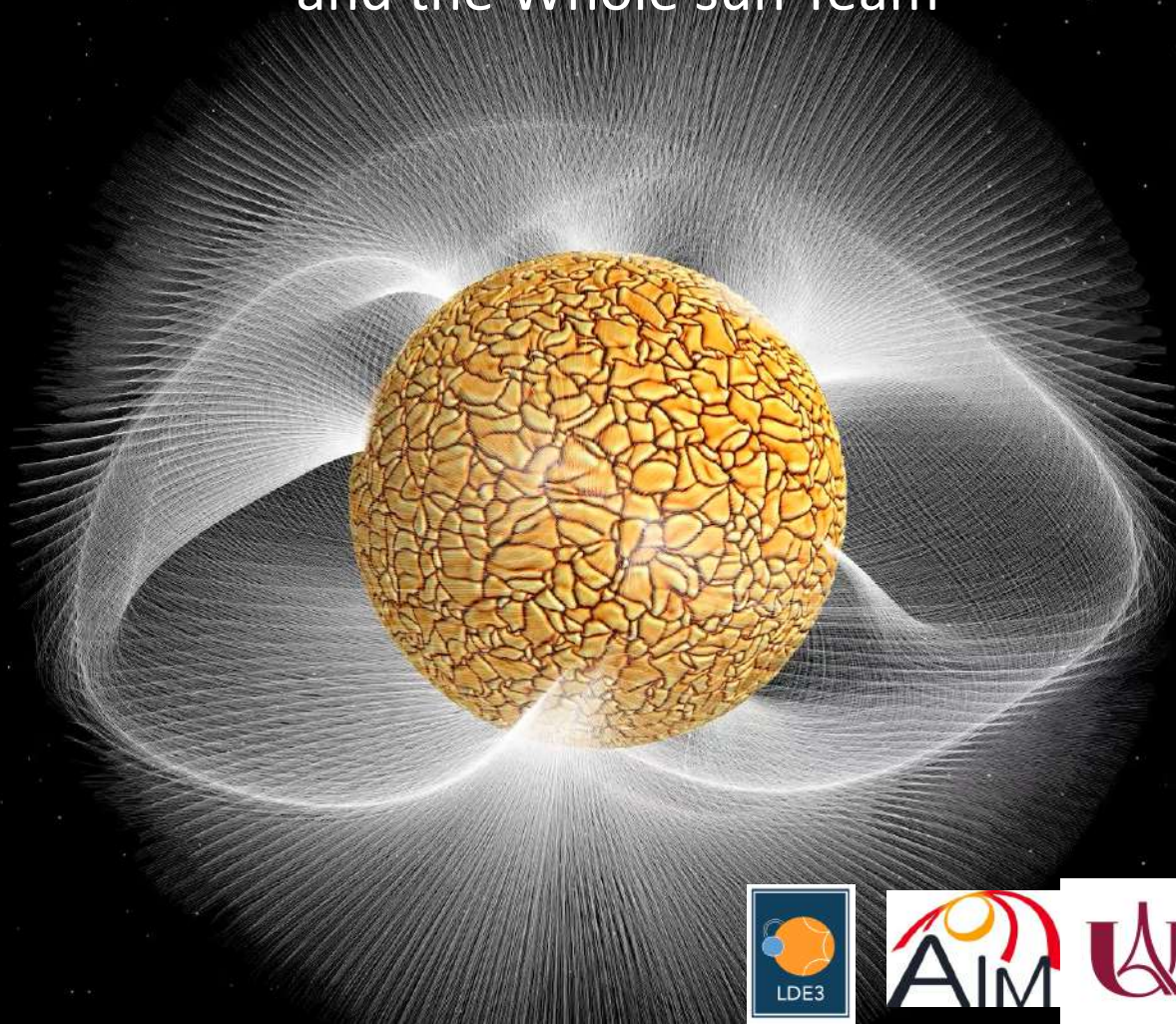


# Magnetochronology of solar-type stars and the Convective Conundrum:

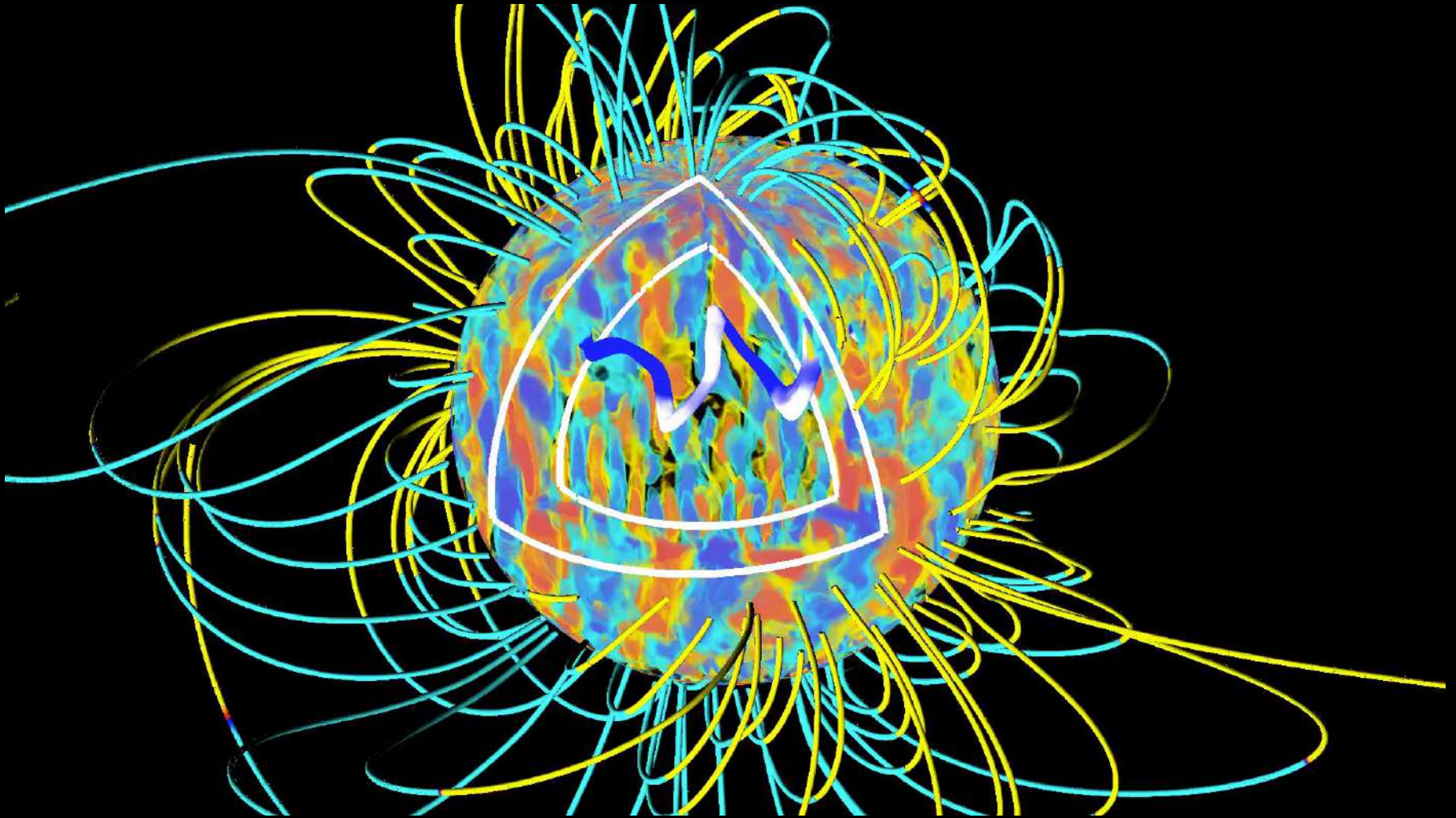
a path theory to study global solar magnetized convection

Allan Sacha Brun (CEA Paris-Saclay/ISEE Nagoya)

and the Whole sun Team

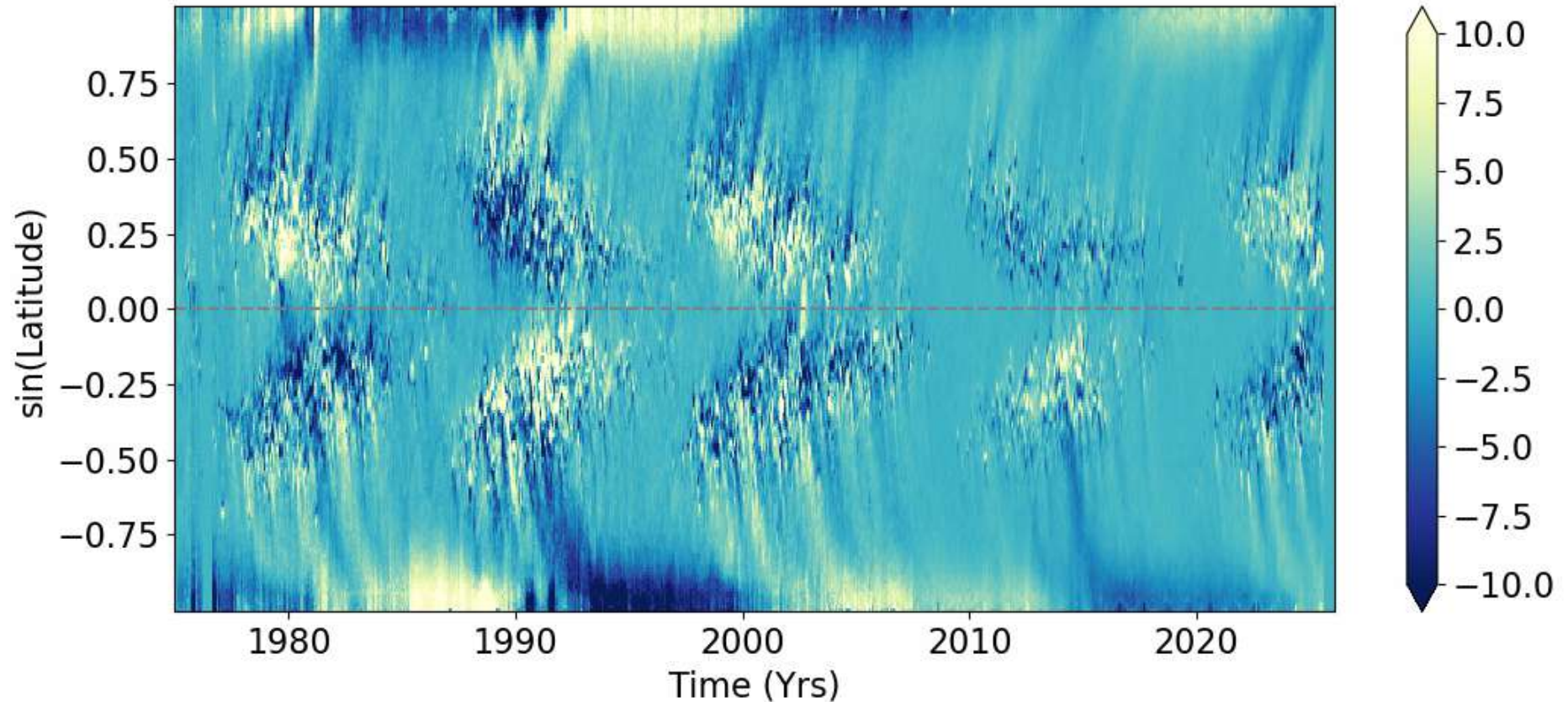


## An exemple of cyclic dynamo action



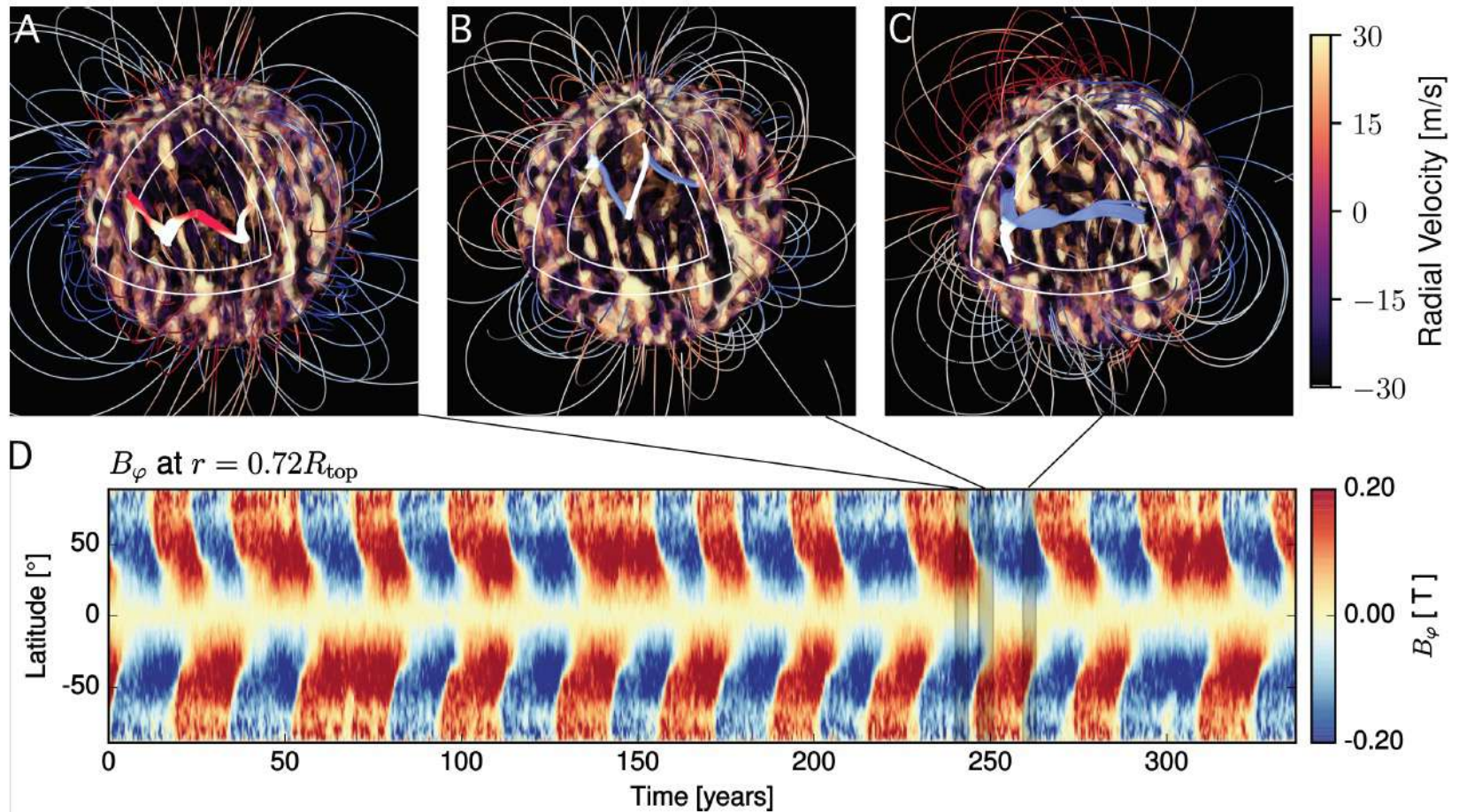


# Solar butterfly Diagram



Butterfly diagram: sunspot migration towards equator during 11 yr cycle

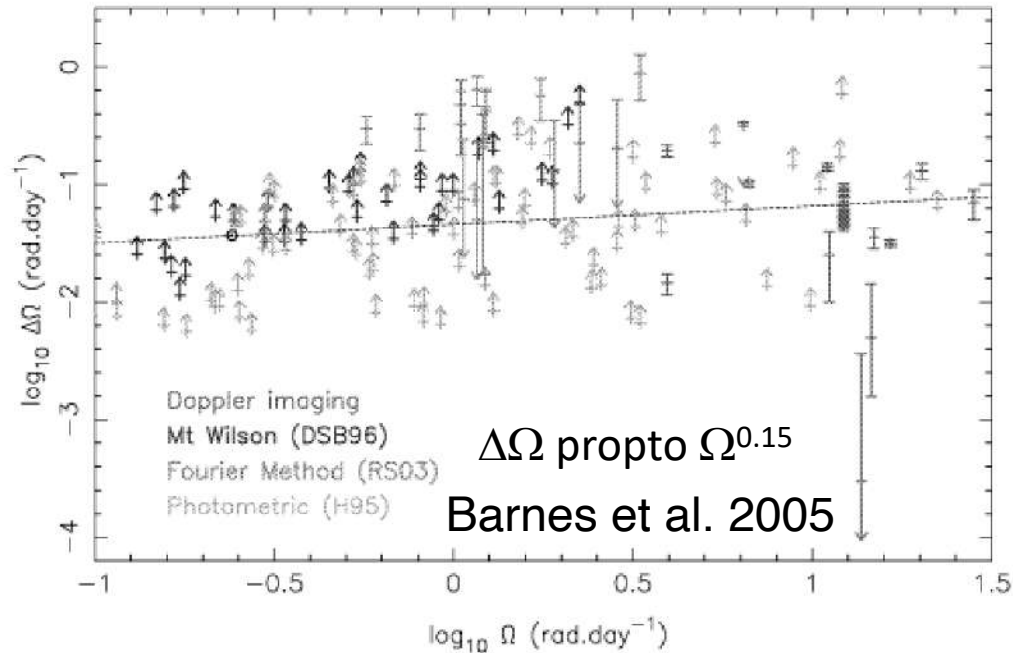
# Successful Cyclic Dynamo with long cycle period



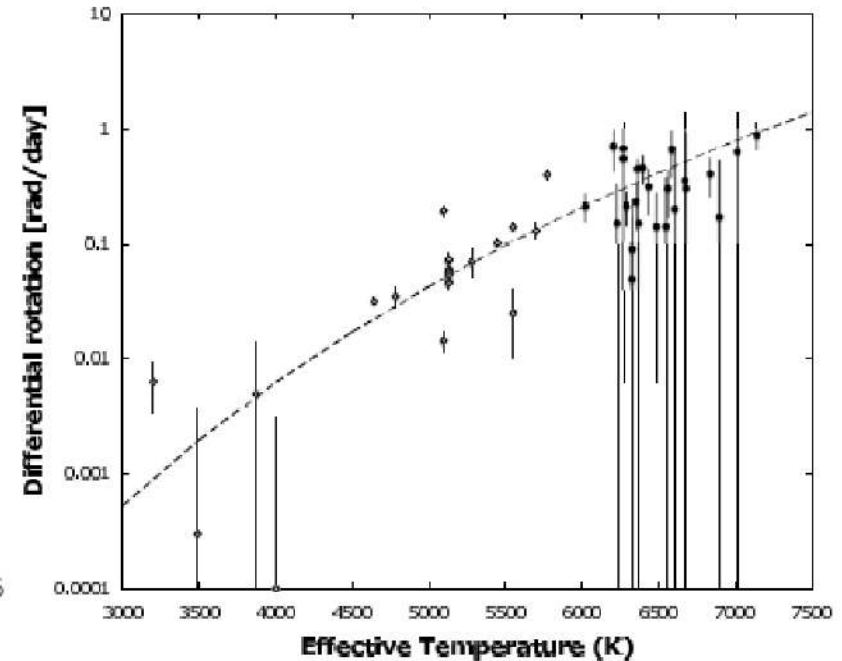
Strugarek et al. 2017, 2018

# Trends in Differential Rotation with $\Omega$ & Mass (Teff)

Weak trend with  $\Omega$



$\Delta\Omega$  increases with  $M_*$



Collier-Cameron 2007

In Donahue et al. 1996:  $\Delta\Omega \propto \Omega^{0.7}$

So currently exponent  $n$  in  $\Delta\Omega \propto \Omega^n$  ranges [0.15, 0.7]

Confirming these observational scaling is key



# Solar Type Stars (late F, G and early K-type)

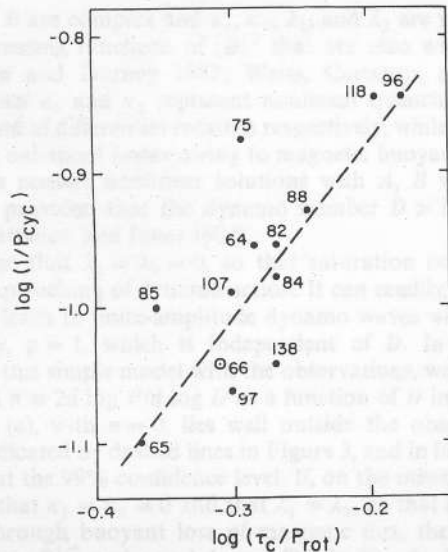


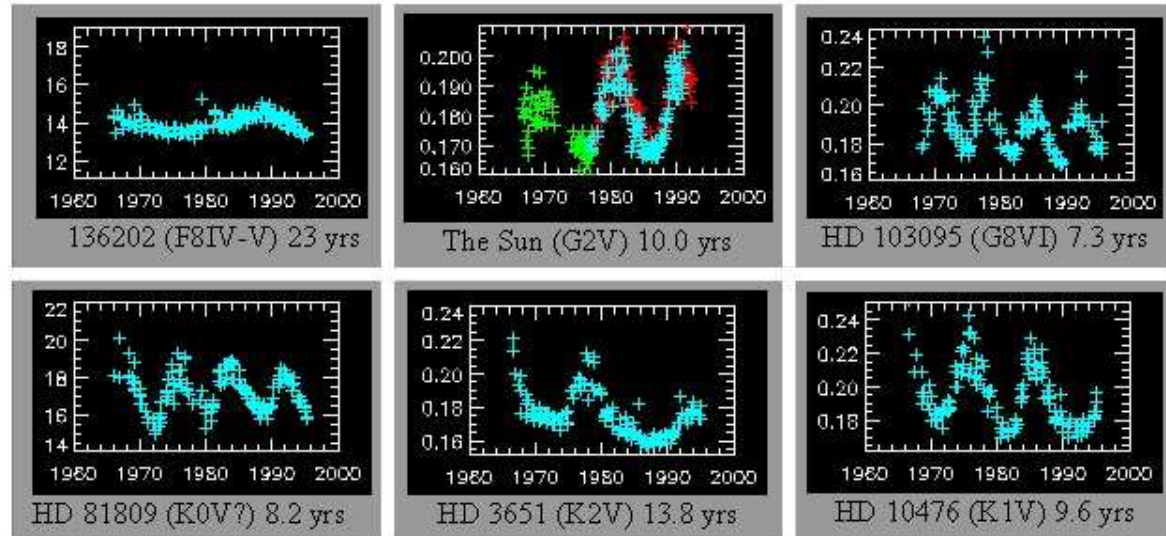
FIG. 2.—Log  $(1/P_{cyc})$  vs. log  $(\tau_c/P_{rot})$  for the stars of Table 1. The dashed line is a linear least squares fit to the data.

Noyes et al. 1984

In stars activity depends on rotation  
& convective overturning time  
via Rossby nb  $Ro = P_{rot}/\tau$   
 $\langle R'_{HK} \rangle = Ro^{-1}$ ,  $P_{cyc} = P_{rot}^{1.25 \pm 0.5}$

Wilson 1978

Baliunas et al. 1995



Call H & K lines,  $\langle R'_{HK} \rangle$

Over 111 stars in HK project (F2-M2):

31 flat or linear signal

29 irregular variables

51 + Sun possess magnetic cycle

=>

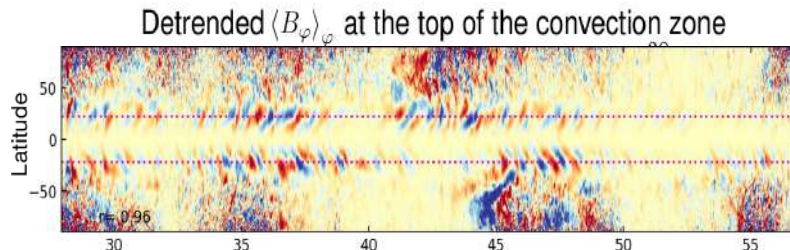
Much more  
coming in  
Asteroseismology  
Era (Mike's talk)

Quid of Star-Planet Interaction and cyclic activity?

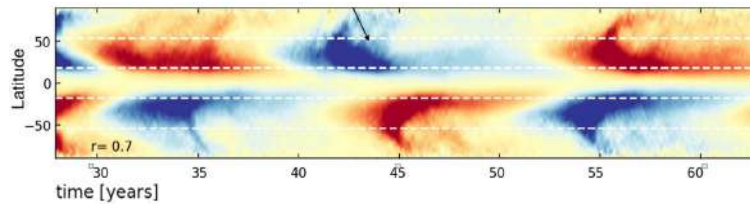
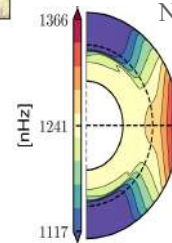
**Magnetic cycles of the planet-hosting star  $\tau$  Bootis**

J.-F. Donati,<sup>1★</sup> C. Moutou,<sup>2★</sup> R. Farès,<sup>1★</sup> D. Bohlender,<sup>3★</sup> C. Catala,<sup>4★</sup> M. Deleuil,<sup>2★</sup>  
E. Shkolnik,<sup>5★</sup> A. C. Cameron,<sup>6★</sup> M. M. Jardine<sup>6★</sup> and G. A. H. Walker<sup>7★</sup>

# Rotational and magnetic transitions

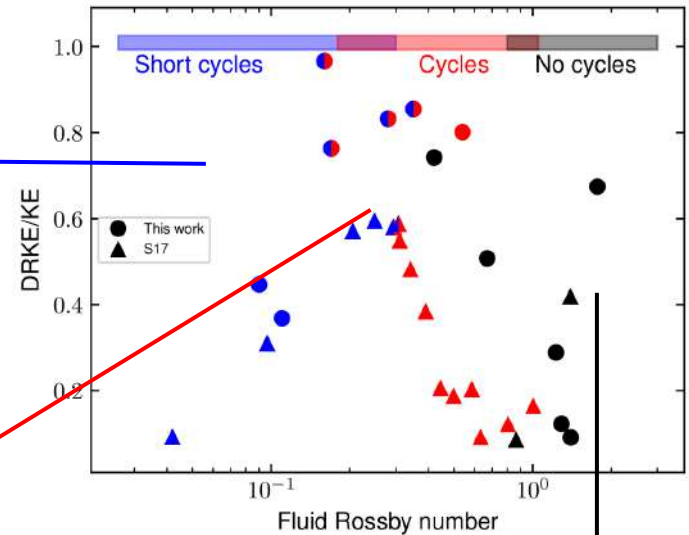


- short cycles ( $\sim$ year) ; **quasi-biennial oscillations ?**
- surface dynamo
- Parker-Yoshimura type ( $\alpha\Omega$ )

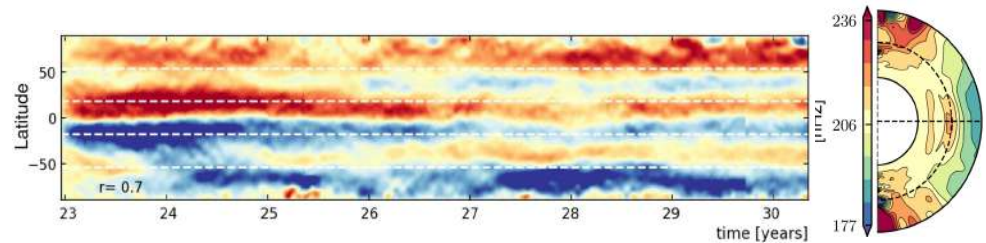


$\langle B_\varphi \rangle_\varphi$  at the base of the convection zone

- long cycles (**decadal solar-like**)
- deeper dynamo
- non-linear retroaction

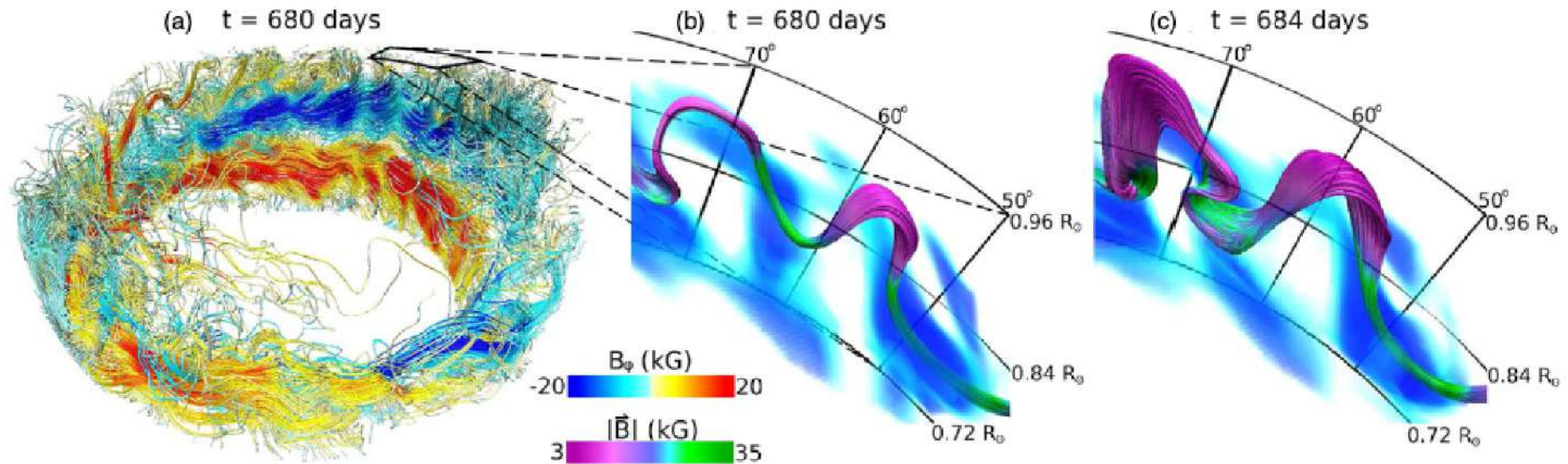


- **Stationnary dynamo**
- hemispherical toroidal field



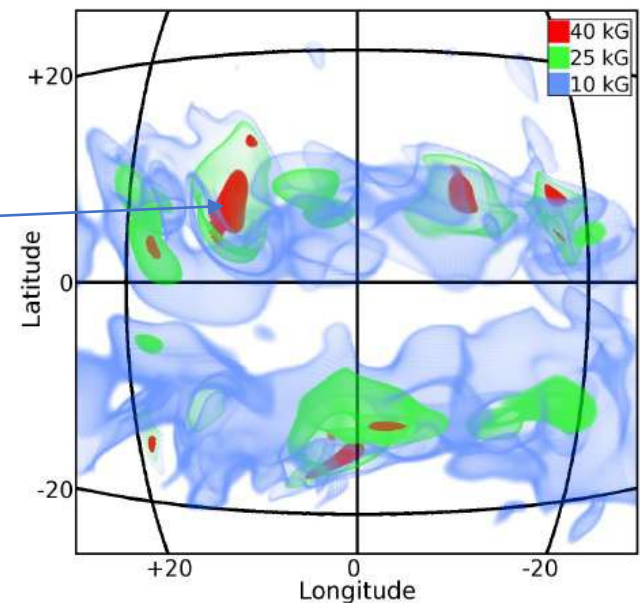
Brun et al. 2017, 2022

# Going Beyond the introduction of flux tube: *Self-consistent buoyant Loops generations*



We have Omega-loops  
but no atmosphere to  
See sunspot formation.  
What are their role?

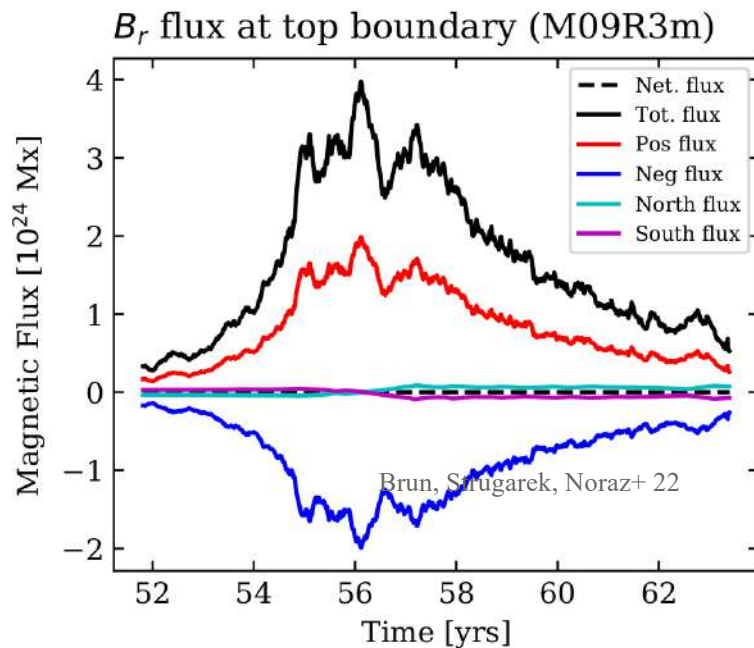
Magnetic seeds



Nelson et al. 2011, 2013a, 2013b,  
Strugarek et al. 2017, 2018  
Brun et al. 2015, 2022, Brun & Browning 2017  
See also Fan & Fang 2014



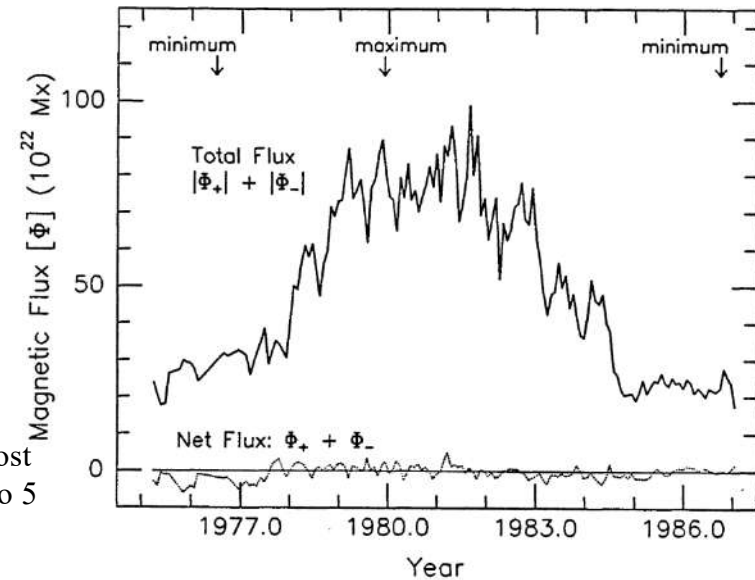
# Magnetic Flux in long cyclic case: comparison with observations



Magnetic fluxes **from 10<sup>24</sup> to 10<sup>25</sup> Mx**, in good agreement with values observed on the Sun.

$$\Phi = \int_S \mathbf{B} d\mathbf{S}$$

Modulation reaches almost a factor of 8 (compared to 5 for the Sun).

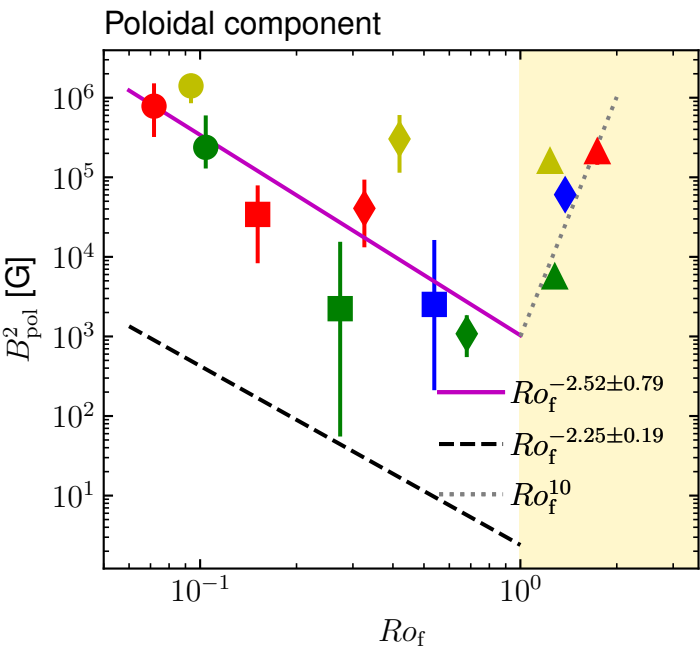


# Magnetochronology of Solar-type Stars

=> good qualitative agreement with observations

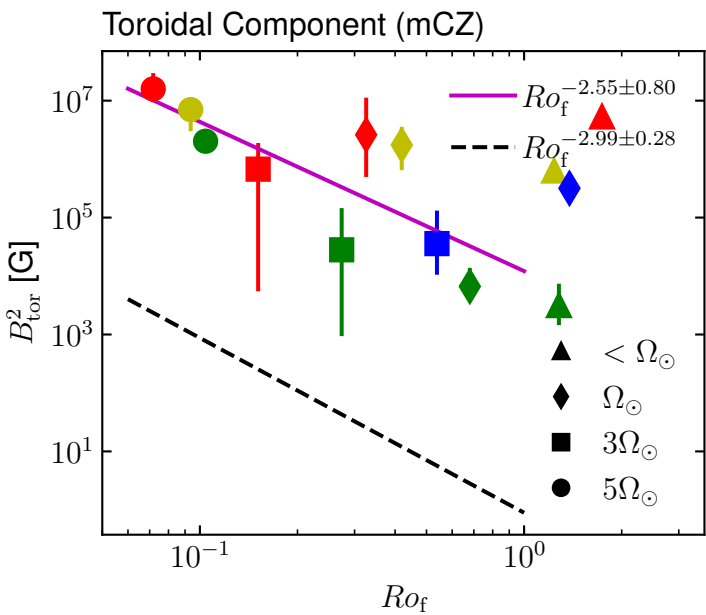
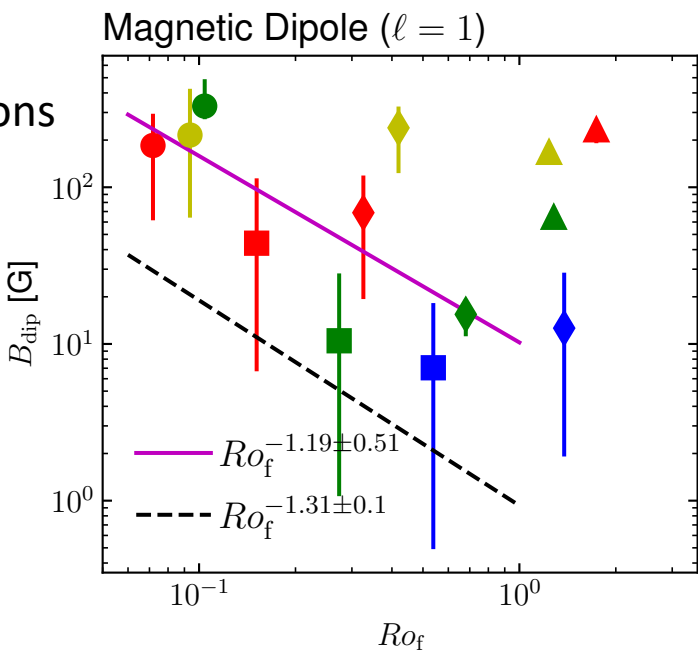
See et al. 2015, 2019  
Vidotto et al. 2014

Noraz, Brun et al. 2024, A&A



Augustson et al. 2019:  $B_{\text{bulk}} \sim Ro^{-0.5}$

Large scale field does not follow same trends

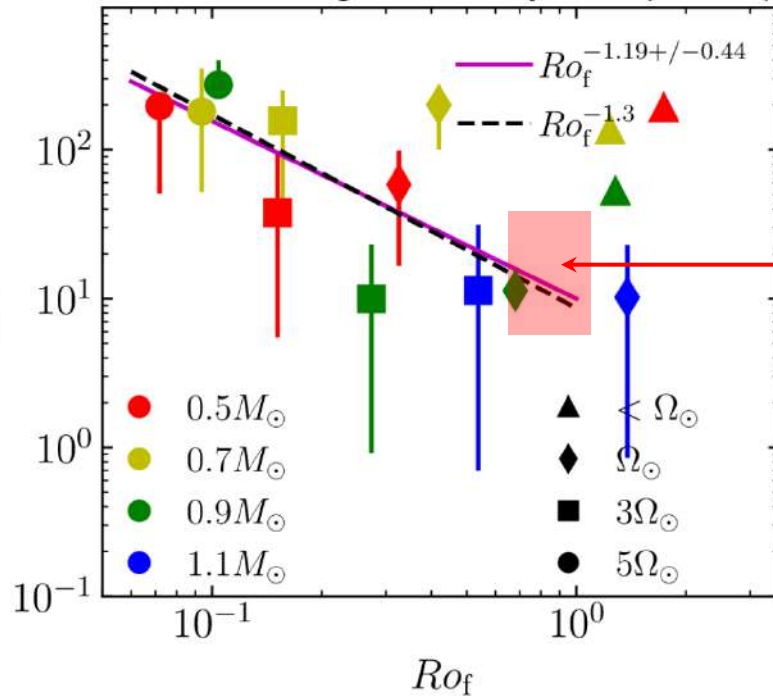




# Recovering Observational Trends

Brun, Strugarek, Noraz+ 22

## Radial Magnetic Dipole ( $l = 1$ )



- The dipole decreases but does not disappear

However, there may be a minimum around the solar Rossby value

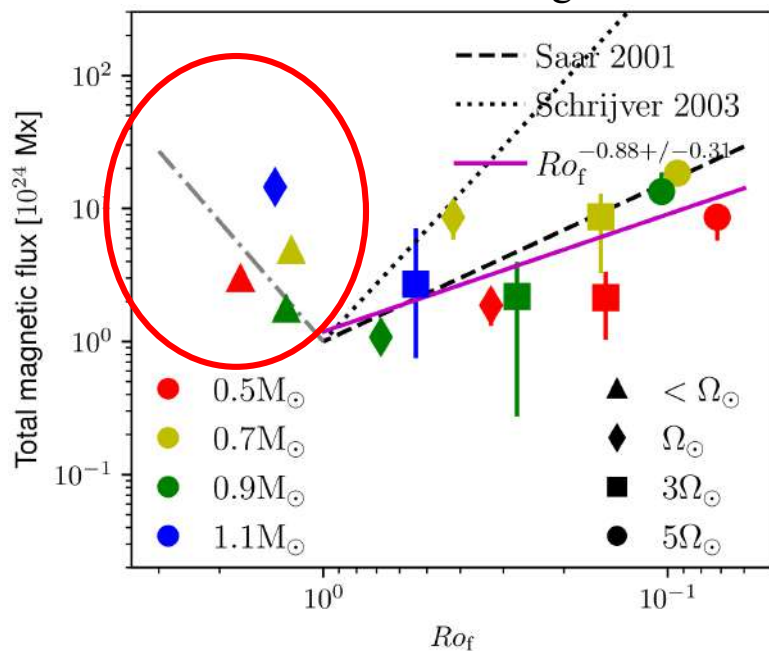
- Can a star be trapped in this regime by a combination of magnetism and mass loss rate?

$$\dot{J} \propto \dot{M} \Omega_* \langle r_A \rangle^2$$

# Larger global field in slowly rotating stars?

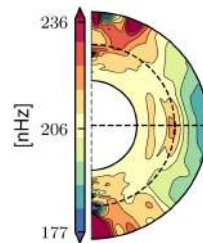
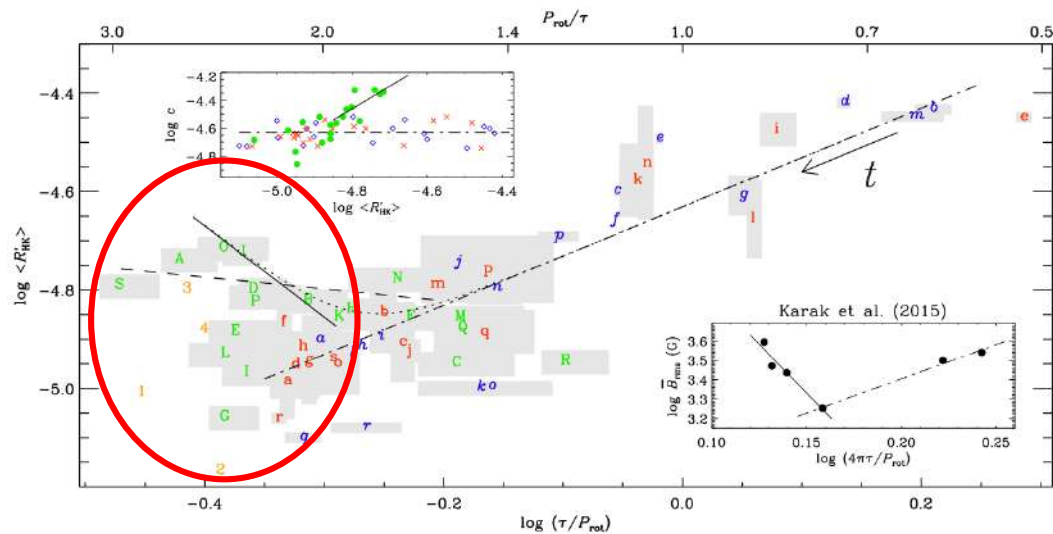
Brun, Strugarek, Noraz+ 22

Possible increase of the magnetic flux



Brandenburg & Giampapa 18

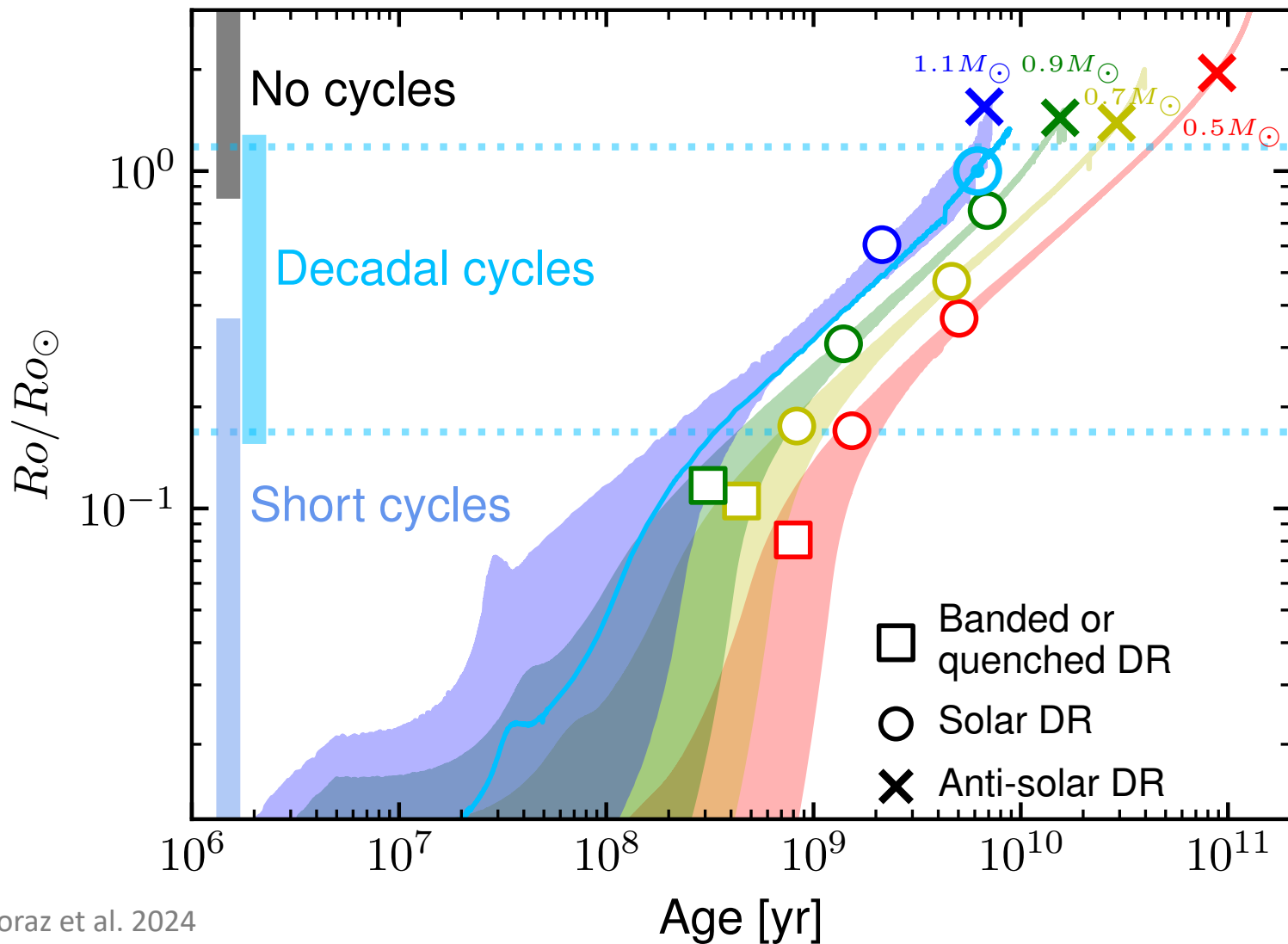
Possible enhancement of the activity



- Need **theoretical** and **observational constraints** to enlighten what occurs in the anti-solar regime



## A plausible « Sun in time » story



Trends of the stellar dynamo simulation

are qualitatively correct,

But the solar case is shifted in parameter space

⇒ Convective conundrum

+ The stellar convective dynamo solutions do not exhibit sunspot/starspots.... Where are they, are they needed?

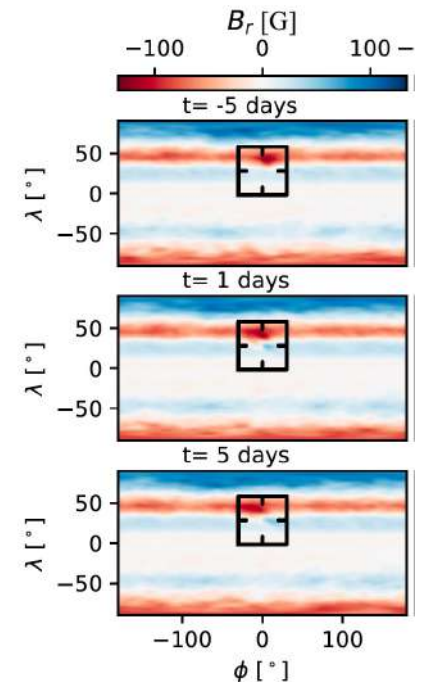
Note: In Cameron, Schunker, Brun et al. 2025, we have made a first analysis of flux emergence events in such convective dynamo and have found interesting bipolar events but not strong enough to perturb convection and lead to progenitor sunspot/starspot.

A&A, 701, A277 (2025)  
<https://doi.org/10.1051/0004-6361/202553844>  
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**Astronomy  
&  
Astrophysics**

### Closing the solar dynamo loop: Poloidal field generated at the surface by plasma flows

R. H. Cameron<sup>1,4,\*</sup>, H. Schunker<sup>2</sup>, A. S. Brun<sup>3</sup>, A. Strugarek<sup>3</sup>, A. J. Finley<sup>3</sup>, W. Roland-Batty<sup>2</sup>,  
A. C. Birch<sup>1</sup>, and L. Gizon<sup>1,4</sup>

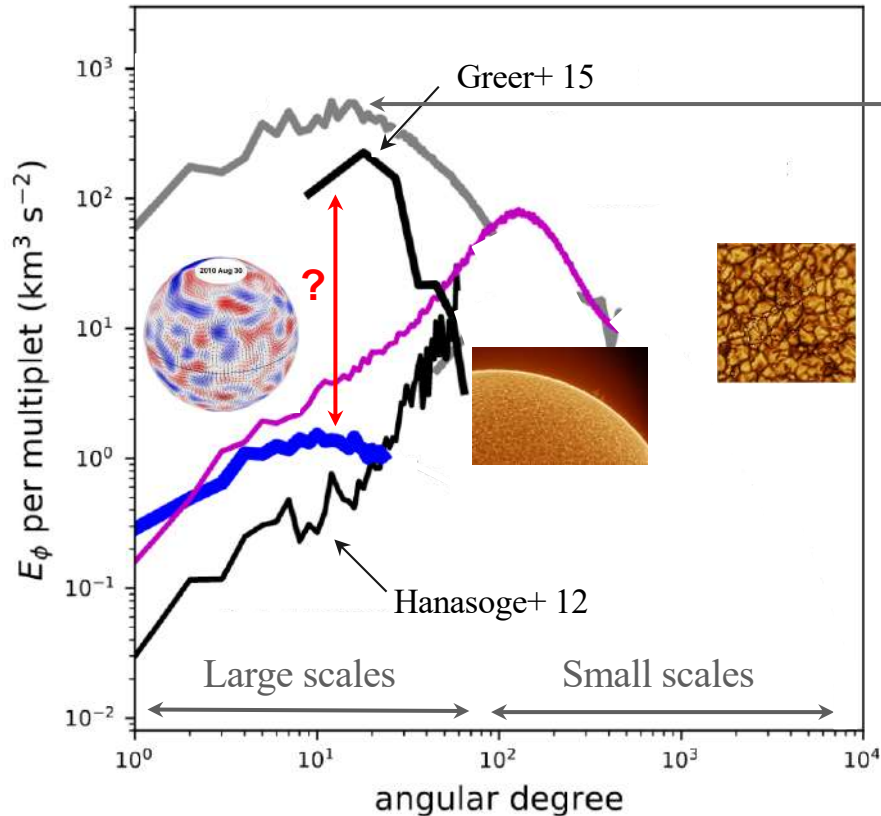




# Convective Conundrum

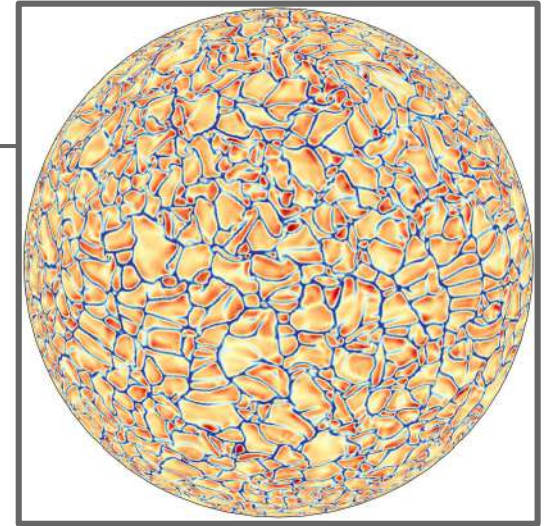
Solar case is qualitatively correct, but slightly misplaced in parameter space. Effective Rossby too high.

© Proxauf PhD thesis



- Numerical simulations as a tool to modelize the process  
→ challenge to reach realistic solar parameter regimes

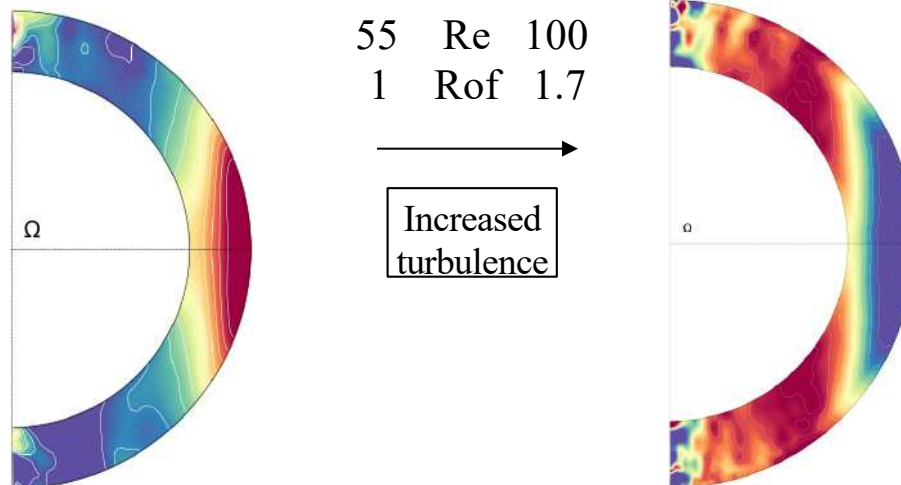
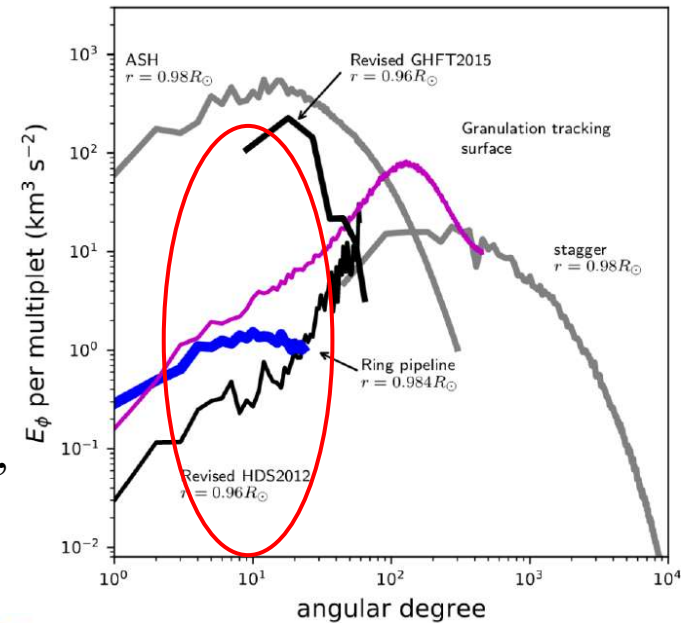
- Actual mismatch between observational results concerning the large scales contribution



How can solar convection models be calibrated to study stellar convection?

# Convective Conundrum

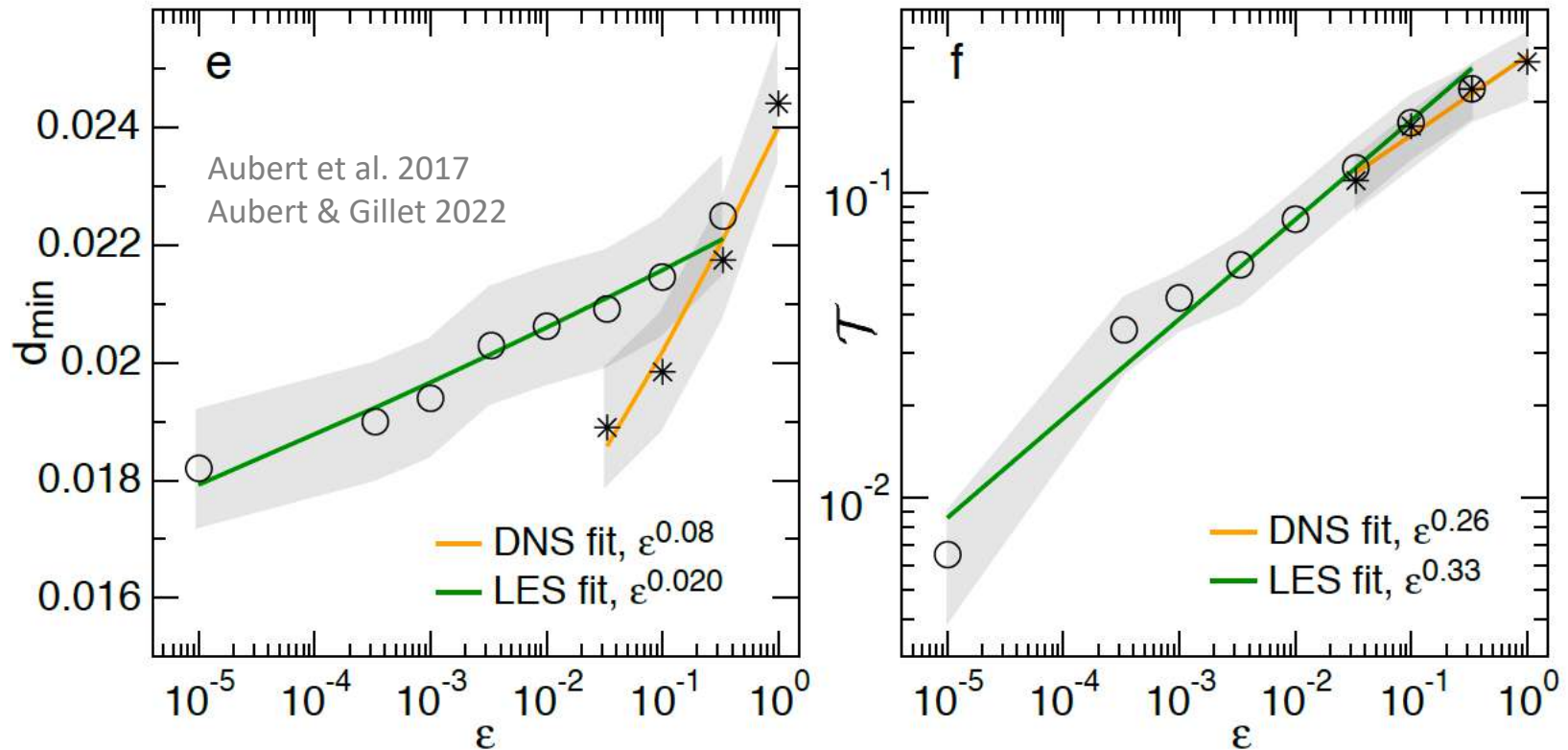
- Current mismatch between **global models** and **helioseismic inversion** regarding giant convective cells
- **Overestimation of the Rossby number** in global models,
  - establishing **anti-solar** DR in turbulent solar models



# Path parameter approach: The geodynamo case

## Path theory in the Earth convection setup:

The calculations do not represent a systematic sampling of the parameter space, but are rather chosen to follow a path connecting the classical numerical models such as the original CE dynamo (Aubert et al. 2013) to Earth's core conditions ( $\varepsilon = 10^{-7}$ )



Shown are results from hyperdiffusive solutions along the path (LES or large-eddy-simulations) up to 71 percent of the path ( $\varepsilon = 10^{-5}$ ), and the direct numerical simulations (DNS) up to 21 percent of the path ( $\varepsilon = 3.3 \cdot 10^{-2}$ ). (fixed  $Rm$  and  $Re$ , decreasing Ekman number).



# On Rossby and Nusselt numbers

- Two solutions are commonly used by the community to recover the solar DR:

$$Ro = \frac{\text{Advection}}{\text{Coriolis}} \sim \frac{v}{2\Omega R_*}$$

Reduced Luminosity  
[e.g. Hotta+ 14]  $\rightarrow L_*/18$

Increased Rotation rate  
Emeriau-Viard & Brun 17  
Hotta+ 18

- Recent highlight of **magnetic contribution**:
- $\rightarrow$  significant retroaction of the small-scale dynamo (Hotta+ 22)
- We propose to control the Nusselt number  $Nu$**  and to keep  $L_{\text{sun}}$  &  $\Omega_{\text{sun}}$  ! (Noraz et al. 2025)  
 $\rightarrow$  How much energy does the convection transport?

$$Nu = \frac{\text{Convection} + \text{Radiation}}{\text{Radiation}}$$

(see also Kapyla+ 17, 19)

# A Nusselt controlled Path at fixed Rossby $Ro$ and increasing turbulence Reynolds $Re$

$$\tau_{\Omega} = 1/2\Omega$$

$$\tau_u = L/u$$

$$\tau_v = L^2/\nu$$

$Ro = \tau_{\Omega}/\tau_u$  we want that number fixed

$Re = \tau_v/\tau_u$  we want that number Big

In today's achievable parameter regime, if you reduce viscosity to increase  $Re$ , you get an increase of  $u$  and hence a decrease of  $\tau_u$  and you change  $Ro$ ! **not good => convective conundrum**

So we need to control the amplitude of  $u$  as we increase  $Re$  by lowering the viscosity  $\nu$

# A Nusselt controlled Path at fixed Rossby $Ro_{nb}$ and increasing turbulence Reynolds $Re_{nb}$

We need to control  $u$  .....

but  $u$  is mostly controlled by the imposed luminosity:  $u \sim L_{conv}^{1/3}$   
and in non diffusion free limit also by  $\nu$

$$\Rightarrow u \sim L_{conv}^{1/3} \nu^{-\alpha} \quad (\alpha \sim 0.2 - \text{exact value depends on stratification } N_\rho)$$

So in order to compensate for  $\nu$ , one needs to adapt  $L_{conv}$

One way is to control the Nusselt nb:  $Nu = (L_{conv} + L_{diff})/L_{diff}$

We will follow that numerical path as a fluid mechanics experiment

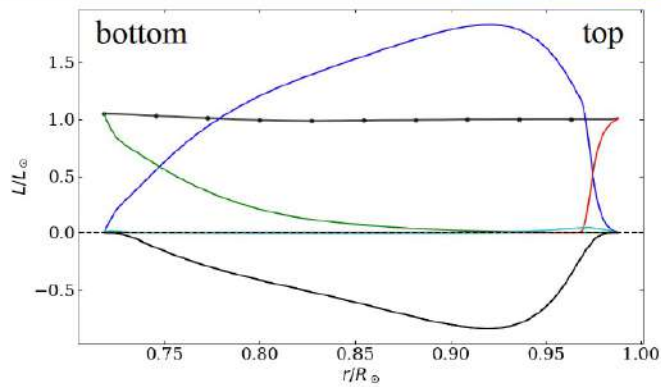
$$L_{conv} = \varepsilon L_{sun}, \tau_v = \varepsilon^{-\beta} \tau_{v0}, \tau_u = \tau_{u0}, \tau_\Omega = \tau_{\Omega0}, R_e = \varepsilon^{-\beta} R_{e0}, L_{diff} = (1 - \varepsilon) L_{sun}$$

a priori  $\beta = 3\alpha$

$$\tau_\Omega = 1/2\Omega; \tau_u = L/u; \tau_v = L^2/\nu$$



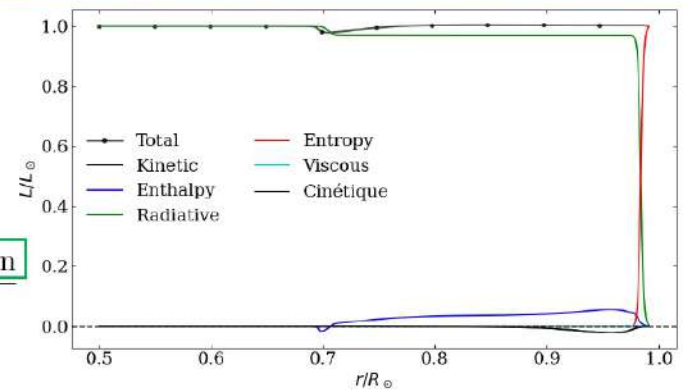
# Nusselt Controlled Experiment: $Re \sim 200+$



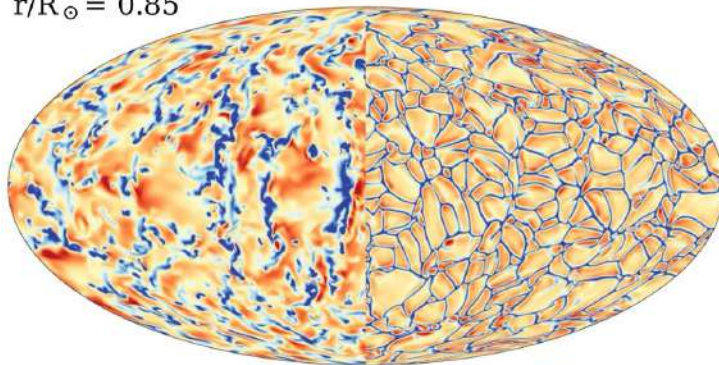
Noraz+22 (PhD)

|      |    |      |
|------|----|------|
| 205  | Re | 270  |
| 2.53 | Ro | 0.9  |
| 26   | Nu | 1.04 |

$$Nu = \frac{\text{Convection} - \text{Radiation}}{\text{Radiation}}$$

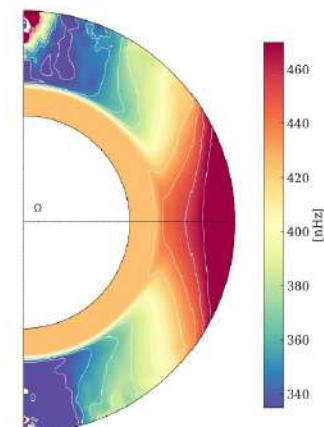
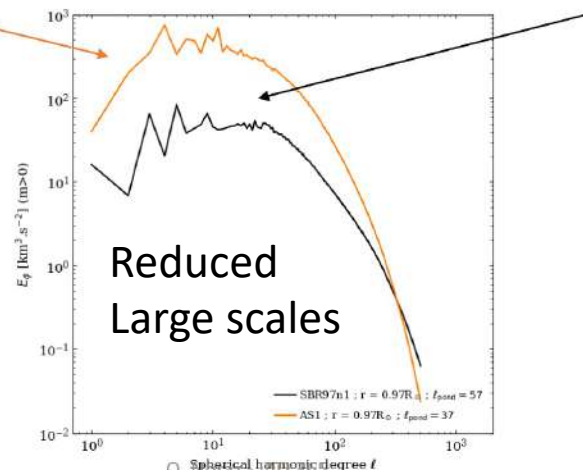
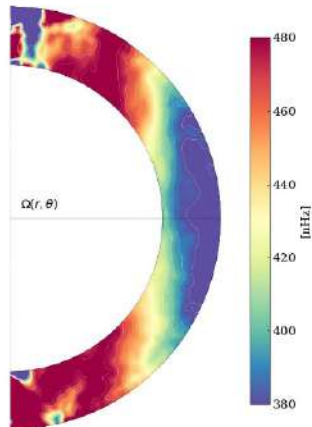
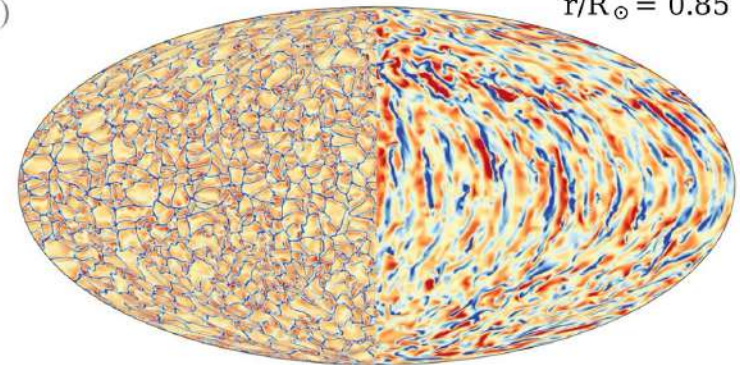


$r/R_{\odot} = 0.85$



Noraz+22 (PhD)

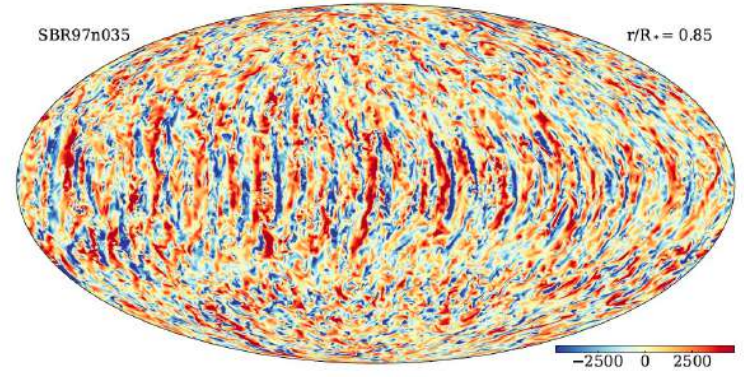
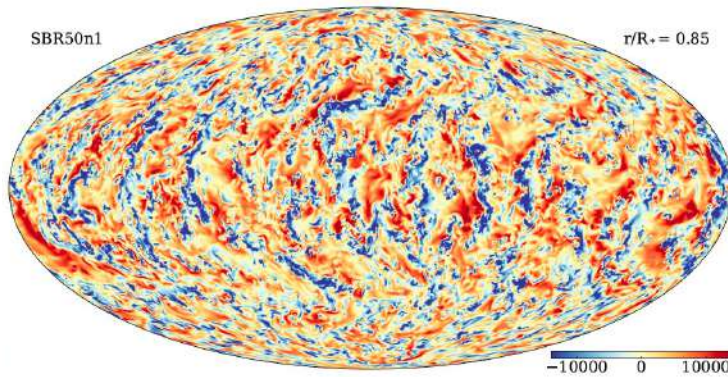
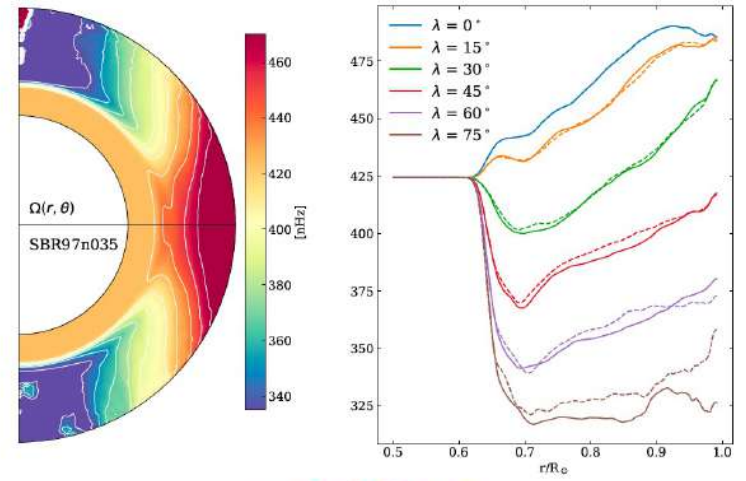
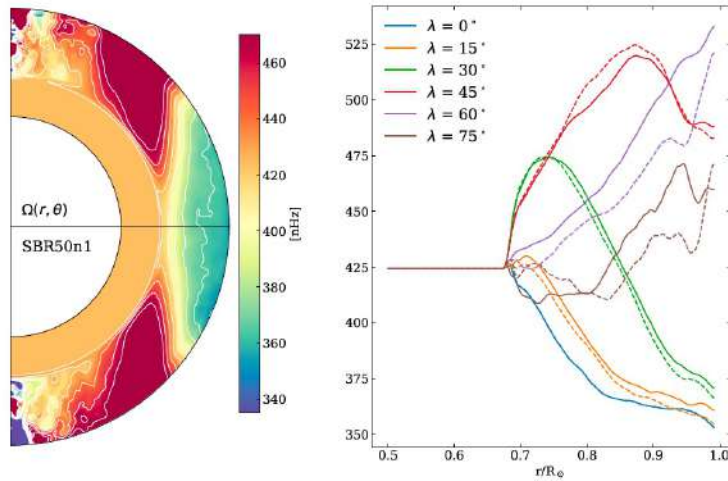
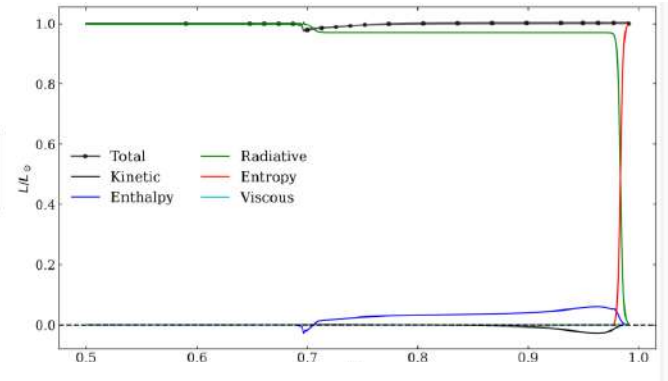
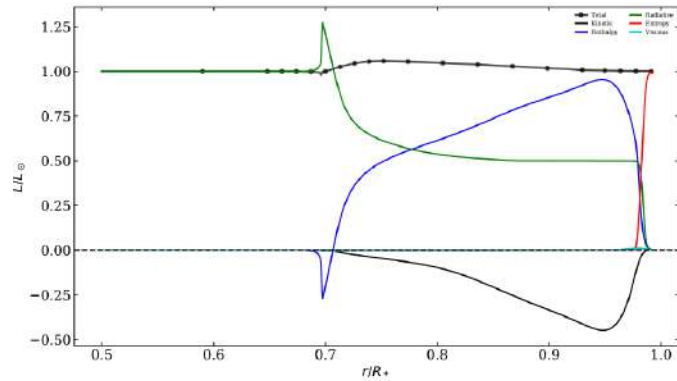
$r/R_{\odot} = 0.99$



# Higher Reynolds Number cases $Re \sim 800+$

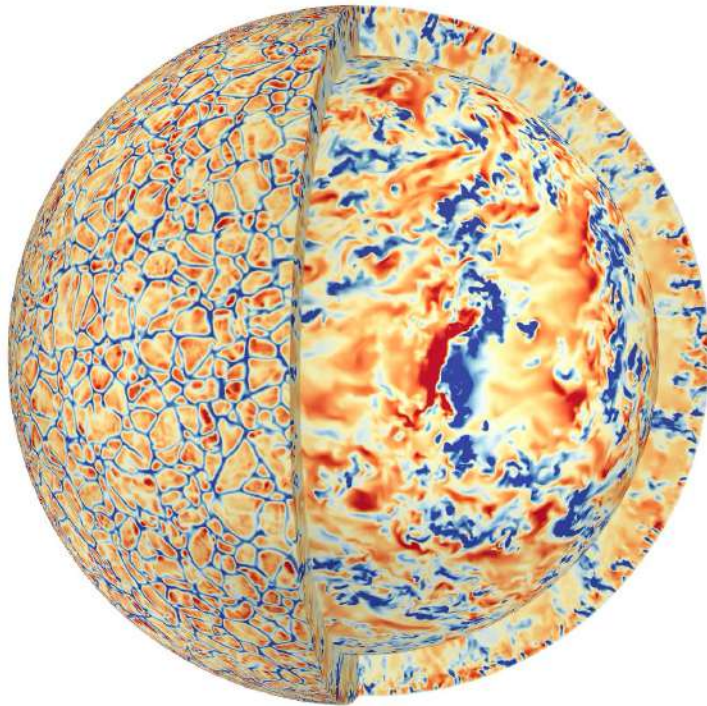
Noraz+22 (PhD)

|      |    |      |
|------|----|------|
| 860  | Re | 811  |
| 4    | Ro | 1.49 |
| 2.45 | Nu | 1.04 |

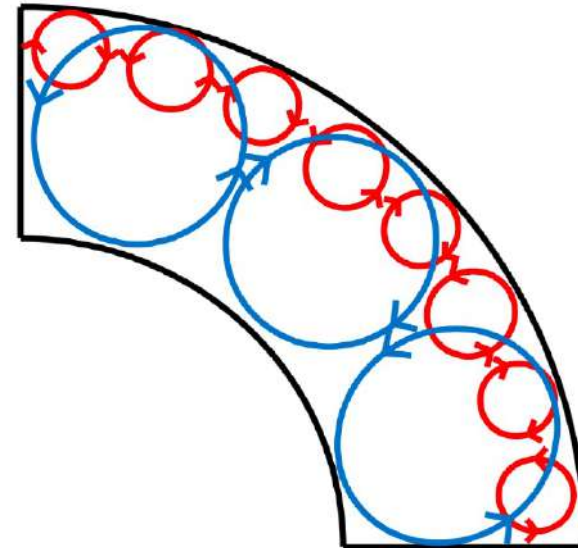




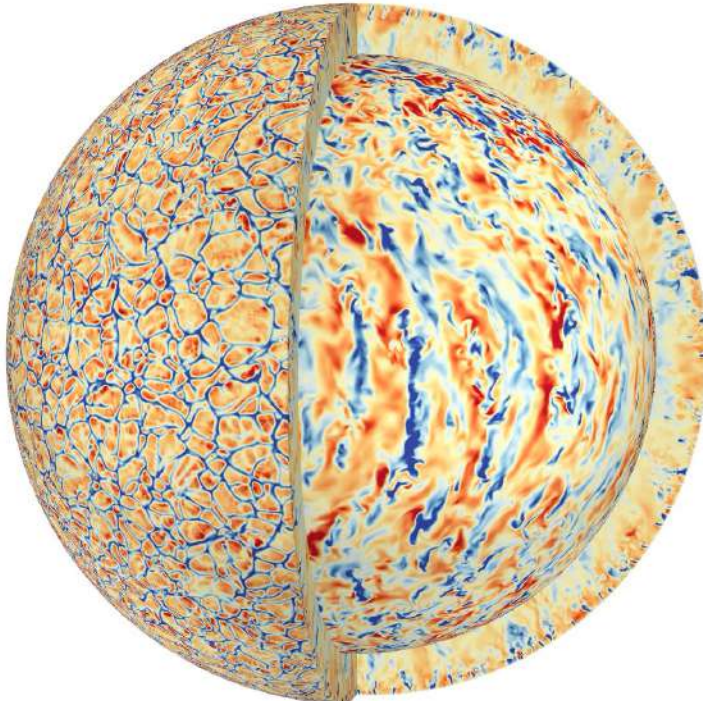
# Convection Dynamics



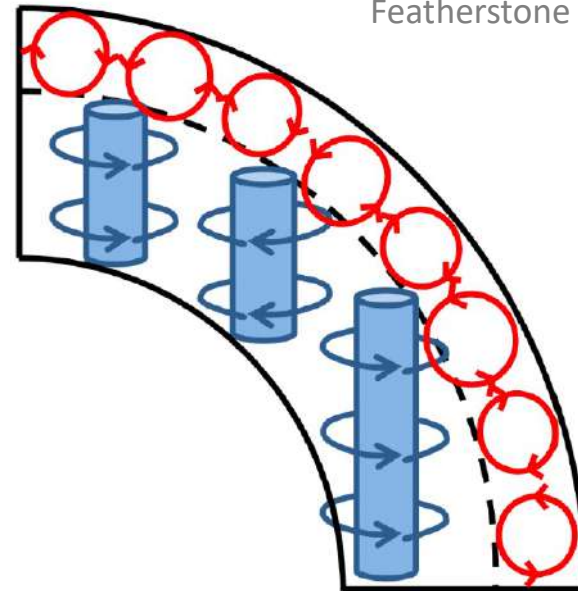
Anti-Solar



Featherstone & Hindman 2016

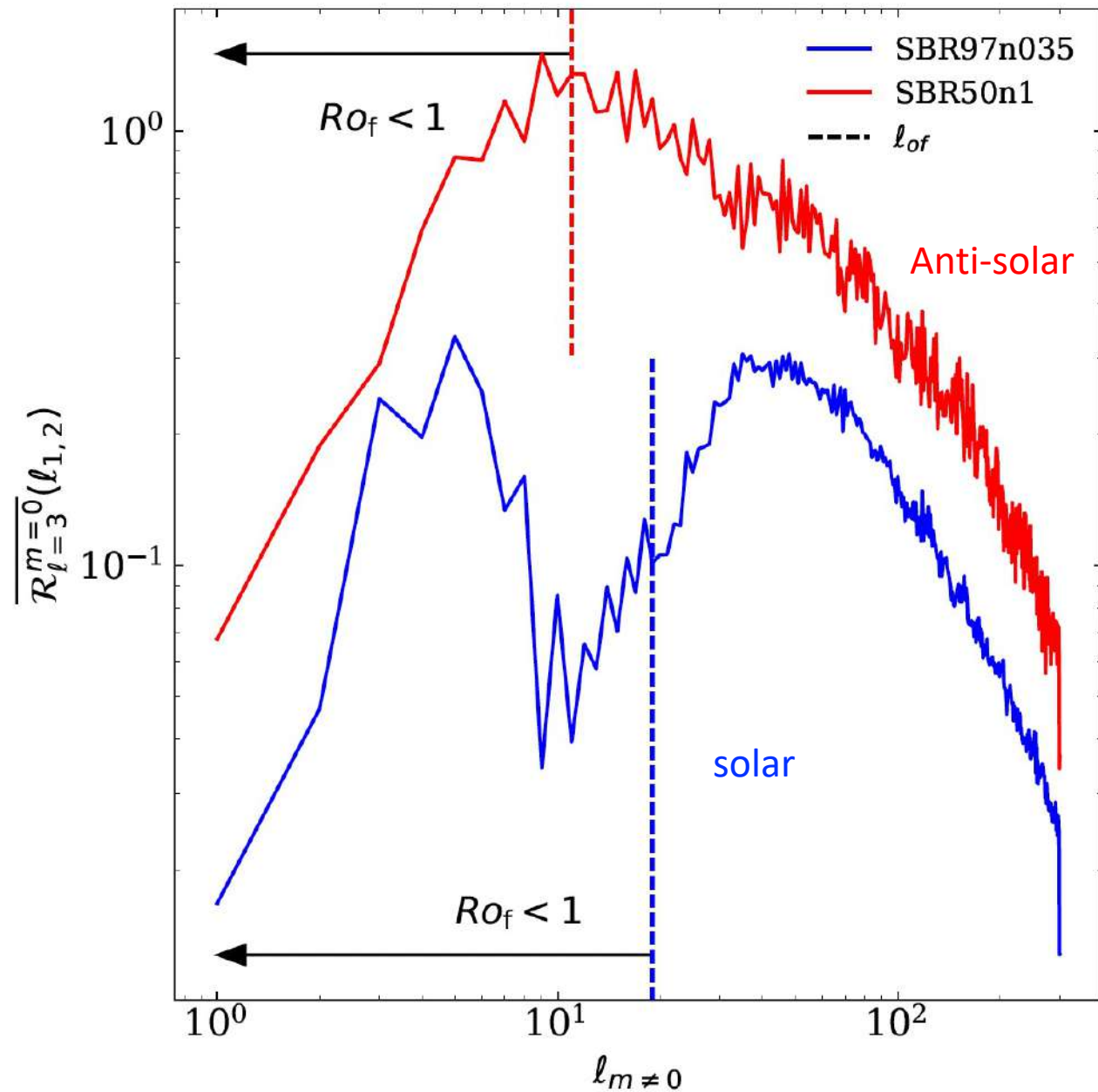


Solar





# Angular momentum spectral transfers via Reynolds stresses

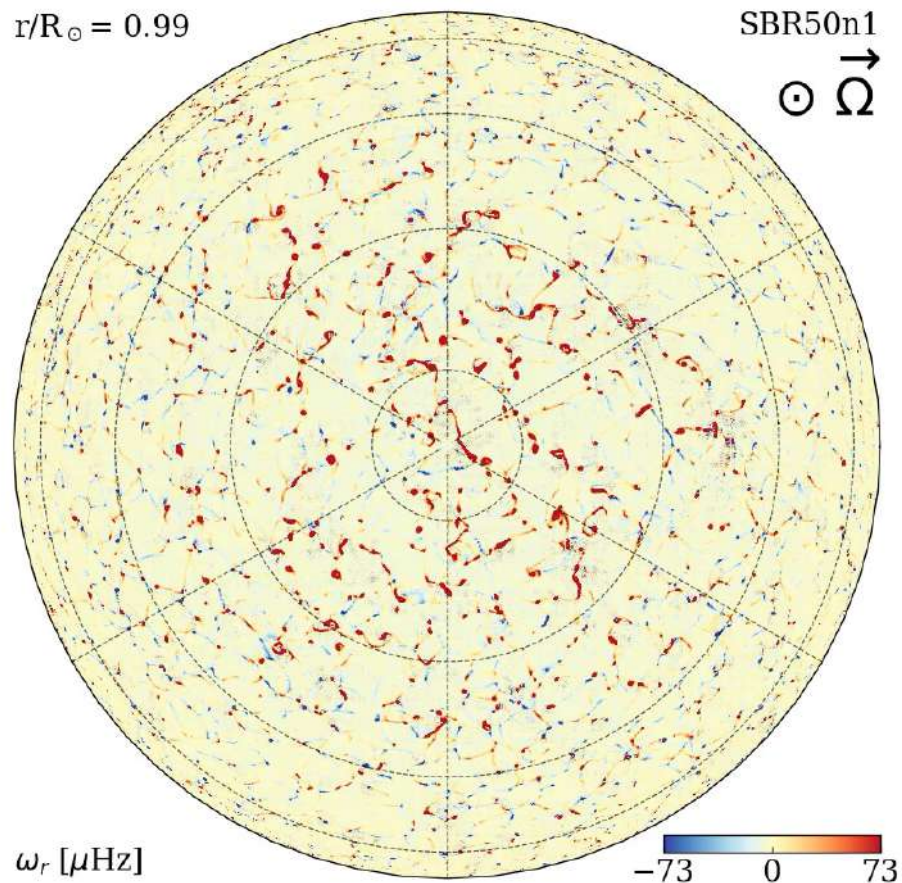


# Polar View

Anti-Solar

$r/R_{\odot} = 0.99$

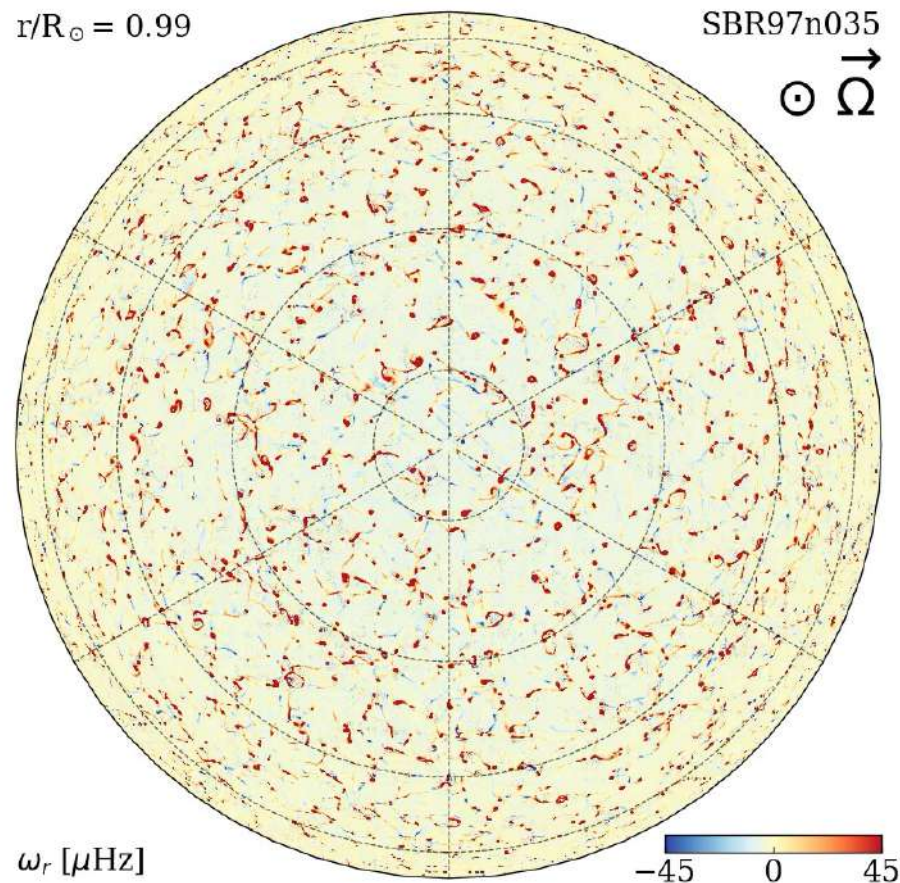
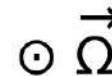
SBR50n1



Solar

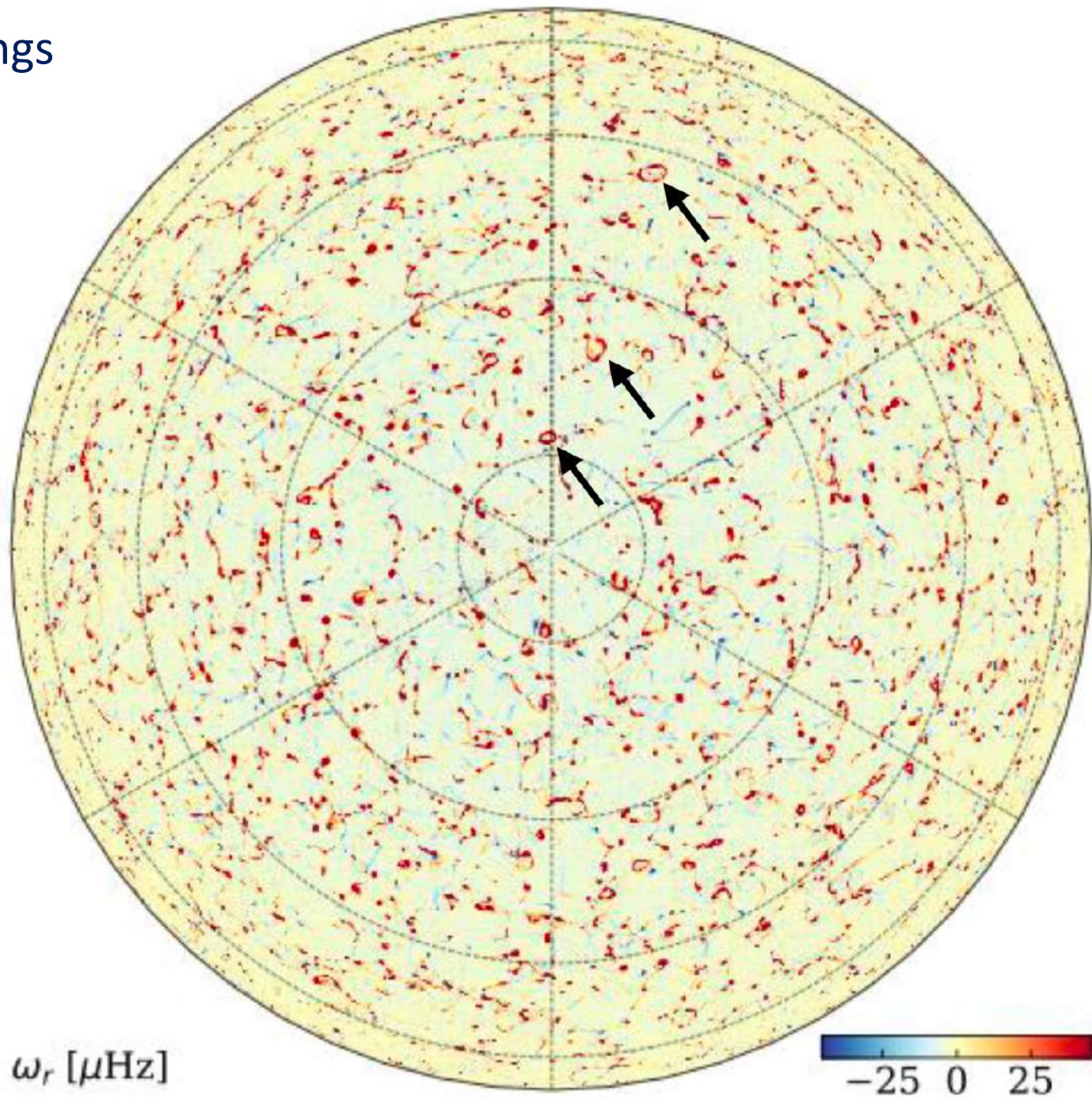
$r/R_{\odot} = 0.99$

SBR97n035





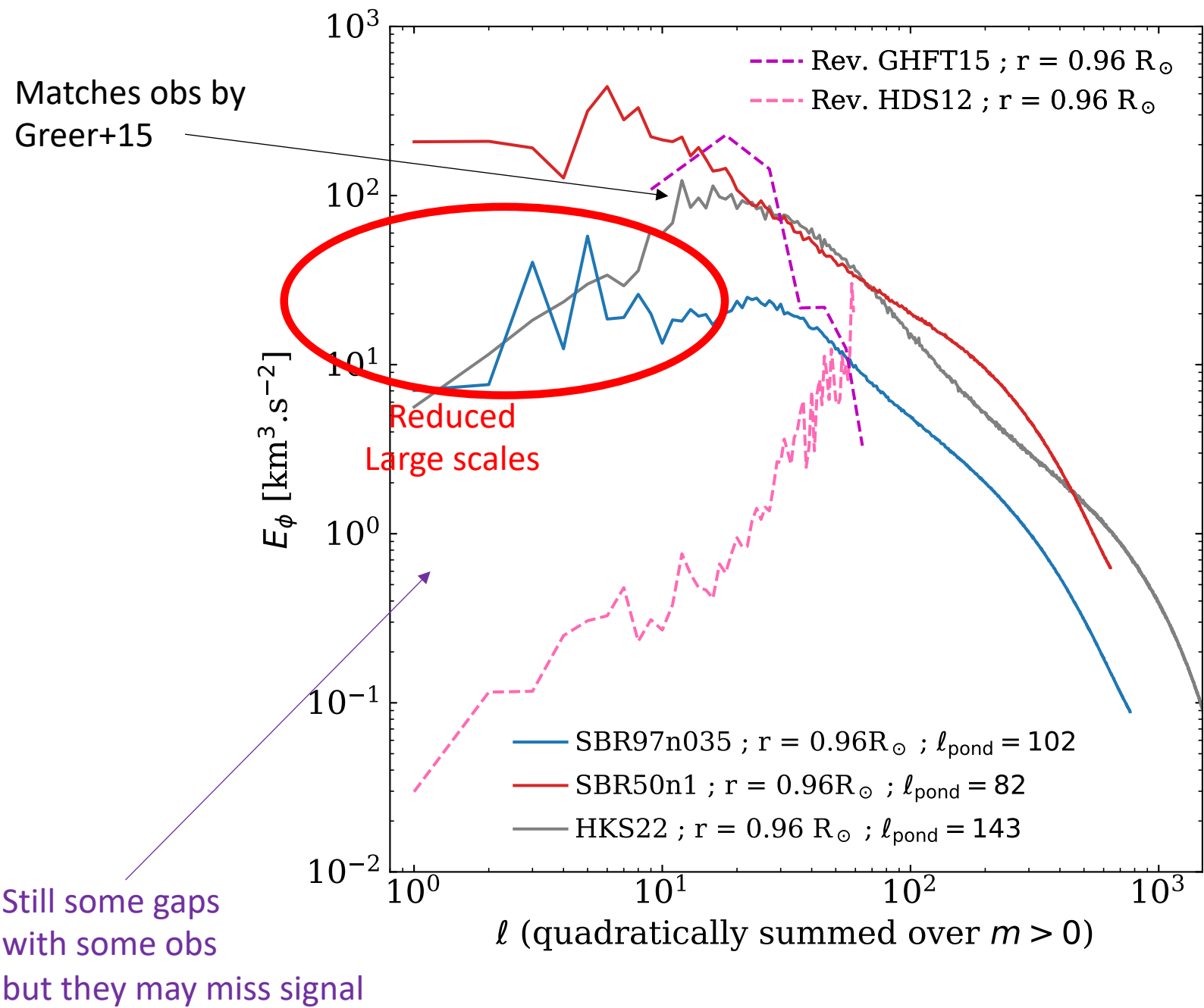
## Polar Rings



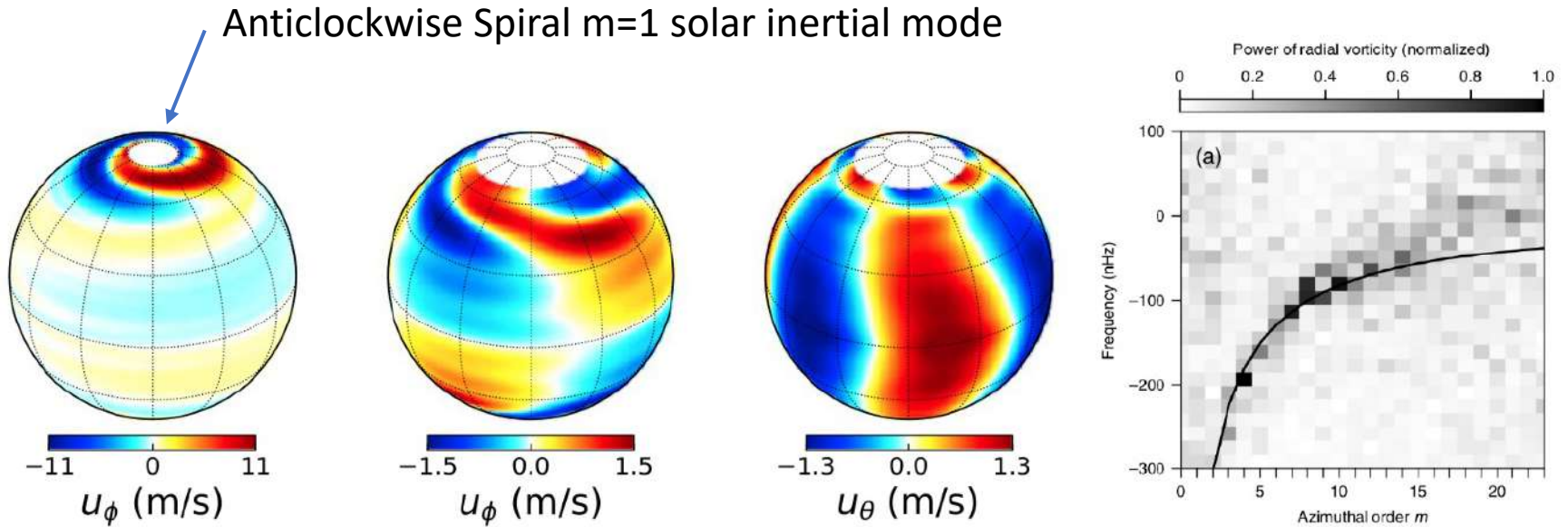
## Confronting simulations to observational (SDO) constraints

- Spectra
- $m=1$  Rossby mode
- Adiabaticity





# Inertial Waves in the Sun



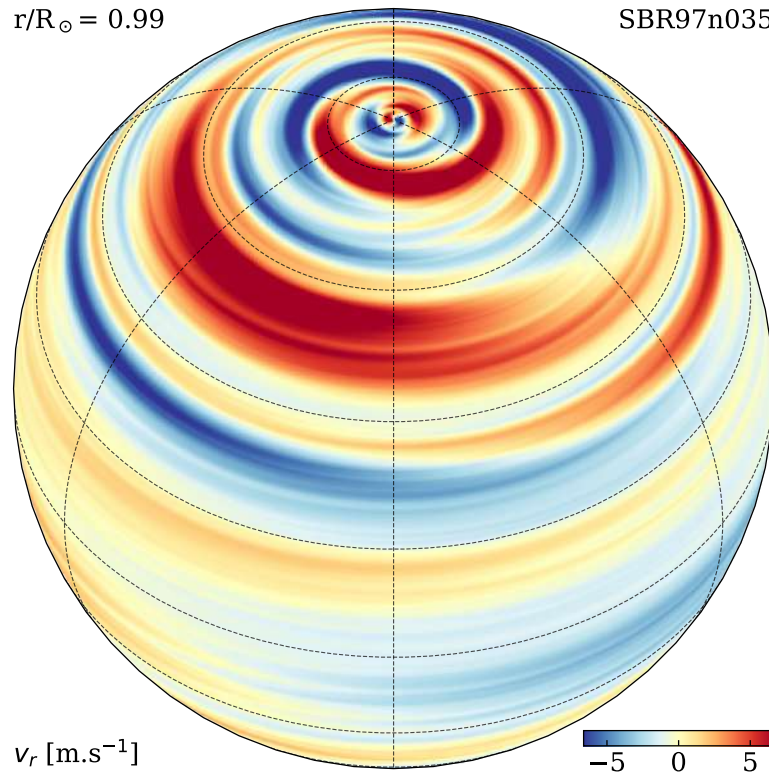
**Figure 2.32 – From left to 2nd panel to the right we show: the  $m = 1$  high-latitude spiral mode at -86 nHz, the  $m = 2$  mid-latitude mode at -73 nHz (Gizon et al., 2021), the  $m = 3$  equatorial (sectoral) Rossby mode at -269 nHz (Löptien et al., 2018a), adapted from (Gizon et al., 2024). Rightmost panel: Power spectrum of radial vorticity from local tracking of granulation, with the sectoral ( $\ell = m$ ) Rossby mode dispersion relation ( $\omega = -2\Omega_\odot/(m + 1)$ ) overplotted in black (Löptien et al., 2018a).**

# m=1 Rossby mode

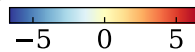
Solar

$r/R_{\odot} = 0.99$

SBR97n035

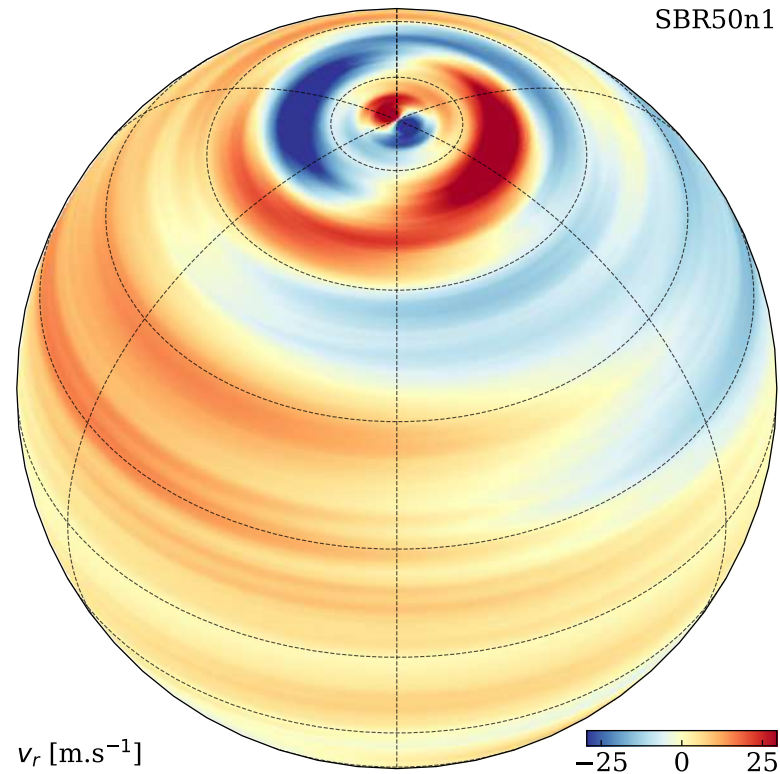


$v_r$  [m.s<sup>-1</sup>]

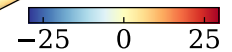


Anti-solar

SBR50n1



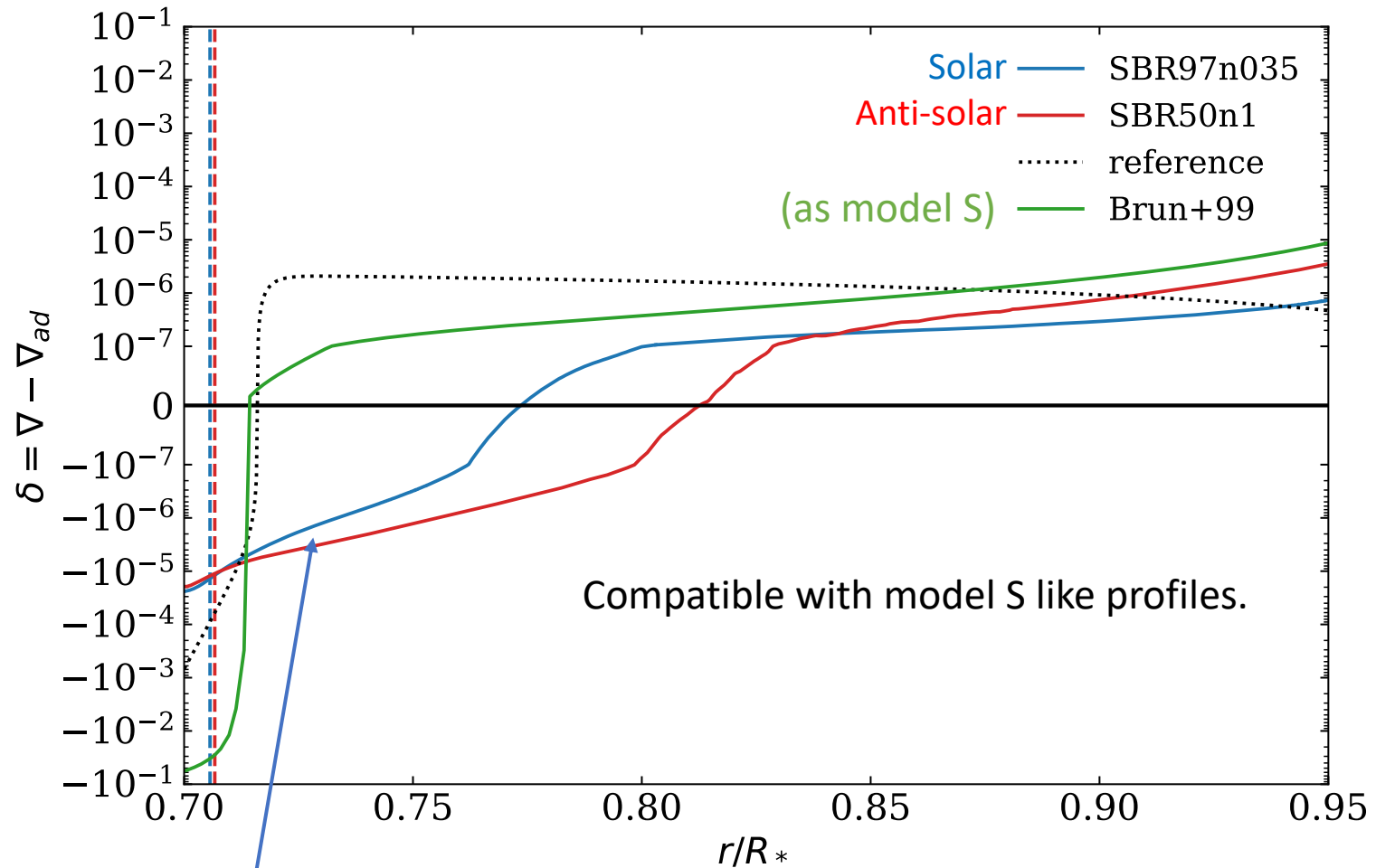
$v_r$  [m.s<sup>-1</sup>]



Correct sign of the spiral

incorrect sign of the spiral

# Adiabaticity Profiles in the simulations



subadiabatic region in both models, unclear you can discriminate....



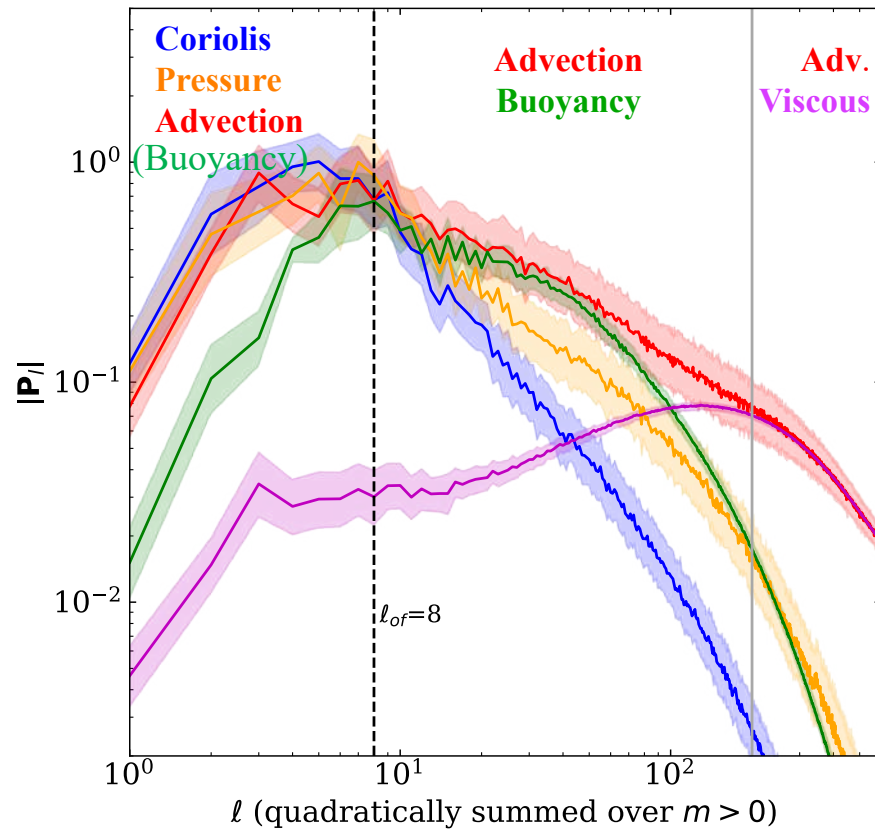
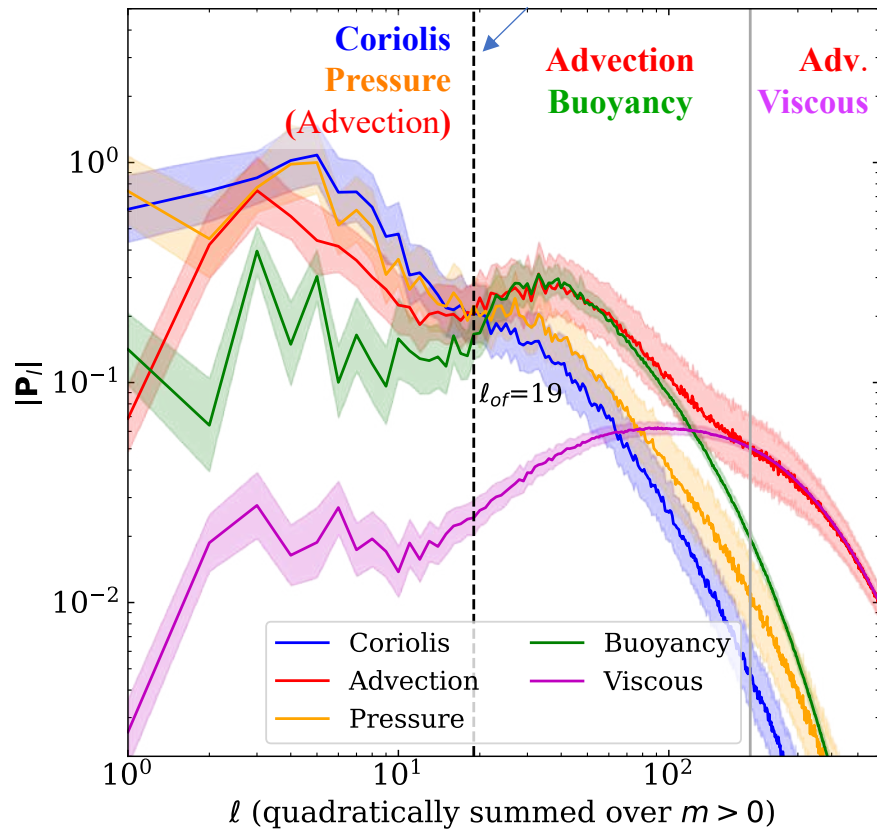
# Kinetic Energy Diagnostic

Solar

Anti Solar

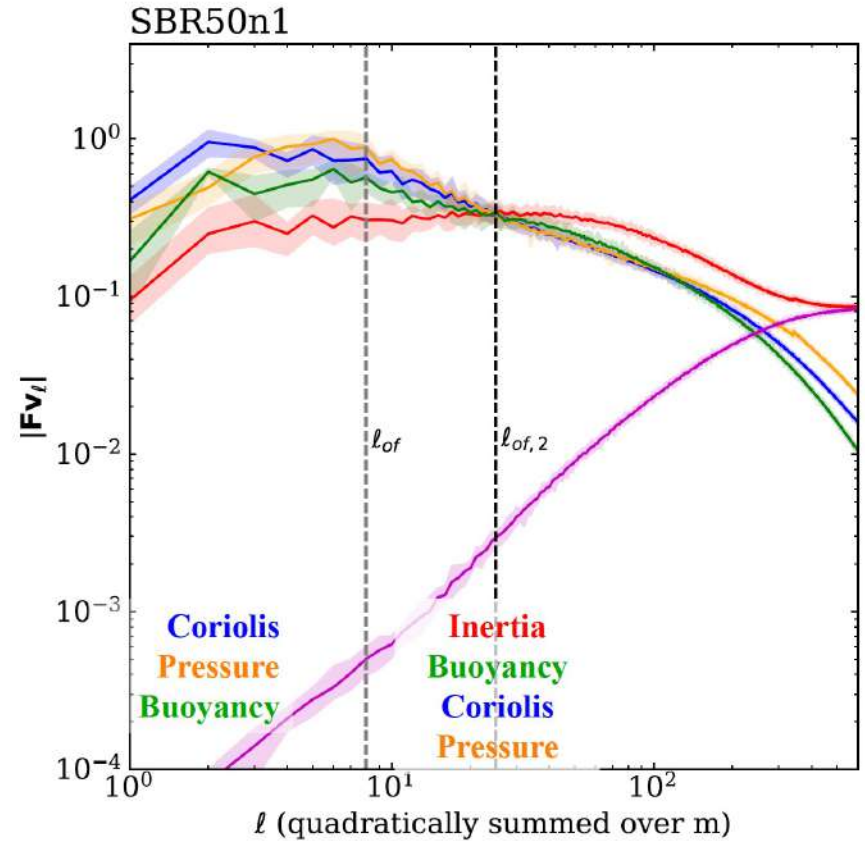
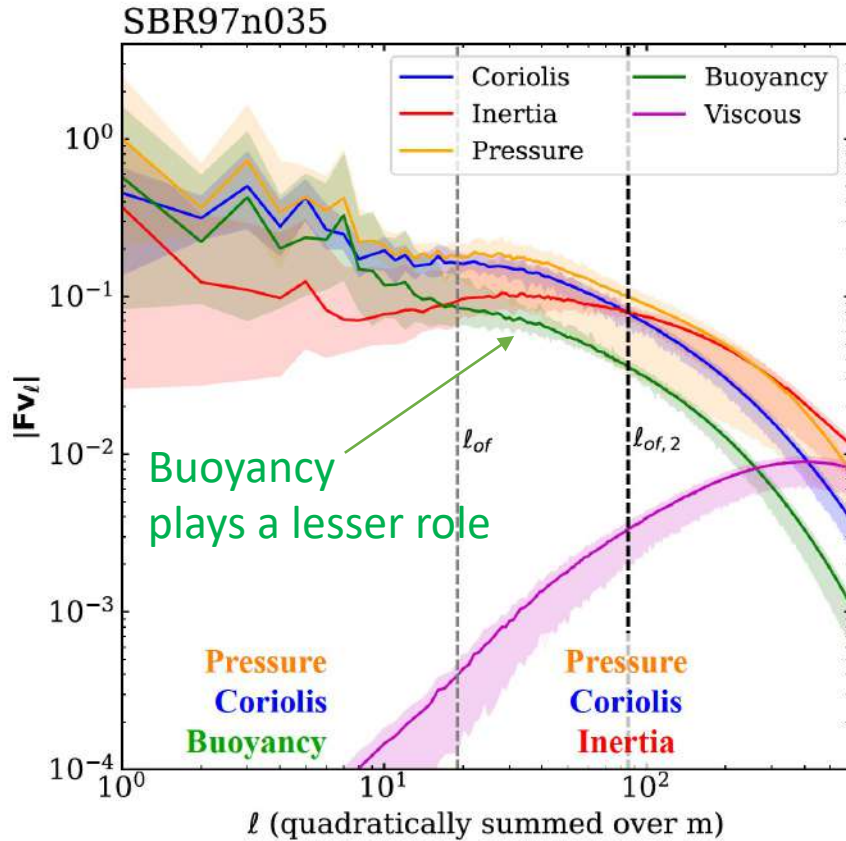
SBR97n035 More scales influenced by rotation

SBR50n1



$$\partial_t E_\ell^K = \underbrace{\sum_{\substack{\ell_1, \ell_2 \\ \ell_{1,2} \geq |\ell_1 - \ell_2| \\ \ell_{1,2} \leq \ell_1 + \ell_2}} [\mathcal{R}_\ell(\ell_1, \ell_2)]}_{\text{Reynolds stress}} + \underbrace{\mathcal{C}_\ell(\ell - 1, \ell + 1)}_{\text{Coriolis force}} + \underbrace{\widehat{\mathcal{H}}_\ell}_{\text{Pressure work}} + \underbrace{\mathcal{B}_\ell}_{\text{Buoyancy}} + \underbrace{\mathcal{V}_\ell}_{\text{Viscosity}}$$

# Vertical Force Balance



$$\underbrace{\frac{\partial \mathbf{v}}{\partial t}} + \underbrace{(\mathbf{v} \cdot \nabla) \mathbf{v}} = - \underbrace{\nabla \varpi}_{c_p} - \underbrace{\frac{S}{c_p} \mathbf{g}} - \underbrace{2\Omega_* \times \mathbf{v}}_{\text{Coriolis}}$$

$$- \underbrace{\frac{1}{\bar{\rho}} \nabla \cdot \mathcal{D}} - [\nabla \bar{\omega} + \bar{\omega} \nabla \ln \bar{\rho} - \mathbf{g}],$$

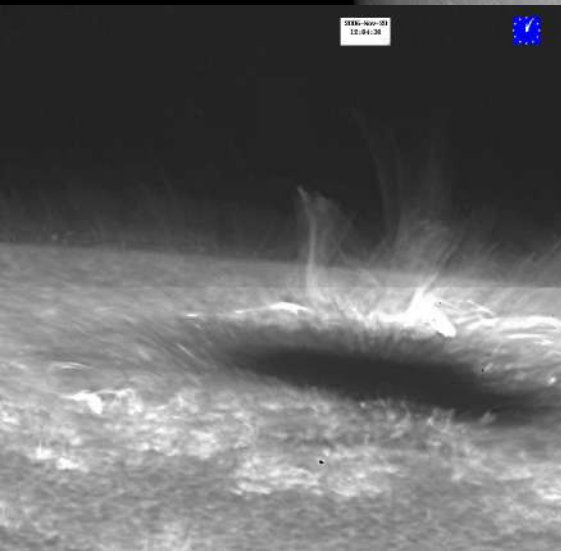
$$|\mathbf{F}_\ell| = \sqrt{\int_t \int_r \mathbf{f}_\ell^2 r^2 dt dr / \int_t \int_r r^2 dt dr}.$$

# So what about the Spotty-Dynamo Paradox?

Where are the spots in current  
convective dynamo simulations?

Are they really needed  
to get the 11yr cycle?

Brun et al. 2015, 2022

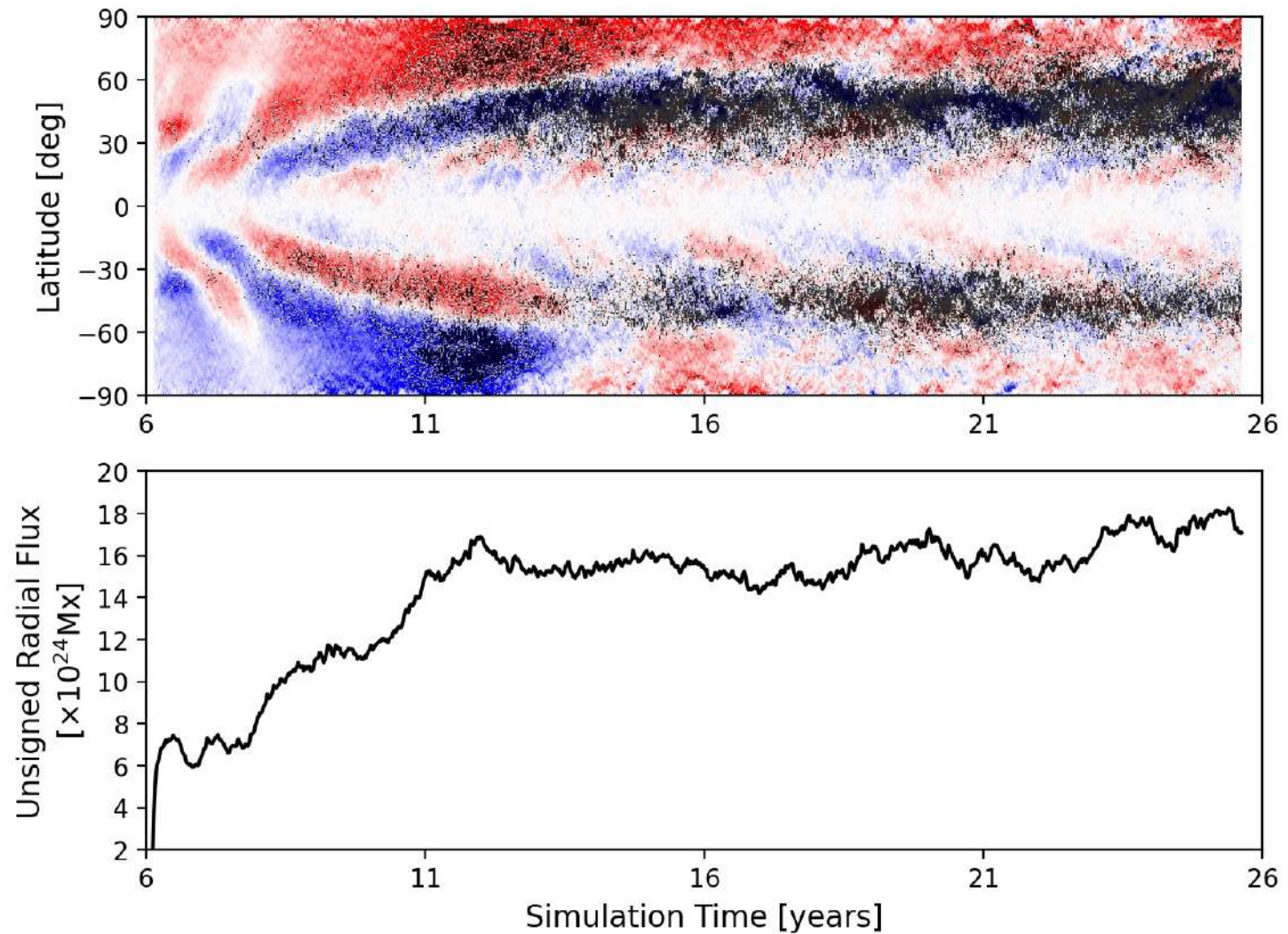


Adding Magnetic field in these Nusselt controlled experiments

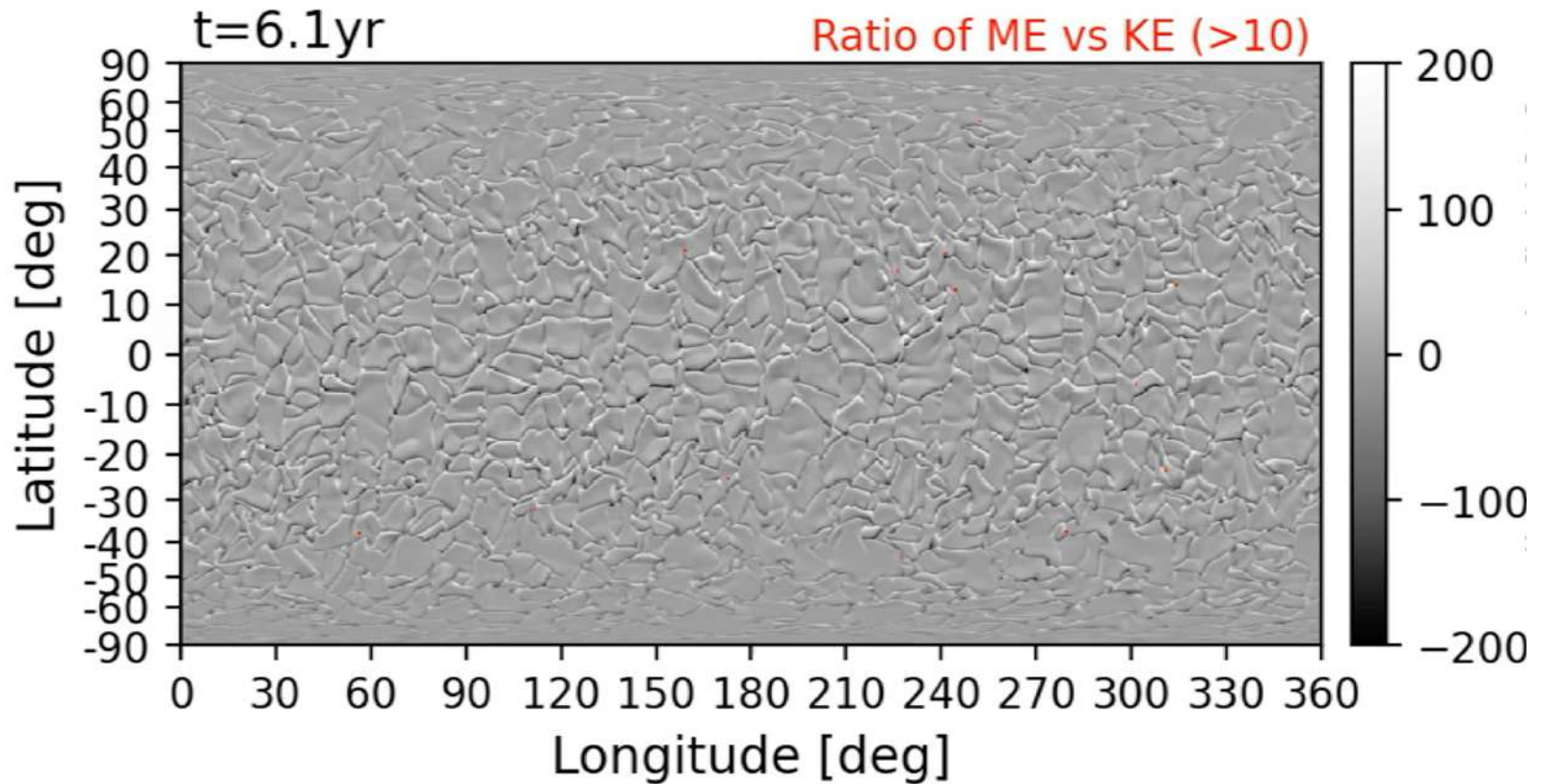
Let's see if that makes a difference about spotty dynamo paradox?



## Current Evolution Stage of the dynamo solution simulation

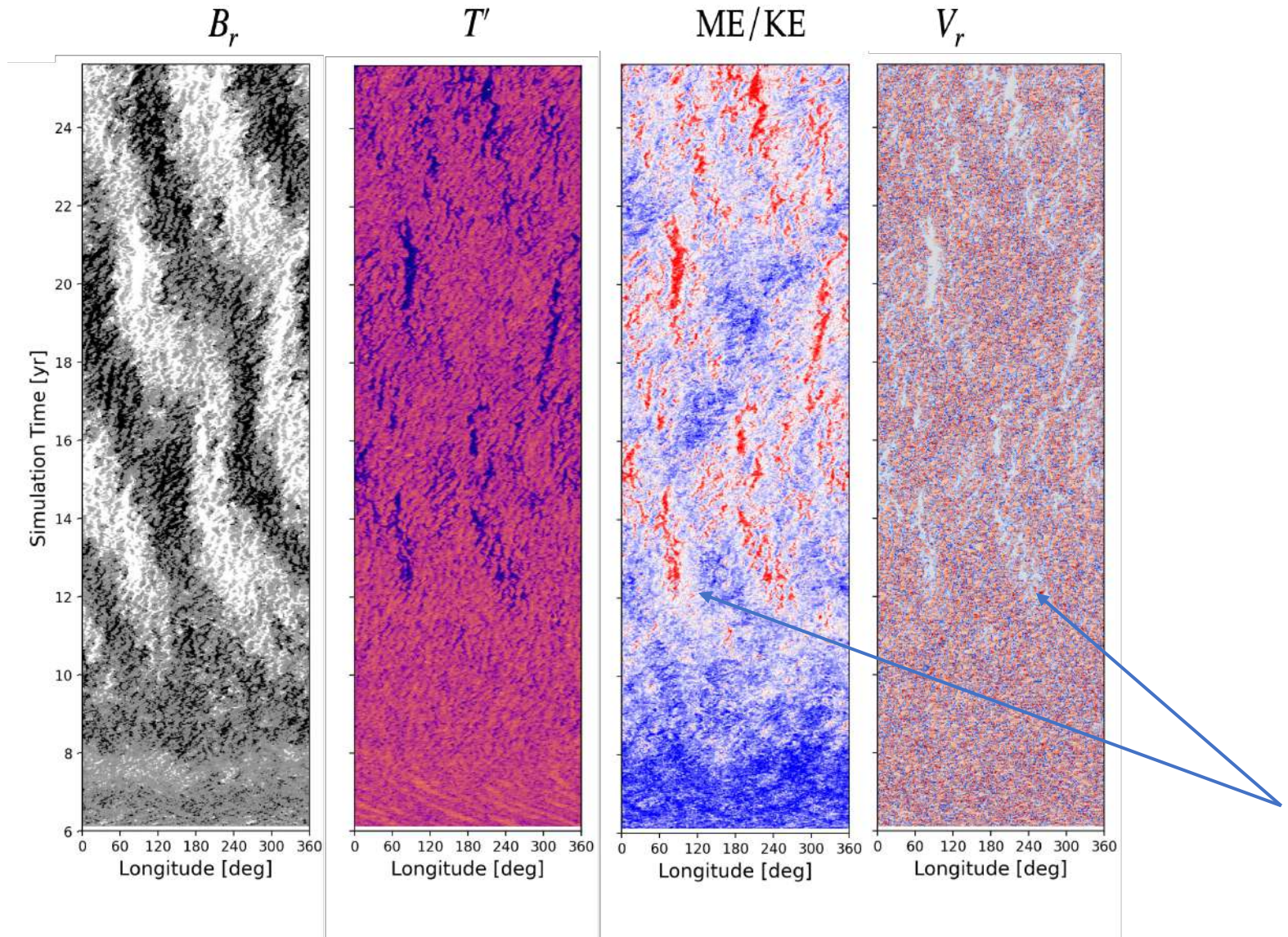


## Progressive Emergence of Strong and Large Events

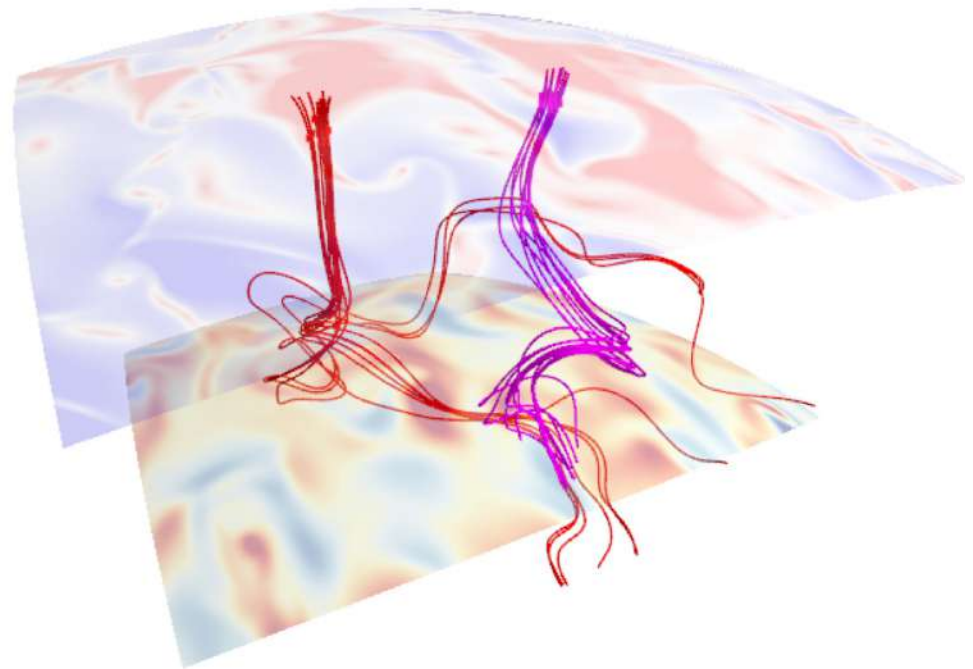
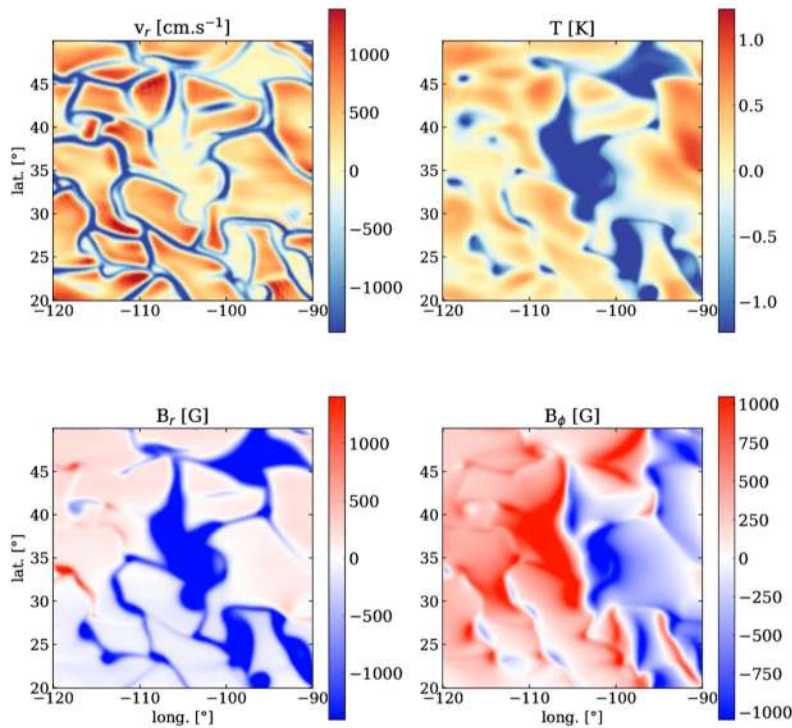




# Time-longitude diagrams



## 3D view on a stronger magnetic feature



Convective inhibition by strong magnetic concentrated flux tubes  
Very promising for progenitor « sunspot » formation



What's Next?

Harvesting exascale supercomputers and new numerical methods

In 2017, we (A.S. Brun, L. Gizon, M. Carlsson, V. Archontis, F. Moreno-Insertis)  
Designed a synergy ERC project to attack some of these difficult solar physics pb.



The image shows a screenshot of the 'Whole Sun Project' website. The header is orange with the 'erc WHOLE' logo on the left and a navigation menu on the right containing links: HOME, NEWS, MEMBERS, RESEARCH, COMPUTING, JOBS, PUBLICATIONS, PUBLIC OUTREACH, and CONTACT. The main content area features a large, colorful 3D visualization of the Sun's interior and magnetic field lines. Overlaid on this is the text 'WHOLE SUN PROJECT' in large orange letters and 'ERC Synergy Grant in Astrophysics' in blue letters. To the right, a smaller 3D plot labeled 'a' shows magnetic field lines with a color scale for  $V_z$  (km/s) ranging from -5 (red) to 5 (blue). A dotted line points from the text 'a 7 yr project' to the main visualization. At the bottom, the website address 'wholesun.eu' is displayed.

erc WHOLE

HOME NEWS MEMBERS RESEARCH COMPUTING JOBS PUBLICATIONS PUBLIC OUTREACH CONTACT

**WHOLE SUN PROJECT**  
ERC Synergy Grant in Astrophysics

a 7 yr project

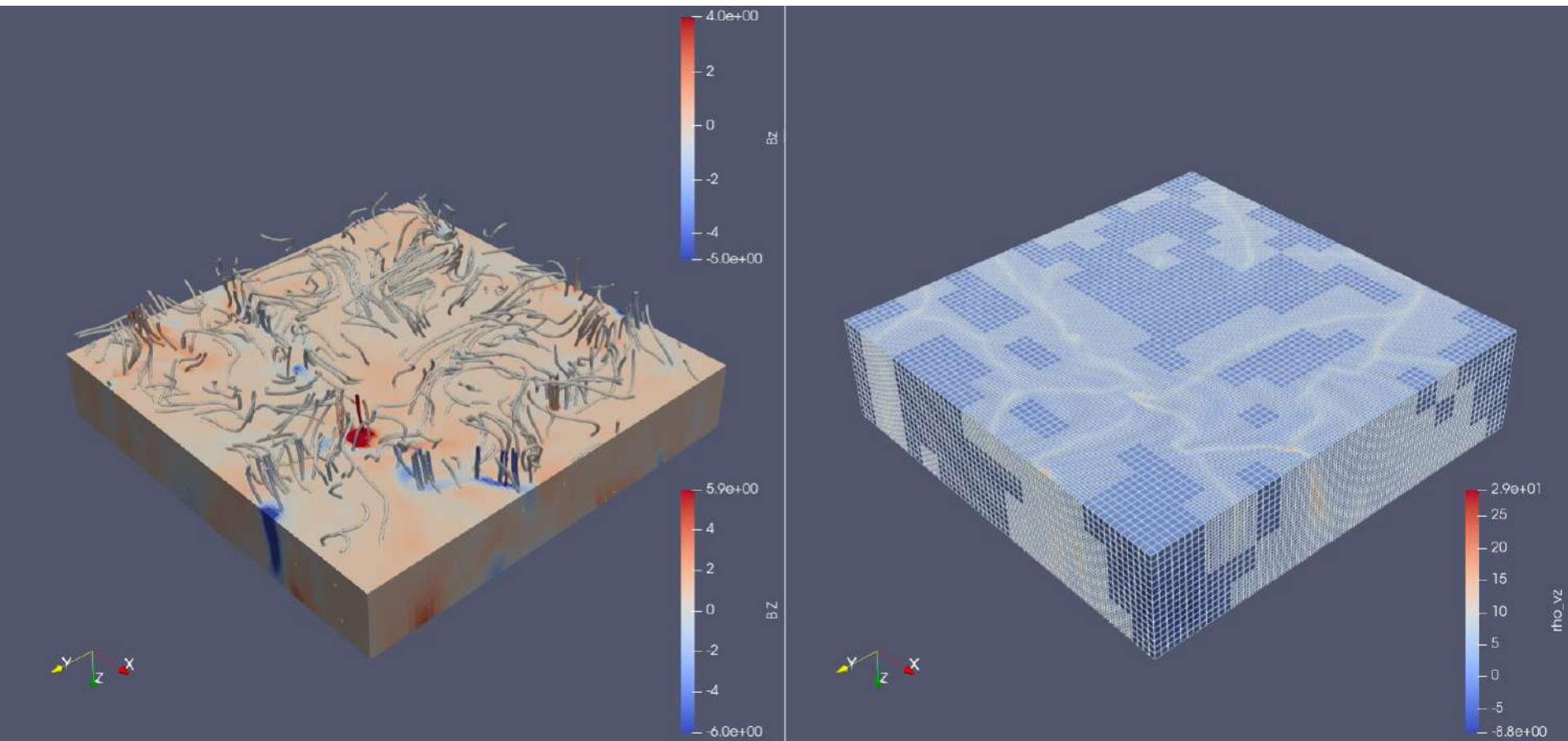
$V_z$  (km/s)

wholesun.eu

Every March since 2020 we have a 3 weeks program in Paris, contact us if you wish to attend

=> New open source Dyablo Code – some recent updates.

# 3D AMR Dynamo Convection simulation with Dyablo

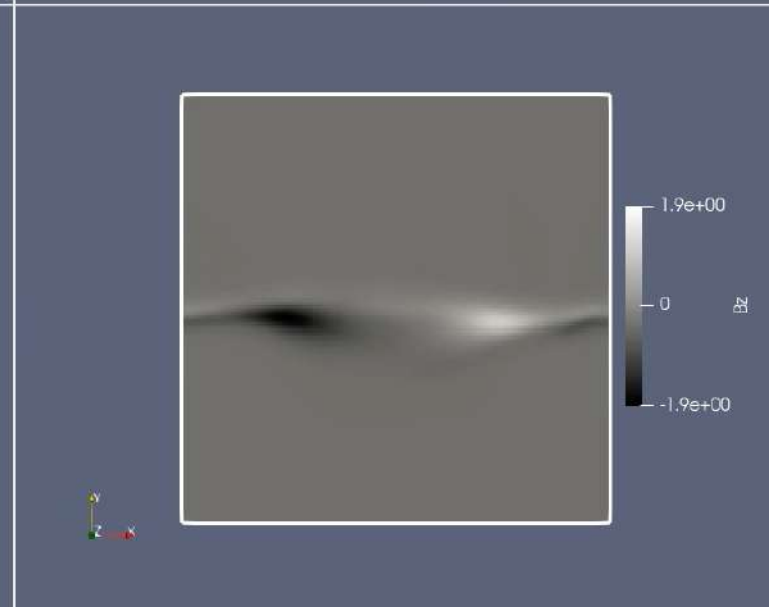
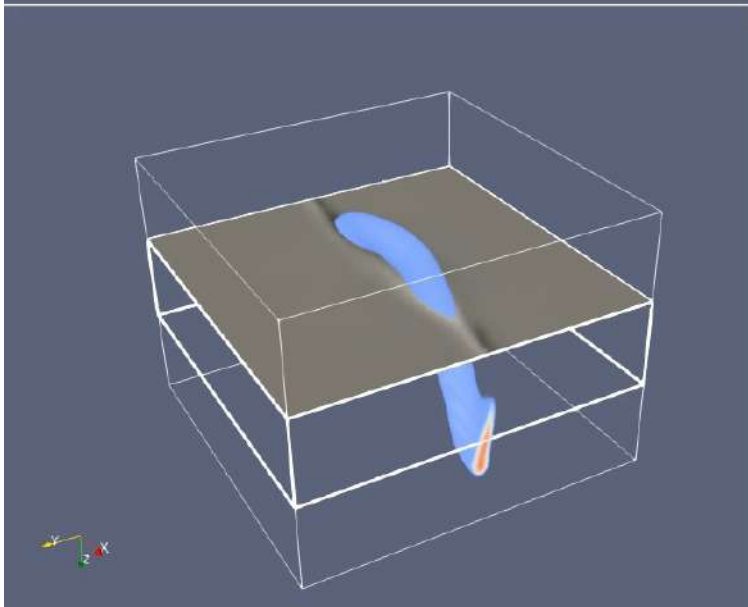
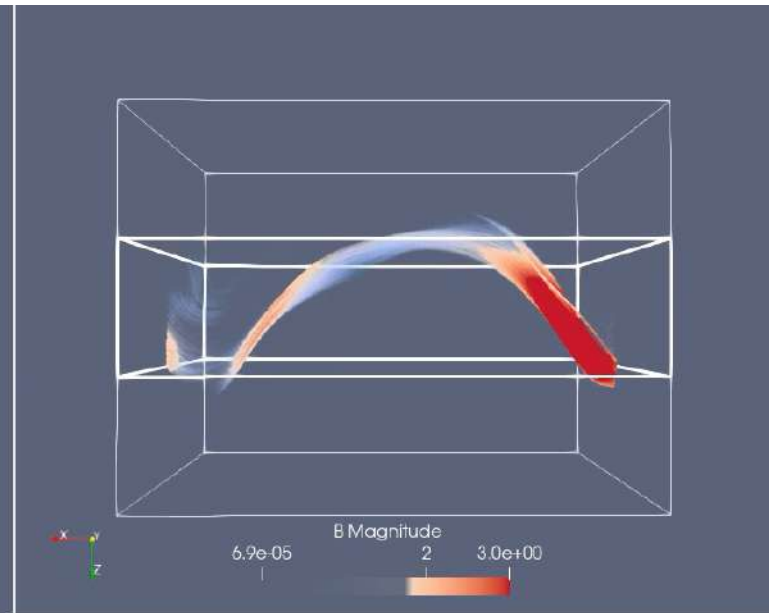
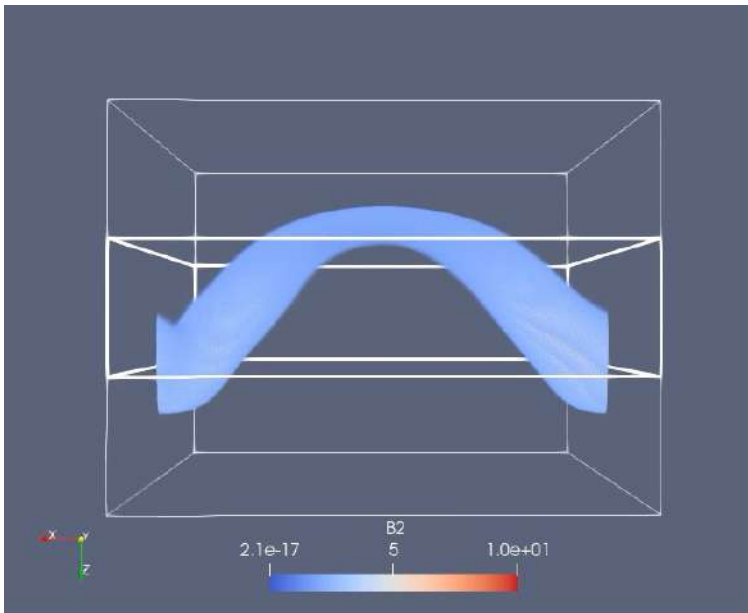


# 3D Tri-layers Convection + Flux Emergence simulation with Dyablo

Stable

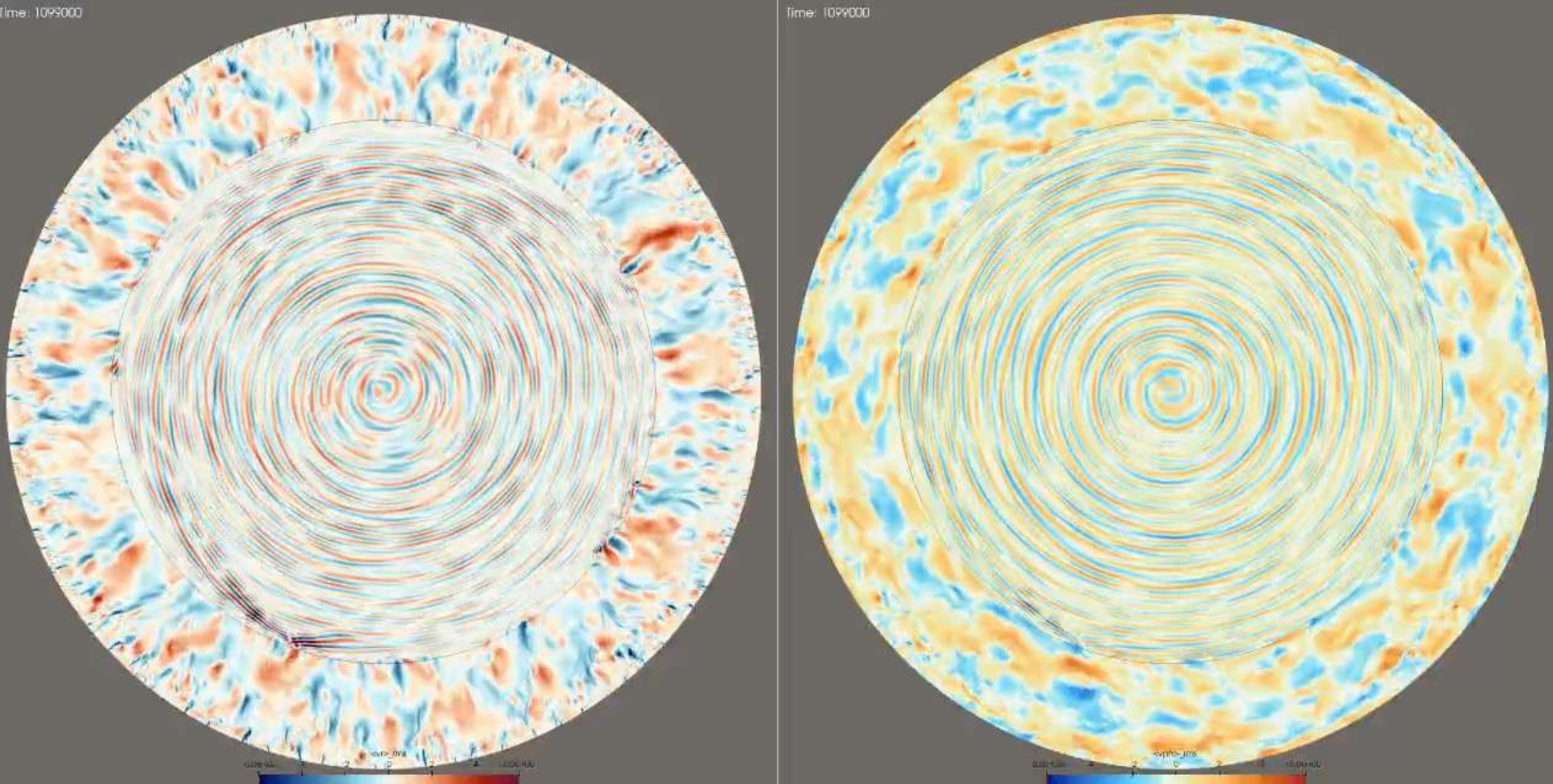
Convection

Stable



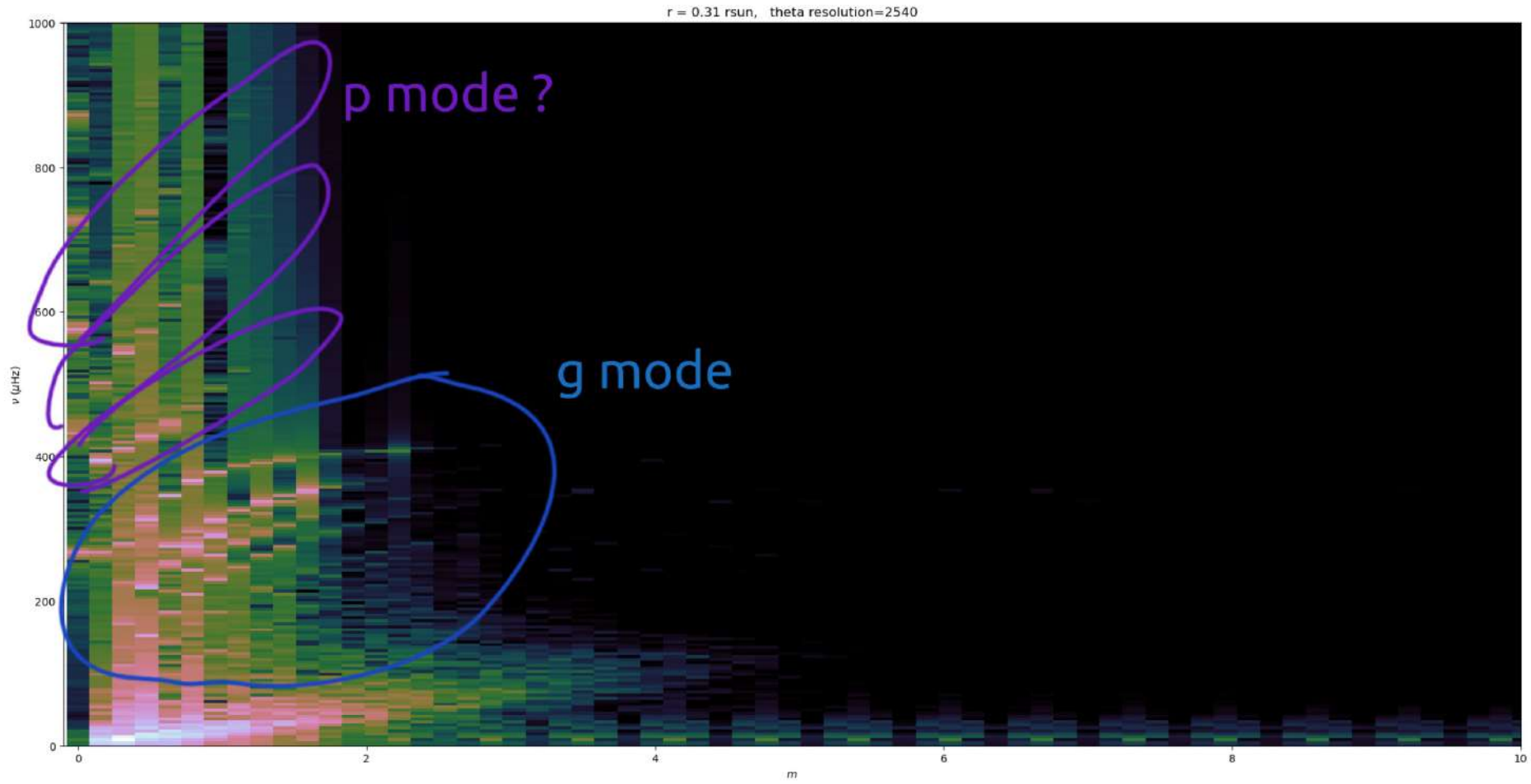


# Solar Convection, Gravity and Acoustic Waves in fully compressible Dyablo Whole Sun Simulations

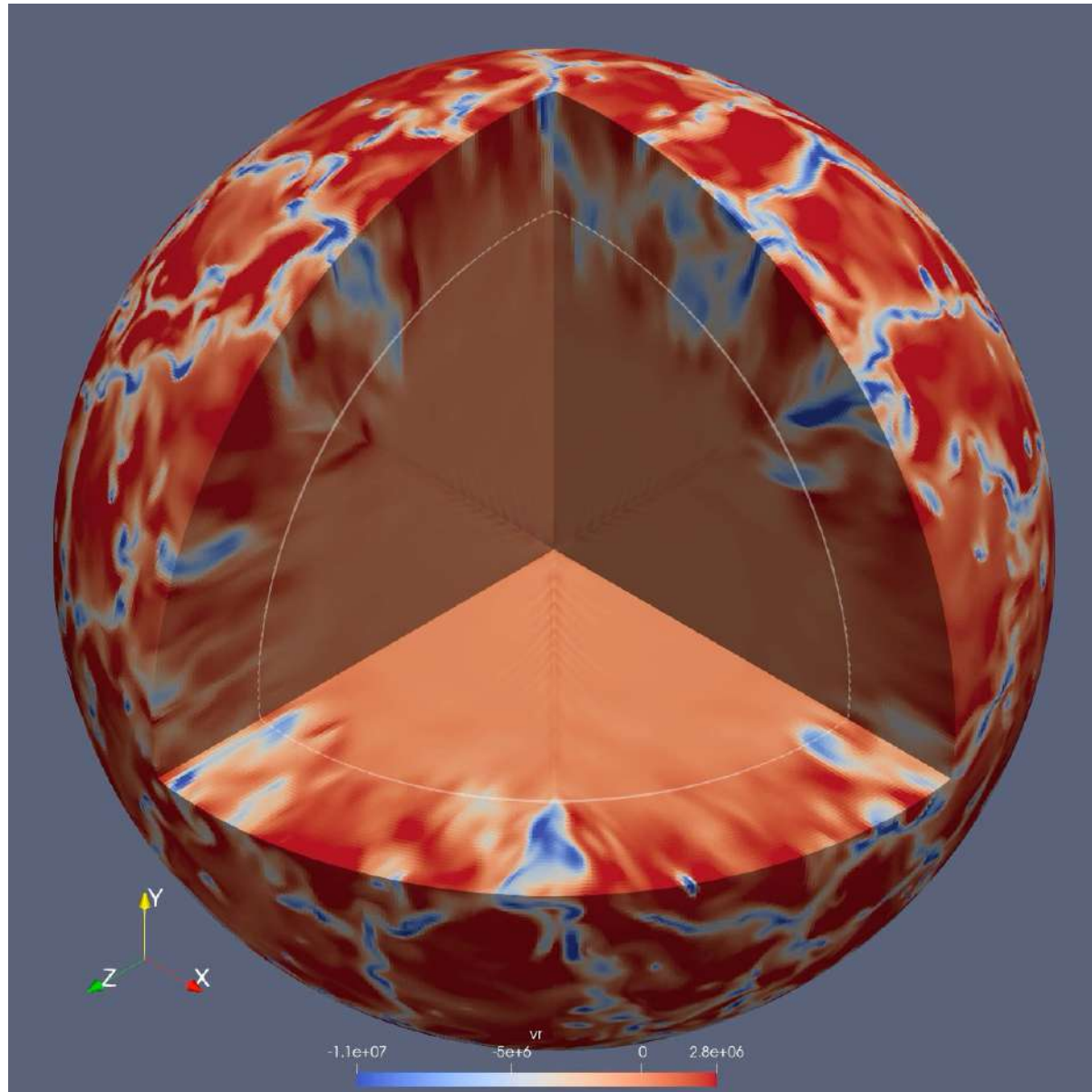


Doboele, Brun, Delorme et al. 2026, in prep

# P and G modes in a Solar simulations



## 3D Convection spherical simulation with Dyablo



## Conclusions (I)

- 1) In solar/stellar dynamo we are able to get decadal long cyclic solutions, that exhibits intense Magnetic wreaths that lead to the formation of self-consistent Omega-loop formation and to Flux emergence events with interesting properties (such as tilt). They also agree with Zeeman-Doppler Imaging observational trends ( $B(Ro) \propto Ro^{-1.4}$ ).
- 2) A *Magnetochronology* story can be presented where young stars have banded/cylindrical differential rotation and short period magnetic cycles, stars like the Sun decadal long cycles and slowly old rotating stars a direct dynamo (no cycles) and a retrograde equator (anti-solar).
- 3) However, these solutions do not possess sunspot/starspot though and are slightly misplaced in Rossby number parameter space.



## Conclusions (II)

- 4) With a control of Nusselt number, we are able to reproduce (maintain) realistic solar differential rotation at high Reynolds numbers
- 5) We may see that the Sun is running deep a C-I balance rather than a CIA (in hydro). This may imply that in MHD case it is a MIC and not a MAC balance that dominates (work in progress)
- 6) In the Nusselt controlled experiment, we start seeing very interesting intense magnetic field concentration that inhibits surface convection, these new generation dynamo solution are very promising, stay tuned !!!



## Reynolds stresses in spectral space

$$\mathcal{R}_\ell(r, \ell_1, \ell_2) = \bar{\rho} \int_S [\mathbf{v}_{\ell_1} \cdot \nabla(\mathbf{v}_{\ell_2})]_\ell \cdot \mathbf{v}_\ell d\Omega,$$

$$\overline{\mathcal{R}_{\ell=3}^{m=0}}(\ell_{1,2}) = \frac{1}{(2\ell+1)\mathcal{R}_\ell^{m>0}} \sum_{\substack{\ell_{2,1} \\ |\ell_1-\ell_2| \leq \ell \leq \ell_1+\ell_2 \\ m_1+m_2=0; m_1>0, m_2>0}} |\mathcal{R}_{\ell=3}(\ell_1, \ell_2)|,$$

$$\text{where } \mathcal{R}_\ell^{m>0} = \sum_{\substack{\ell_1, \ell_2 \\ |\ell_1-\ell_2| \leq \ell \leq \ell_1+\ell_2 \\ m_1+m_2=0; m_1>0, m_2>0}} \mathcal{R}_{\ell=3}(\ell_1, \ell_2).$$