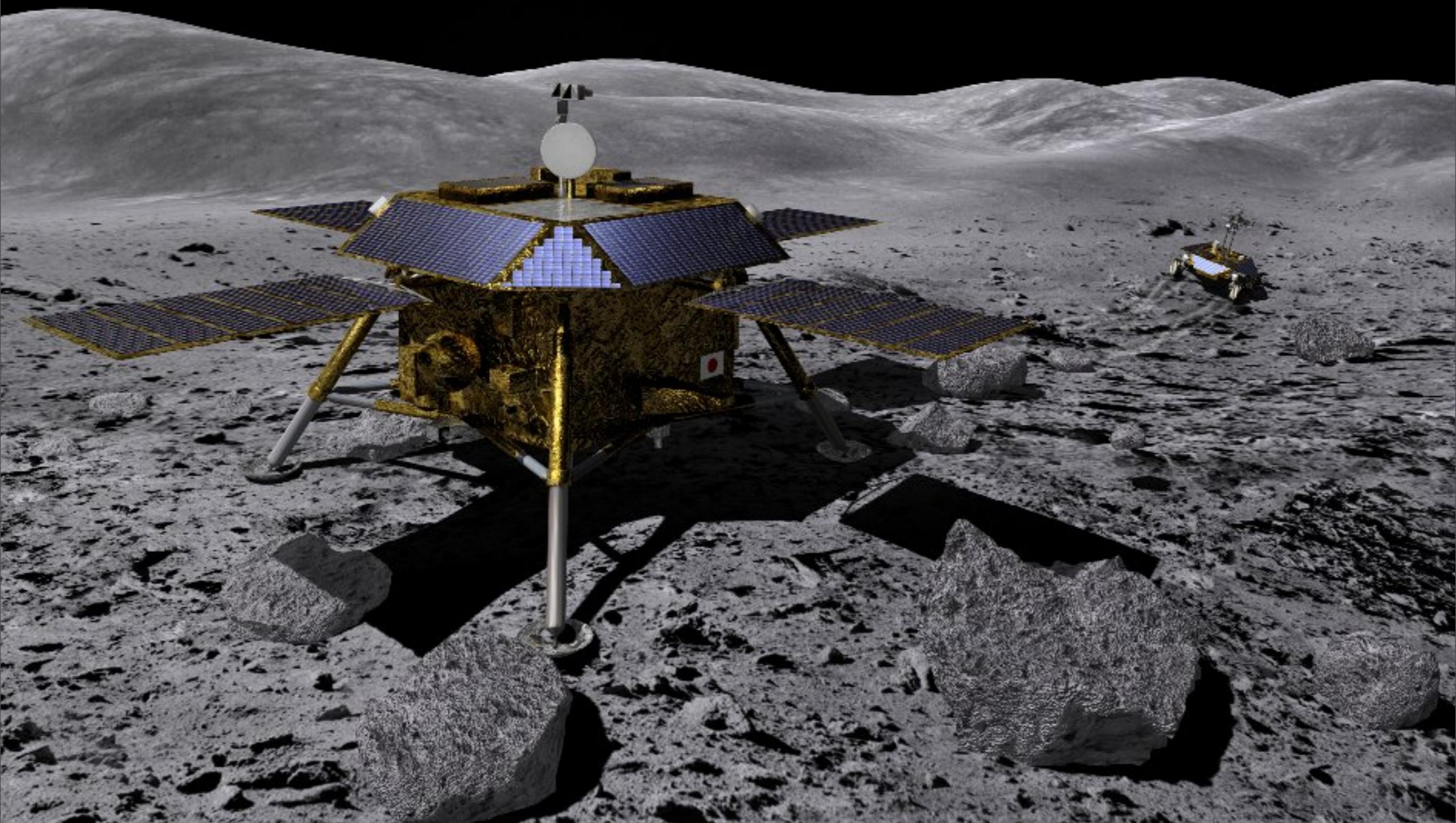
Human
(US)

The activity of deep moonquake nests is correlated with the tides (27 days, 6 years, 9 years, and 18.6 years). We need long time spans of data!

Lunar near
Future



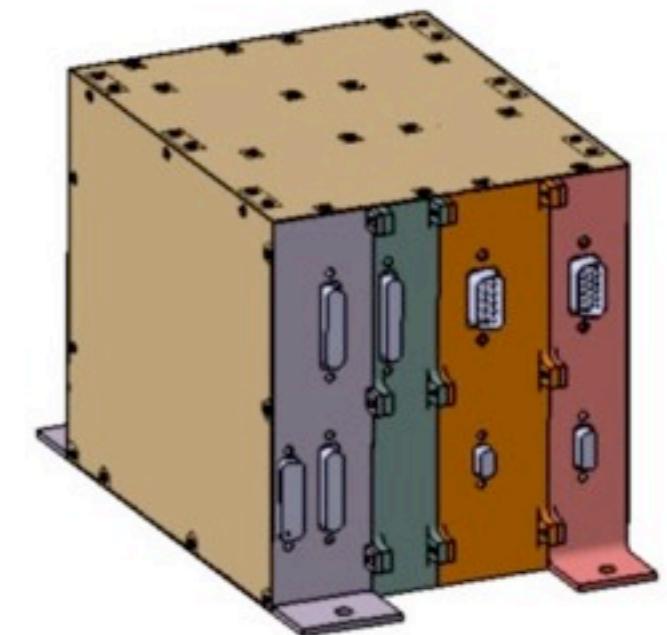
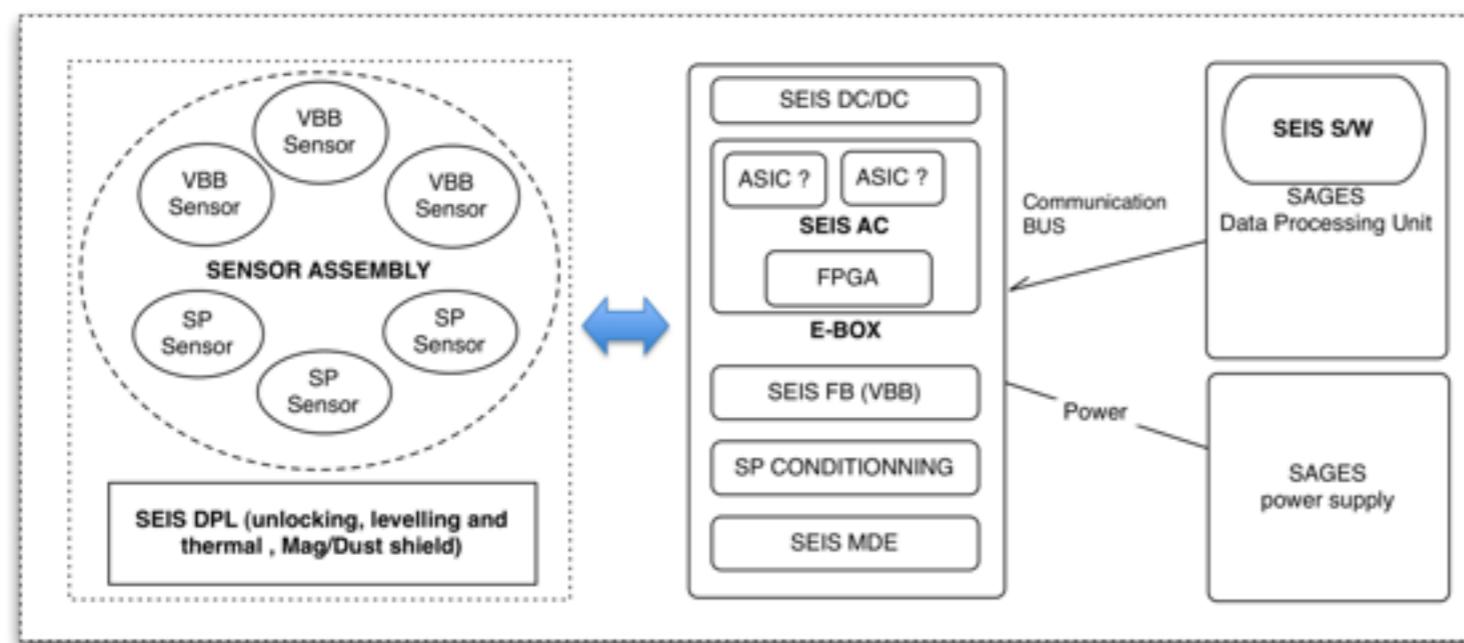
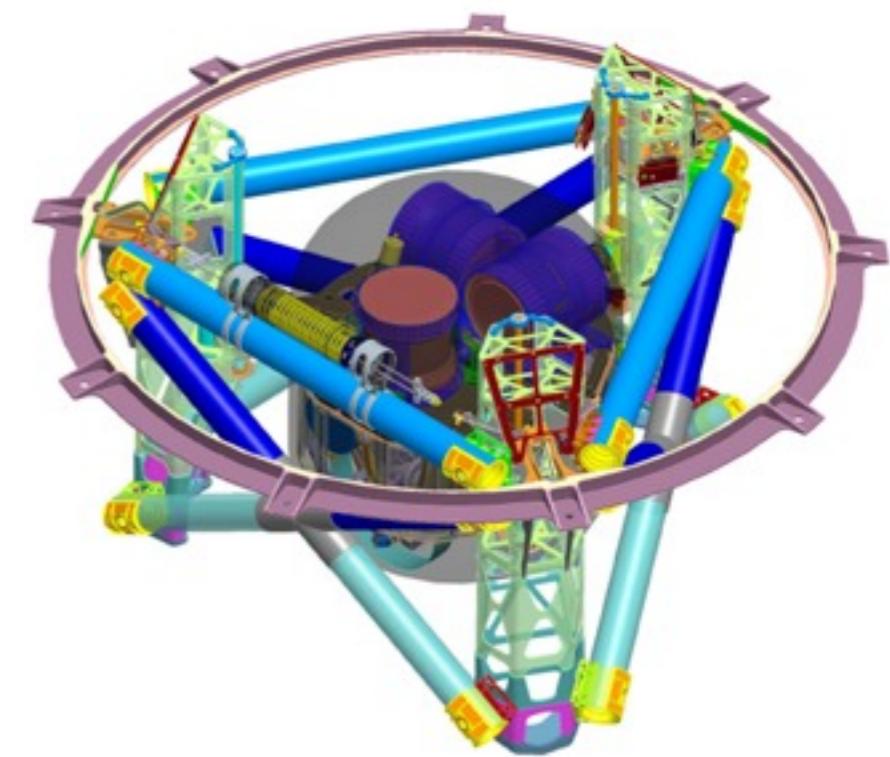
SELENE2





Lunar SELENE2 seismometer

- The Seismometer Experiment is composed of :
 - Three Short period seismometers (ISAS,J, N.Kobayashi)
 - Three Very Broad Band seismic sensors (IPGP/CNES, F)
 - An installation and leveling system (MPS, D)
 - An acquisition electronics (ETHZ, CH)
- The seismometer shall be serviced by a survival module
 - Provides power, data storage, communication with Earth
 - Maintain the seismometer in an adequate thermal range

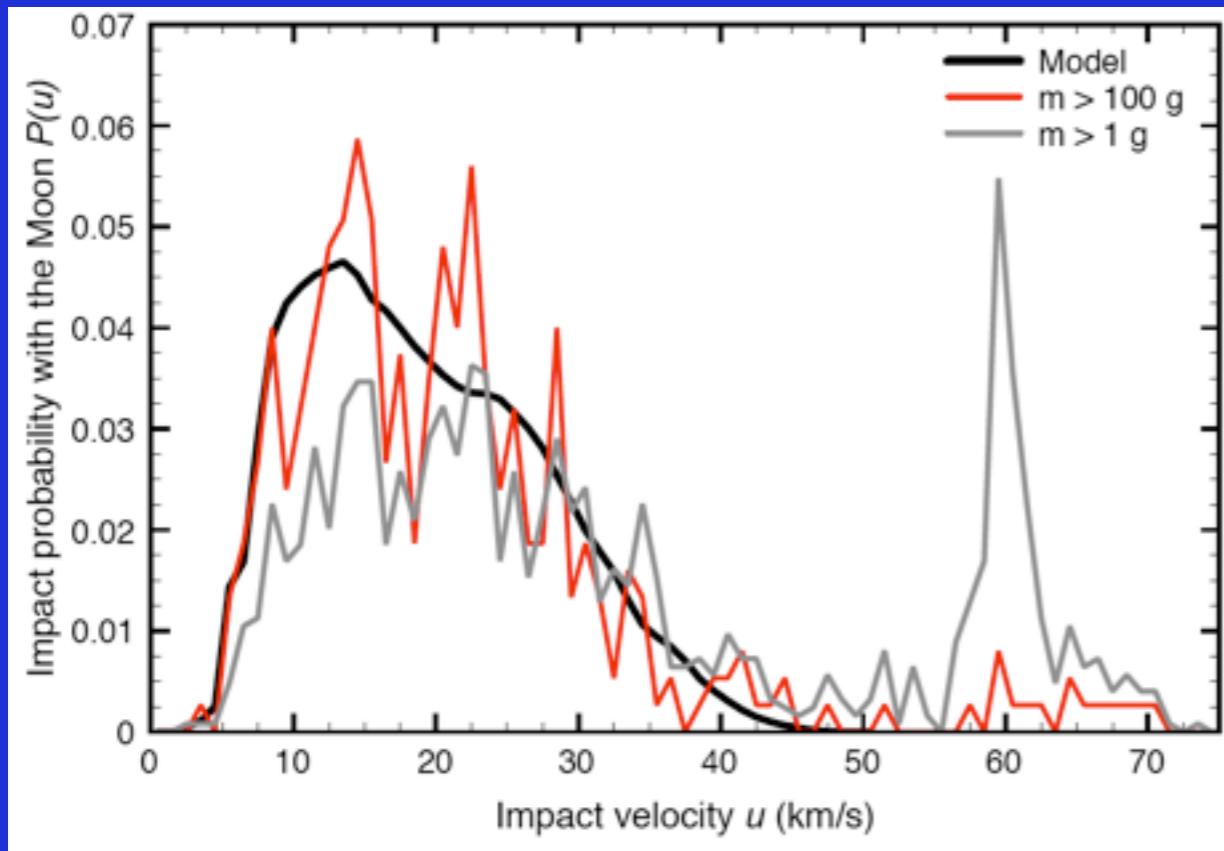


Lunar seismic Seismic Noise

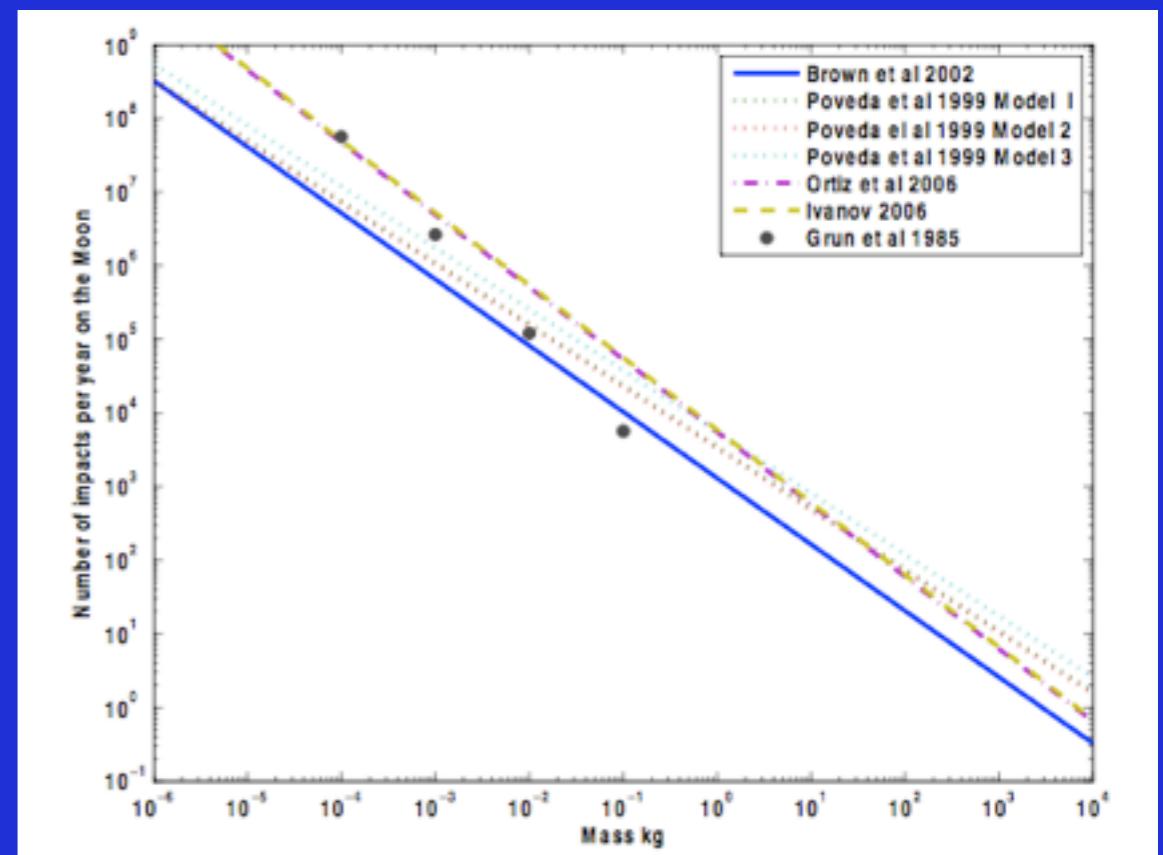
No atmosphere but continuously impacting
meteorites...

Impacting rates

- The Moon, as all other planetary or small bodies without atmosphere is impacted continuously by meteorites.
 - Scattering and low attenuation are generating a “long” time diffusion
 - Direction of impacts are given by a priori distribution of NEO in the internal solar system (Bottke et al., 2002)
 - Mass/frequency of impacts are given by different models, but typically 3000/5000 impacts > 1 kg on the Moon

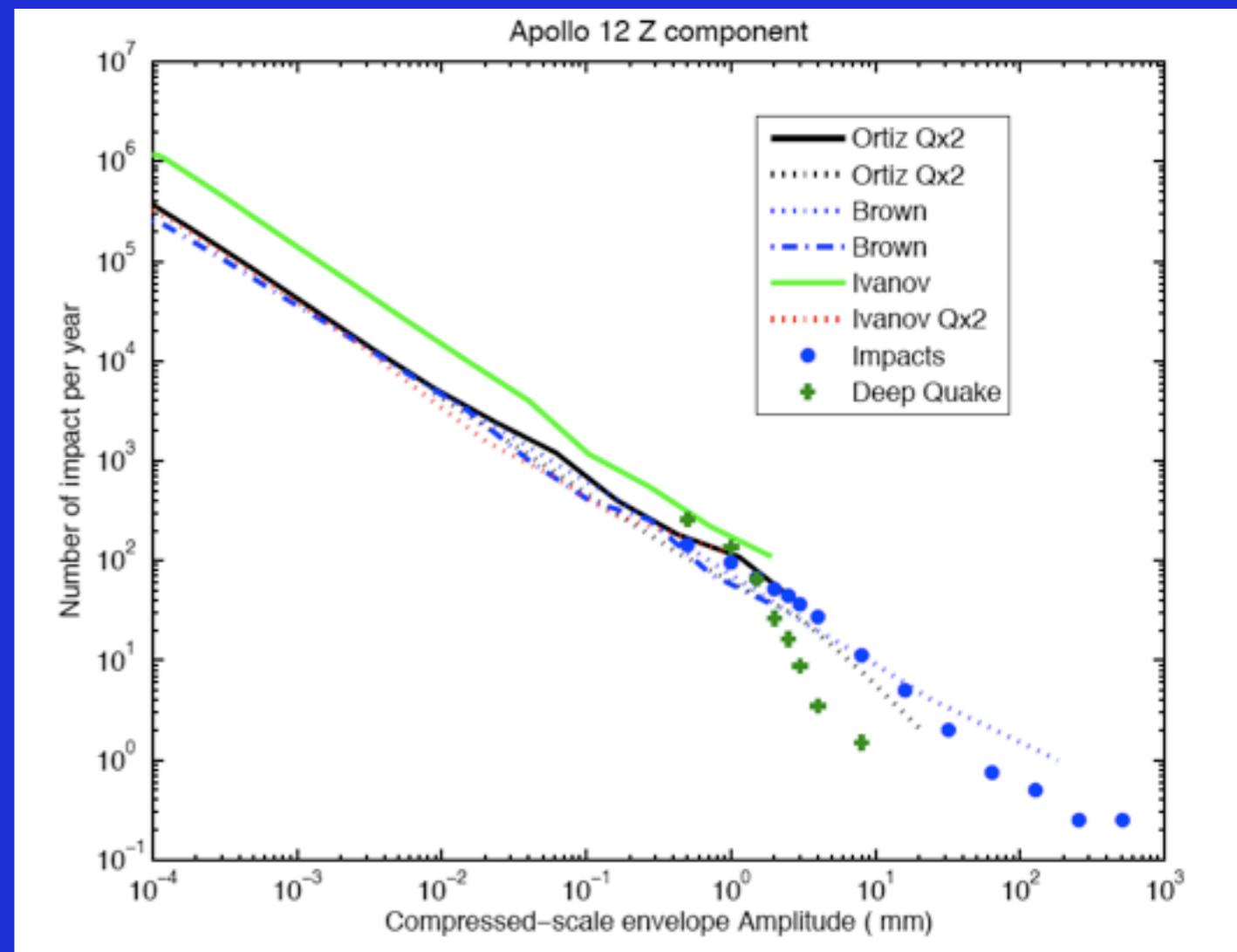
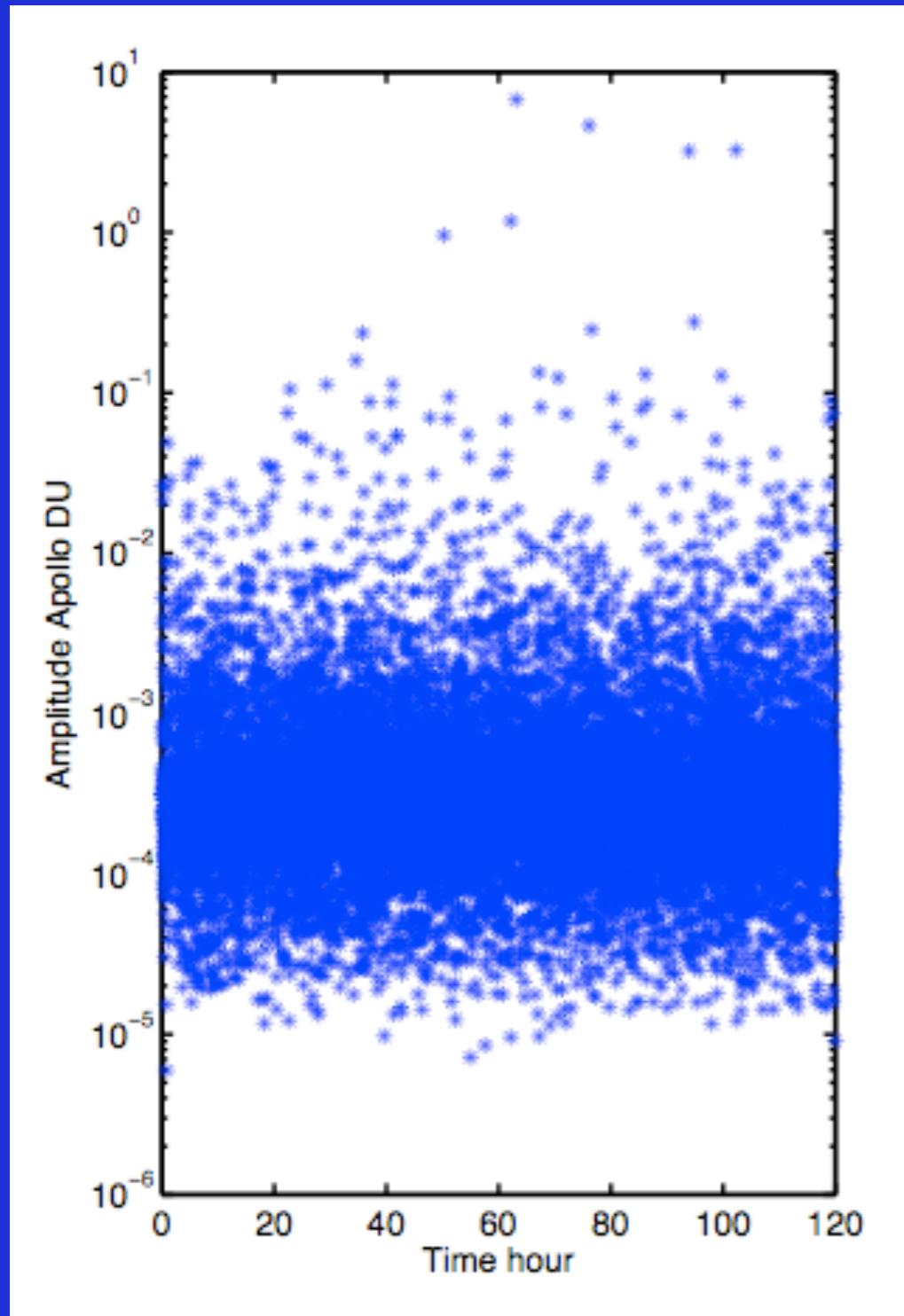


velocities



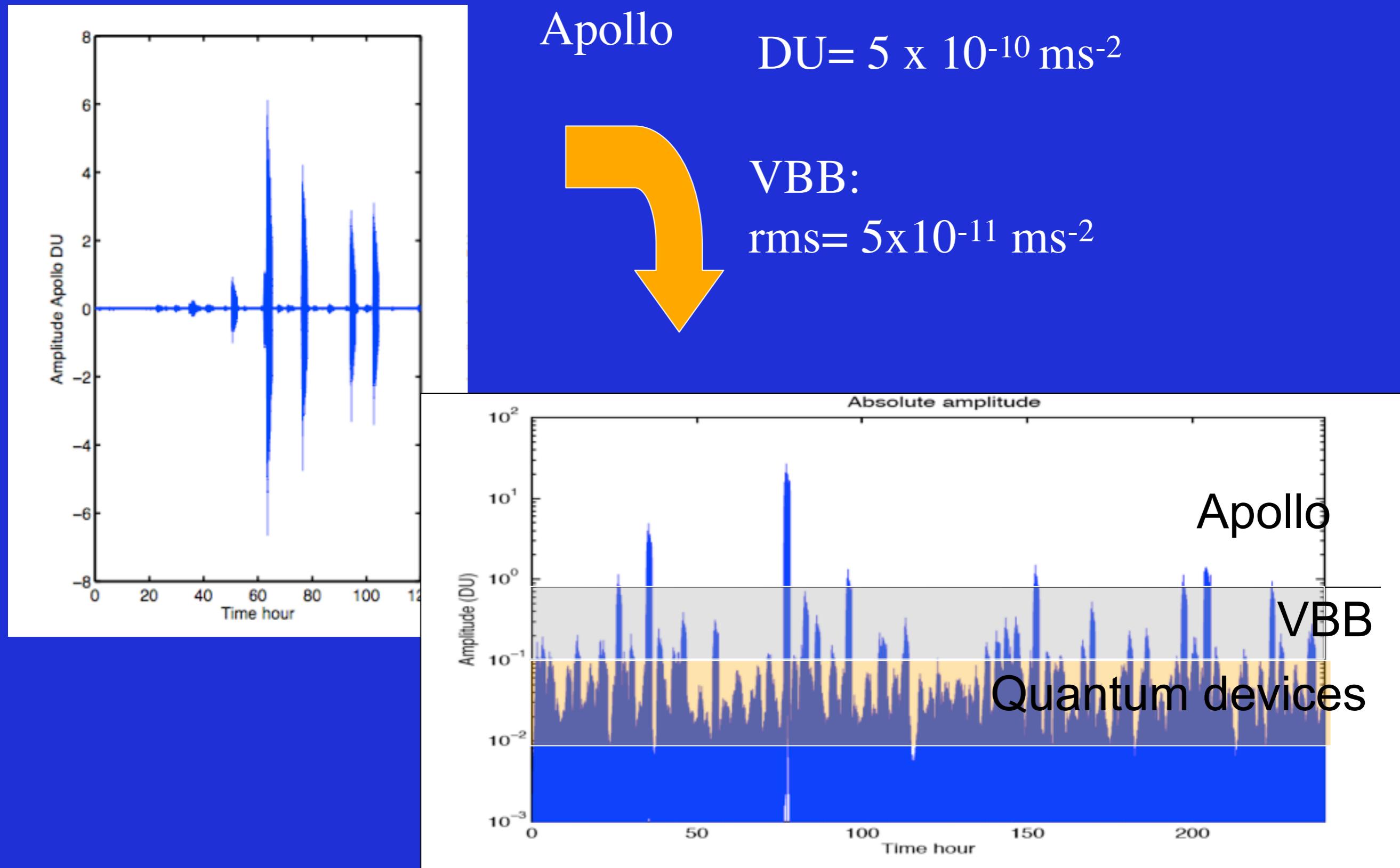
mass

Impact/hum transitions



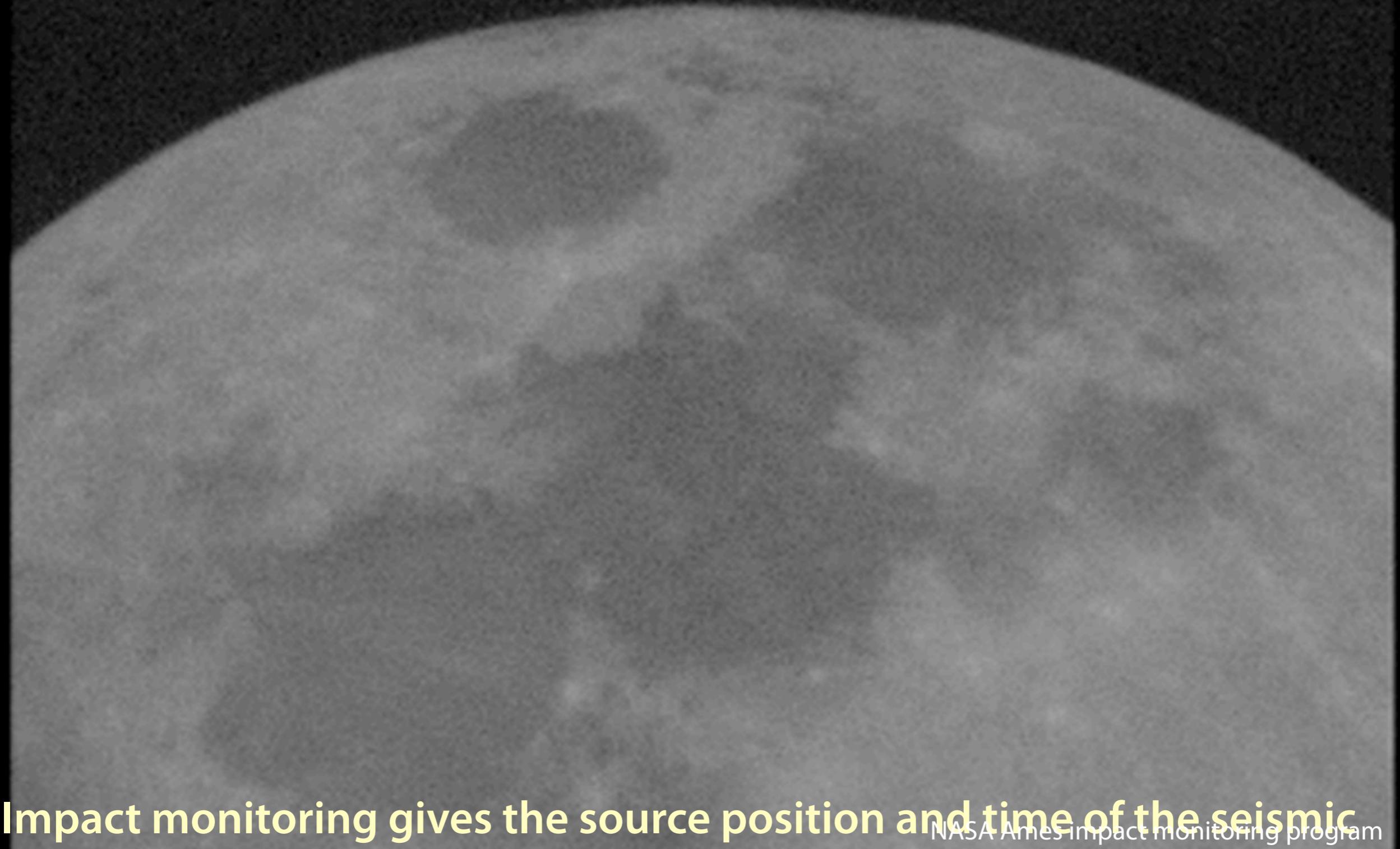
Maximum amplitudes

Event frequency



Active seismology using impacts

Near side of the Moon (illuminated by Earthshine)



Impact monitoring gives the source position and time of the seismic event, allowing seismic investigations with a single station.

NASA Ames impact monitoring program

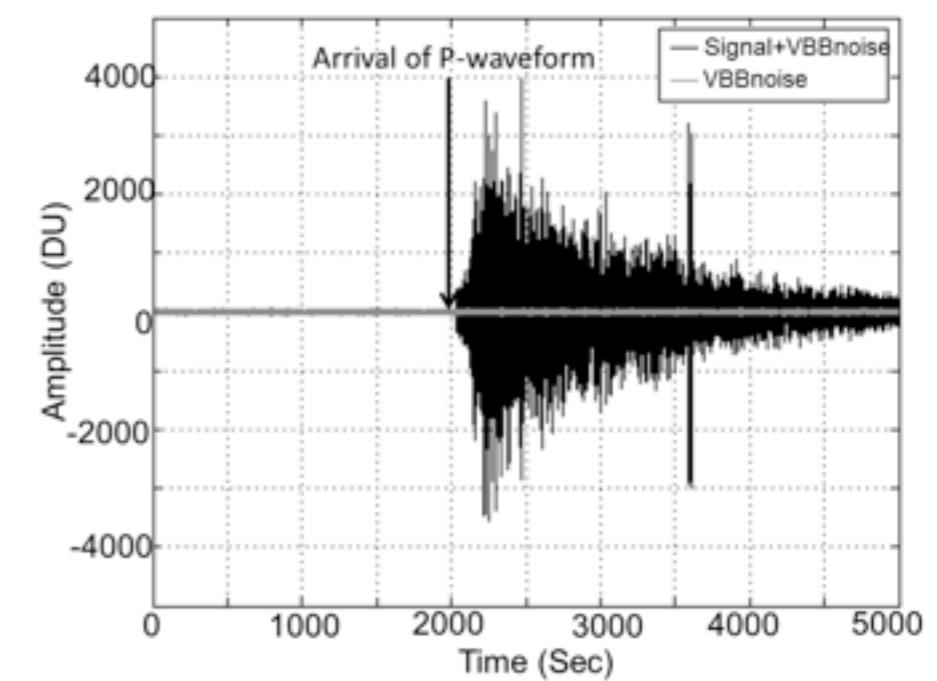
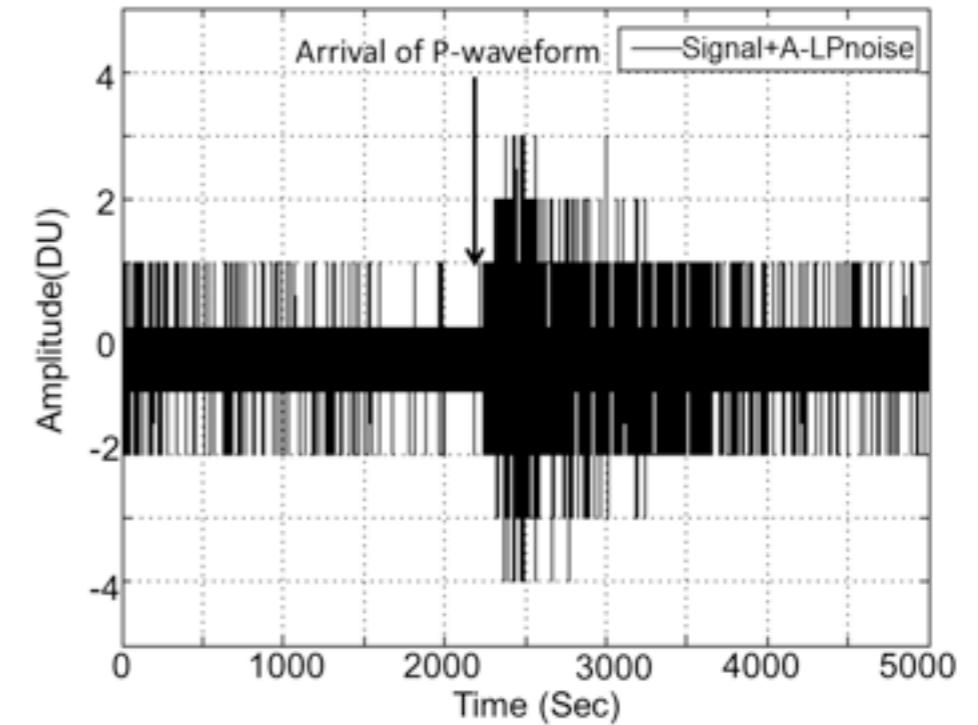
Expected improvement with respect to Apollo will enable new seismic discoveries

- Core phases and core size
- High resolution crustal model from joint Earth/Moon impacts monitoring
- Detailed seismic source dynamics of impacts and DMQ

Apollo LP

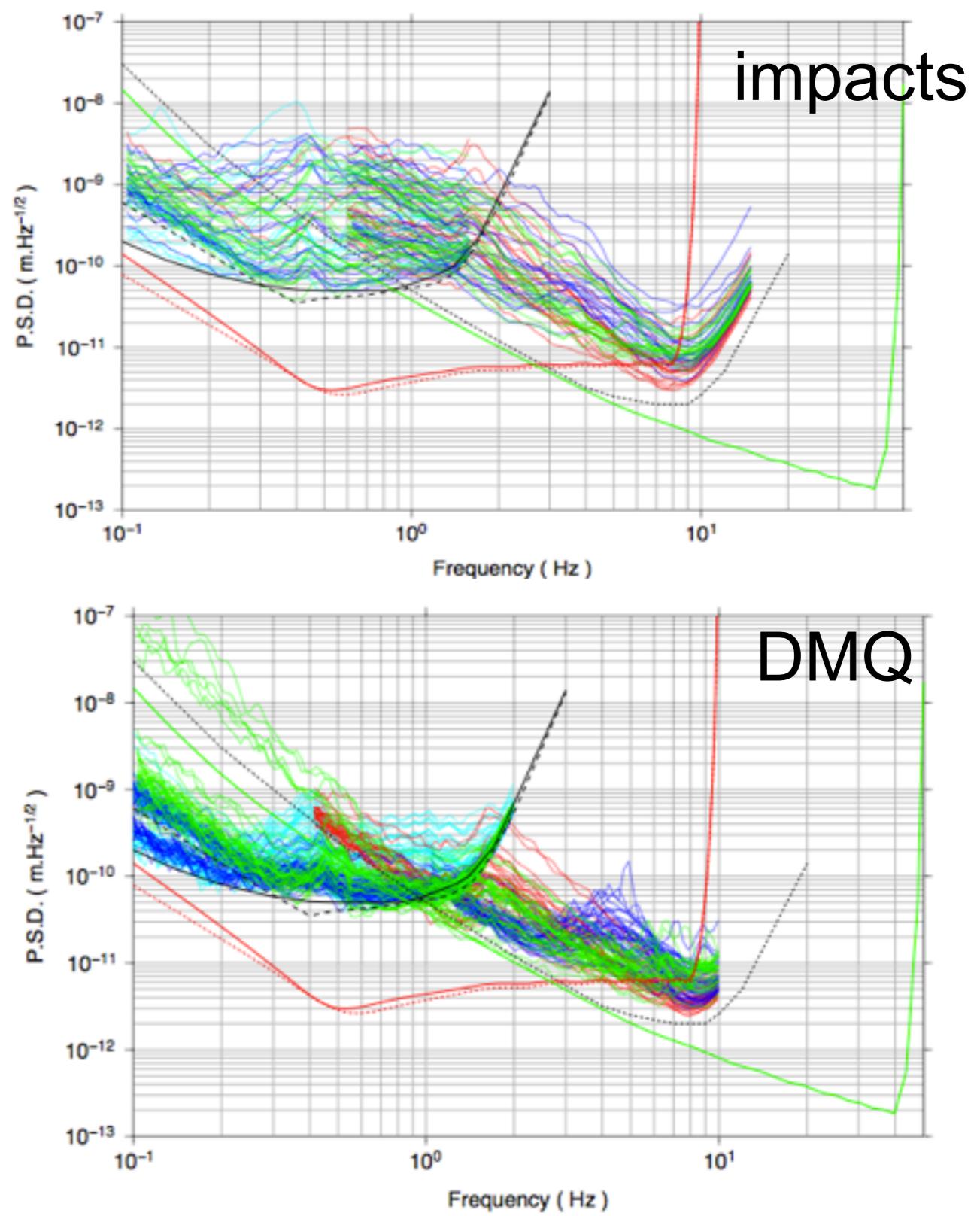
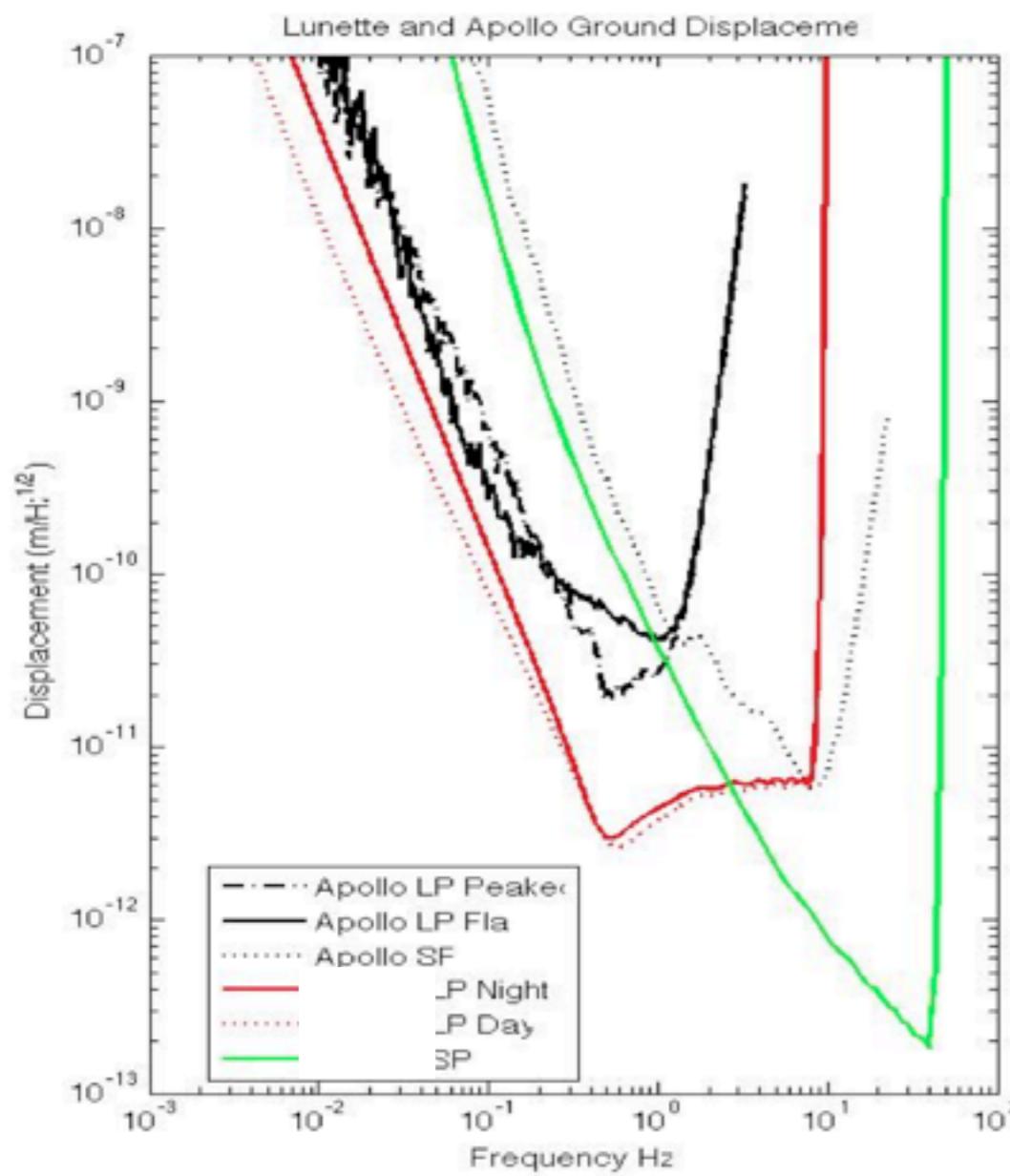


SELENE LP

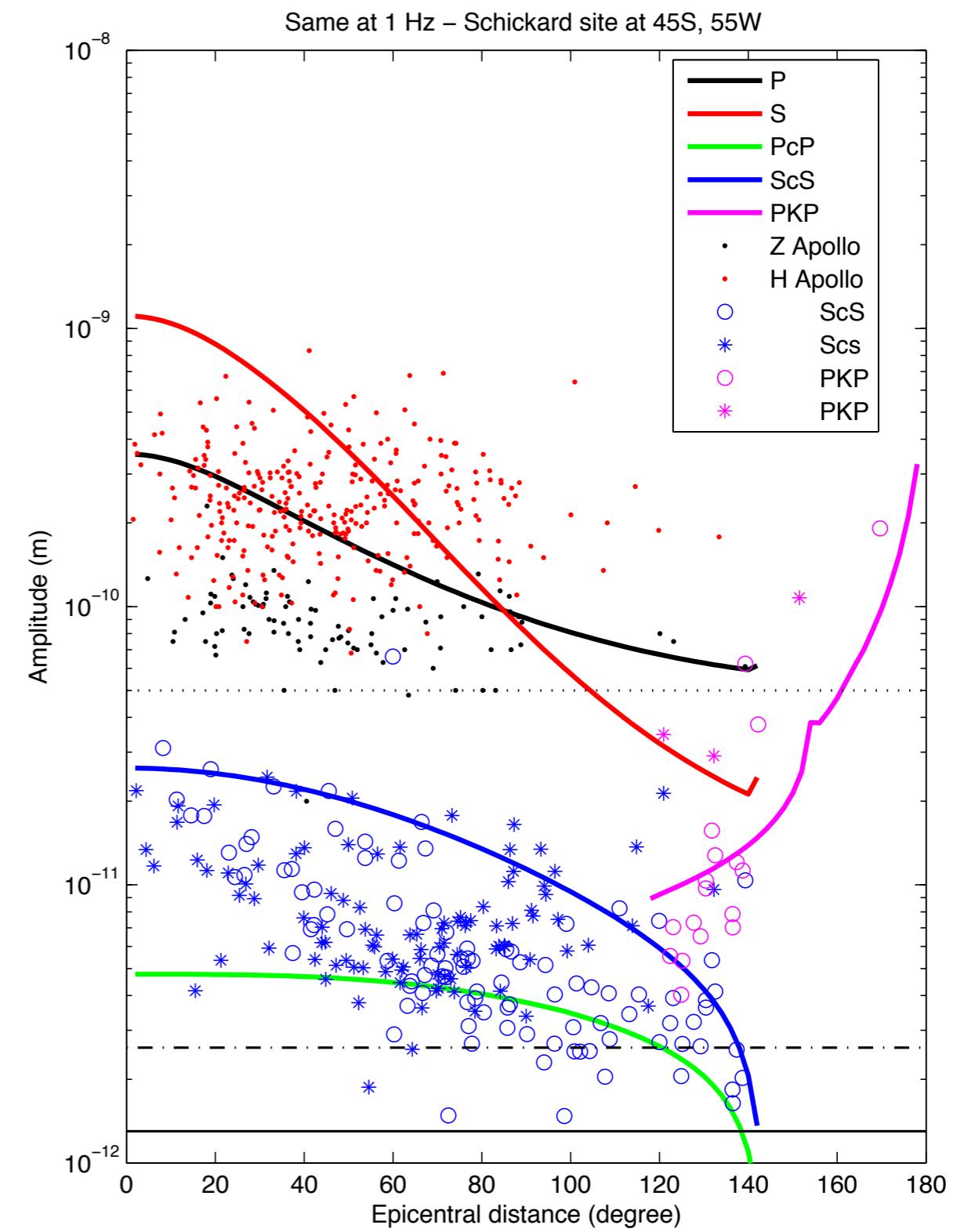
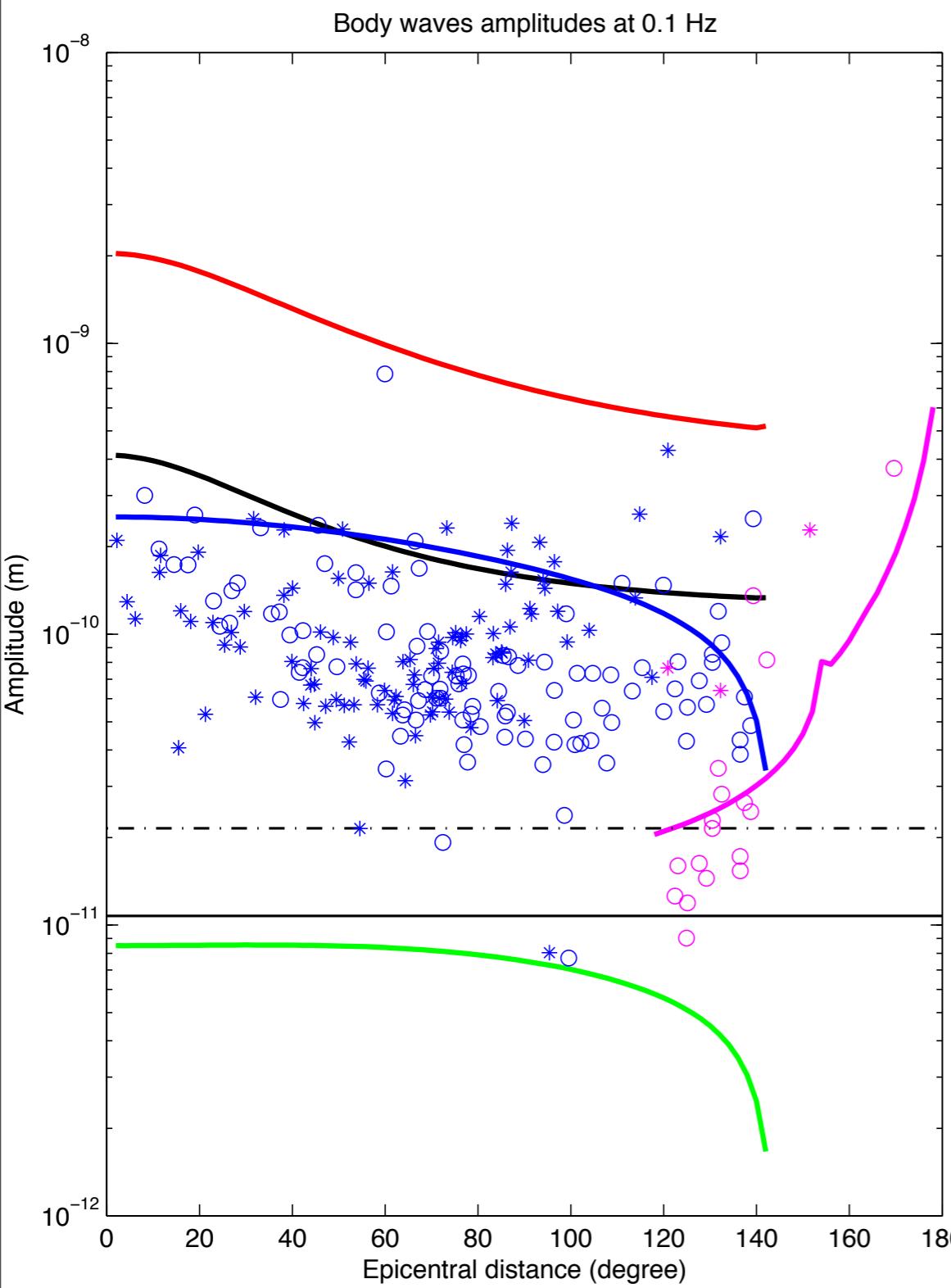


Yamada et al., 2012

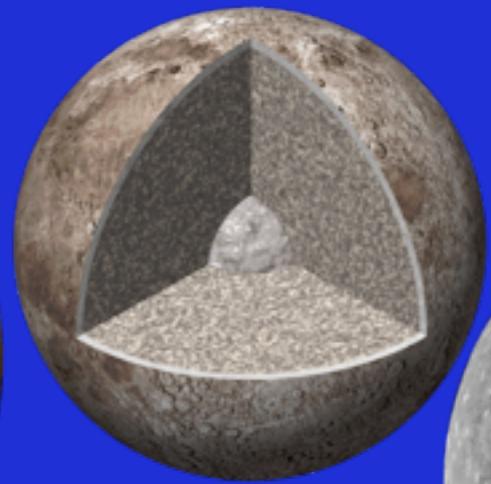
Performances improvements...



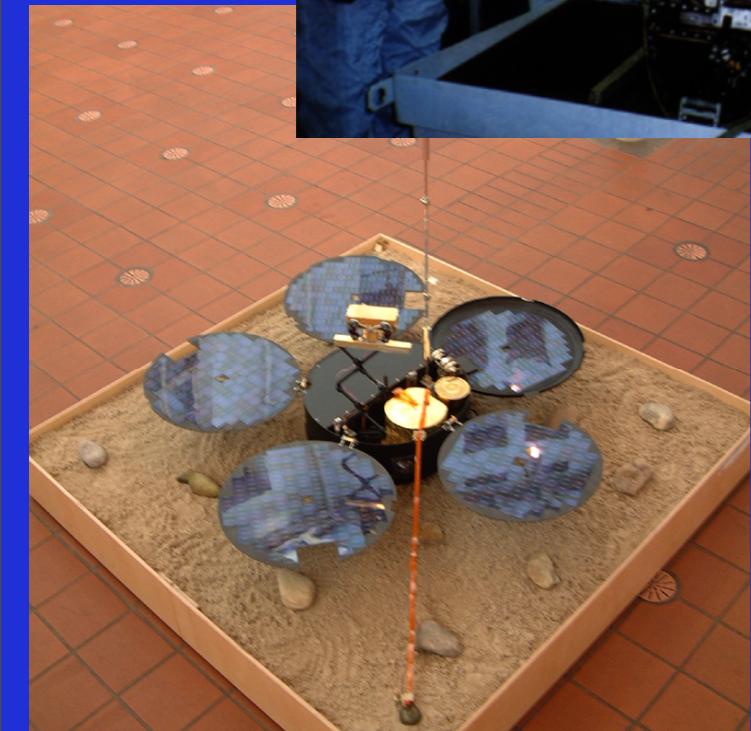
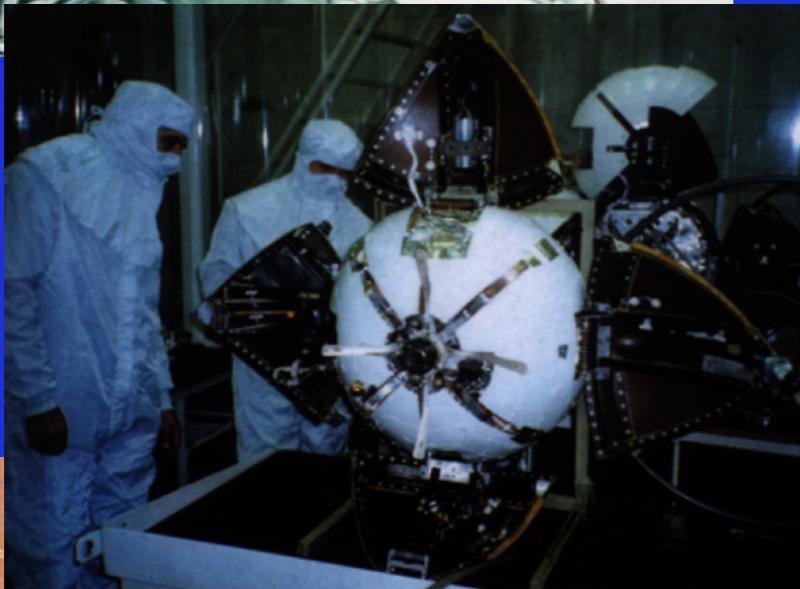
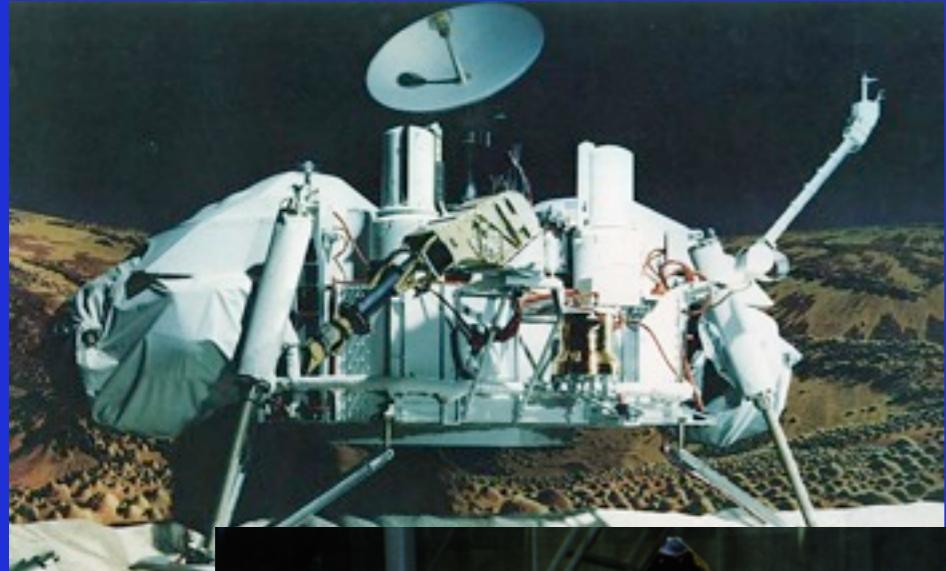
Better detection of core phase...



Mars Future

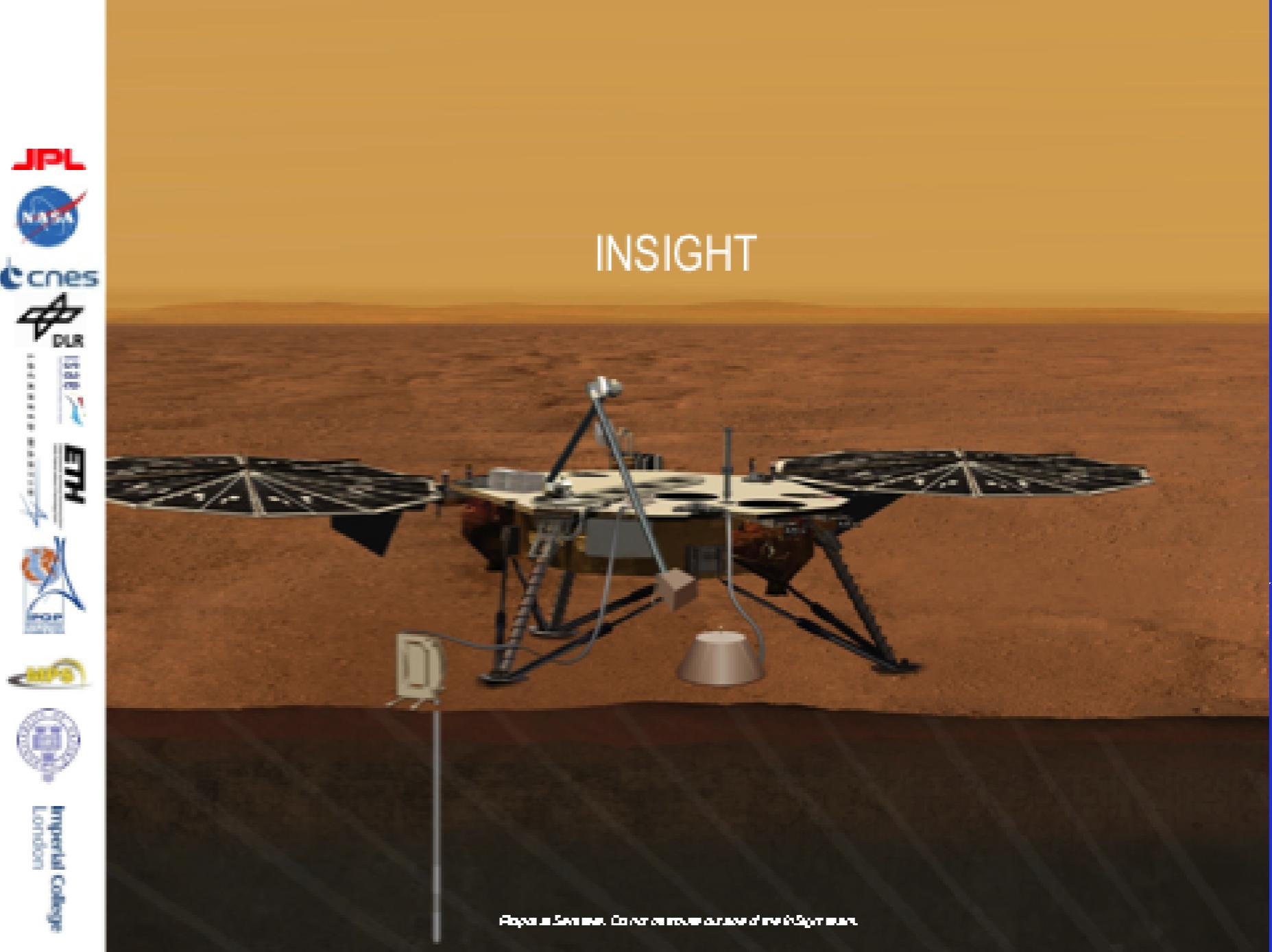
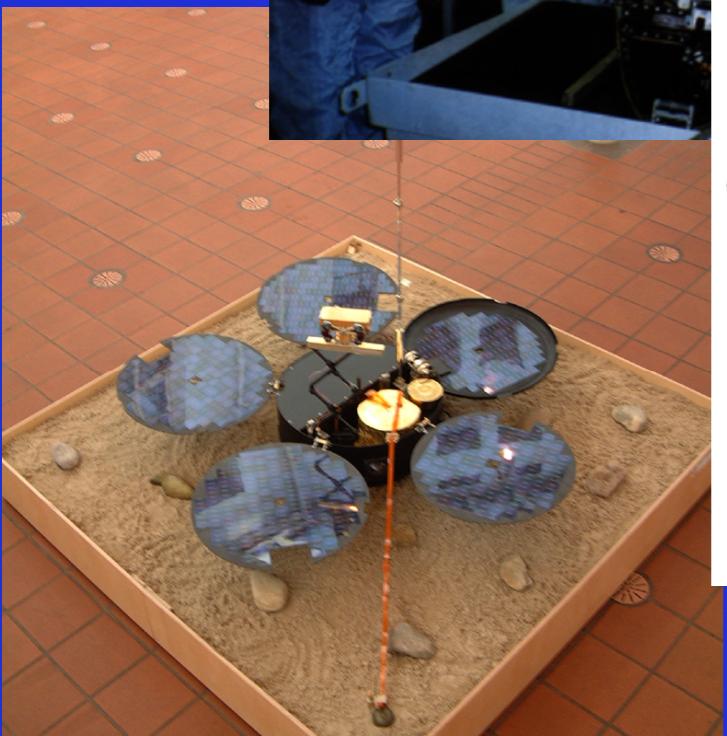
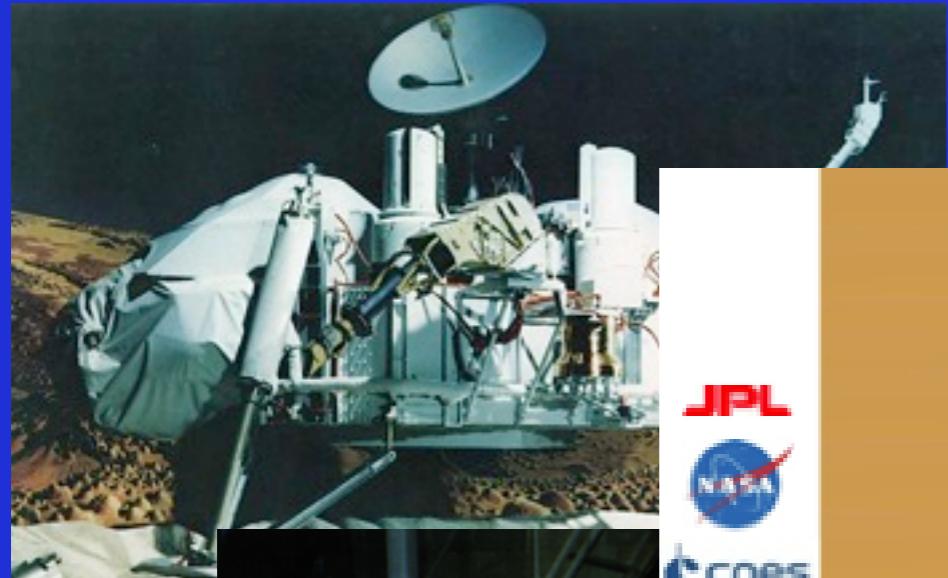


Mars seismology: history



- 1975: 2 Viking landers equipped with seismometers. Possible detection of one quake on one lander
- 1996: Failure of the launch of Mars96, with 2 surface stations equipped with BRB Z axis seismometers and 2 penetrators with SP geophones
- 2003: The NetLander mission is stopped by CNES and NASA before phase B completion.
- 2008: Humbold/ExoMars project is stopped by ESA after phase B

Mars seismology: history



The Discovery Insight

- **Science**

- InSight (former GEMS) is investigating the interior of an Earth-like planet for the first time.
- Scientific payload is highly focused on geophysics
 - ✓ 3 axis Seismometer
 - ✓ Heat flow
 - ✓ geodesy experiment
- Will utilize sophisticated single-station analysis techniques to derive geophysical information from one site on Mars.
- InSight is a necessary pathfinder for any future Mars geophysical network.

- **Mission**

- Low risk development and mature Instruments, Phoenix spacecraft
- InSight mission is nearly identical to Phoenix from launch to landing and stays within all Phoenix capabilities except mission duration.
- After a short deployment period, surface operations require very little interaction (Deploy & Forget).
Final NASA decision is expected in about 3 weeks!



PARIS
DIDEROT

Pathway to (science) success

- How can a single lander perform the seismic monitoring of a whole planet:
 - Installation and noise of the seismometer will be critical
 - What will be the detection threshold and how many quakes can be detected?
- How can single seismic record of quakes can be used to constrain the interior
 - How well can be the seismic source and interior structure determined?

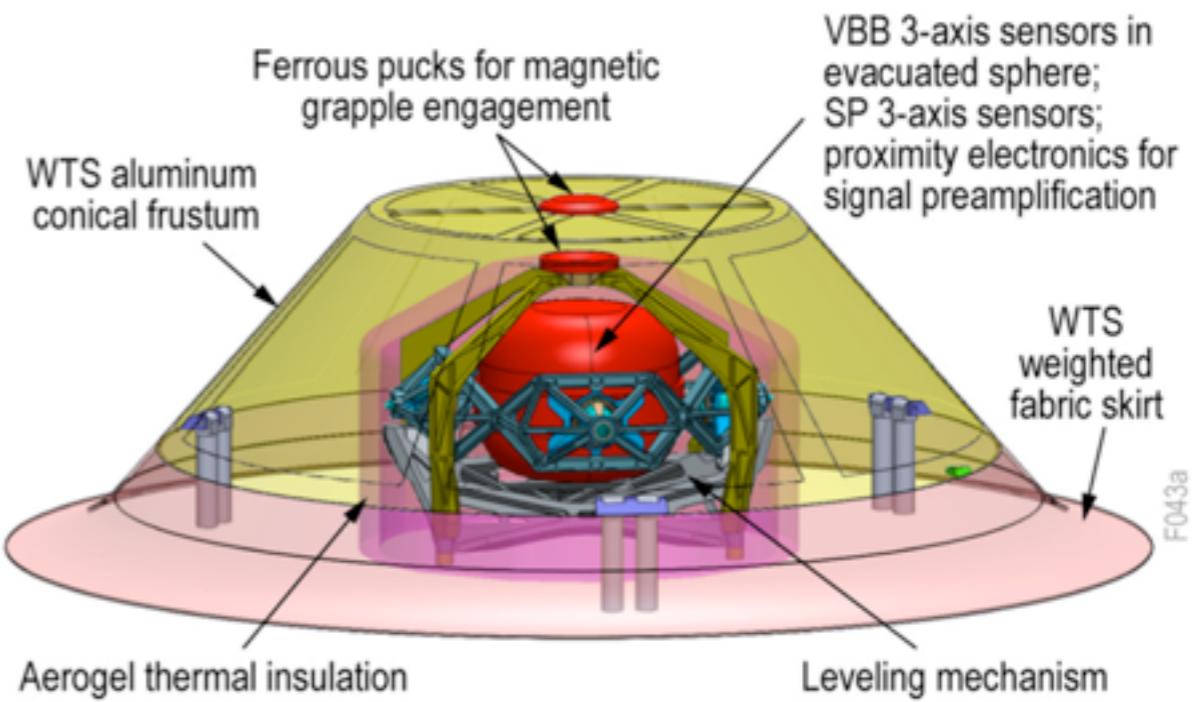


Deploying a seismic vault on Mars : why?

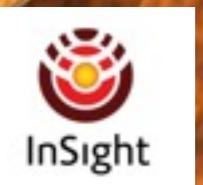
- Most of the quality of an Earth seismic station is directly associated to the quality of the seismic vault
- Most of the Viking seismometer failure was related to the bad installation of the seismometer (on the lander deck, e.g. on a suspension...)
- Most of the success of the Apollo seismometers



Deploying a seismic vault on Mars : how?



- Request a large mass made available by the Phoenix-type lander capability
- Will put the expected direct wind and thermal noise below the capability of space qualified VBB seismometers (see posters 1493 and 2025)
- Will allow to reach the (surface) micro-seismic noise of the planet

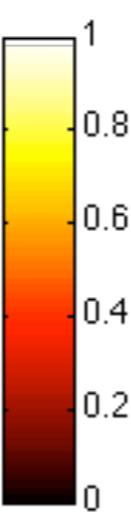
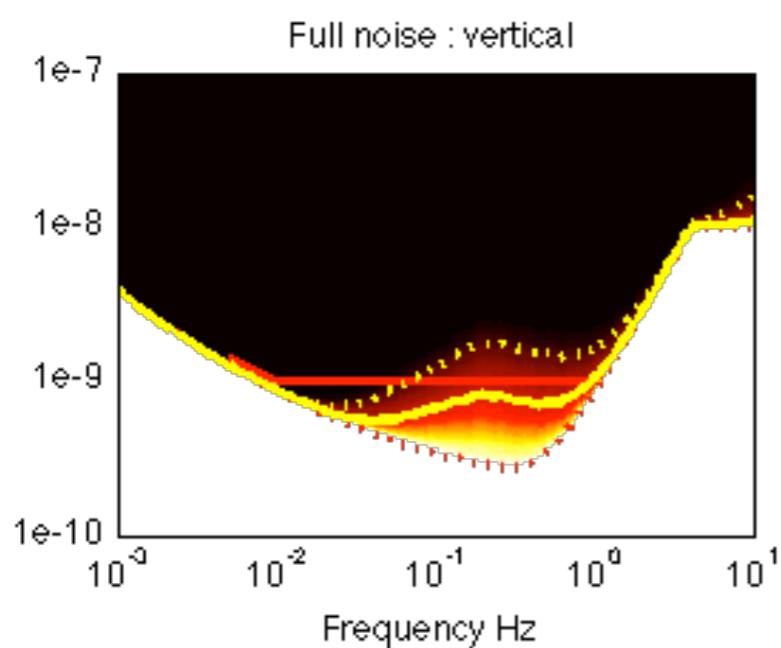


Imperial College
London

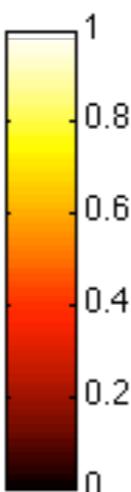
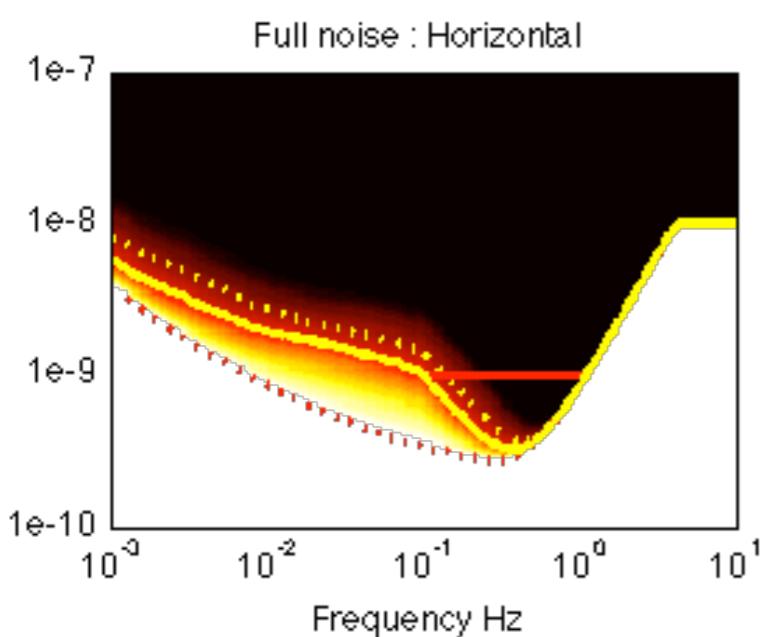


PARIS
DIDEROT

Mars Micro-seismic noise estimation



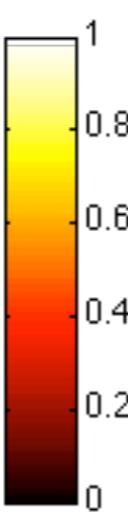
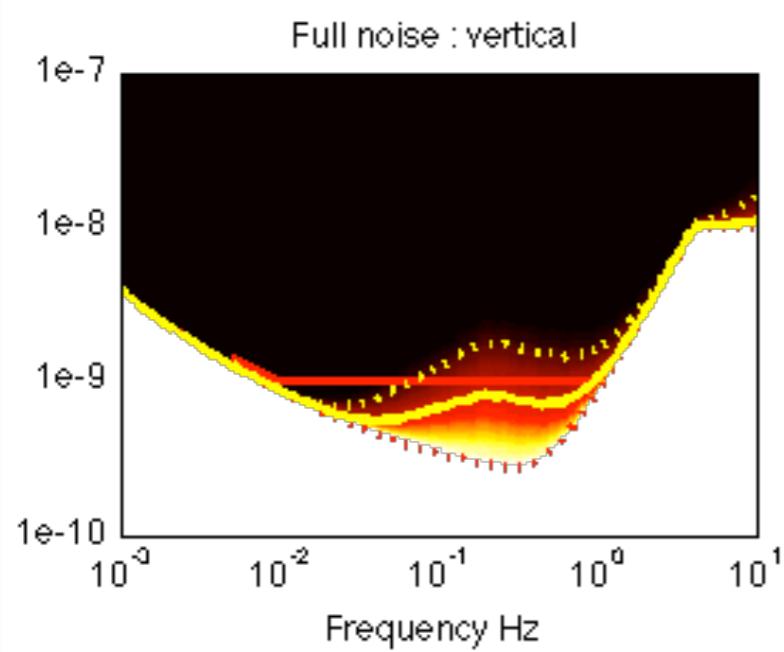
- Can be estimated with GCM and Large Eddies simulation
- Is expected to be below 10^{-9} ms $^{-2}$ /Hz $^{1/2}$ 70% of the time (10^3 less than Viking)
- Is expected to reach Apollo level with pressure decorrelation (10 x more)



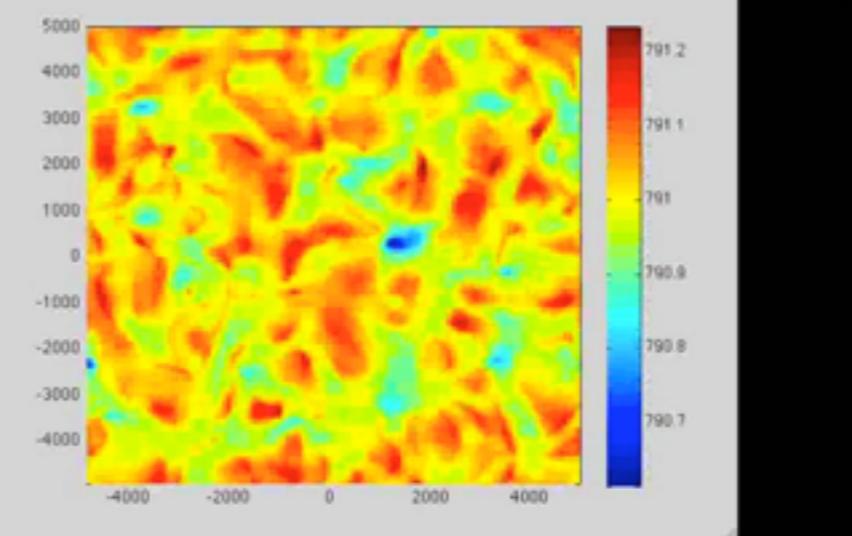
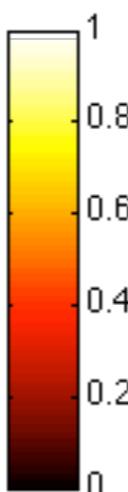
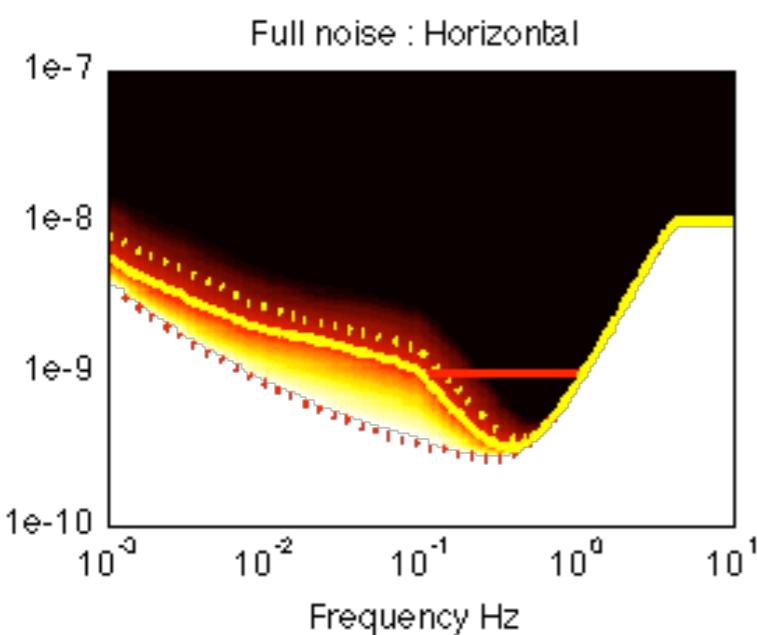
Pressure fluctuation on the ground => ground tilt



Mars Micro-seismic noise estimation



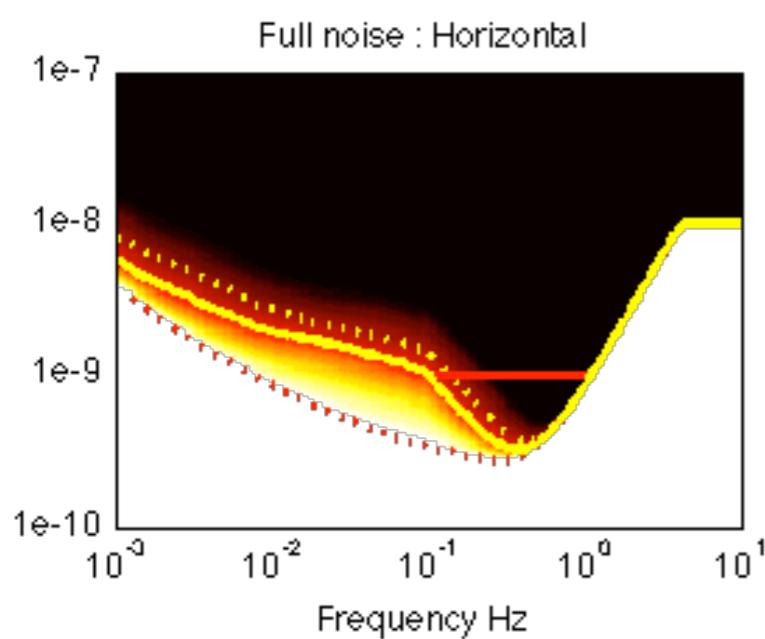
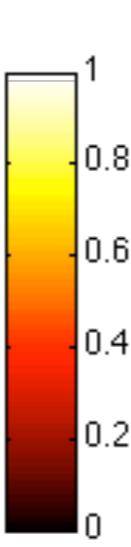
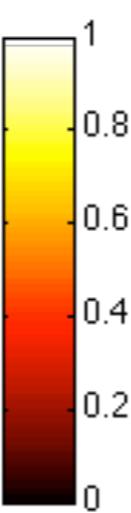
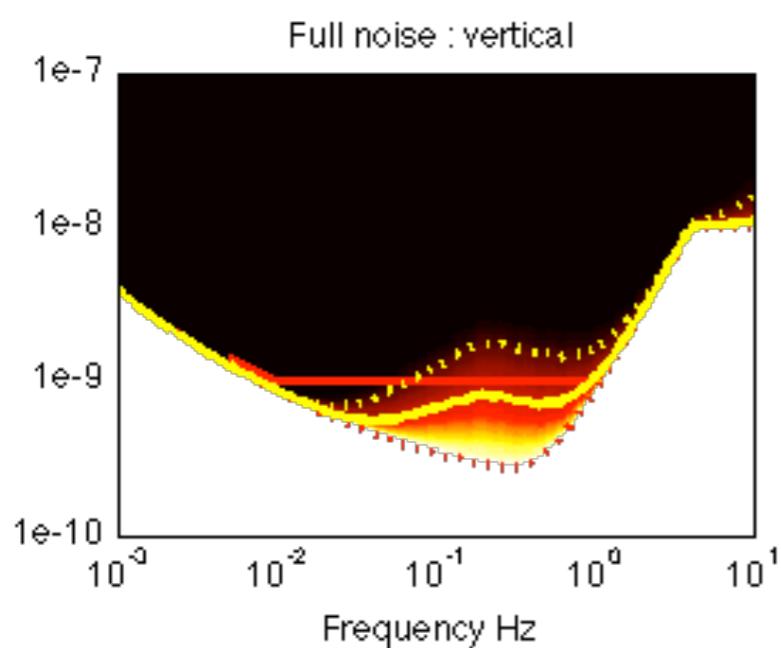
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Mars Micro-seismic noise estimation

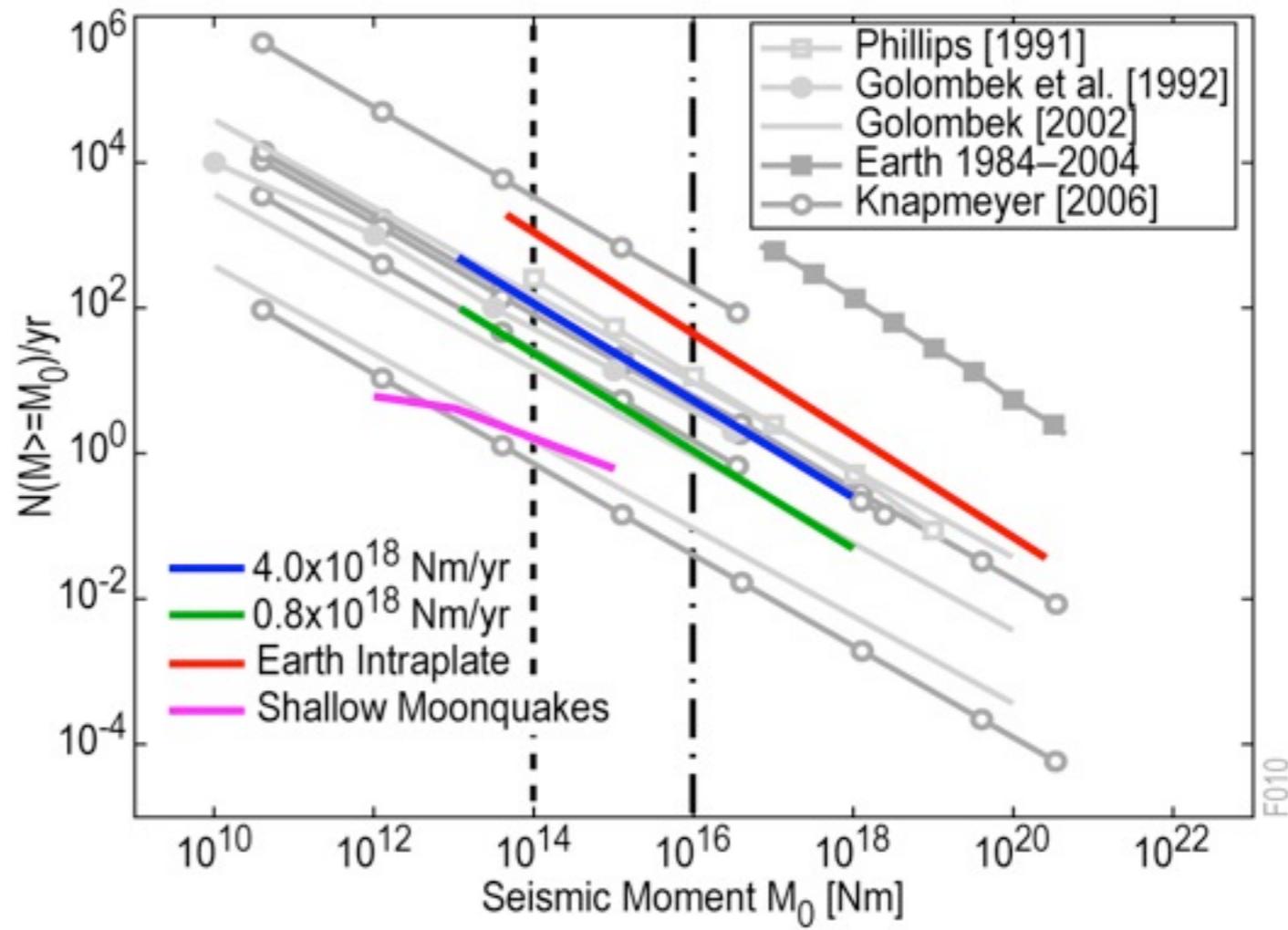


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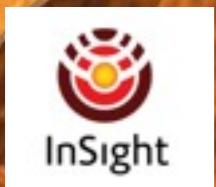
Pressure fluctuation on the ground => ground tilt



Mars seismicity



- Seismicity of Mars remains unknown, even if MRO has brought back some indications on present activity with avalanche and fallen boulder (e.g. Roberts et al., 2012)



JPL
IPGP

ETH

MPS

cnes

Imperial College
London

LÉON

ISAE
SUPAERO

CNRS

INSU
CNRS
PARIS
DIDEROT

Seismic targets

M~5.5 a few/yr

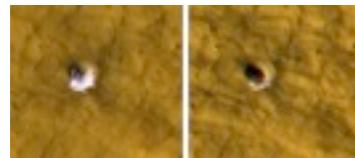
Global

M~4.5 ~ 10/yr

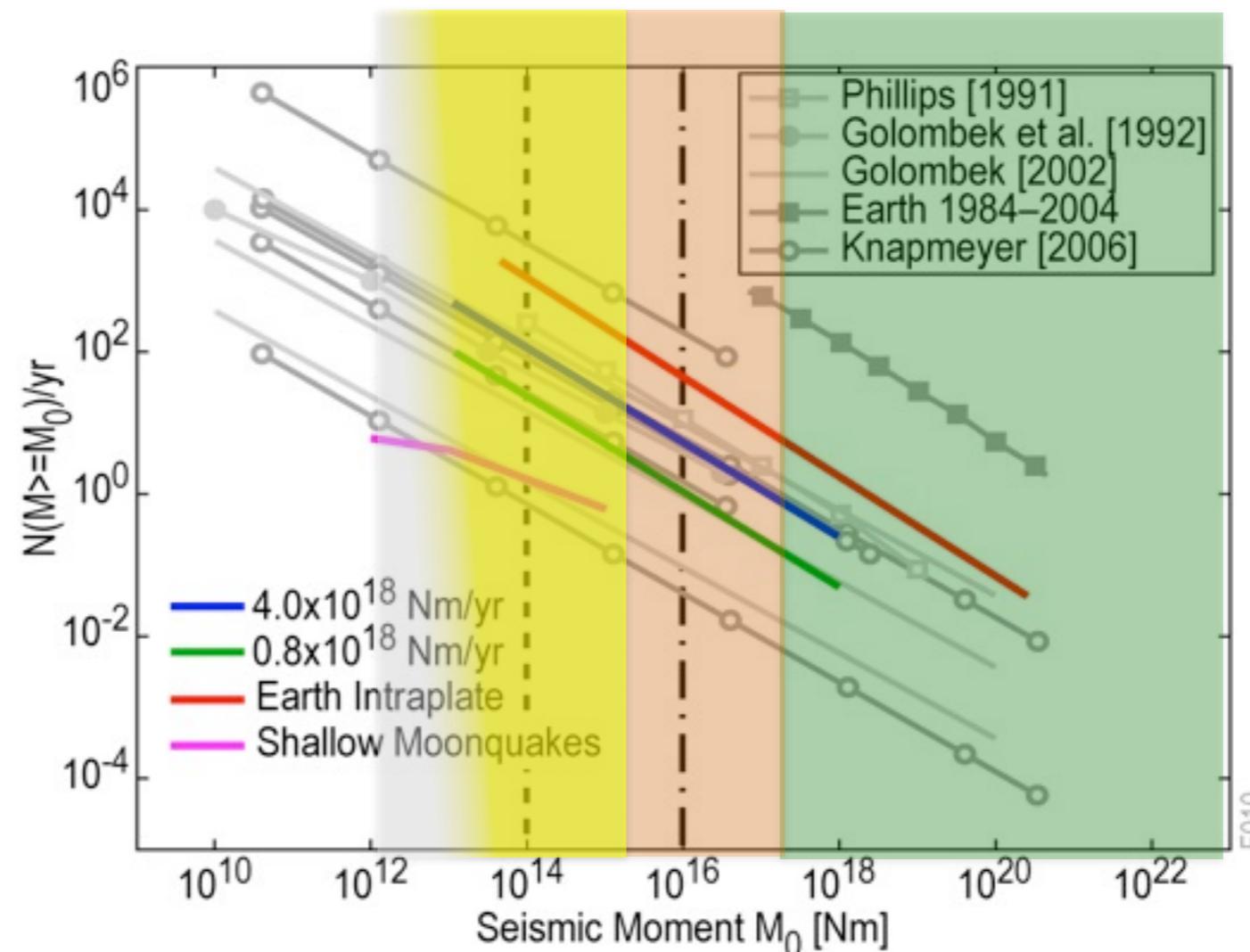
Global to regional

M~3.5 ~100/yr

Regional

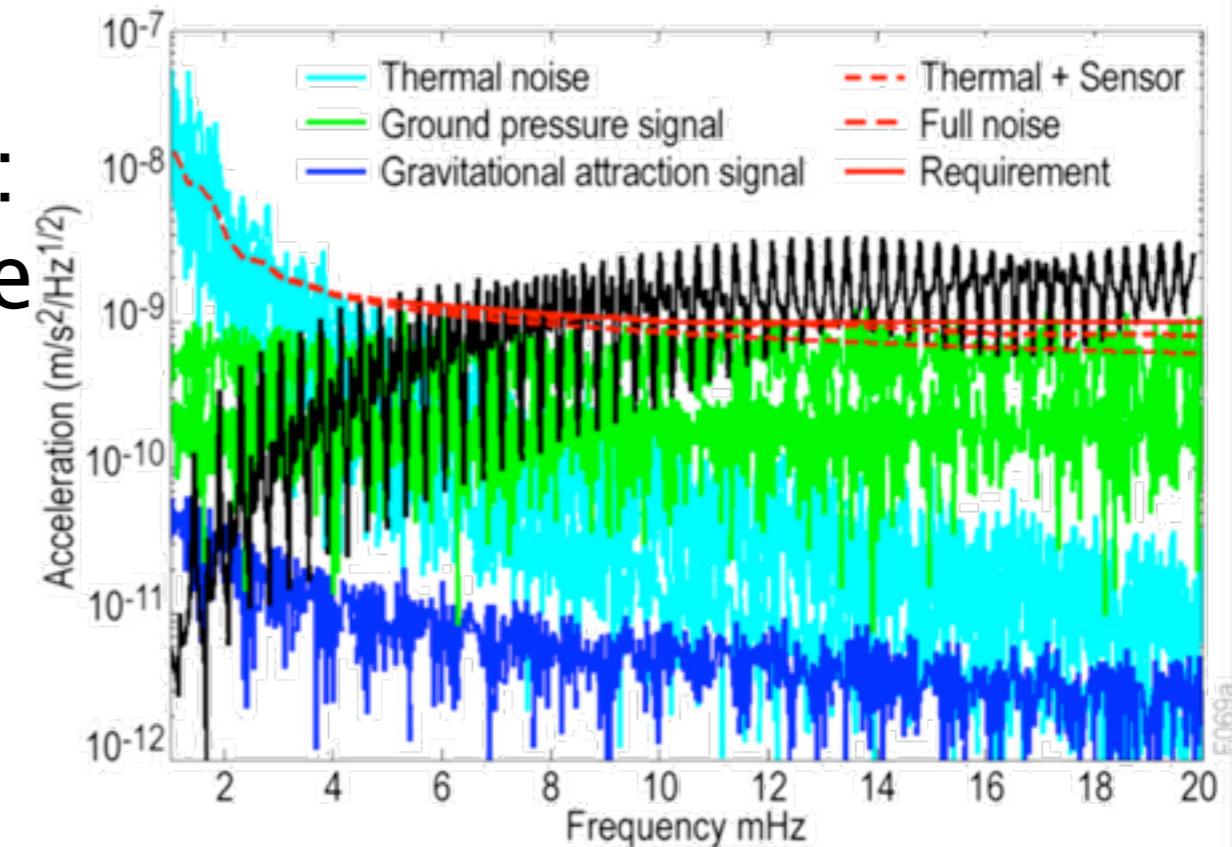
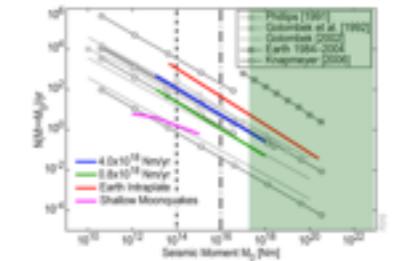


Plus impacts...

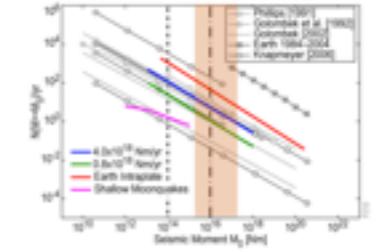


Seismic target #1:

- Normal modes of a 2×10^{17} Nm quake
- « spectroscopy » seismology: does not need the knowledge of the source location
- will constrain the upper mantle with the normal modes frequency inversion (e.g. PREM on Earth)



Seismic target #2:



- Epicentral distance will be determined from Surface waves arrival of R1, R2
- Most of the error in the Distance will be related to the 3D structure as seen by the surface waves
- Full great circle travel time (e.g. $T_R = T_{R3} - T_{R1}$) will be determined from analysis of the largest events (and refined from joint analysis of all events)
- Analysis principle:

$$t_{R2} - t_0 = \frac{2\pi a - \Delta}{v_R}$$

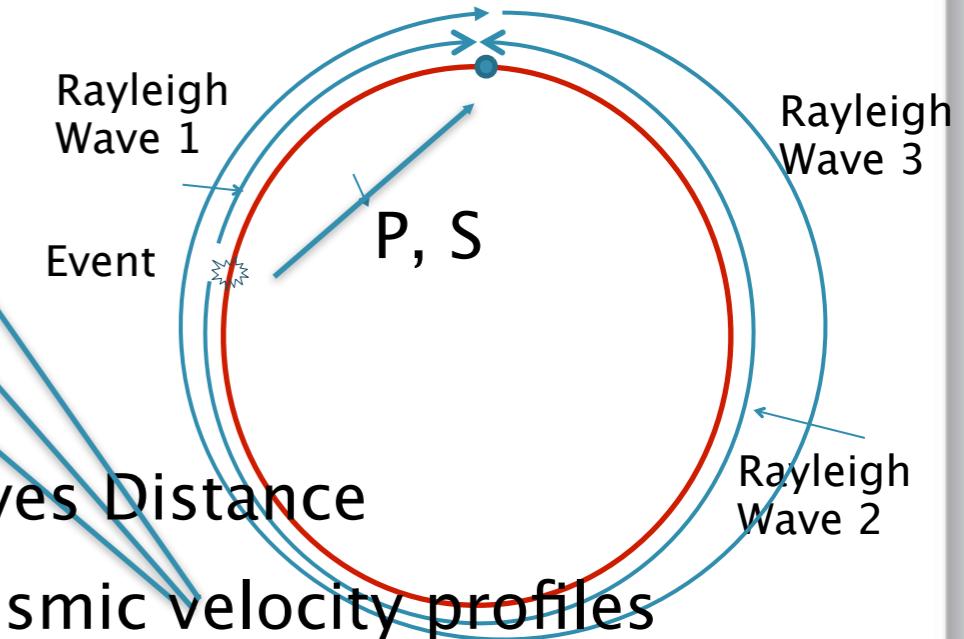
$$t_{R3} - t_{R1} = \frac{2\pi a}{v_R}$$

Depends on lateral variations: gives Distance

$$\frac{\Delta}{\pi a} = 1 - \frac{t_{R2} - t_{R1}}{T_R}$$

$$t_S - t_P = f_1(\Delta, v_s, v_p)$$

$$T_R = f_3(f, v_s, v_p)$$

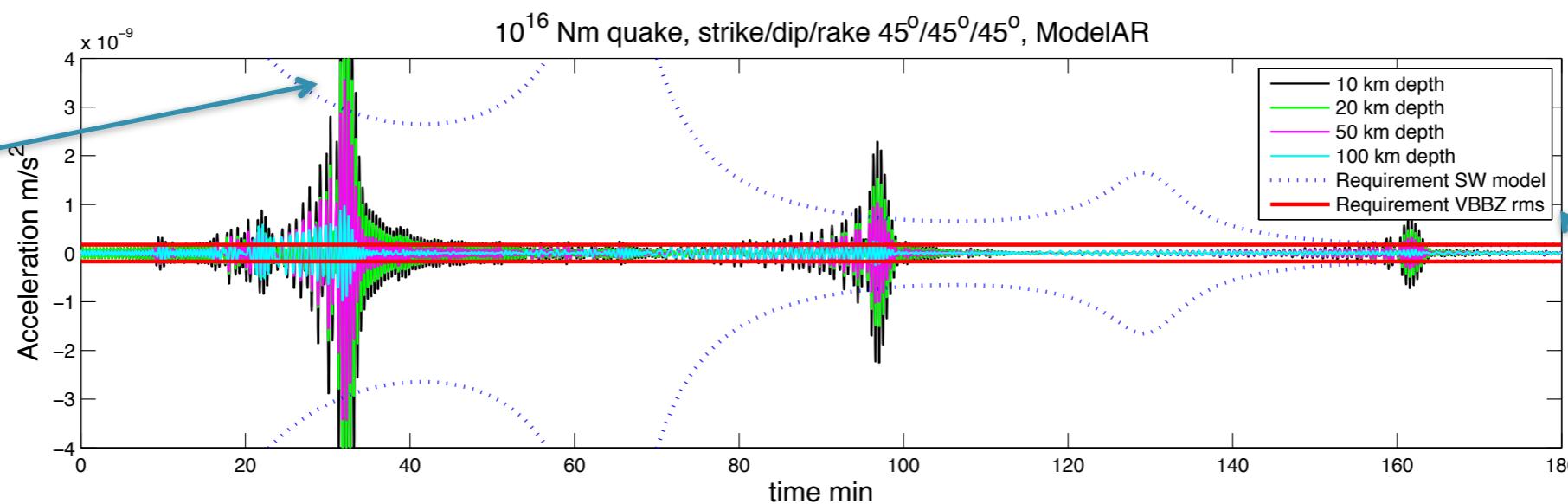


Depend on both lateral and depth variations: gives seismic velocity profiles

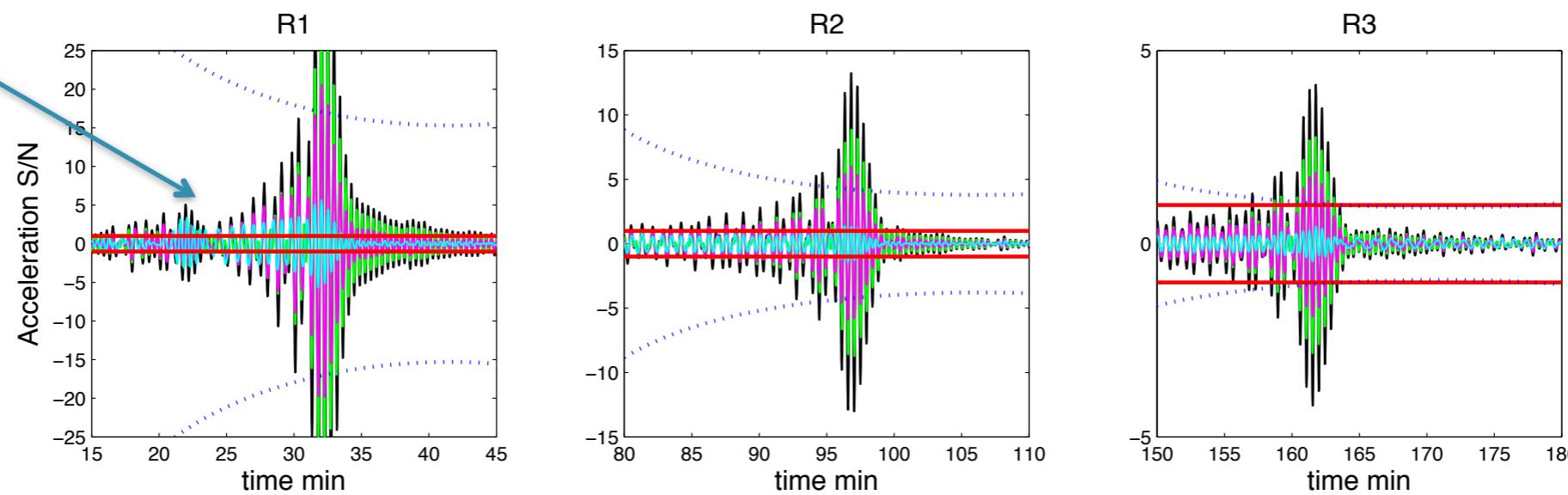


Typical Signal to noise : Rayleigh

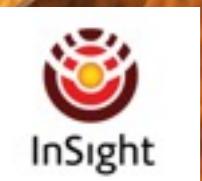
Rayleigh



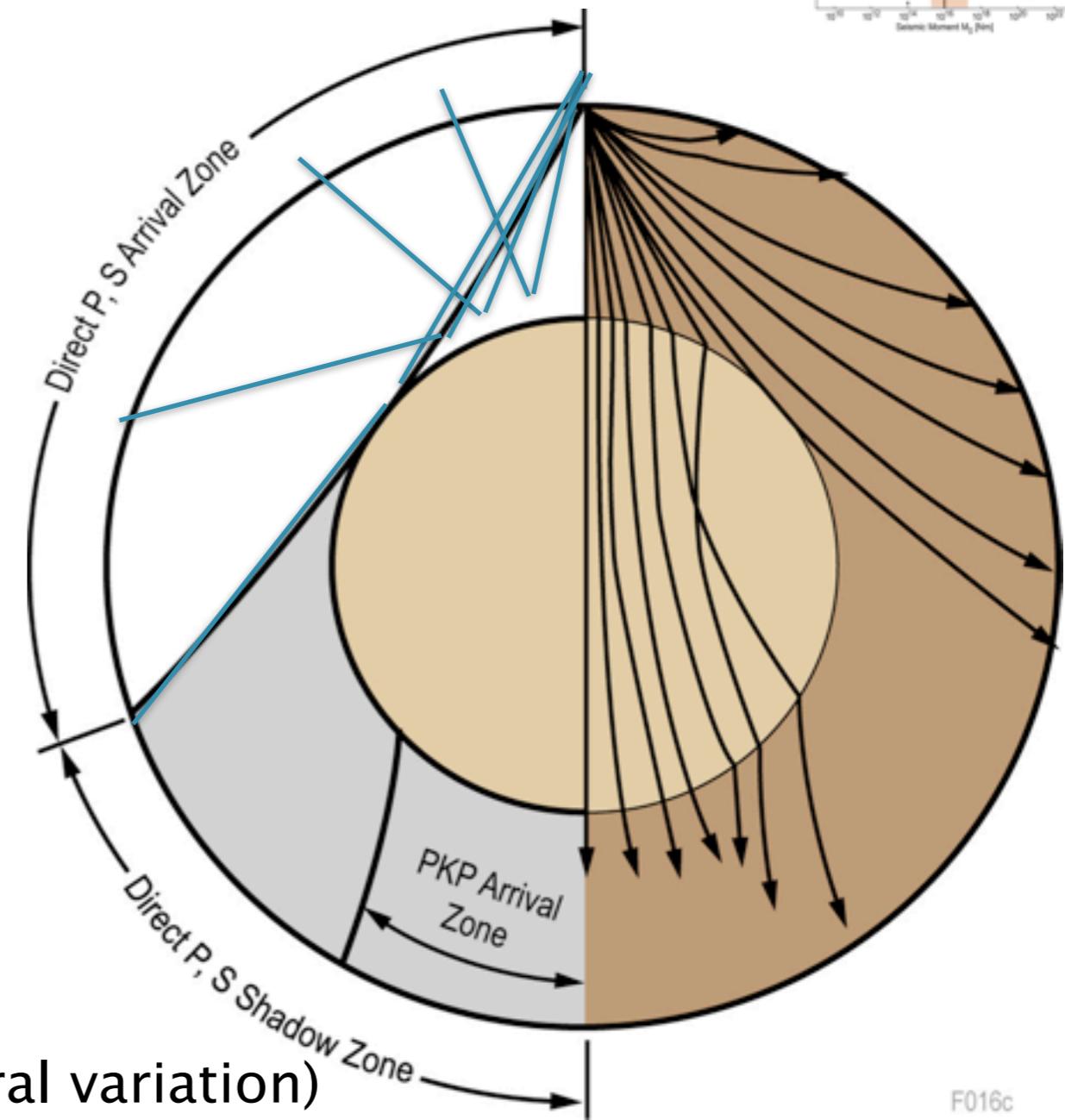
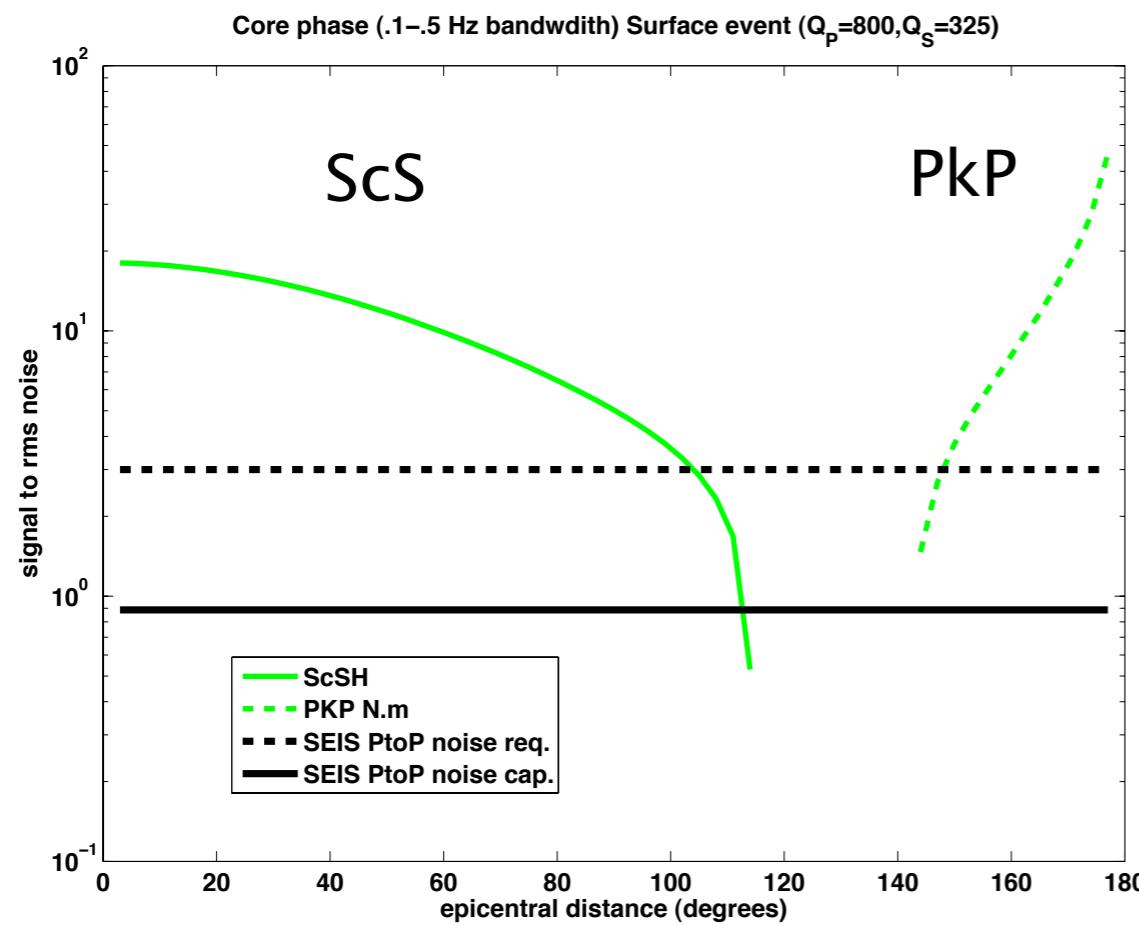
Overtones



Rms Noise
in
bandwidth



Typical Signal to noise : core phase

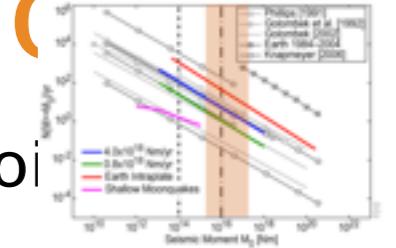


Expected Distance error ~10%
(less with a priori on crustal lateral variation)

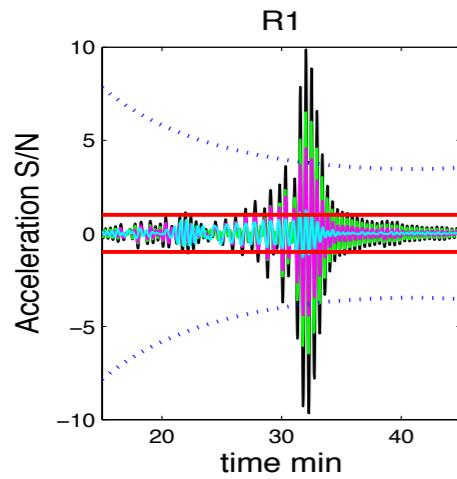


Earth data/Mars Model validation

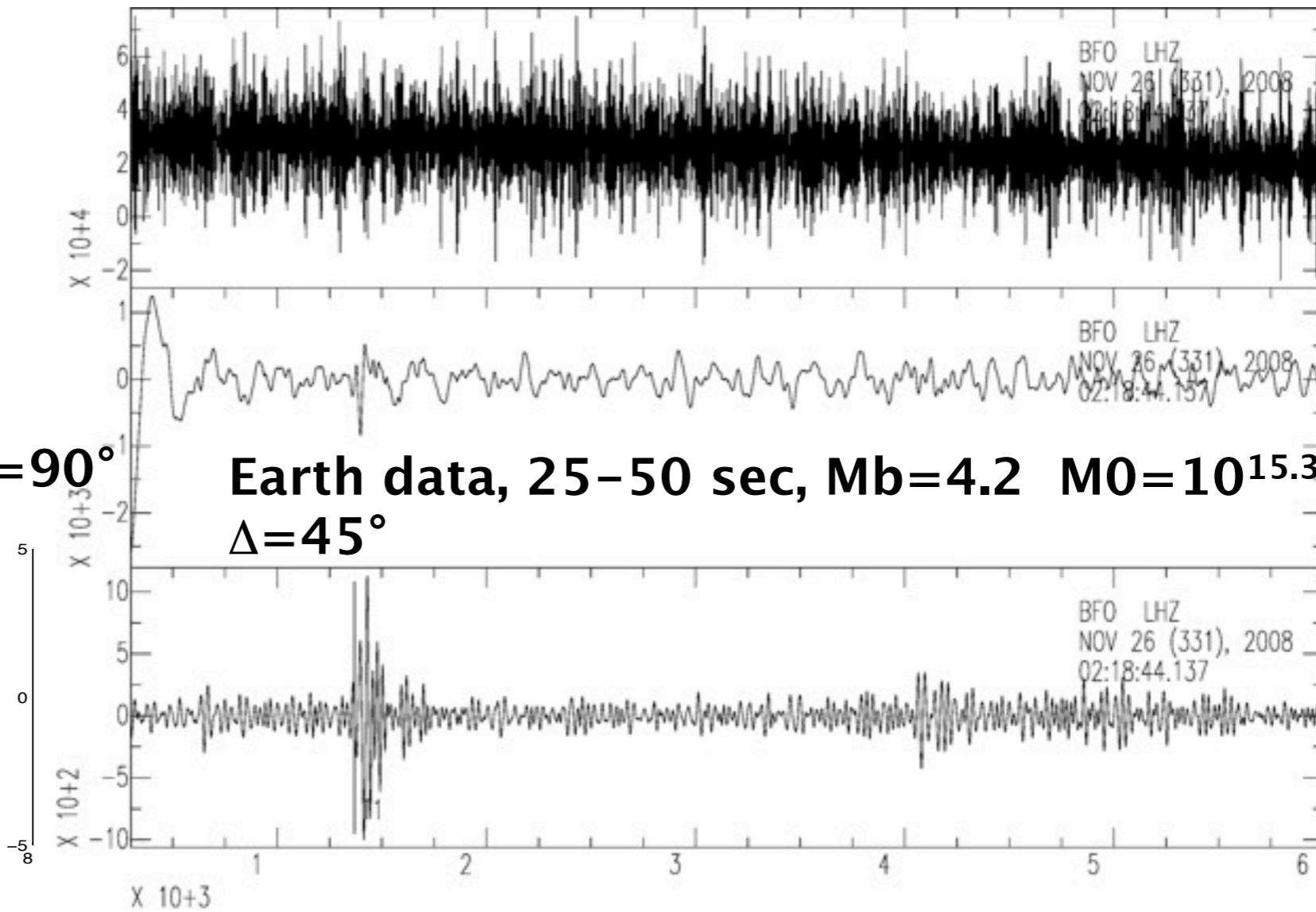
Body waves non observed due to Earth noise



Mars synt data, $\Delta=90^\circ$



Earth data, 25–50 sec, $M_b=4.2$ $M_0=10^{15.35}$ nm,
 $\Delta=45^\circ$



Noise level $\sim 10^{-9} \text{ ms}^{-2}/\text{Hz}^{1/2}$

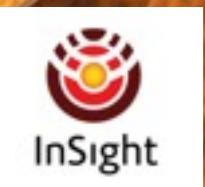
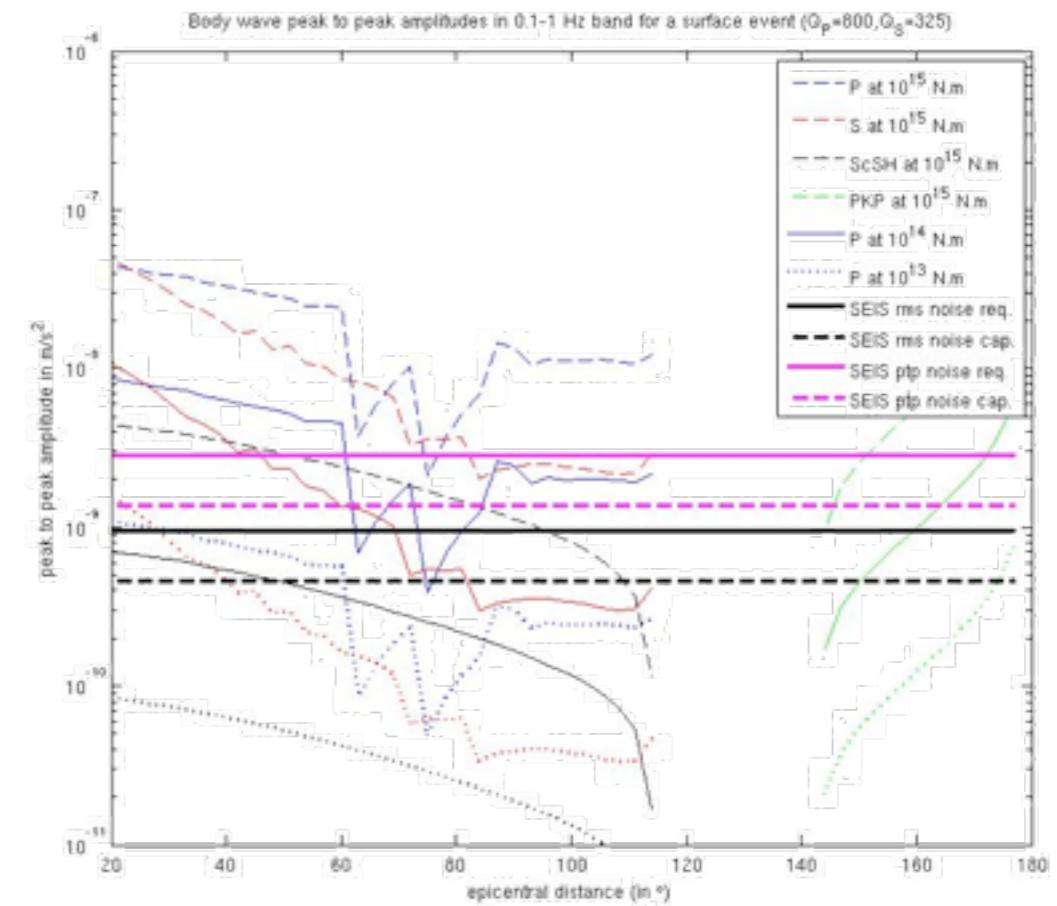
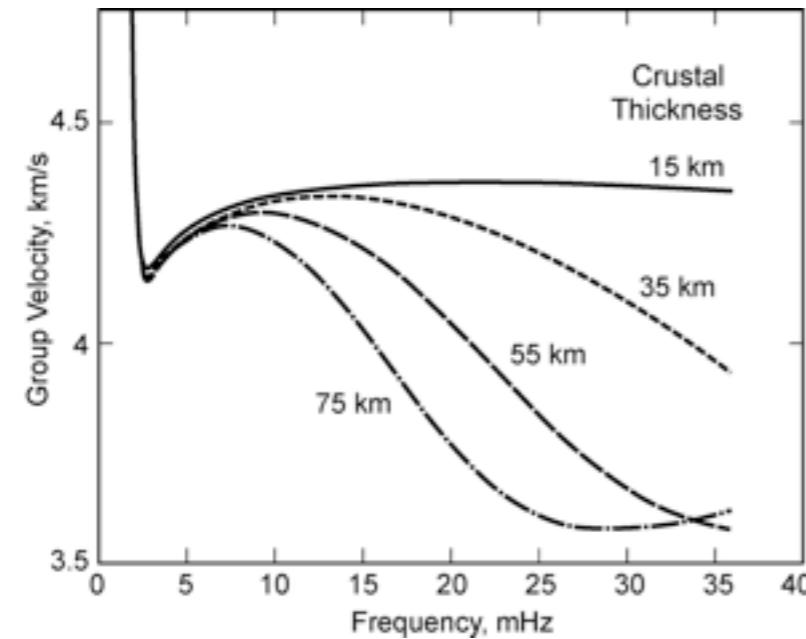
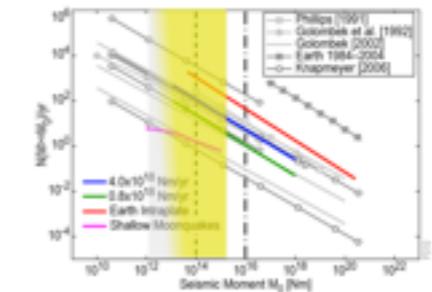
More in poster 1515



Seismic target #3:

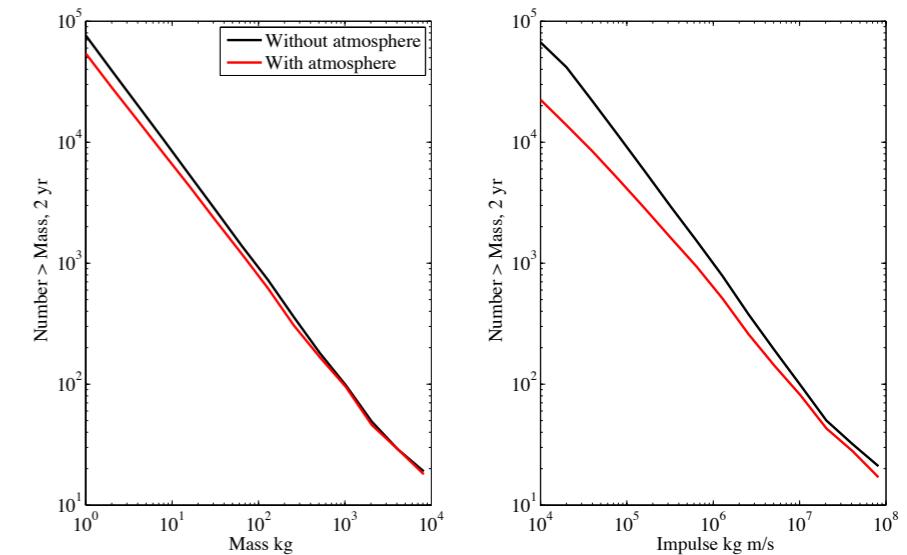
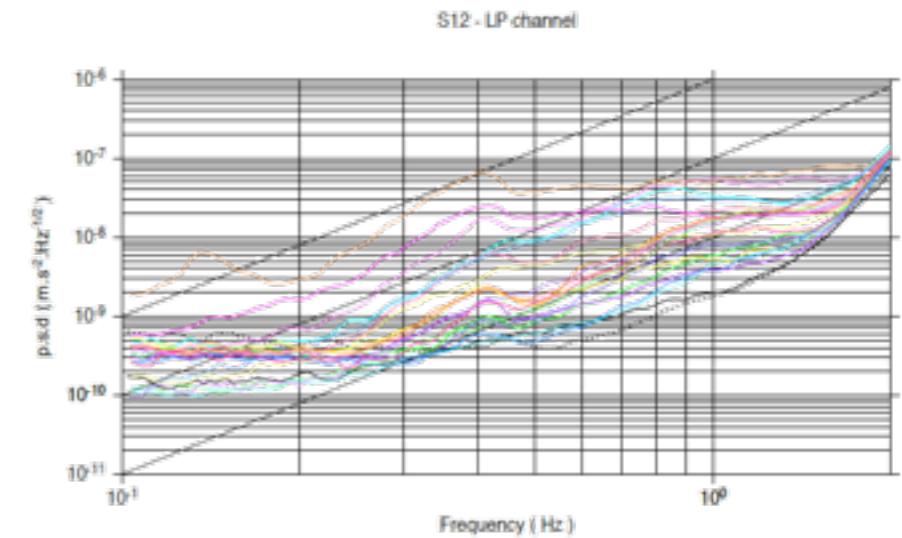
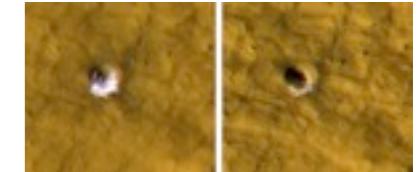
- 10^{14} – 10^{15} Nm quakes will provide P,S and Surface waves records enabling

- Regional crustal inversion from surface waves and receiver functions analysis for the 10^{15} Nm quakes
- Quake location for the $\leq 10^{14}$ Nm quakes

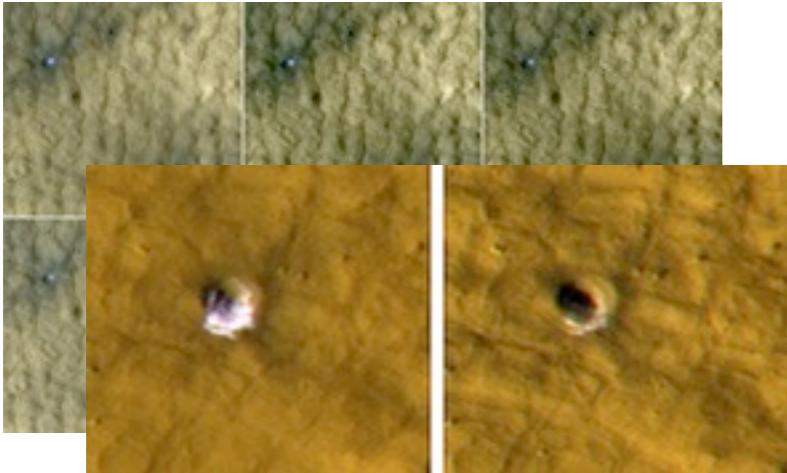


Seismic target #4:

- Seismic signals generated by impacts can be calibrated with Moon Apollo data
 - Amplitude must be corrected by the larger a priori mantle and crust attenuation
- Impactor flux can be estimated with Monte-Carlo modeling
 - Ground mass/velocity must however be computed with the atmospheric ablation and shielding

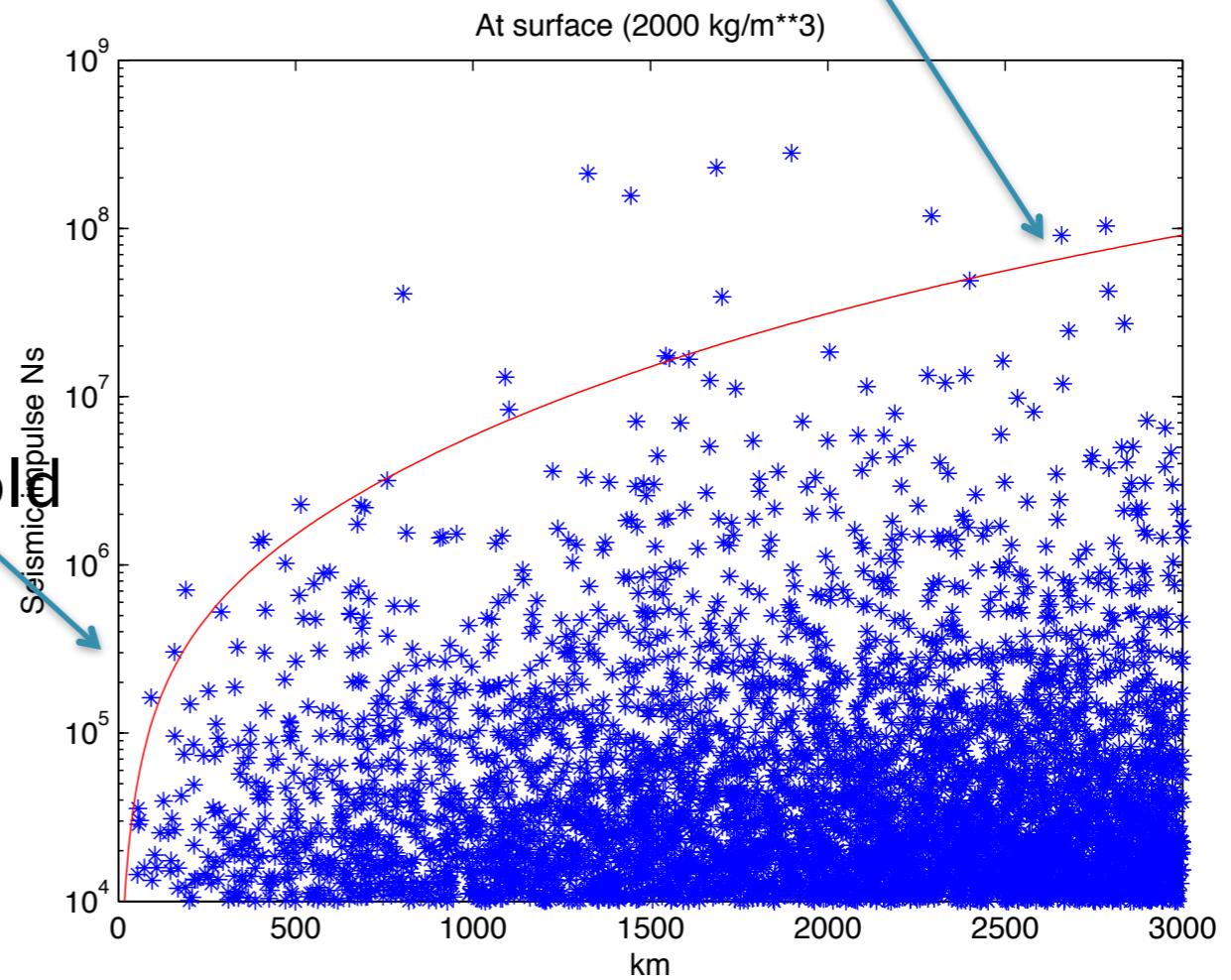


About 20 impacts in 1 Mars yrs with S/N > 3 ($D < 3000$ km)
(16 for $D < 2000$ km and 4 for $D < 400$ km) Seismic SN ~3



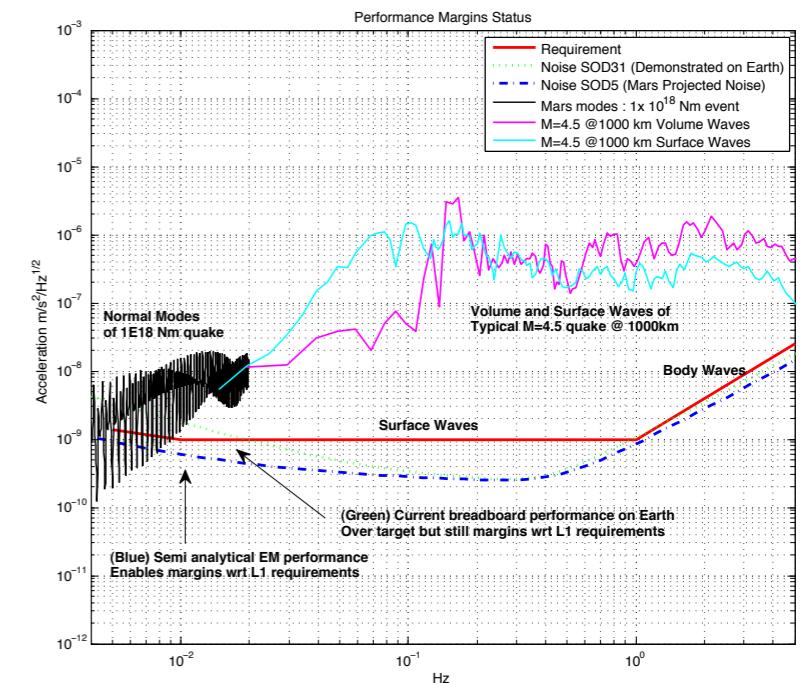
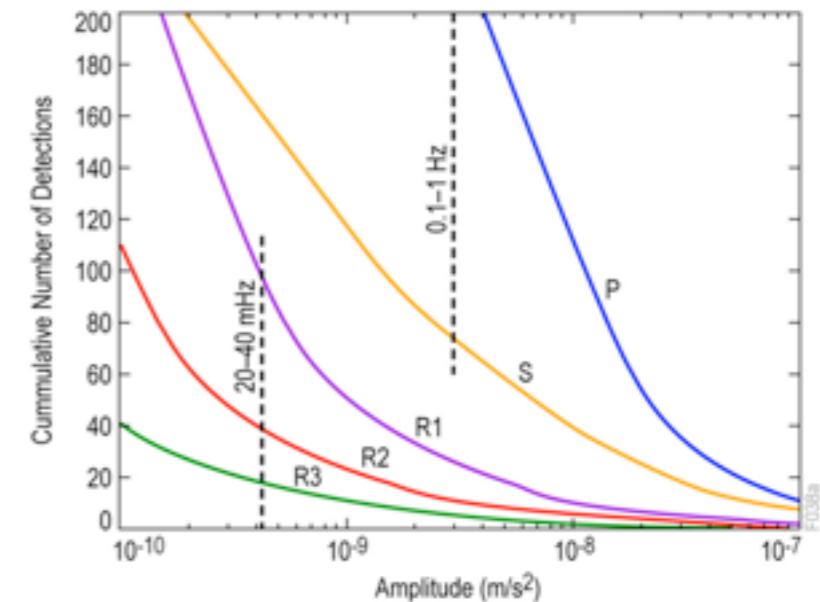
MRO Optical detection threshold

Joint MRO/InSight impacts observation will allow location constrained seismic analysis and amplitude constrained impact analysis with science return similar to the artificial impacts of Apollo!



Summary

- Modeling indicate that a Low noise (e.g. $<10^{-9} \text{ ms}^{-2}/\text{Hz}^{1/2}$) can be reached on Mars
- Such a low noise enable in 0.7 Mars yr
 - > 10 quakes with R3 and core phases
 - > 40 quakes with P,S,R1 including > 25 with R2
- Such a data set will made possible (with margin of 100%)
 - The determination of the absolute crustal thickness to $\pm 10 \text{ km}$
 - The determination of the seismic velocities of the upper mantle to $\pm 0.25 \text{ km/s}$
 - And the determination of the rate and location of Marsquakes (location within

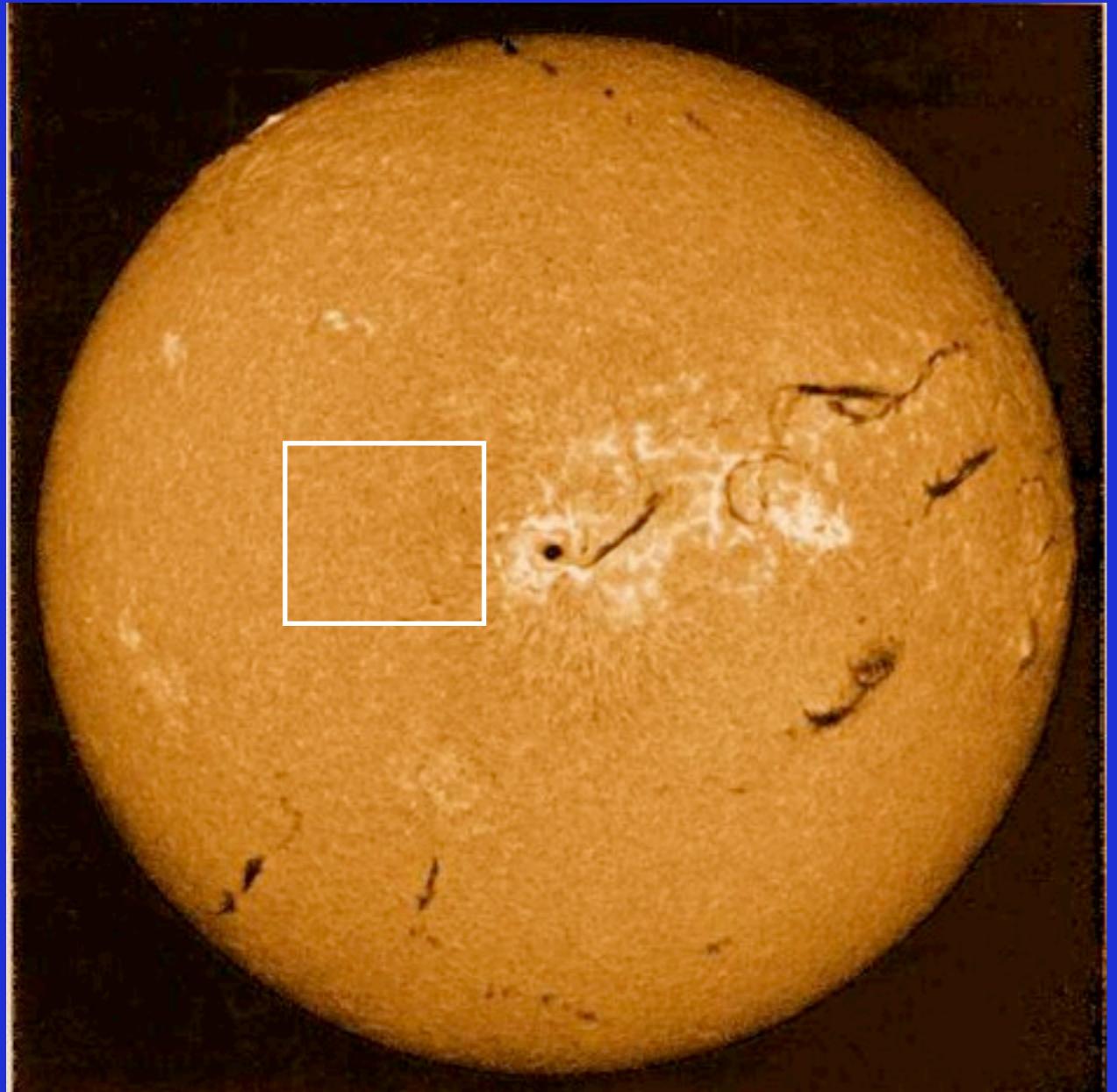




Venus Future
and remote
sensing

Remote sensing planetology

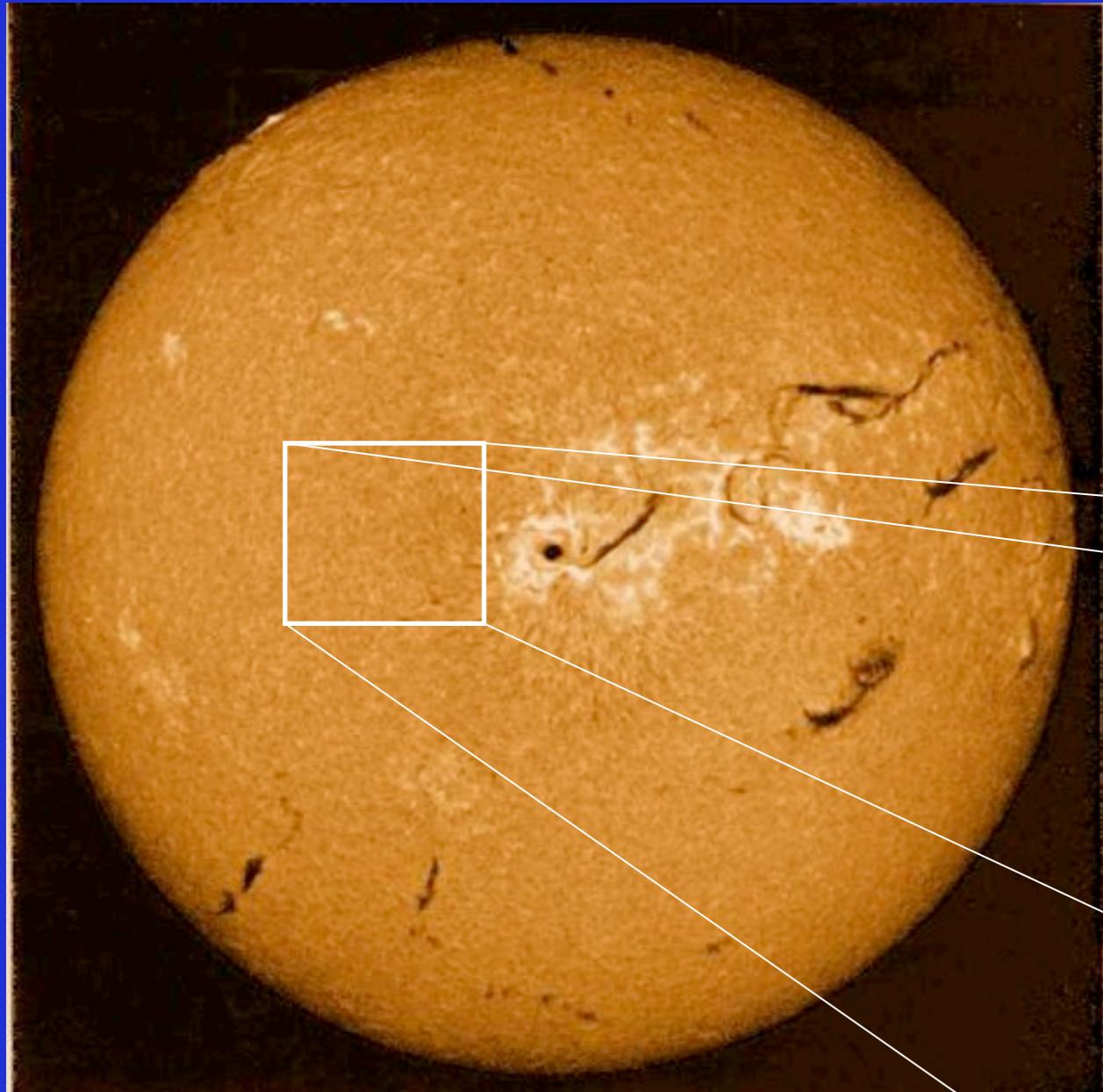
Exemple 1: seismic remote sensing of the Sun



1,400,000 km

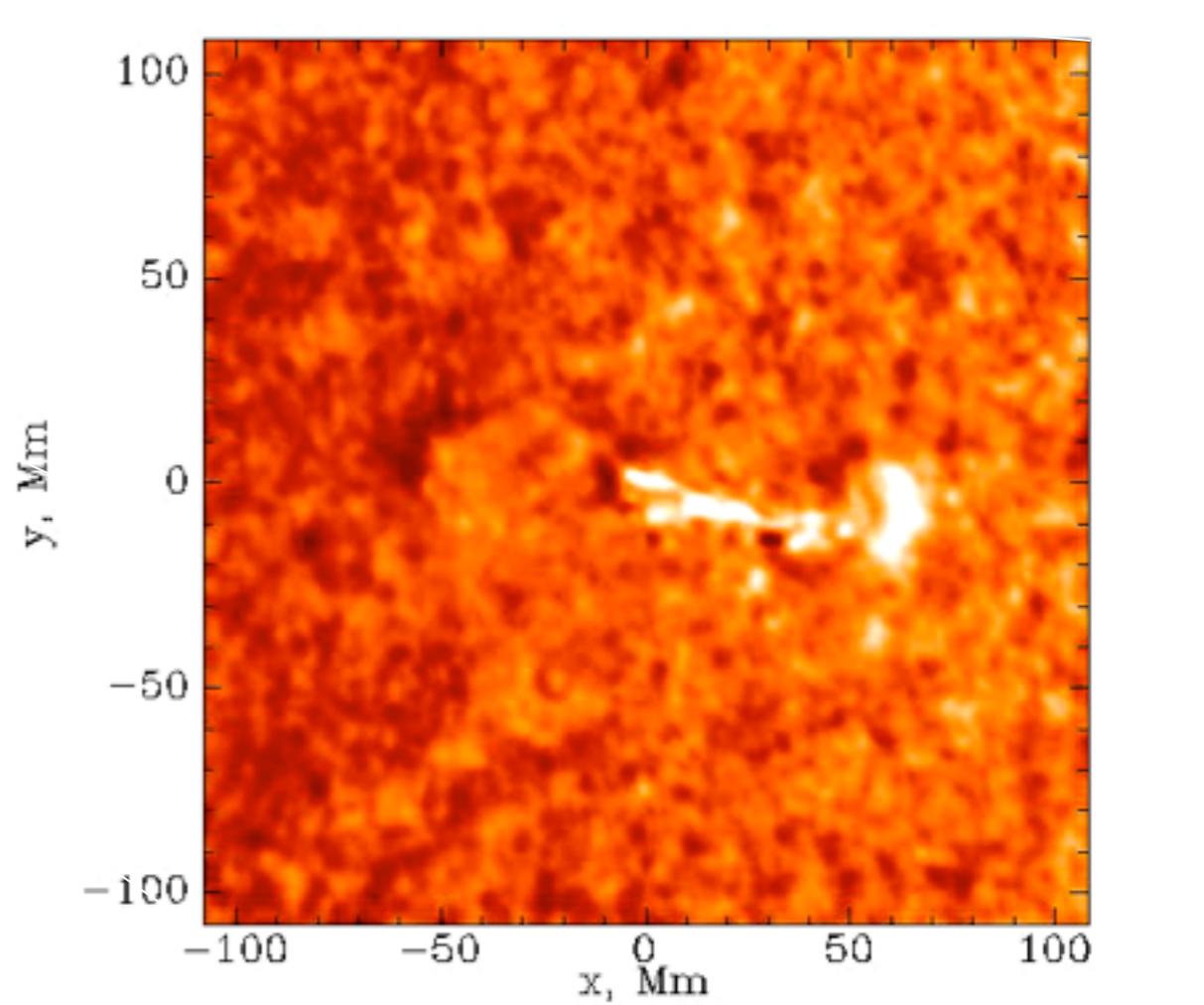
- ESA/NASA spacecraft observation with MDI (Michelson Doppler Interferometer Instrument)
- Sun velocity is measured by using emission of Ni in the photosphere
- 1024x1024 pixels provide the vertical velocity of the Sun every 60 sec with 20 m/s of error

Exemple 1: seismic remote sensing of the Sun

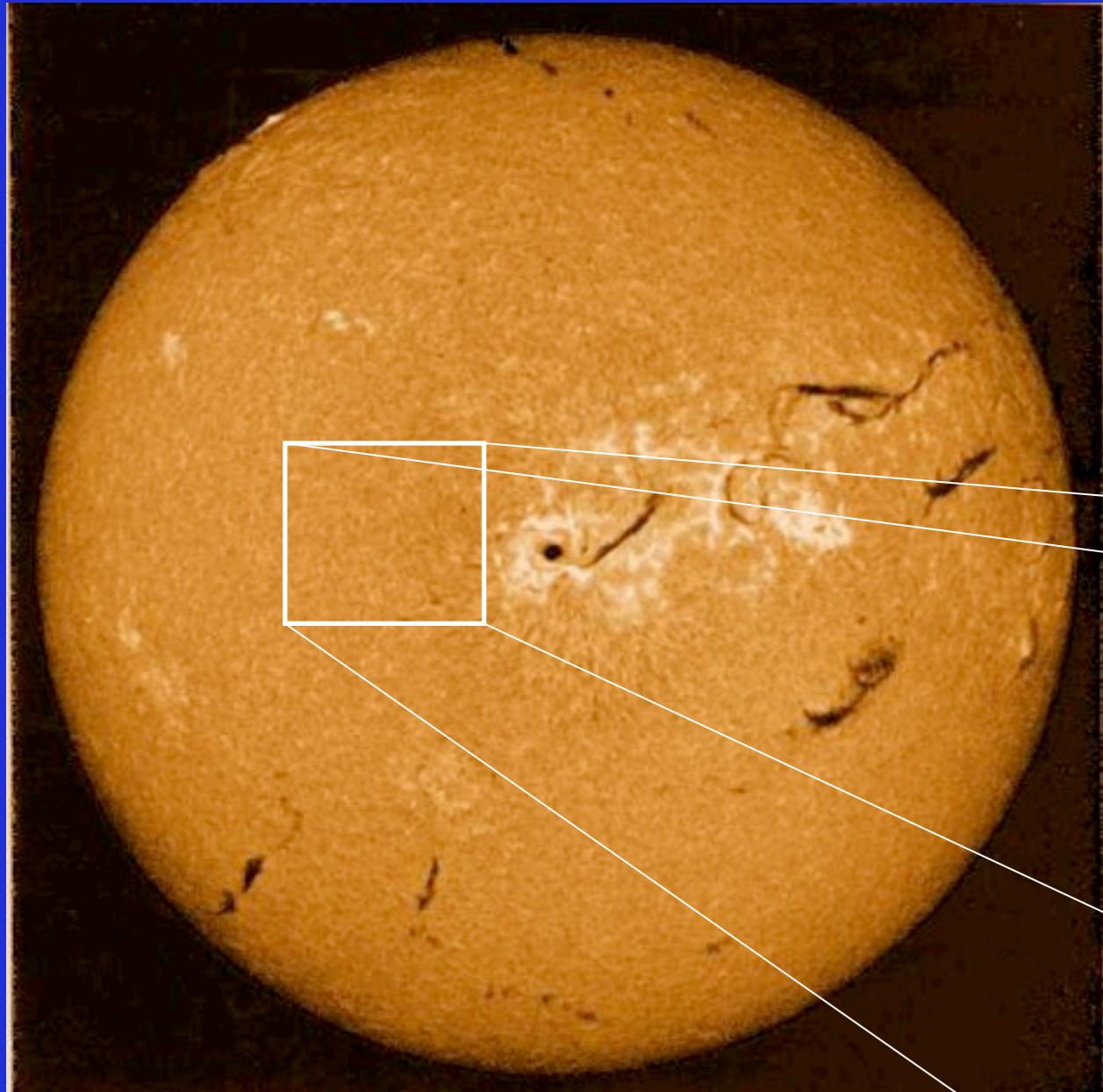


A. G. Kosovichev, V. V. Zharkova, Stanford Un.

- July 9, 1996 solar flare
- Quake equivalent magnitude $M=11$
- Vertical displacement of about 3 km

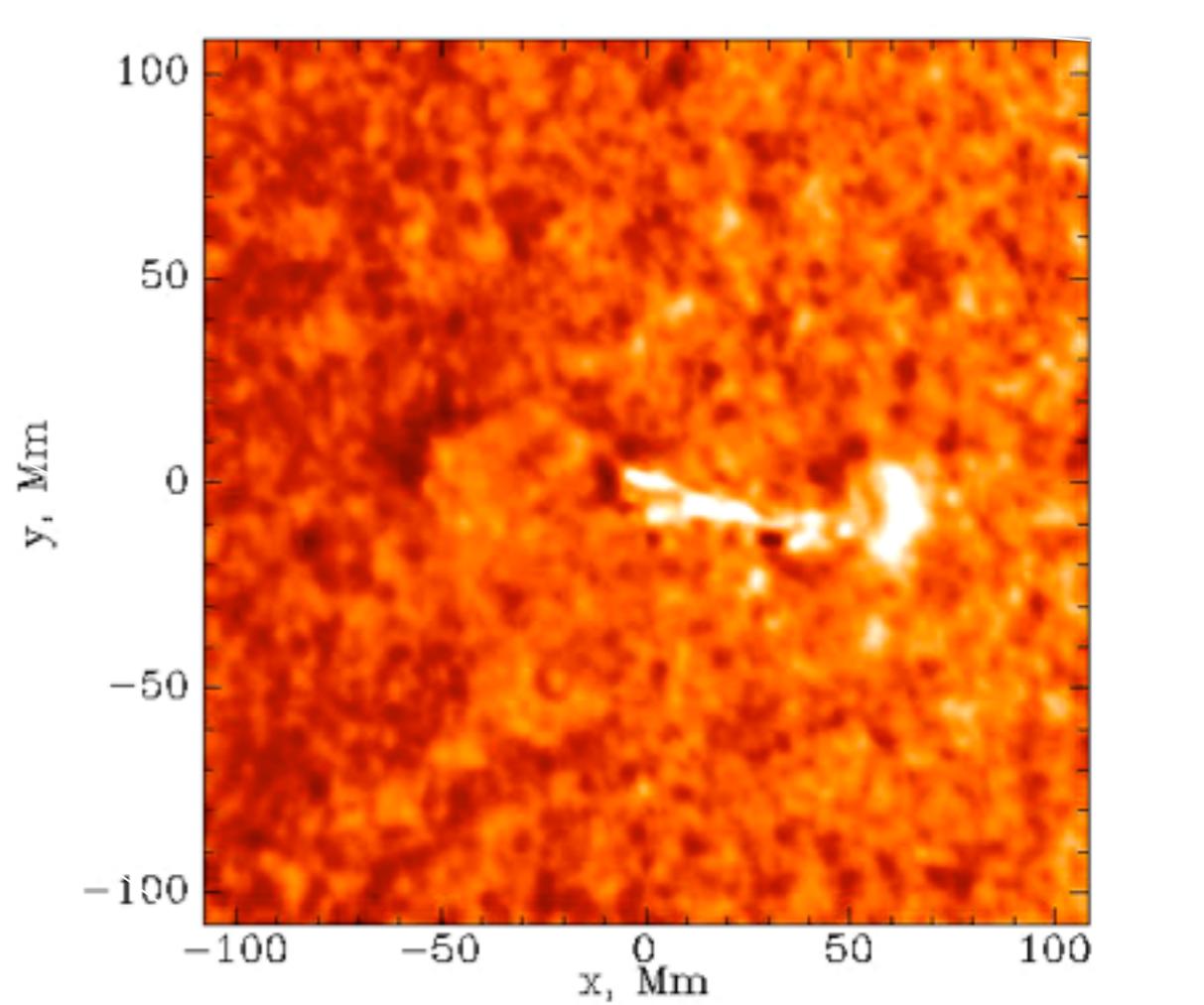


Exemple 1: seismic remote sensing of the Sun

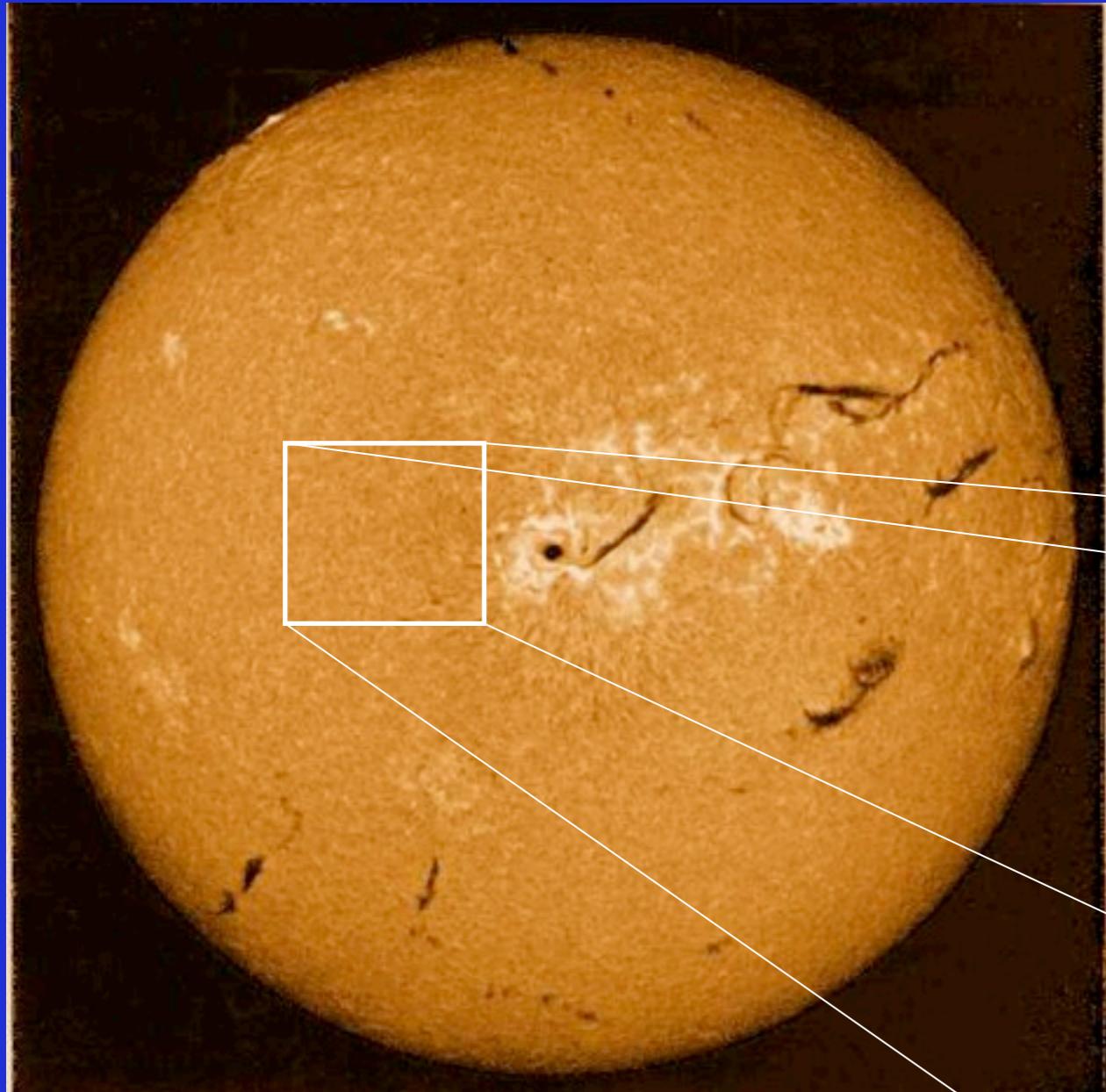


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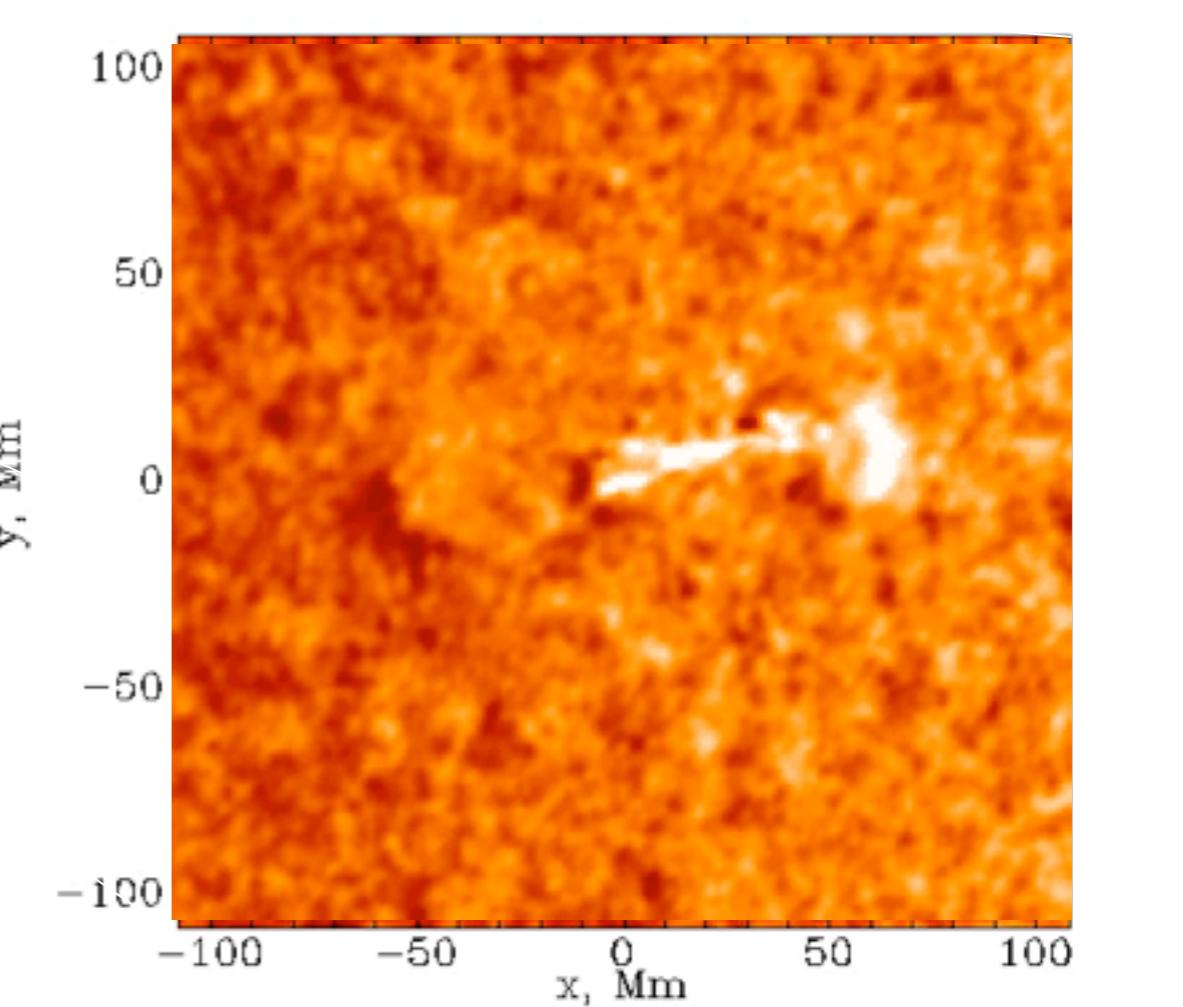


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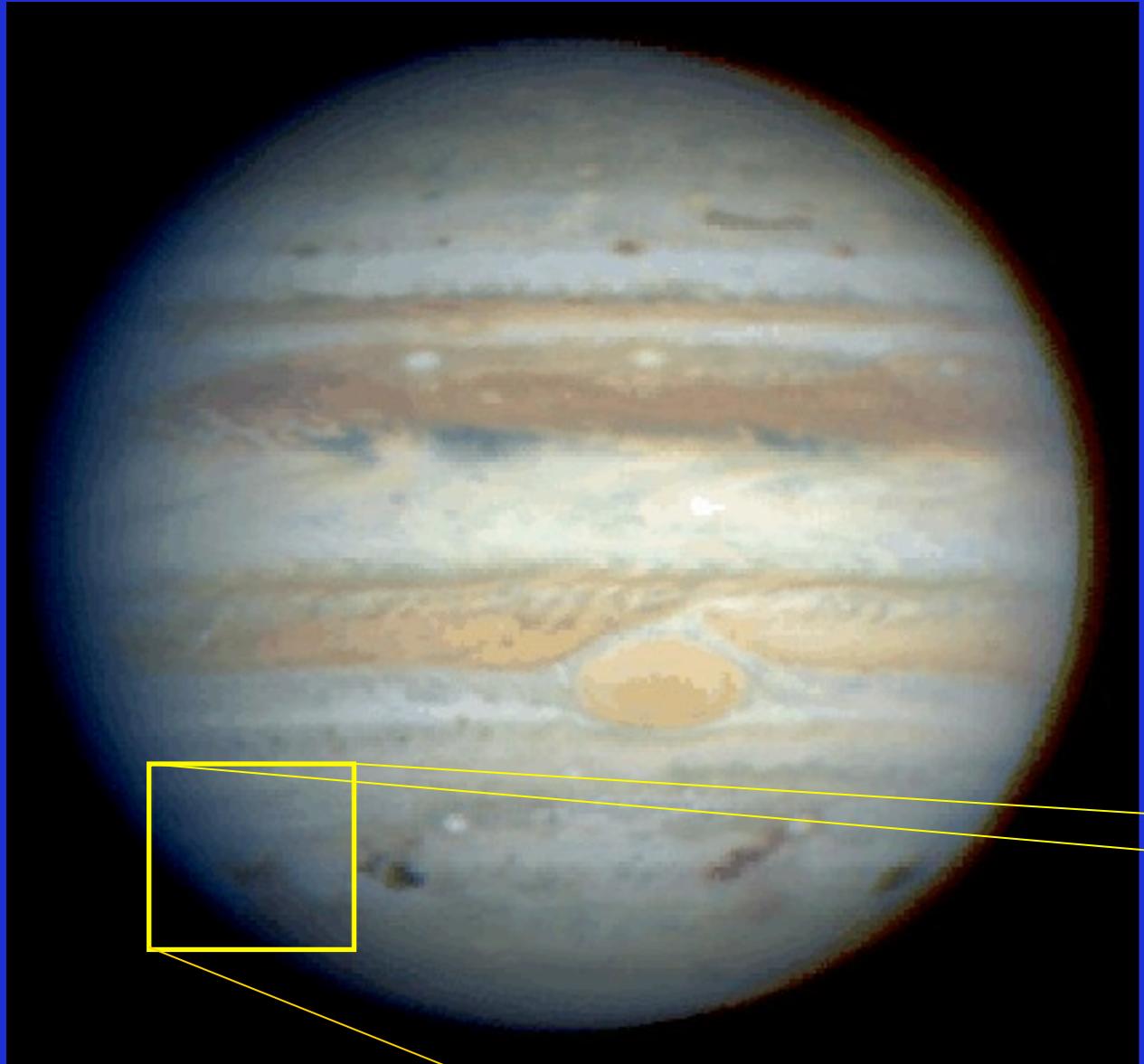


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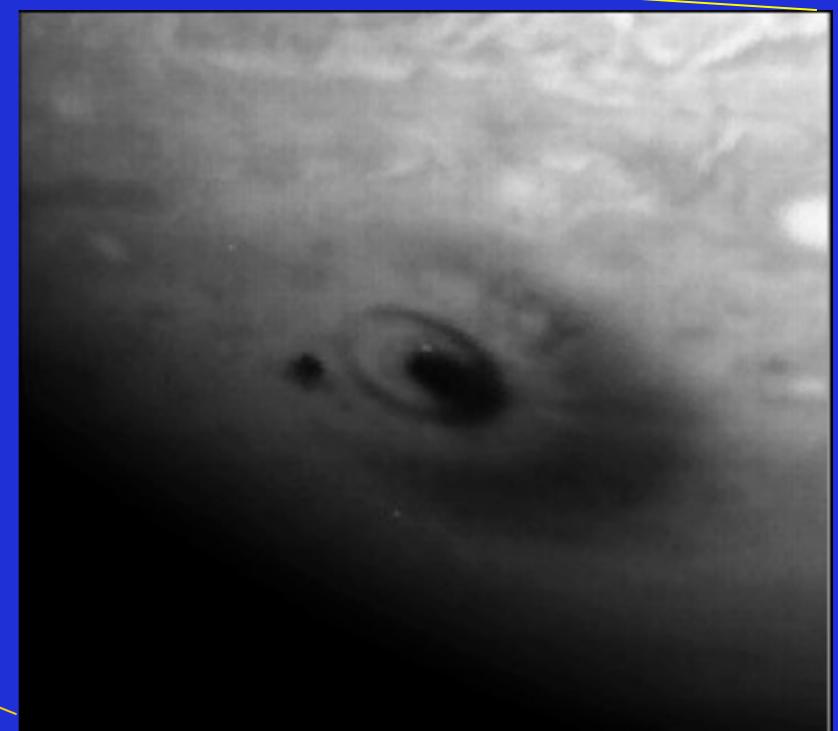


Exemple 2: seismic remote sensing of Jupiter



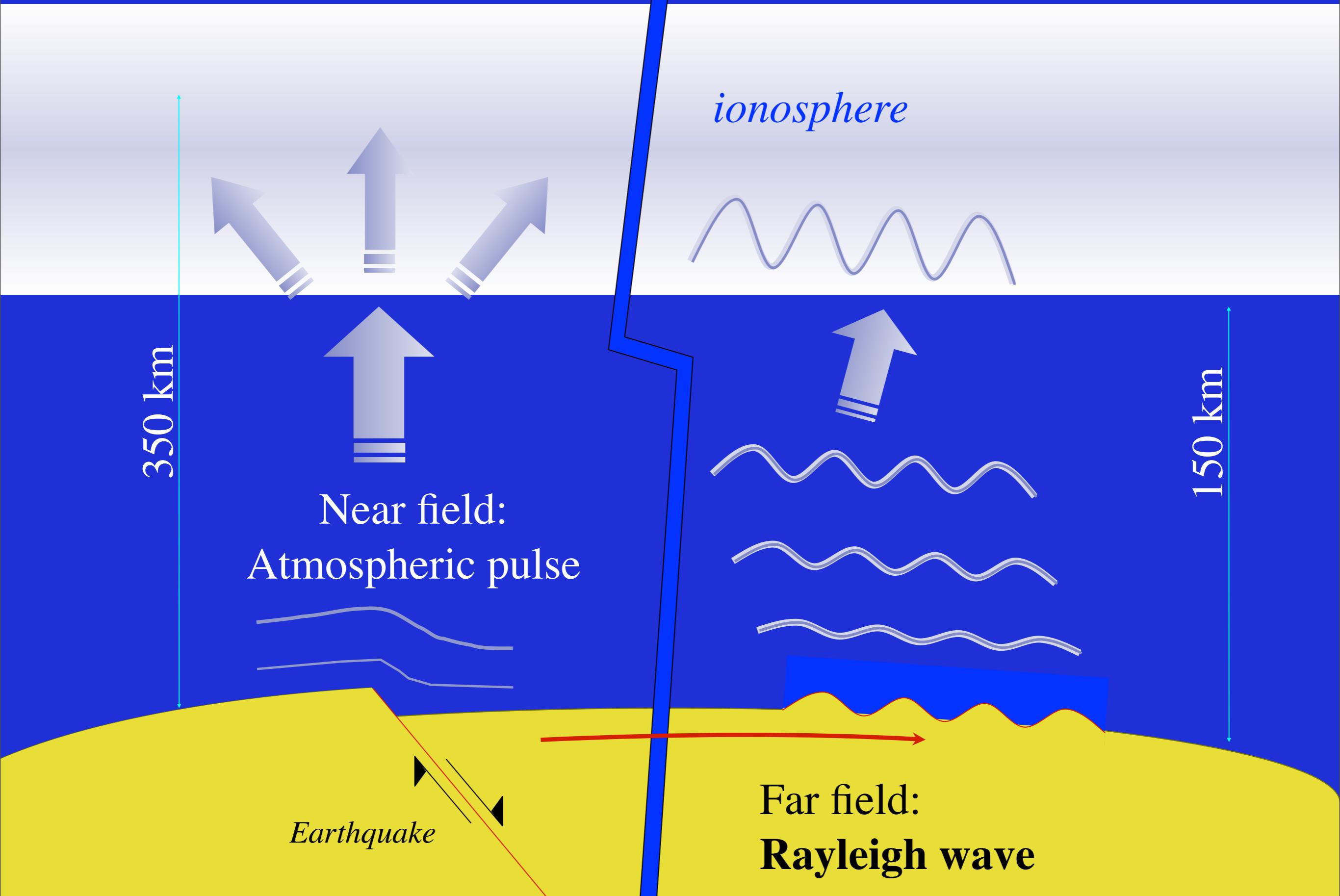
130,000 km

- NASA HST, WFC in optical mode
- July 22, 1994 Shoemaker-Levy 9 impact
- Quake equivalent magnitude $M=9$
- Vertical displacement 100m but with clouds-albedo modification
- No seismic waves observed on ground and space observations
- Tsunami/gravity waves observed

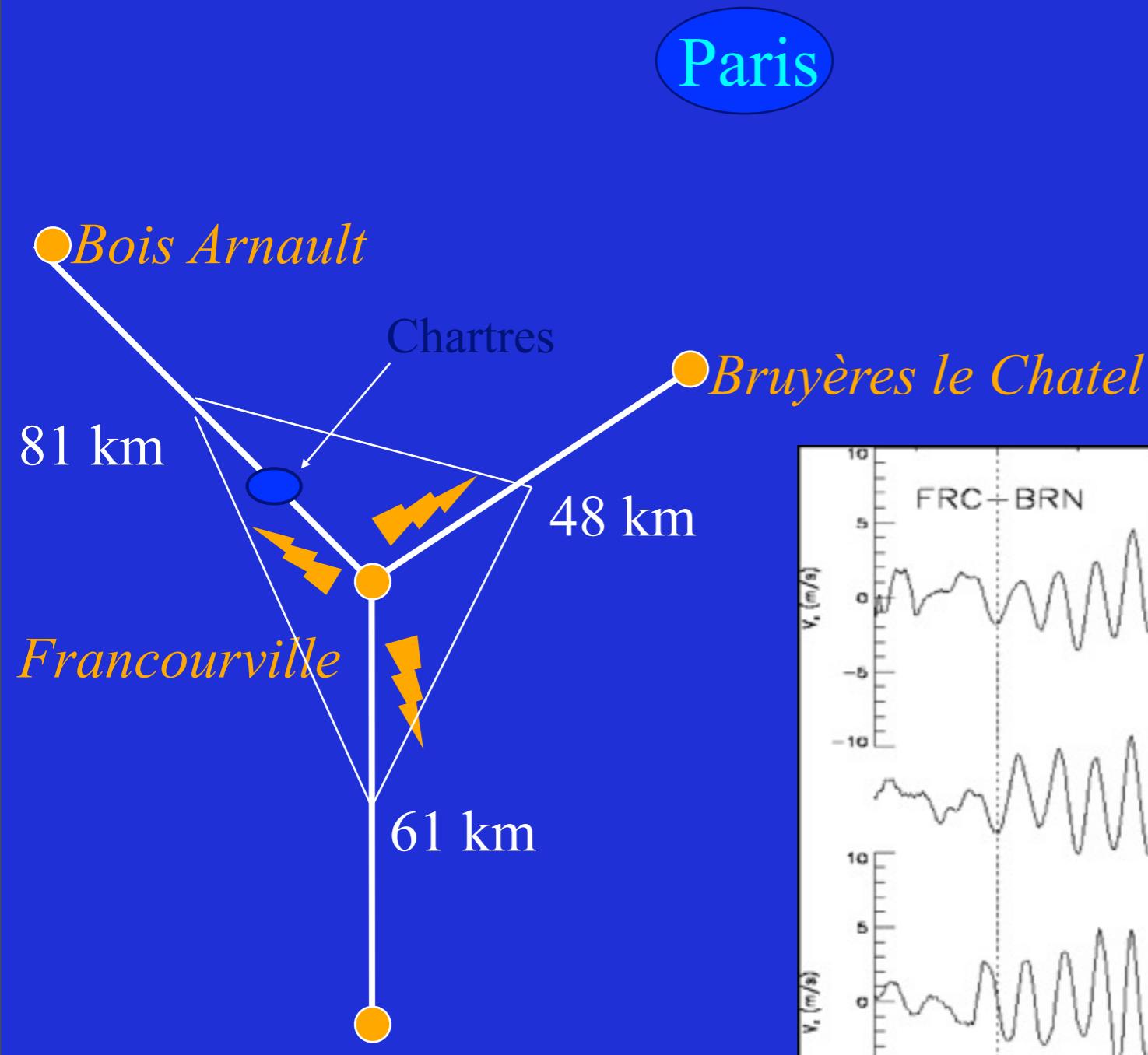


H. Hammel et al, MIT

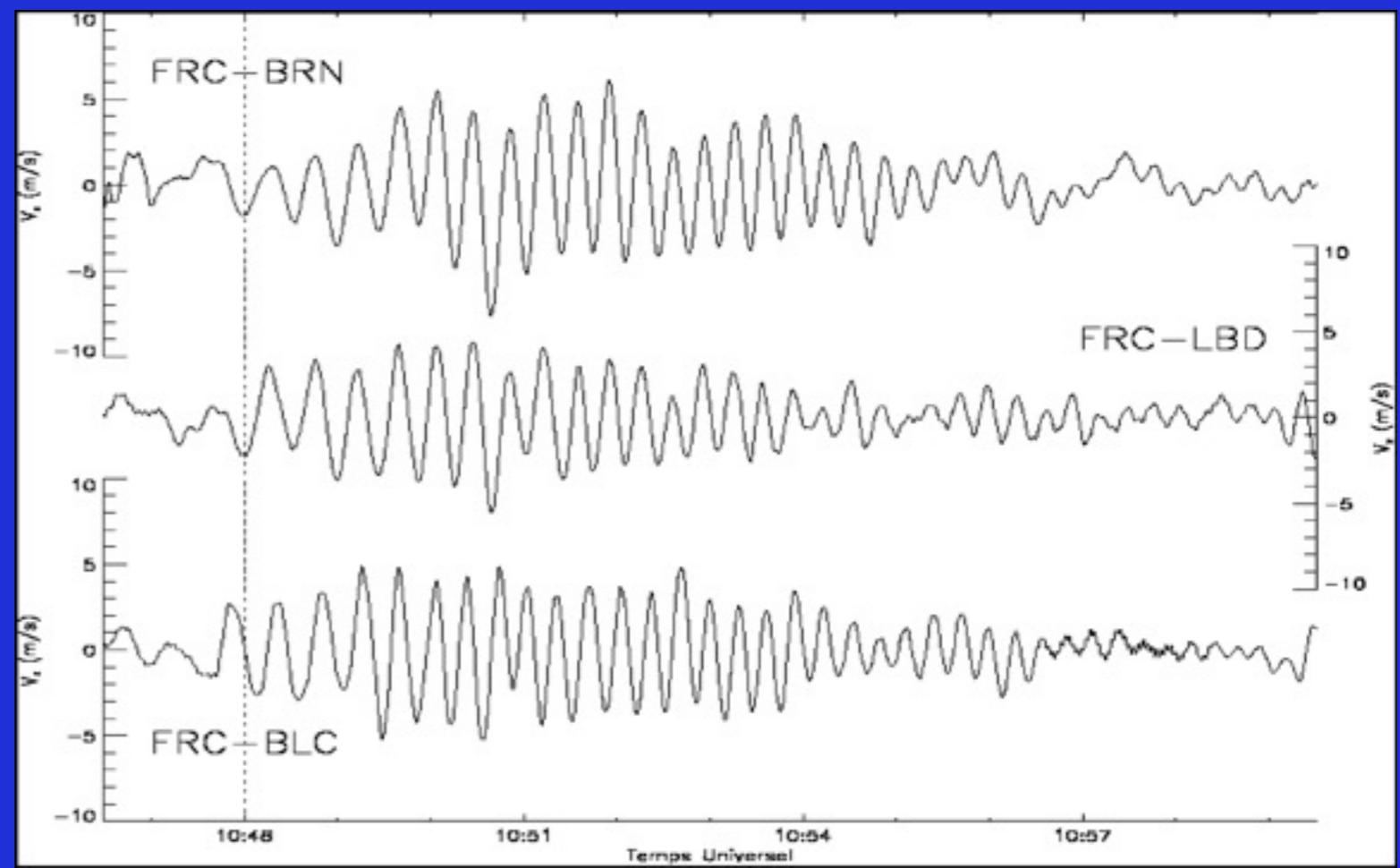
Generation mechanism of infrasonic waves by seismic waves



Francourville ionospheric sounding network



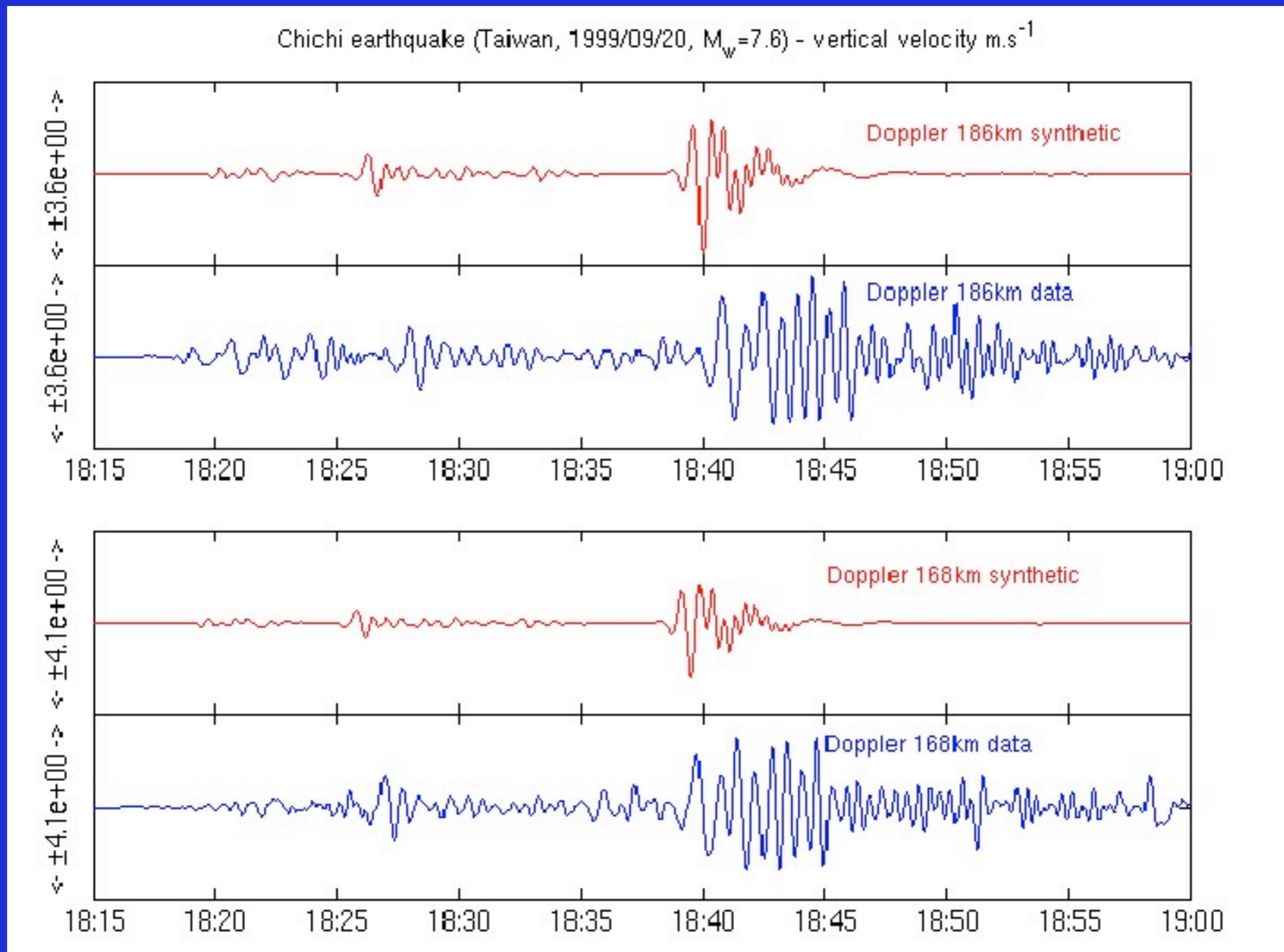
Seismic ionospheric oscillations detected at Francourville 1999/08–2000/06
Artru et al, 2006



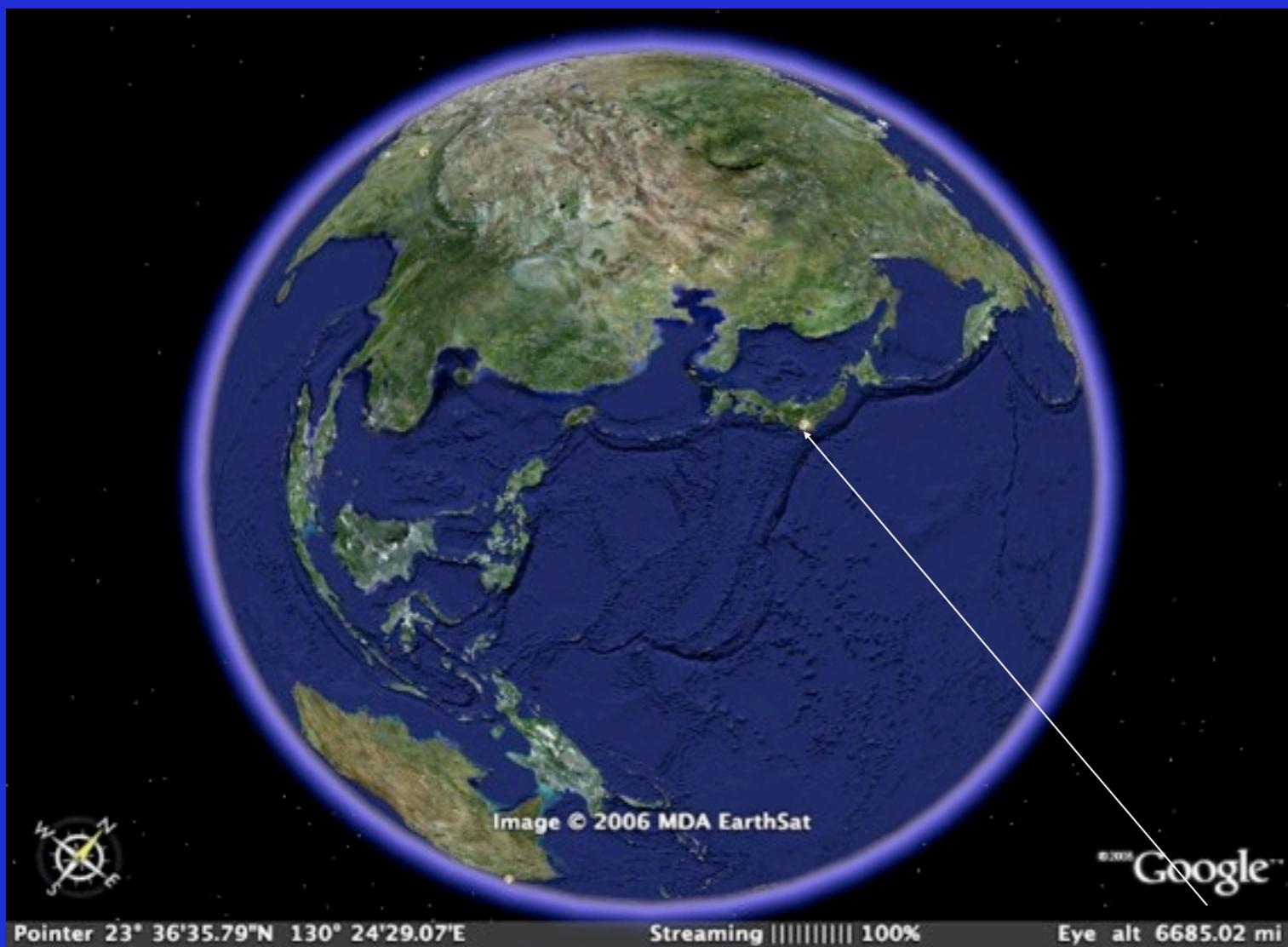
4.6 Mhz, Costa Rica, August 20, 1999
High pass at 200 sec

The network has been working continuously since August 1999, most of $M > 6.5$ earthquakes have been observed.

3D waveform complexity

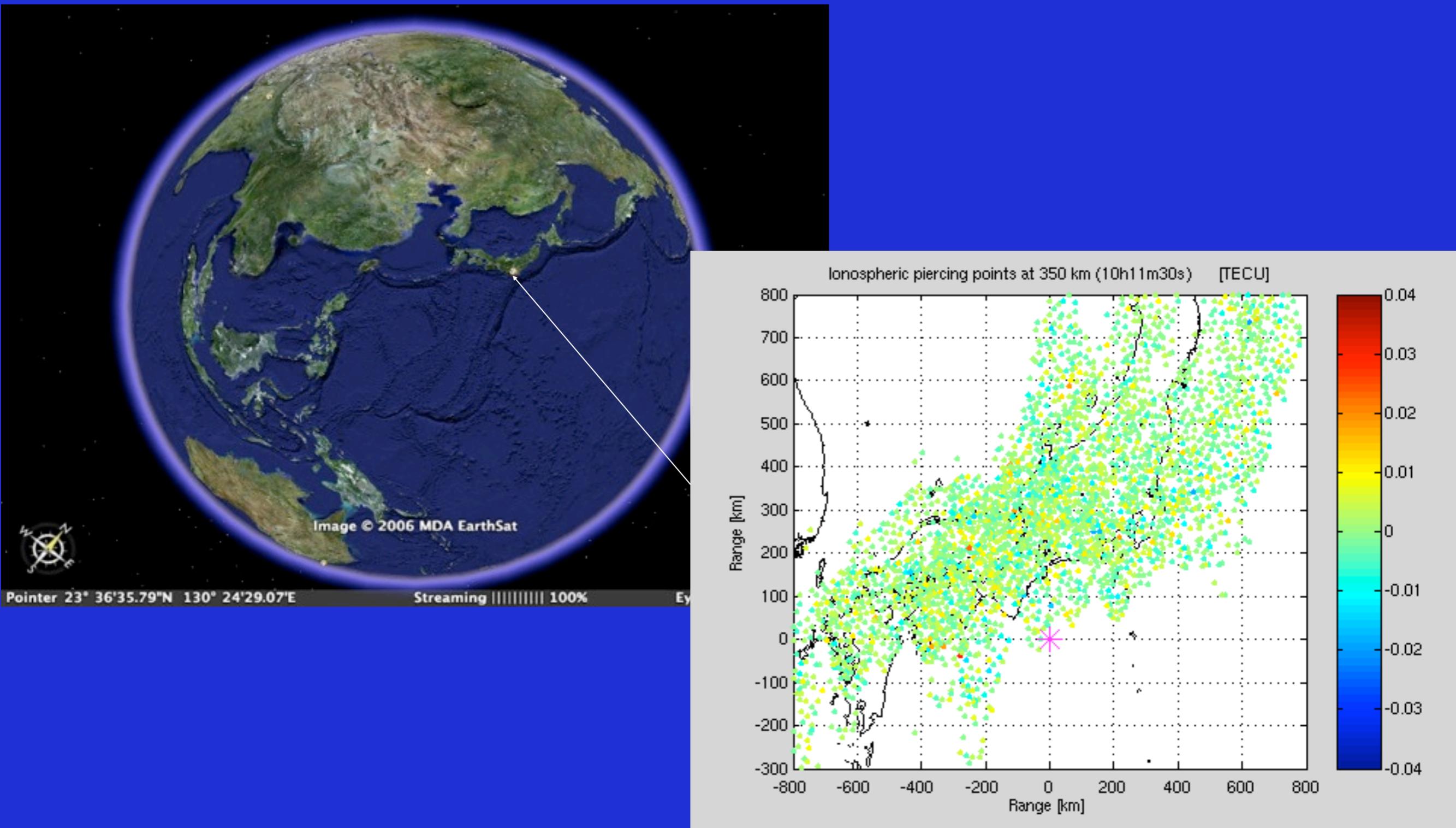


Example 3: remote sensing on Earth



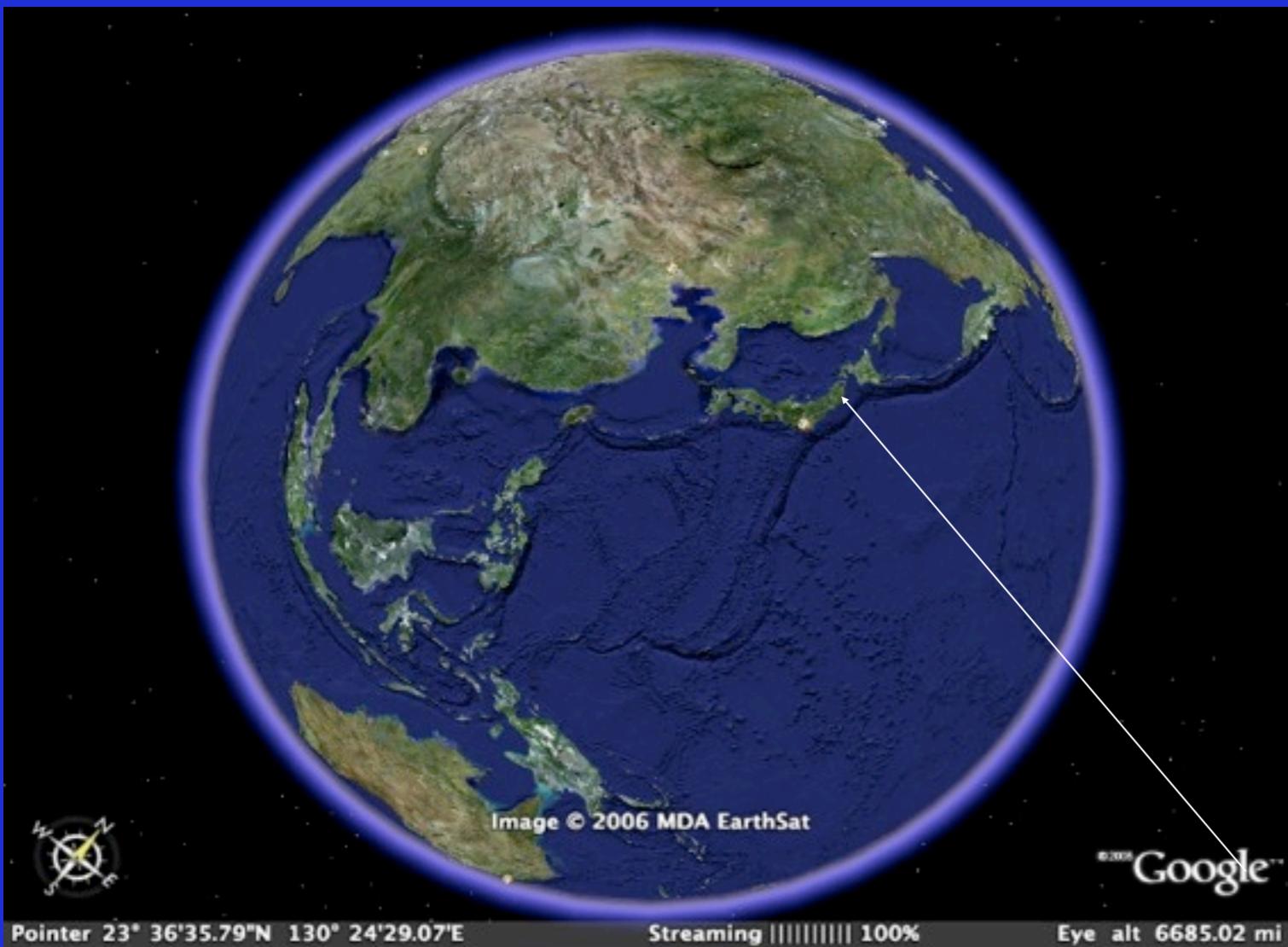
Tohoku 11/3/2011 M~9

Example 3: remote sensing on Earth



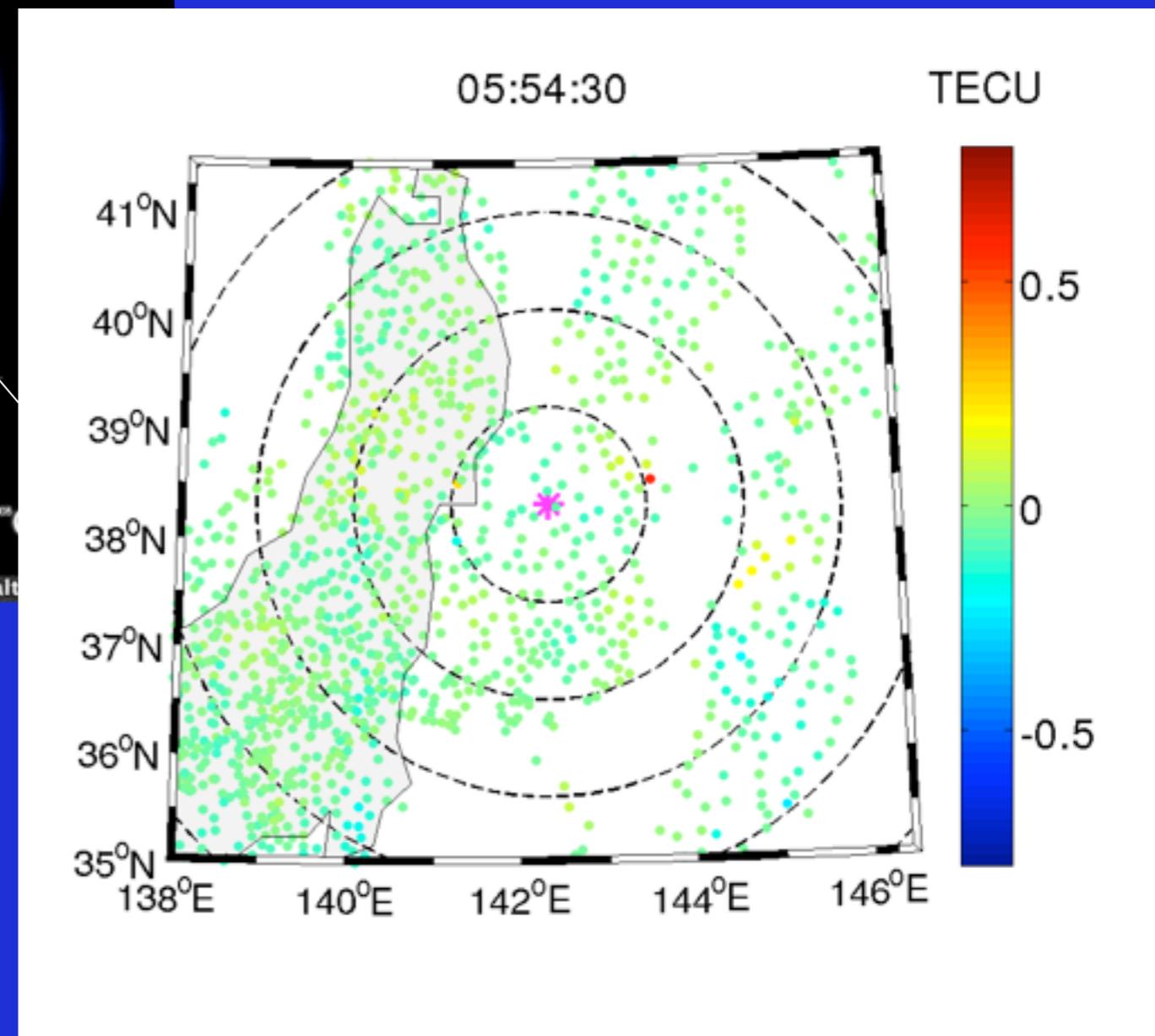
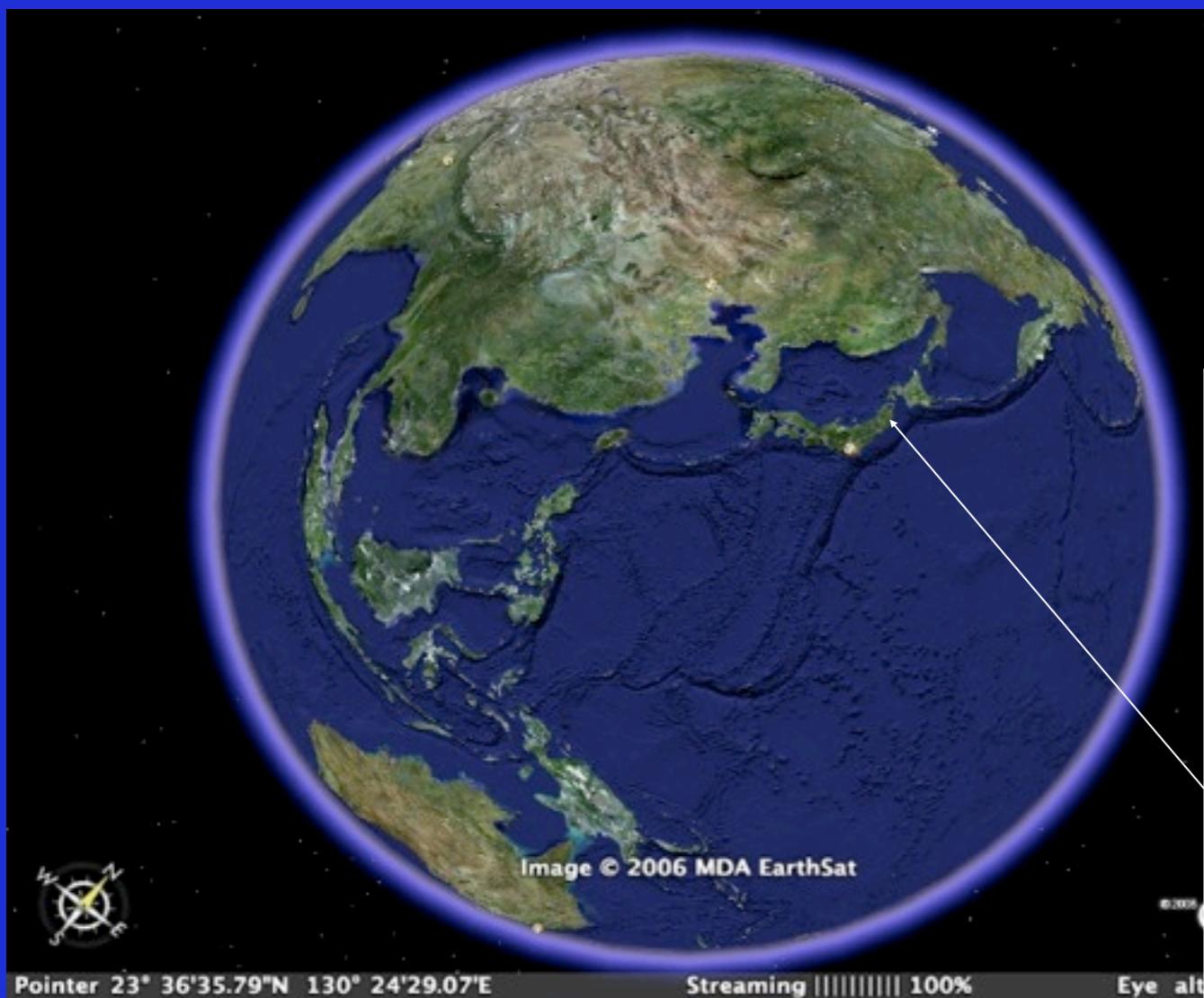
Tohoku 11/3/2011 M~9

Example 3: remote sensing on Earth



Tohoku 11/3/2011 M~9, Astafyeva et al, Rolland et al, 2011

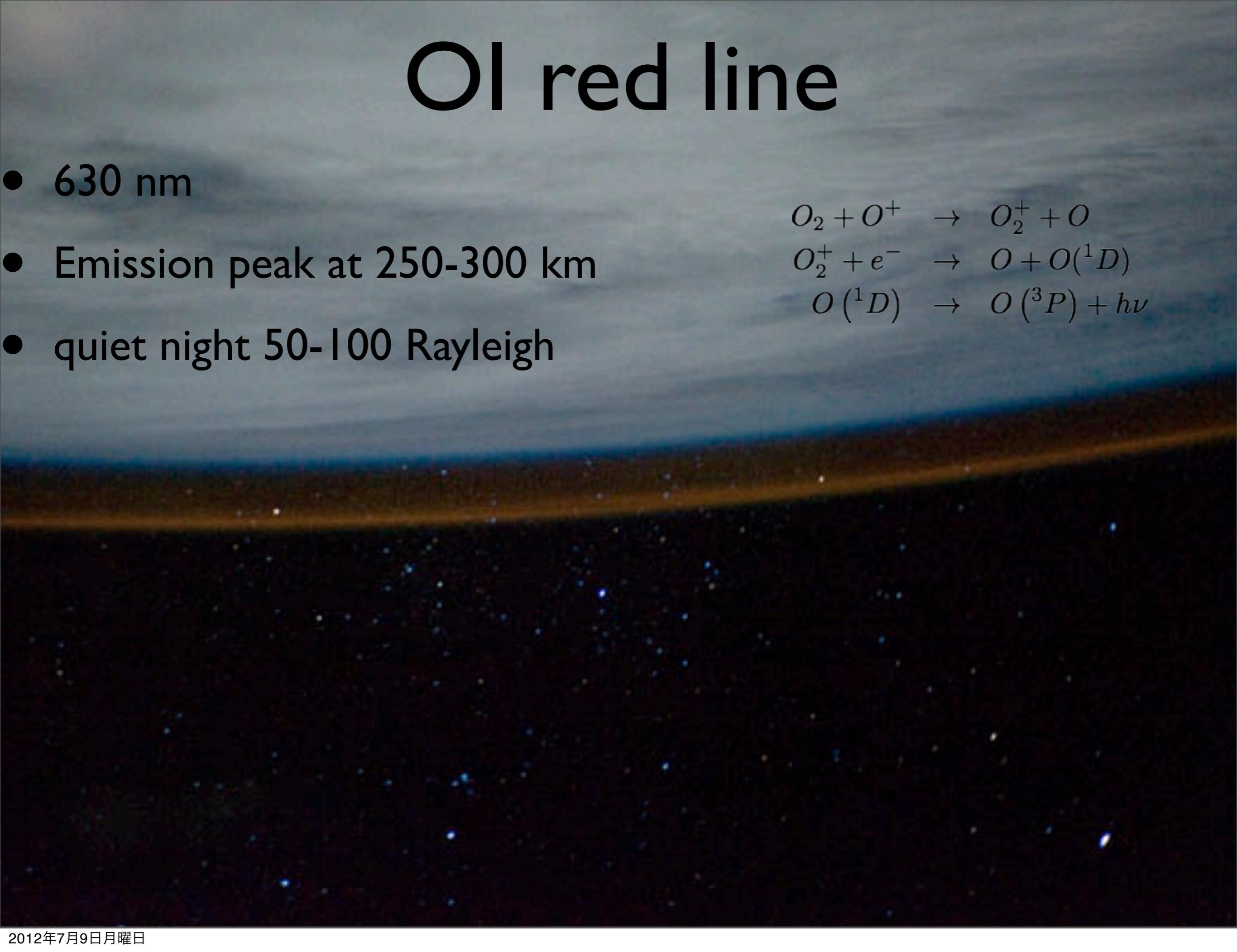
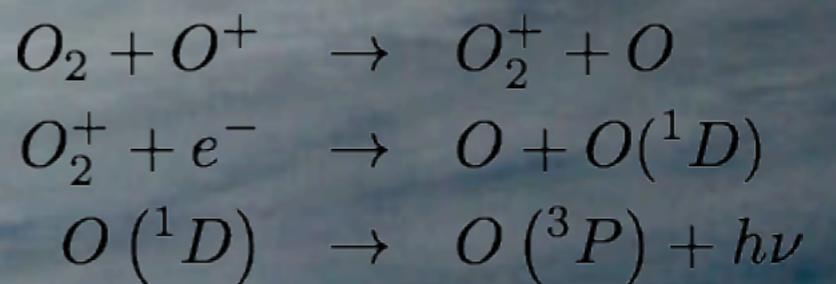
Example 3: remote sensing on Earth



Tohoku 11/3/2011 M~9, Astafyeva et al, Rolland et al, 2011

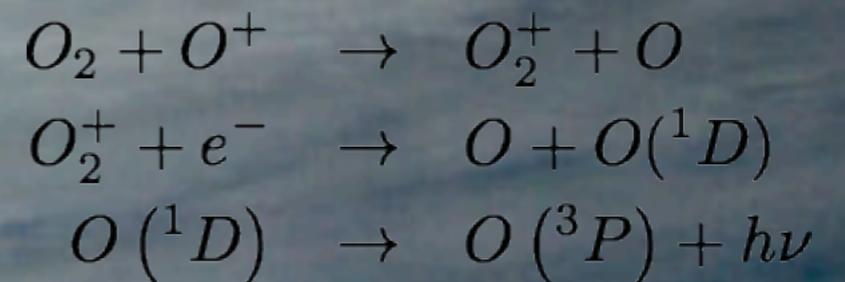
OI red line

- 630 nm
- Emission peak at 250-300 km
- quiet night 50-100 Rayleigh

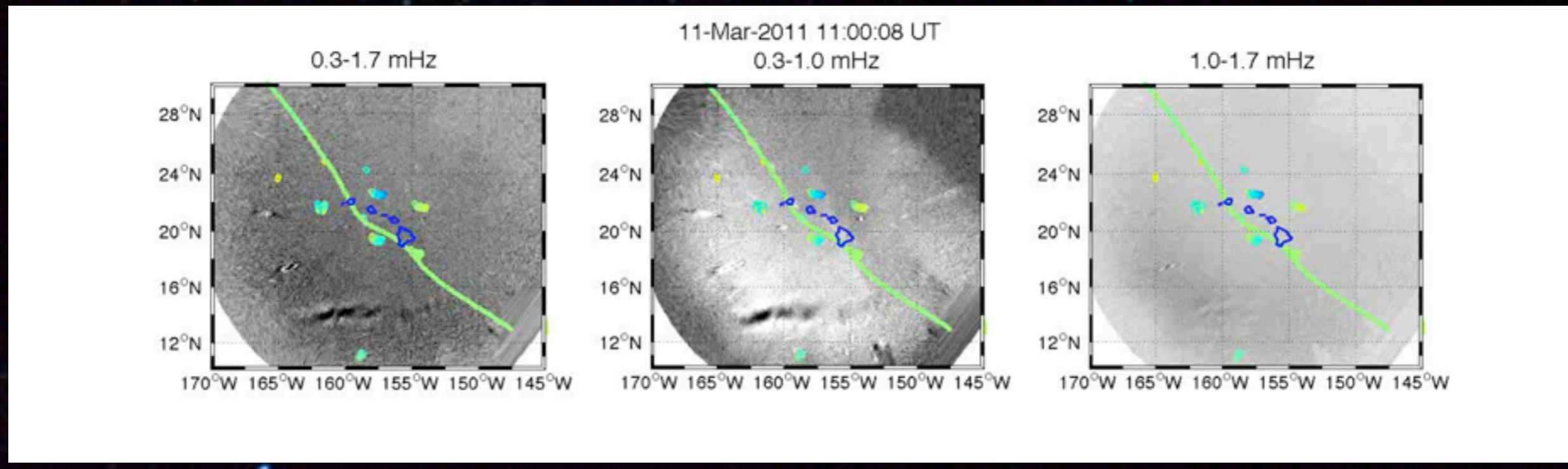


OI red line

- 630 nm
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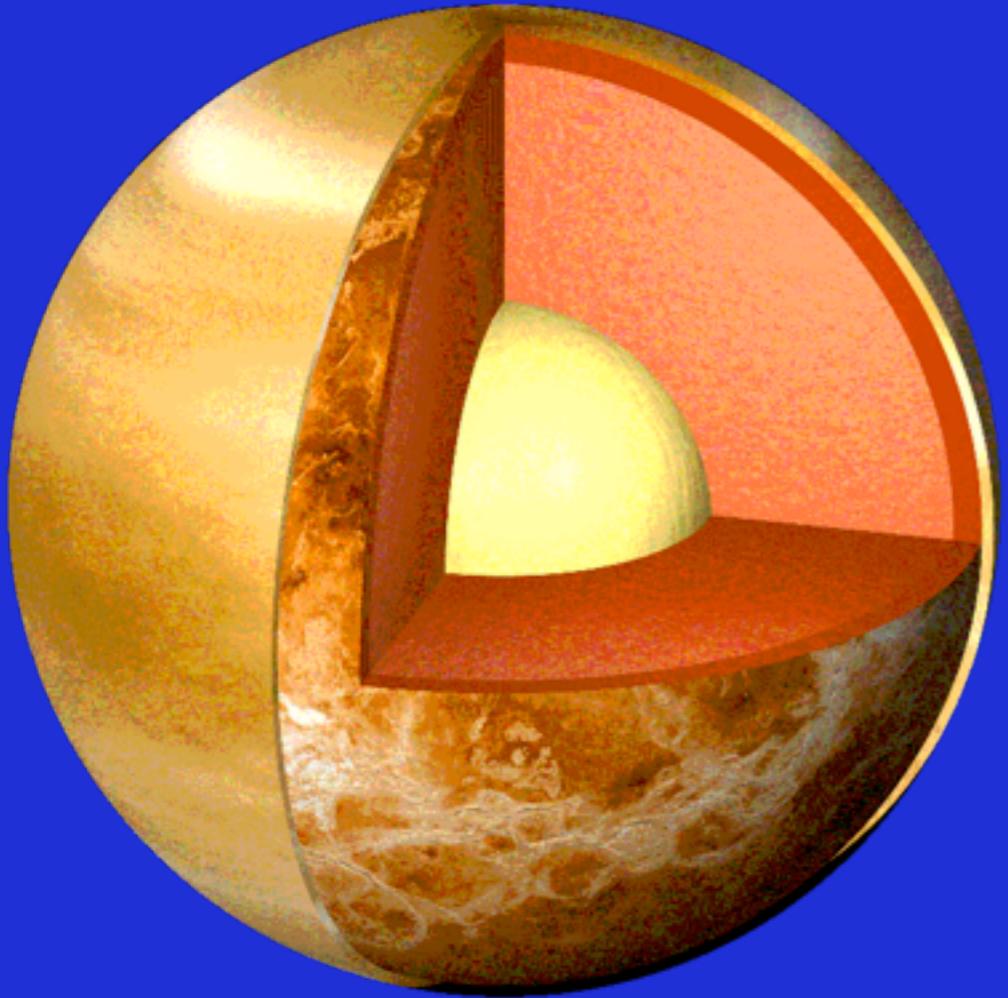
Makela et al., 2011



Example 4: Venus?



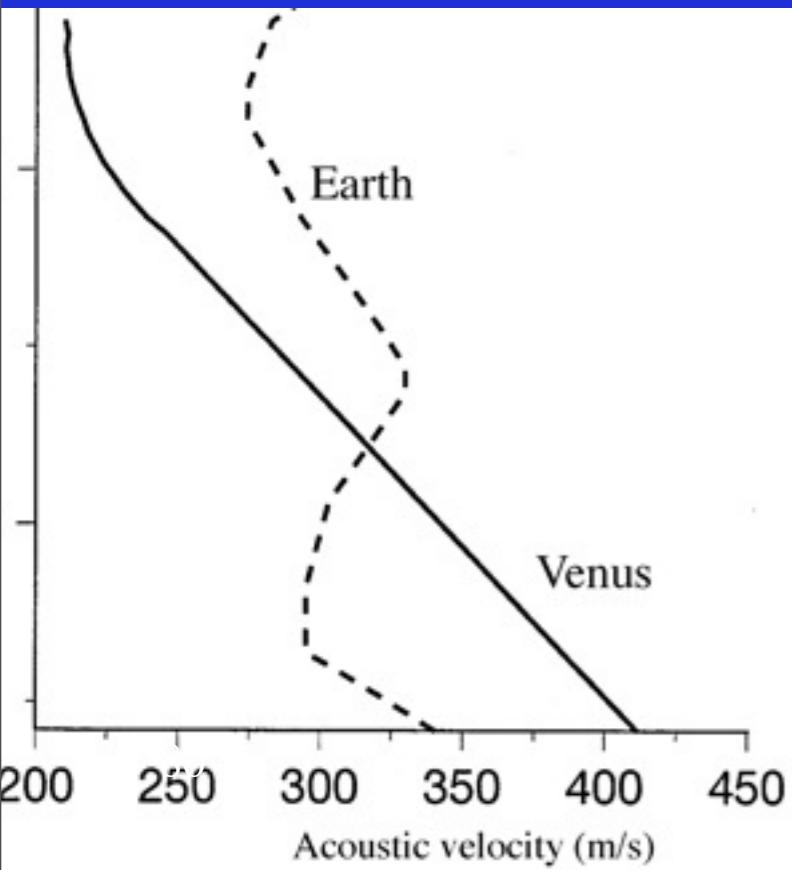
Example 4: Venus?



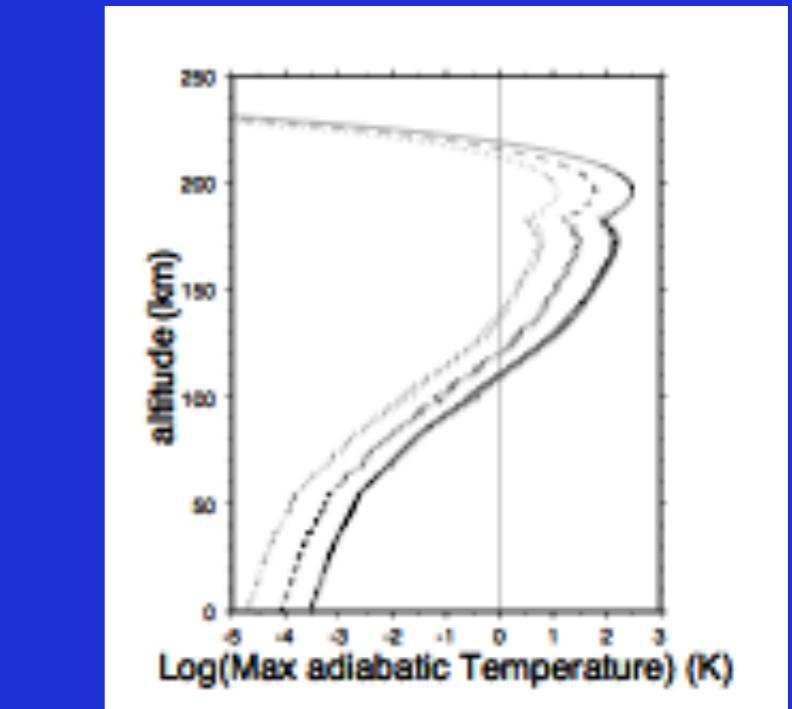
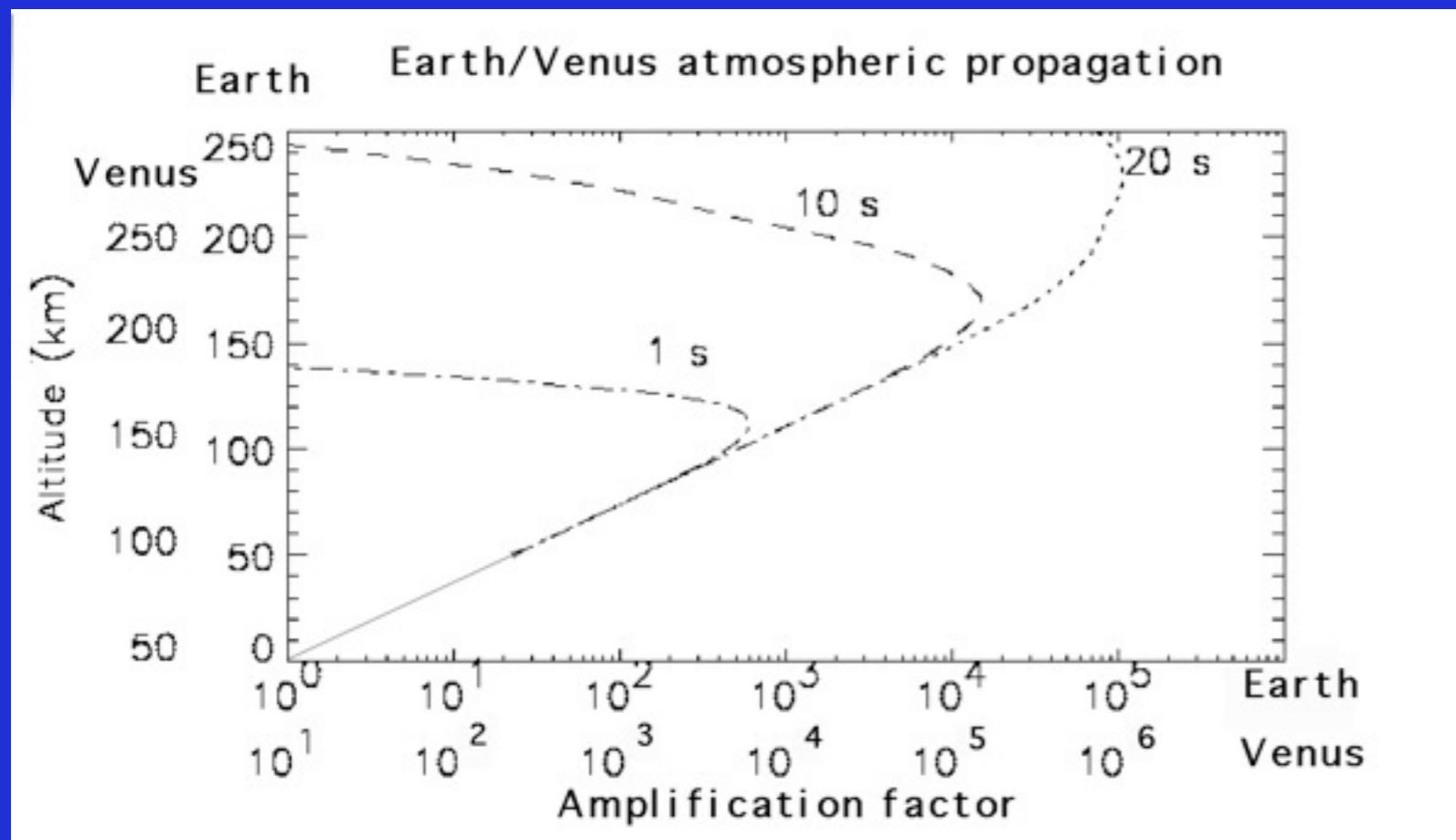
- The resurfacing history of Venus provide an average age of 300-500 Myears for most of the planetary surface
- Rate of volcanism comparable to Earth intraplate activity are found
- Seismic activity of Venus might generate a few Ms=6 per month
- And at the surface, pressure is about 90 bar, density of about 60 kg/m³, acoustic velocities slightly higher (410 m/s)... Ideal planet for atmospheric seismology

Venus Background for atmospheric seismology

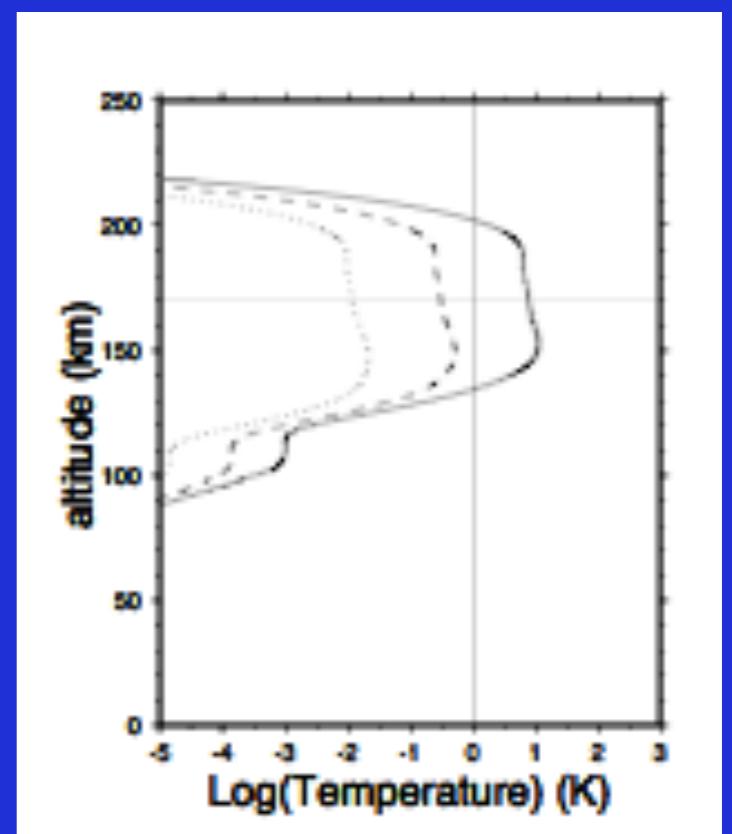
- Maximum ionisation in Venus ionosphere is reached at about 140 km, an altitude comparable to HF sounding altitude on Earth
 - Ground acoustic jump is much better
 - At the surface, pressure is about 90 bar, density of about 60 kg/m^3 , acoustic velocities slightly higher (410 m/s)
 - Ground coupling (ρc) is about 60 greater than on Earth
 - One bar level is reached at about 50 km of altitude, after an amplification by about 10 for acoustic waves
 - Acoustic signals from ground are expected to be about 600 times greater at the same altitude and for the same quake (almost 2 magnitudes)



Body waves.... And high altitude dissipation



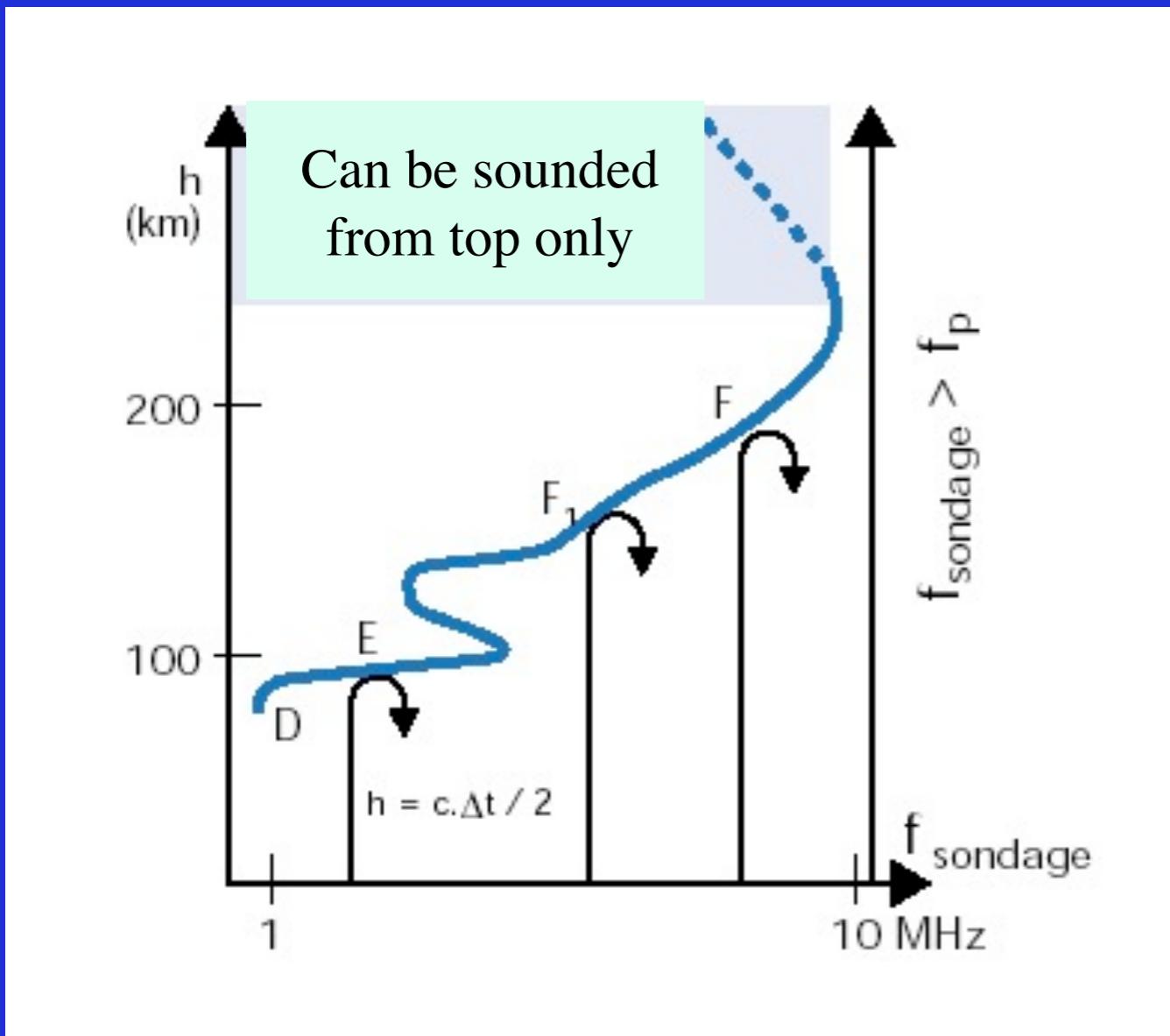
Adiabatic oscillations



Non-adiabatic heating

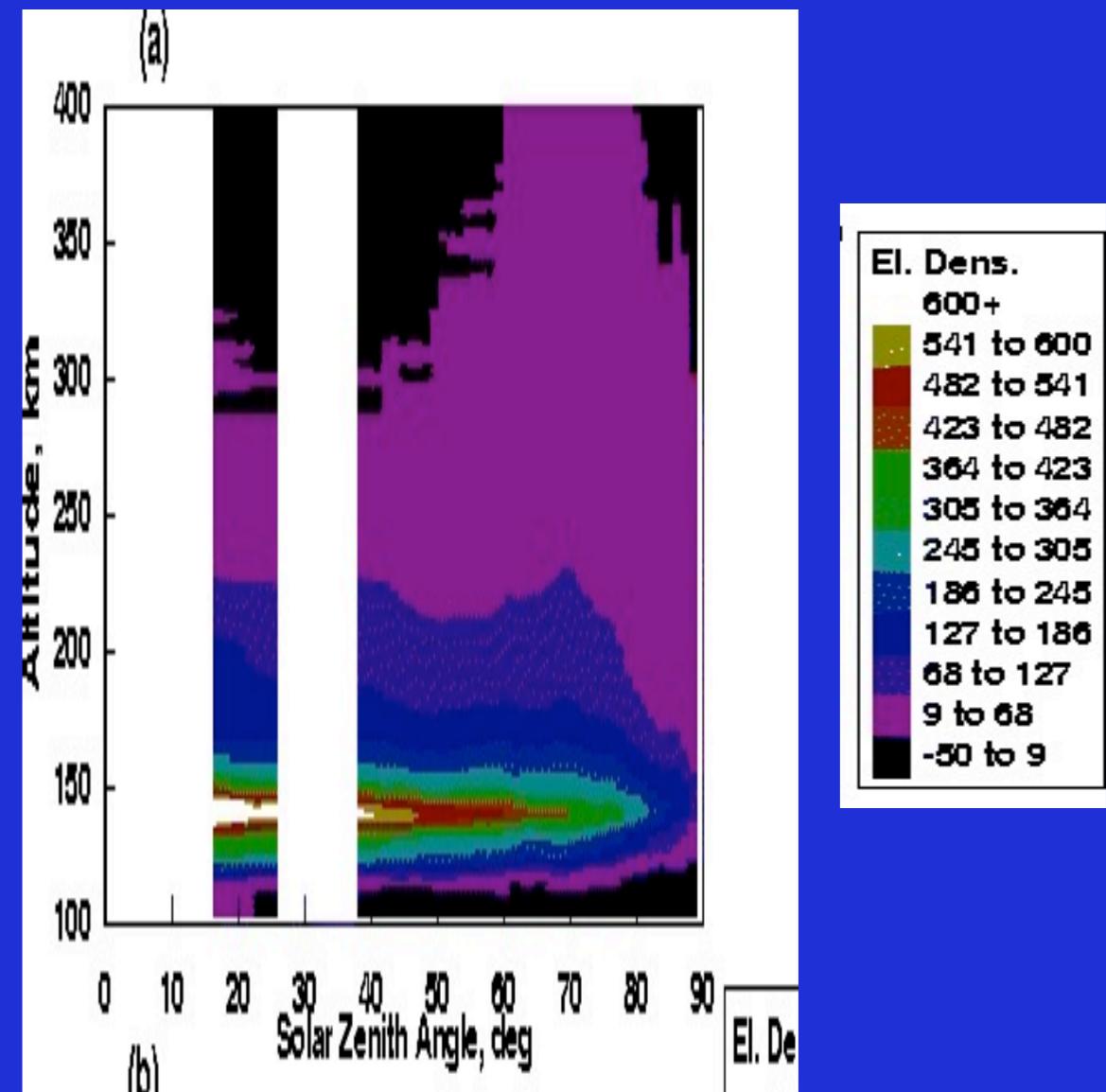
- Event will be associated to a thermal signal...
- Event characteristic (Garcia et al., 2005)
 - Magnitude : 5,5.5, 6
 - Haskell model for rupture and frequency generation
 - 30 km of focal depth

Ionosphere and remote sensing seismology



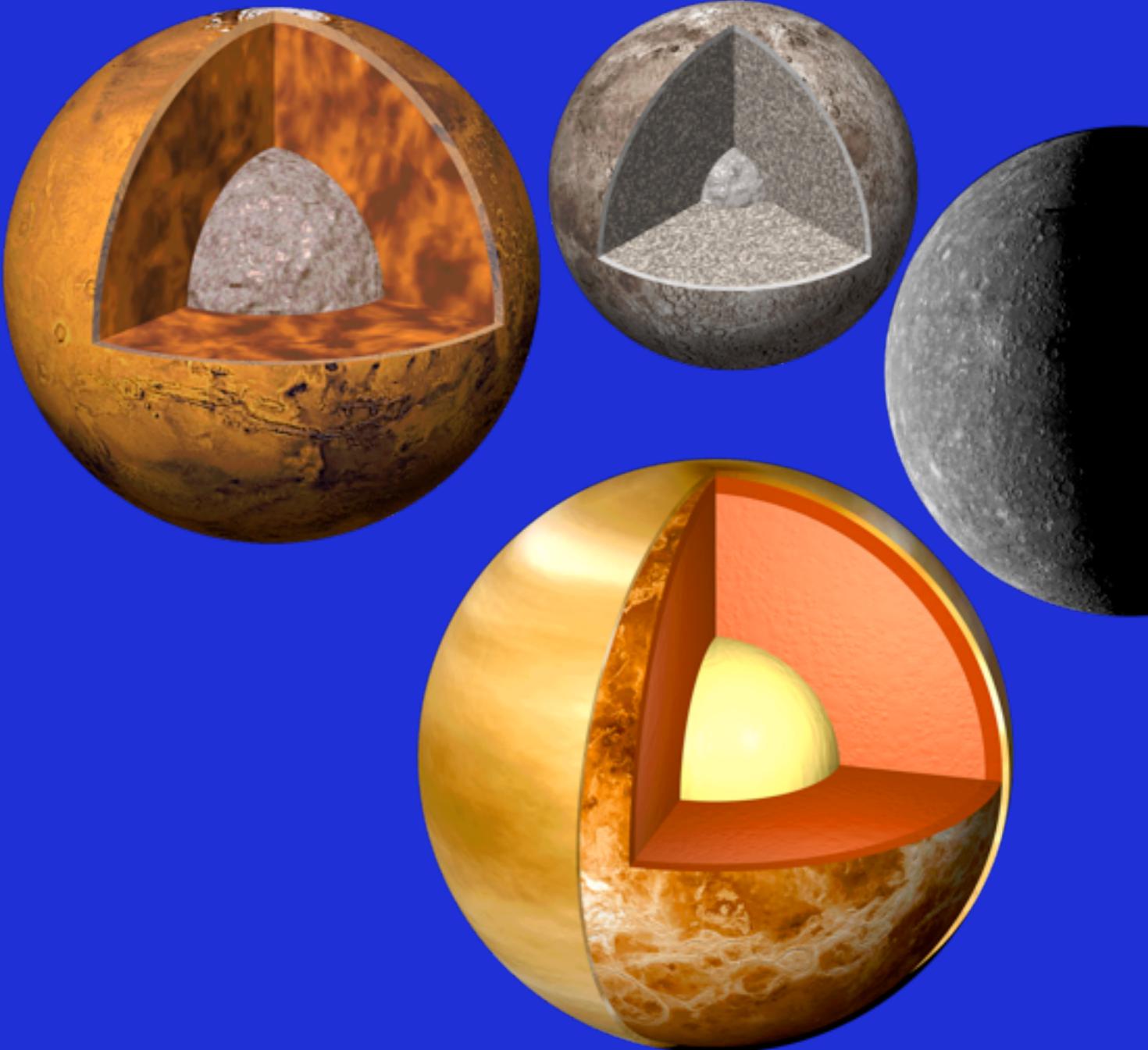
Earth

- Top side sounder might detect oscillations below 150 km



Venus

Thank you.



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