

惑星研究集会@CPS , 2017/2/23

modeling small scale processes in the ocean

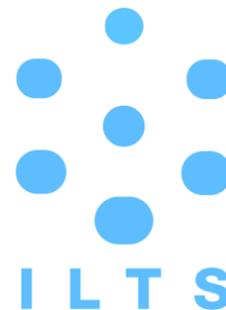
Lagrangian frazil ice simulation using a Particle-in-Cell type ocean model

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Arctic Challenge for Sustainability



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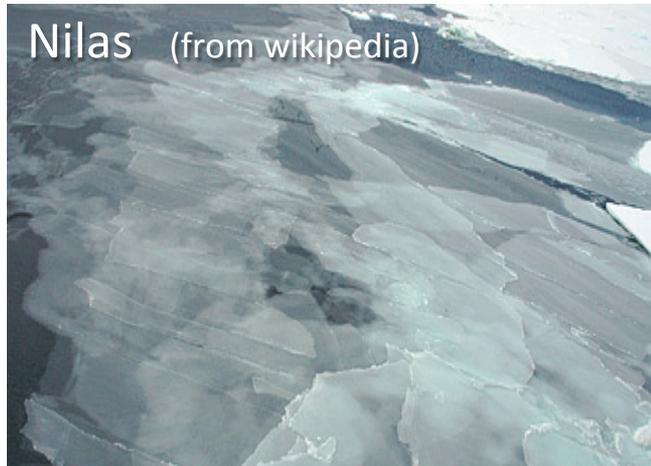
Introduction

Sea ice cover controls atmosphere-ocean heat exchange

Solid Ice cover has very low thermal conductivity (**insulating effect**)

→ Reduce upward heat flux → Restrict new ice formation

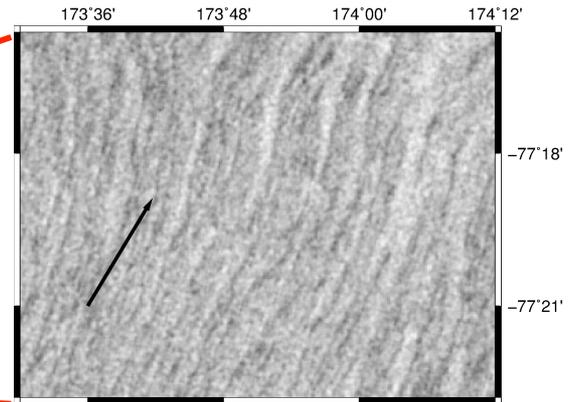
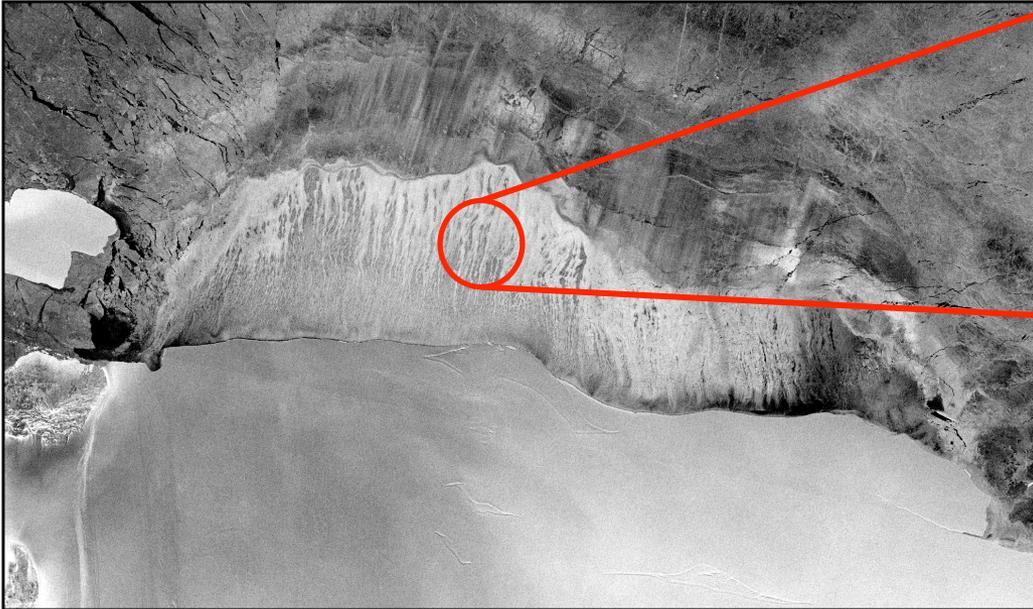
However, the state of newly formed sea ice highly depends on the condition of the ocean surface.



Turbulent sea surface condition forms **grease ice, mixture of sea ice and small frazil crystals**, which has less insulate effect because seawater is directly exposed to the cold atmosphere even after freezing begins.

Introduction

Sea ice cover controls atmosphere-ocean heat exchange



Grease ice cover is typically characterized by the **streak-structure** in satellite images when coastal polynyas develop

Sea ice models widely used in OGCMs/CGCMs can not explicitly deal with such difference of the sea ice state ,

Uncertainty in air-sea heat flux estimation, particularly in the period of active new ice formation

Frazil crystals in supercooled seawater

Surface heat loss → ocean surface is **supercooled** ($\sim 0.01\text{K}$)

→ fine **frazil crystals** precipitated → accumulate near the surface

if strong wind: **grease ice** (granular ice)

otherwise: solid ice (columnar ice)

- Drucker and Martine (2003):

Direct observation of supercooling and frazil at 20m depth by upward sonar

- Smedsrud (2001)

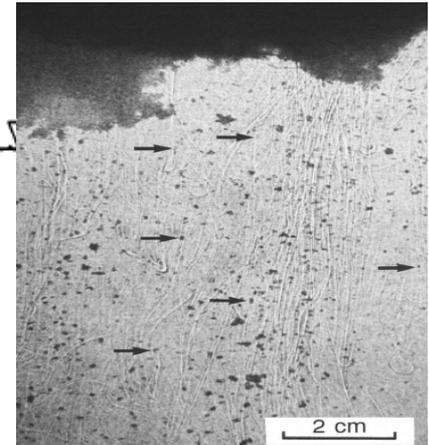
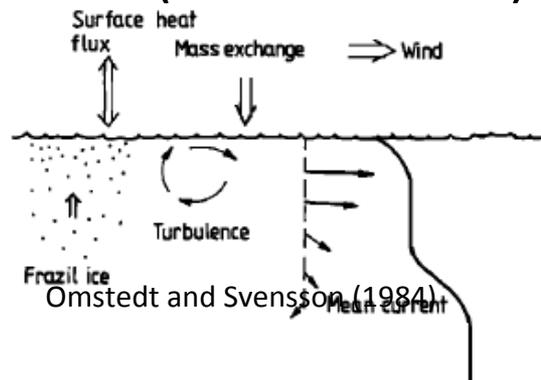
Laboratory experiments,
Frazil crystals of up to 2cm diameter

- Ushio and Wakatsuchi (1993):

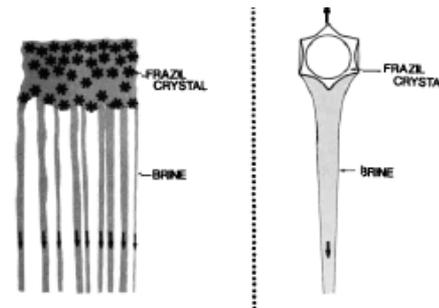
Laboratory experiments,
Visualize Frazil crystal, 0.2K supercooling.

- Bauer and Martine (1983):

Laboratory experiments,
consolidation and transformation to
grease ice.



Ushio and Wakatsuchi (1993)



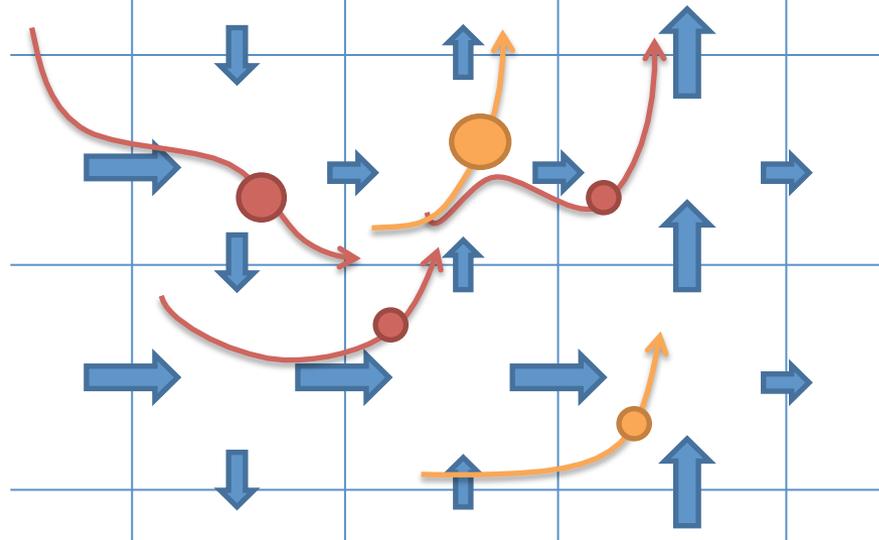
Smedsrud (2001)

Goal of the present study

- Sea ice component in GCMs does not explicitly deal with grease ice
→ **large uncertainty in the period of new ice formation**
- Previous modeling studies of frazil ice only deal with **grid-averaged quantity, assume constant crystal size**
- Explicit simulation of **frazil generation and their transition to grease ice** has not been performed yet.
- **Develop a new modeling framework for ice-ocean coupled system which deal with dynamic and thermodynamic effects of underwater frazil ice by using online Lagrangian particle tracking**
- Perform an Idealized experiment of active ice formation at polynyas in the coldest periods.
→ **Quantitatively estimate the effect of frazil ice/grease ice on the atmosphere-ocean heat exchange and net sea ice production.**

“On-line” Lagrangian Particle tracking

- Trace the location and properties (mass, rise/fall velocity etc.) of each particle (dispersive phase) **simultaneously** with the ocean model (continuous phase), **Particle-in-Cell (PIC)** type simulation
- Each particle has unique ID and we can trace their history.
→ **Particles can dynamically and thermodynamically affects on the ocean state, i.e., dispersed multi-phase flow**



We developed a **numerically efficient particle tracking system** built-in a **3D non-hydrostatic** ocean model

Dynamic coupling of ocean flow and dispersed particles

- Each particles subject to **gravity (body force)** and **pressure-gradient (surface force)**

- Buoyancy: difference between gravity and the hydrostatic pressure gradient

$$b = -mg + \rho \Delta z \delta g = -m \rho \Delta s - \rho \Delta z / \rho \Delta s g$$

- Residual of pressure gradient: **the form drag**

$$f \approx -S \rho \Delta z C_D |v - U| (v - U)$$

Cd: depends on the shape and orientation, UNKNOWN

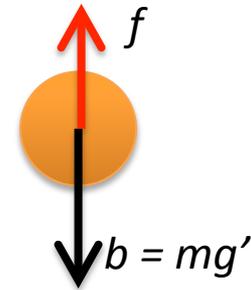
- Water phase feels sum of the reaction of drag force acts on each particle

The question is, how to estimate f (or Cd)?

- We assume all particles are in equilibrium state with terminal fall/rise velocity relative to the ocean flow s.t. buoyancy and drag-force is balanced,

$$f = -b \quad (\text{valid if particles are so small that inertia can be ignored})$$

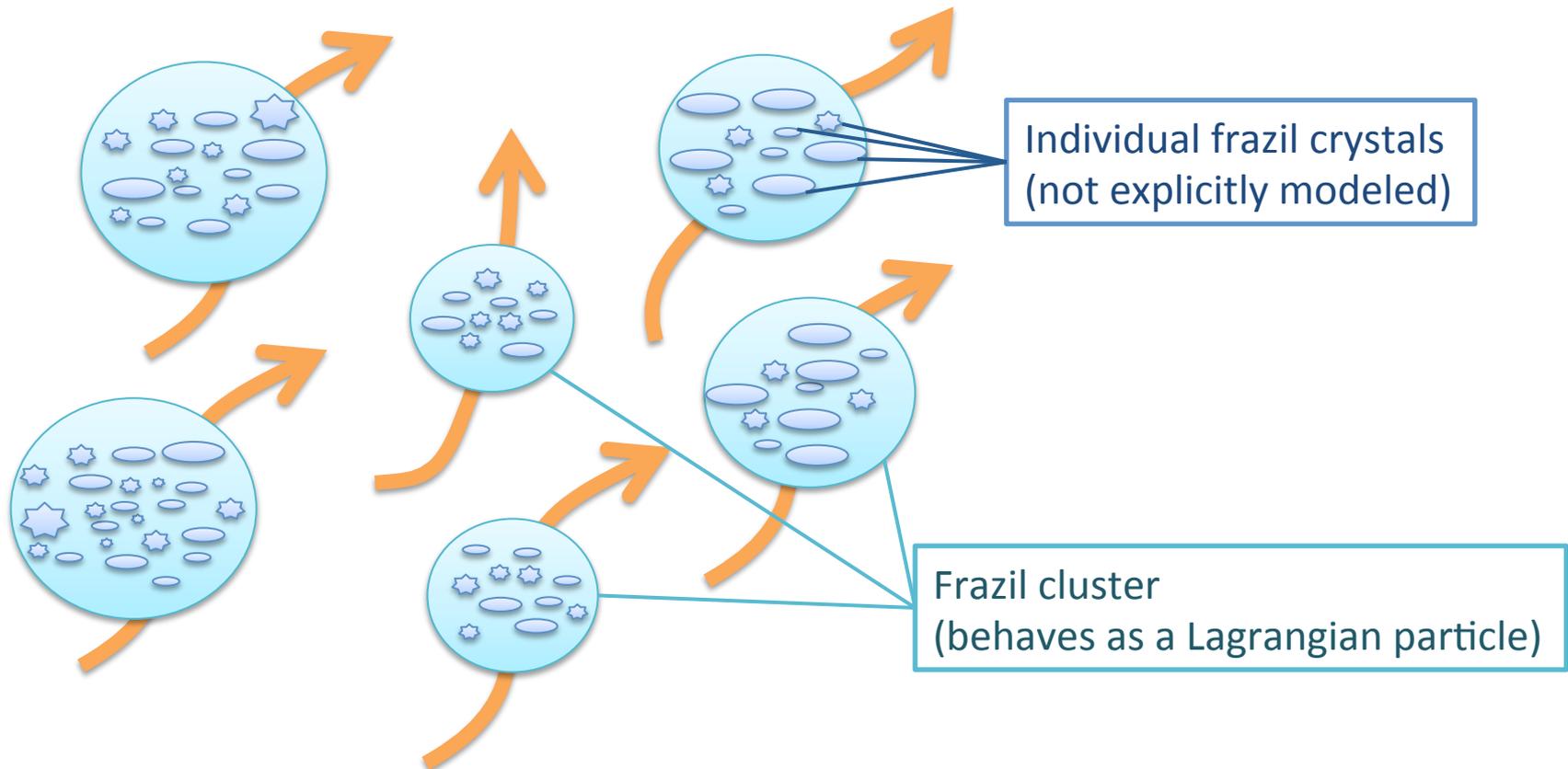
$$\begin{aligned} \rightarrow dw/dt &= -g - 1/\rho \Delta z \partial p / \partial z - 1/\rho \Delta z \sum_i \uparrow \downarrow f_i \\ &= -g - 1/\rho \Delta z \partial p / \partial z - 1/\rho \Delta z \Delta V \sum_i \uparrow \downarrow m_i \rho \Delta s - \rho \Delta z / \rho \Delta s \\ g &= -\rho \uparrow^* / \rho \Delta z \quad g - 1/\rho \Delta z \partial p / \partial z \end{aligned}$$



Dynamic effects of suspended particles yields the change of effective water density ρ^*

Modeled frazil particles

- The actual number of frazil crystals in the real ocean is countless, **impossible to simulate all of them**
 - Modeled particle as a **cluster/packet of many frazil crystals**
 - **Total ice mass** and **average size** of crystals are simulated for each particles.



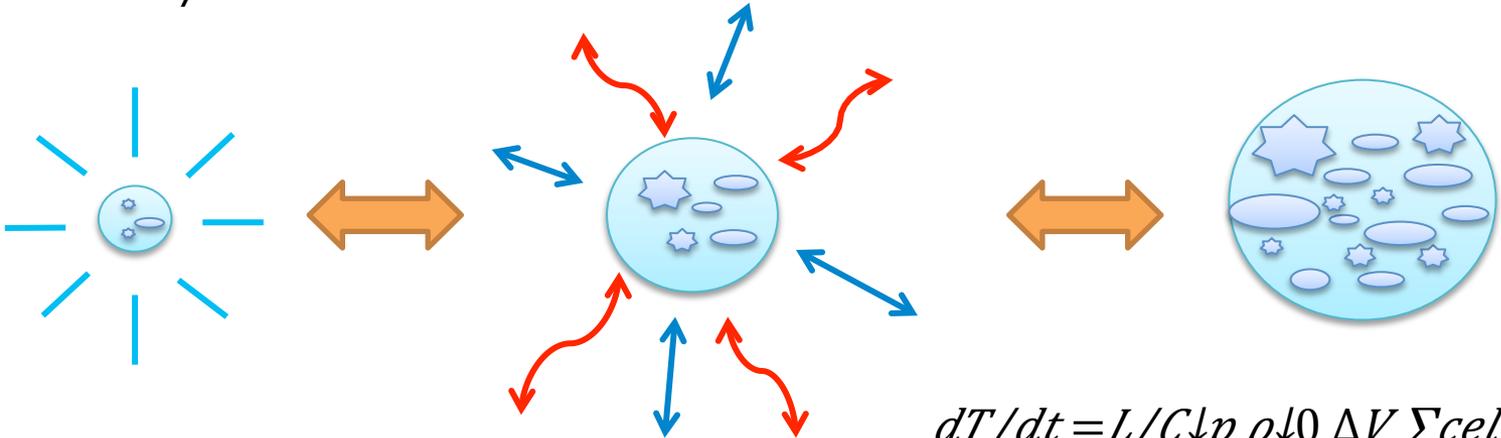
Thermodynamics

- Generate frazil particles of the minimum mass when the prognostic in-situ temperature falls below the local freezing point

(sustainable in-situ supercooling state is not allowed)

- Each particle thermodynamically grows/decays depending on the in-situ temperature **relative to the local freezing point $T_f(S, p)$**
- The rate of heat exchange depends on the mean crystal size

$$\frac{d}{dt} M_{\text{frazil}} = (T_{\text{freeze}} - T_{\text{insitu}}) C_p \rho / L \gamma^2 M_{\text{frazil}} / r_{\text{ice}}$$



Latent heat absorption/emission

$$dT/dt = L / C_p \rho \Delta V \sum_{\text{cell}} d/dt M_{\text{ice}}$$

Brine rejection/fresh water supply

$$dS/dt = S_{\text{li}} - S_{\text{li}} / \rho \Delta V \sum_{\text{cell}} d/dt M_{\text{ice}}$$

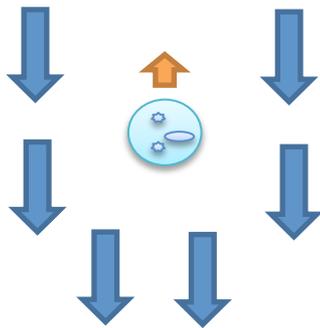
Buoyant rise velocity

- Inertia of frazil crystal are ignored, i.e., all crystals are in equilibrium with terminal buoyant rise velocity
- In the present model individual crystal is not simulated, **just parameterized by using total ice mass of each cluster.**

$$w_{\downarrow rise} = w_{\downarrow 0} M_{\downarrow frazil} / M_{\downarrow 0} \quad , \quad \text{where } w_0 = 1\text{mm/s}$$

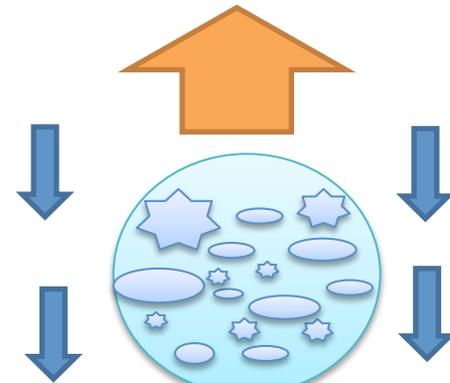
(from Omstedt and Svensson, 1984)

Small particles:



less buoyant force
→ advected by convection

Large particles:



greater buoyant force
→ float up to the surface

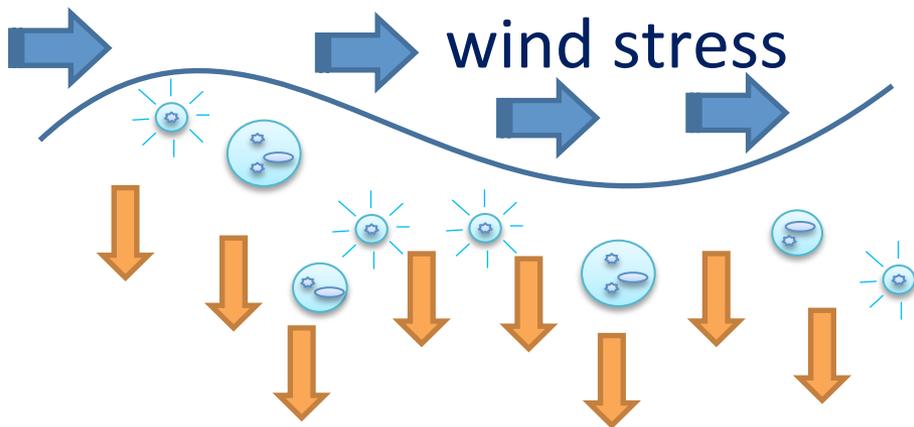
Turbulent mixing by wind stirring

- Net vertical transport of frazil particles is realized by
 - Linear interpolation of the predicted ocean current
 - + buoyant rise velocity w_{rise}
 - + **Subgrid-scale turbulent eddy transport w_{eddy}**
- Downward frazil transport increase potential energy, require energy source: Surface wind stress forcing → **SGS EKE (or TKE)**

$$\epsilon = 2\nu S_{ij} S_{ij}, \quad S_{ij} = 1/2 (\partial u_j / \partial x_i + \partial u_i / \partial x_j)$$

- The ratio of energy dissipation used to the turbulent eddy transport
 “Critical Flux Richardson Number”: $R_{f} = \frac{\sum \uparrow \rho \epsilon}{\sum \uparrow \rho g w} \approx 0.15$

efficiency of TKE → PE conversion
(from Osborn 1980)



Strong surface wind forcing
→ **downward turbulent transport**

Enhanced viscosity of slurry

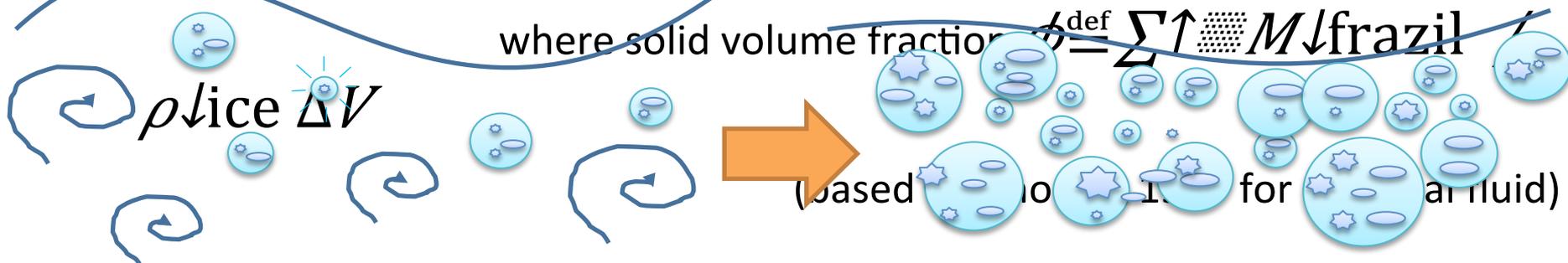
- **Grease ice:** viscous mixture of frazil crystals and sea water
 - dynamical effects is represented by **enhanced viscosity** as a function of solid mass fraction

$$\nu^* = \nu_{eddy} + \nu_{mol},$$

- Sub-grid turbulence model: Smagorinsky-type LES, $\nu_{eddy} = (C_{smag} \Delta)^2 |S|$

- Molecular viscosity is enhanced as a function of solid mass fraction of ice

$$\nu_{mol} = (1 + 2.5\phi + 10.5\phi^2 + 2.73 \times 10^{-3} e^{16.6\phi}) \times 10^{-6} \text{ m}^2/\text{s},$$



Large crystals tend to float up to the surface → **viscous grease ice**

Insulating effect of surface ice cover

- Increased solid mass fraction at the surface results in insulating effect
- Net heat flux is parameterized by the effective ice thickness:

$$Q = -\gamma \downarrow T \kappa \downarrow_{ice} / \gamma \downarrow T h \downarrow_{ice} \uparrow^* + \kappa \downarrow_{ice} (T \downarrow_{air} - T \downarrow_{surface}),$$

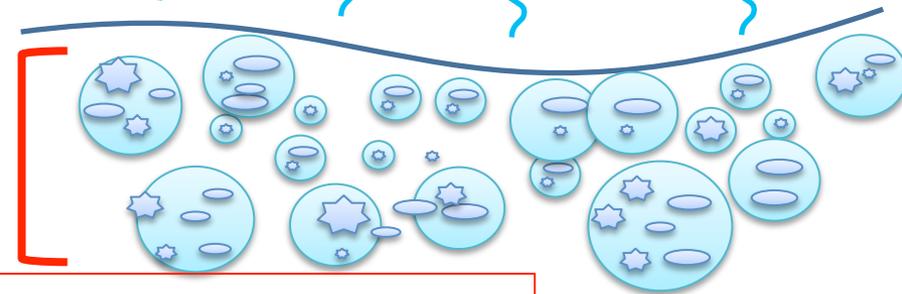
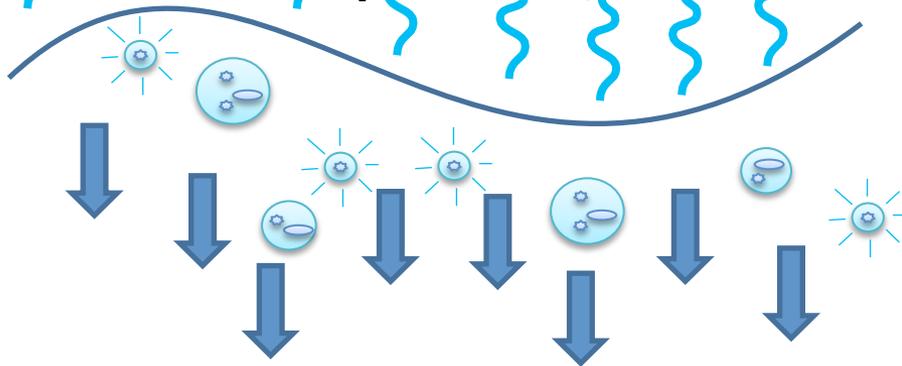
where effective ice thickness $h \downarrow_{ice} \uparrow^* \stackrel{\text{def}}{=} \int z \uparrow^{\text{ice}} \exp(-z/\delta)$

$$M \downarrow_{frazil} dz / \rho \downarrow_{ice} \Delta S$$

Greater heat flux

Less heat flux

$\gamma \downarrow T$ Haney type heat relaxation coefficient ($40 \text{ W m}^2 \text{ K}^{-1}$)

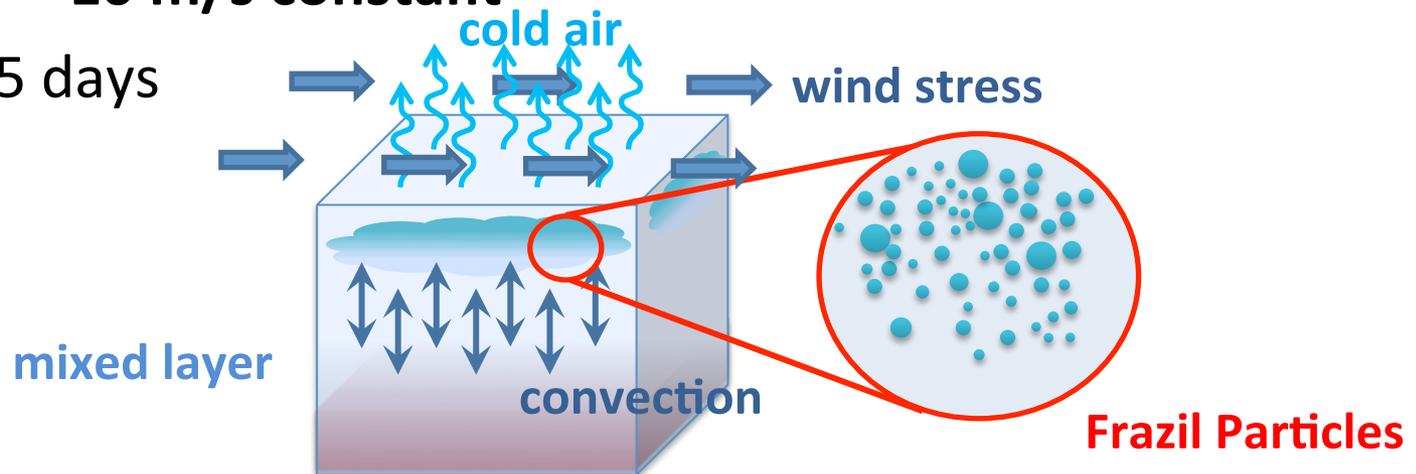


Grease ice layer $\sim O(10 \text{ cm})$

Active thermal convection
Frazil generation

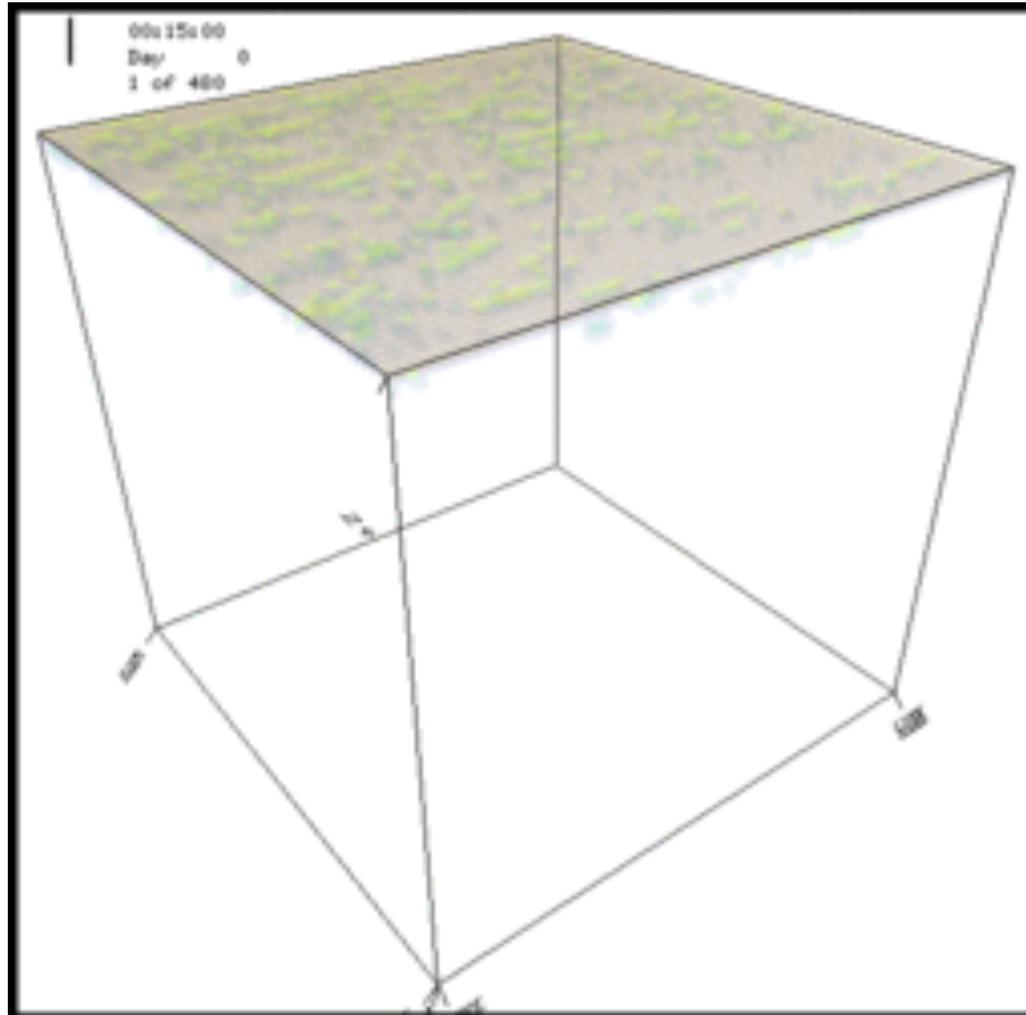
A simple idealized experiment

- Ocean component: kinaco (nonhydrostatic, Matsumura and Hasumi, 2008) + **Lagrangian frazil ice component** (developed in the present study)
- Domain: 64m x 64m x 64m, horizontally periodic boundaries.
- Resolution: 1m x 1m x 1m
- Subgrid-model: Smagorinsky-type shear-dependent LES + **molecular viscosity enhancement as a function of solid volume fraction**
- Initial condition: $\Theta = -1.6^{\circ}\text{C}$, $S = 30\text{psu}$ uniform
- Air temperature: -20°C (Up to $\sim 730\text{ W/m}^2$ heat flux at the open water)
- Wind forcing: $U = 10\text{ m/s}$ constant
- Integration for 5 days



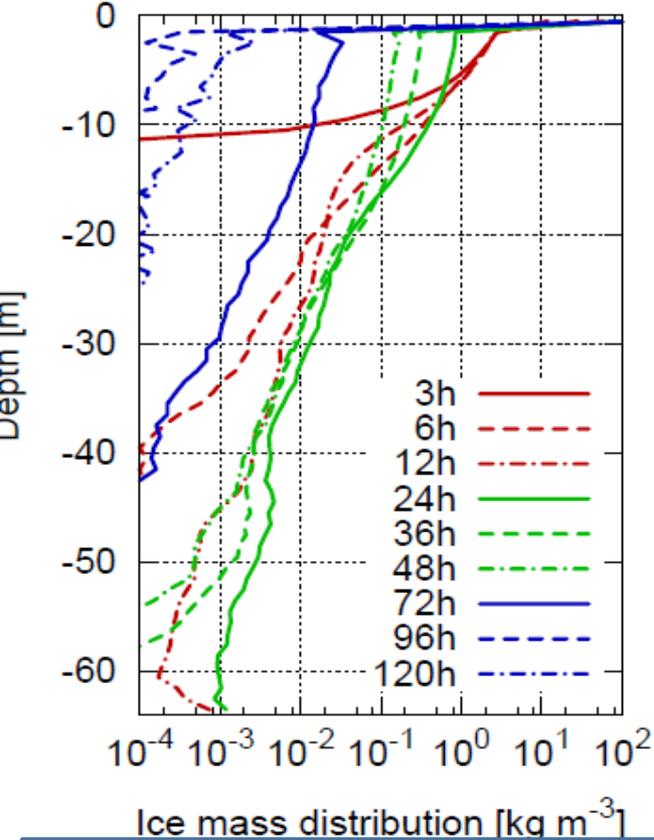
Results

Frazil distribution (log scale, blue 10^{-2} kg/m³ -- red 10^2 kg/m³)

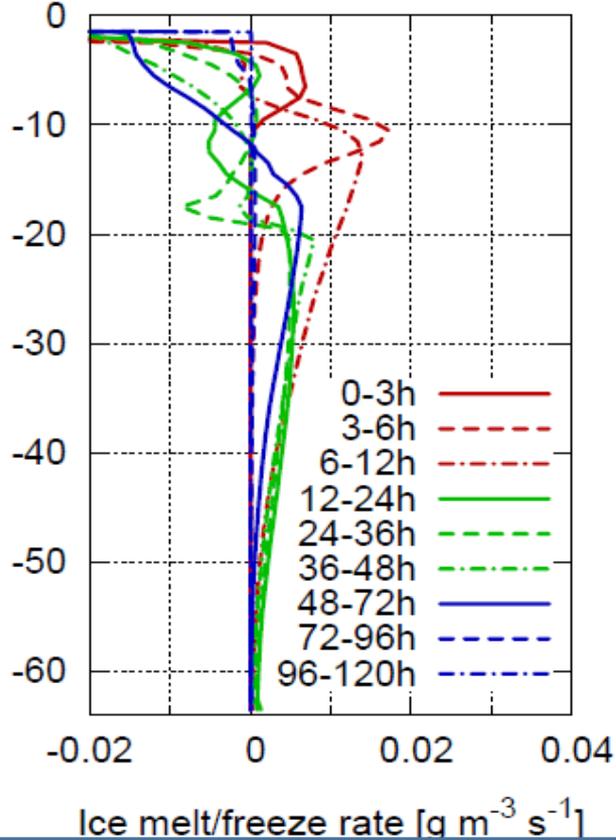


Vertical profiles

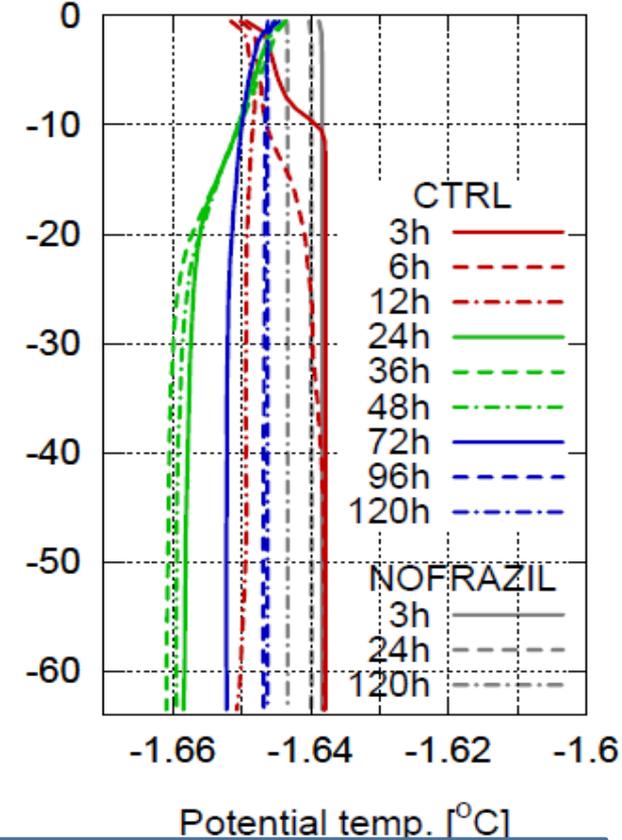
a) Frazil distribution



b) Melt/Freeze rate



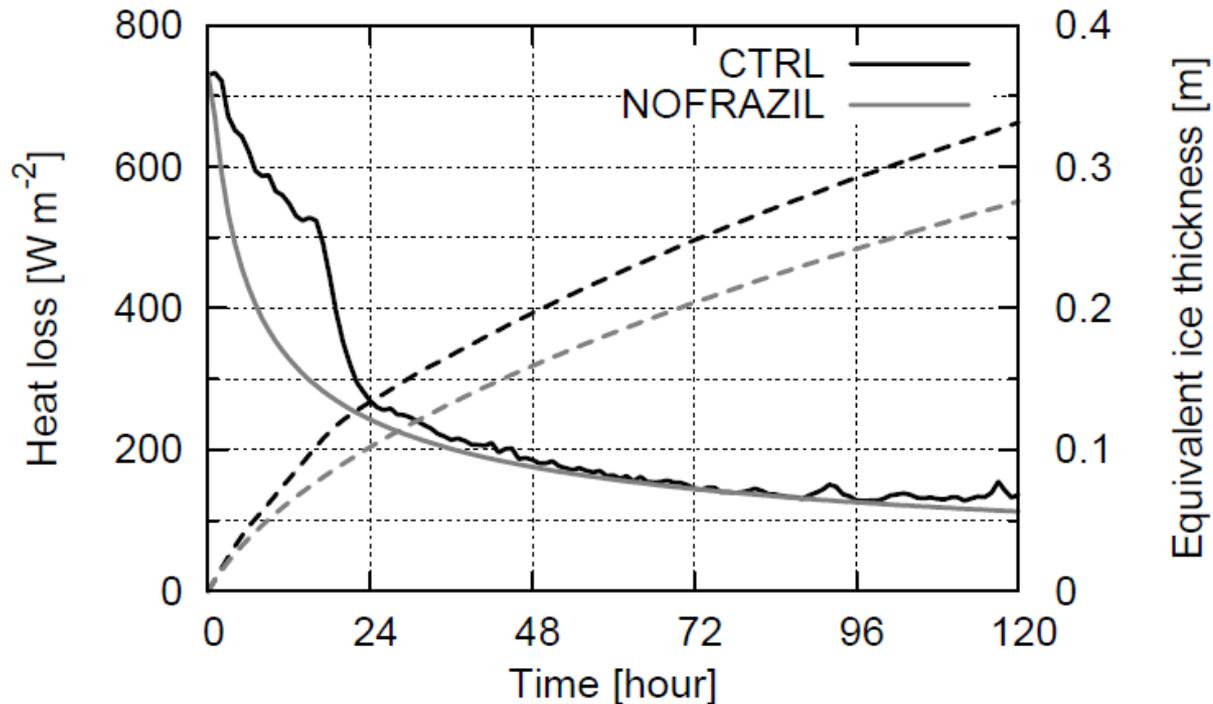
c) Potential temp.



Frazils generated at surface → transported downward by convection
→ melt at deeper level (absorb latent heat) → cool the water column
→ **potential supercooling** due to freezing point decline with depth

Surface heat flux and net ice production rate

Compare with the “0-layer” solid ice thermodynamics



Newly developed Lagrangian frazil ice model **keeps open water (high heat flux $> 500\text{W}/\text{m}^2$) relatively longer periods** than 0-layer solid ice

41% greater total heat loss and

34% greater total ice production in the initial 24 hours

both cases become almost equal after the surface is entirely covered

Idealized coastal polynya experiment

→ wind (10m/s)

Day 1 00:05

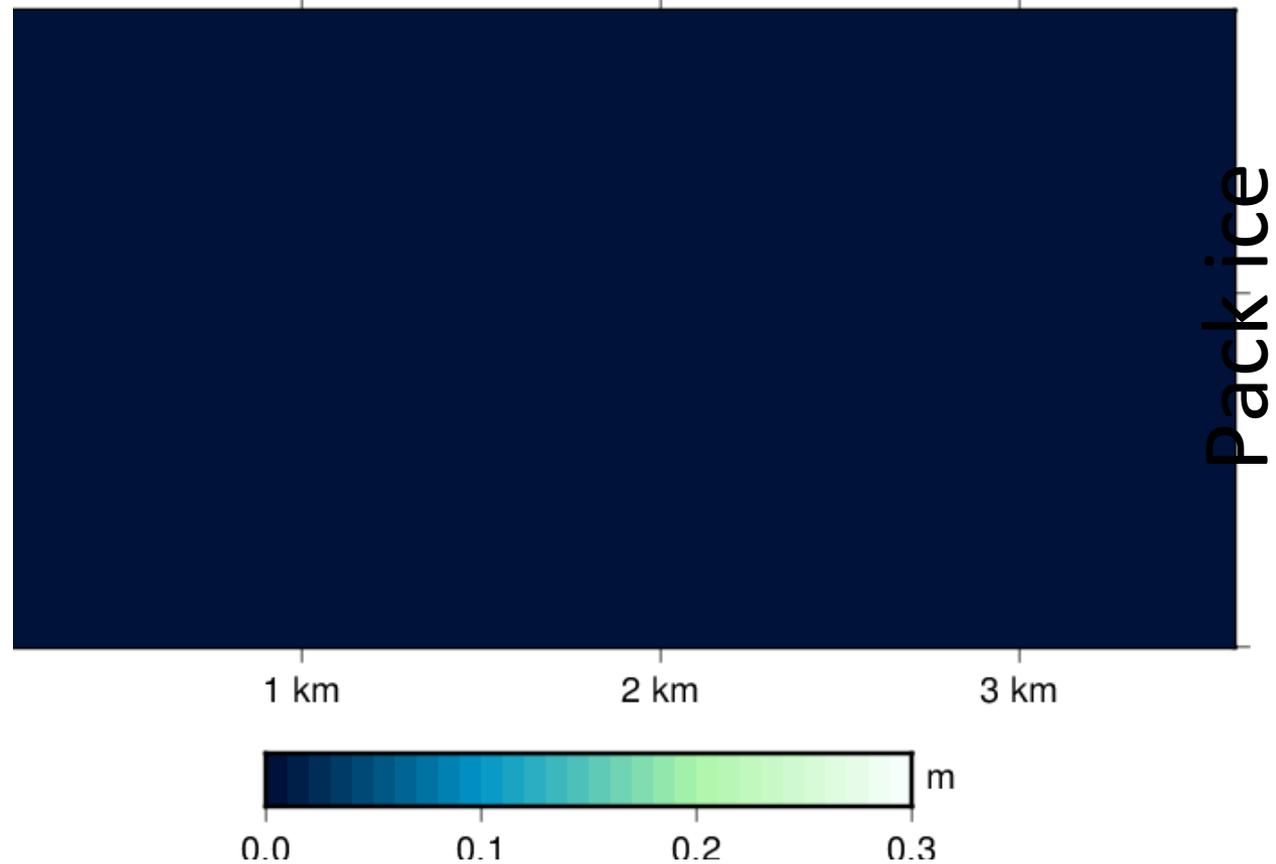
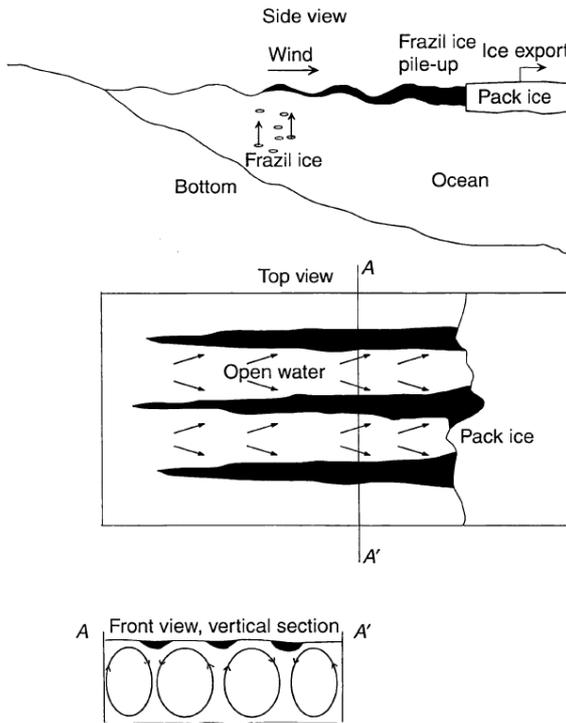
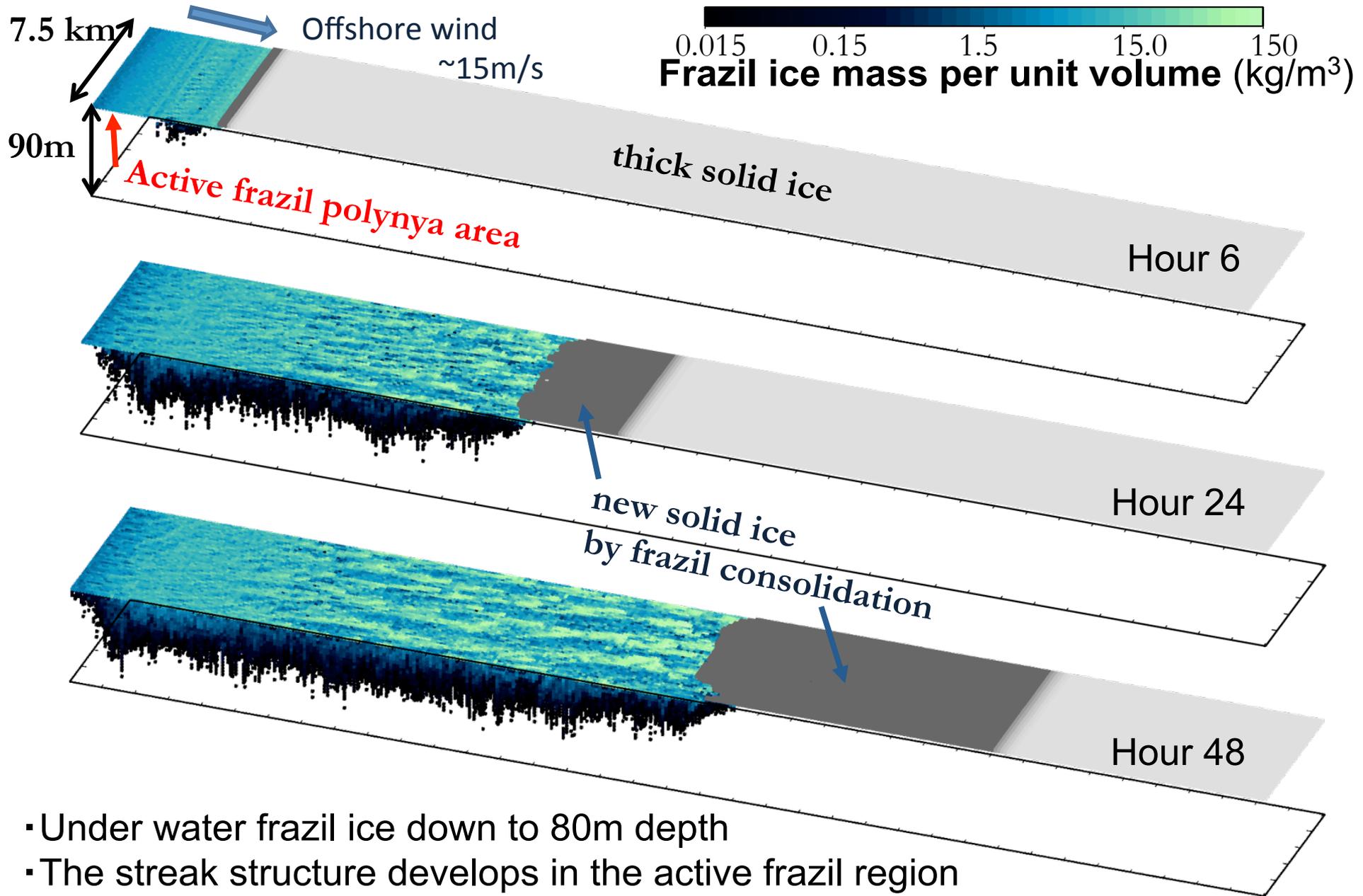
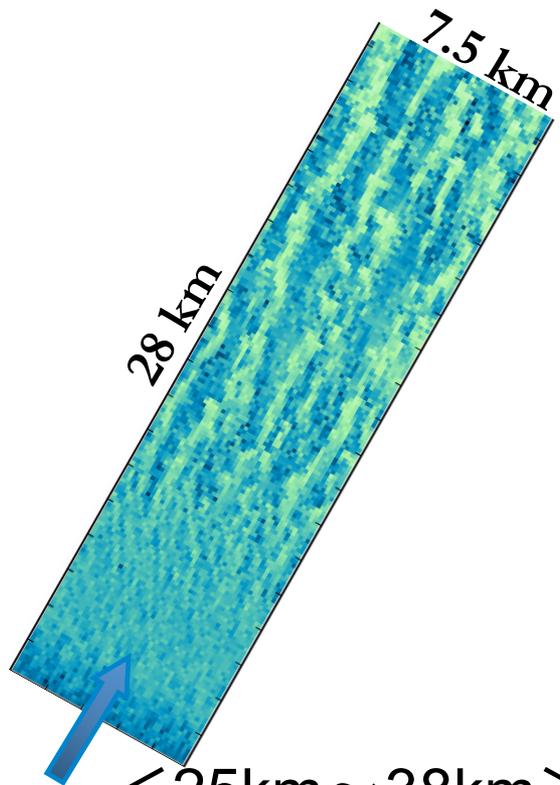
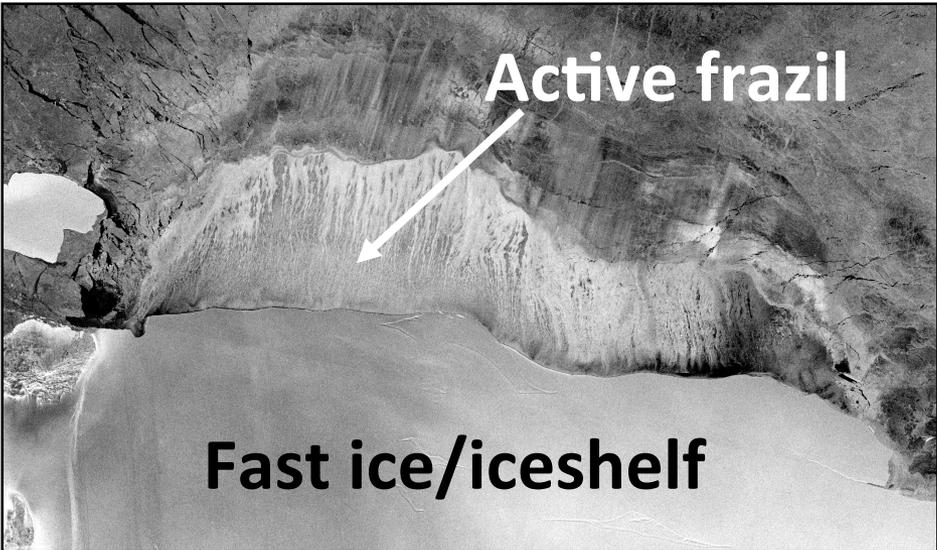


Figure 2 A schematic drawing of a coastal polynya and top and vertical views.

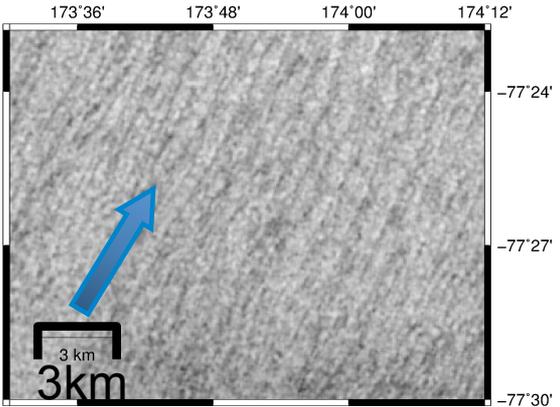
Developing polynya experiment: (by Kazuki Nakata, Ph.D. thesis)



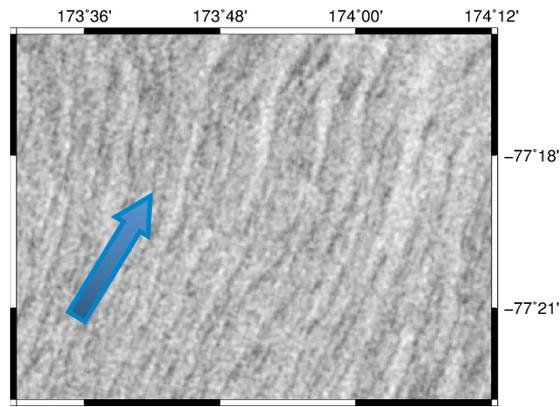
Satellite image active polynya
(day with 15 m/s offshore wind,
air temperature -17°C)



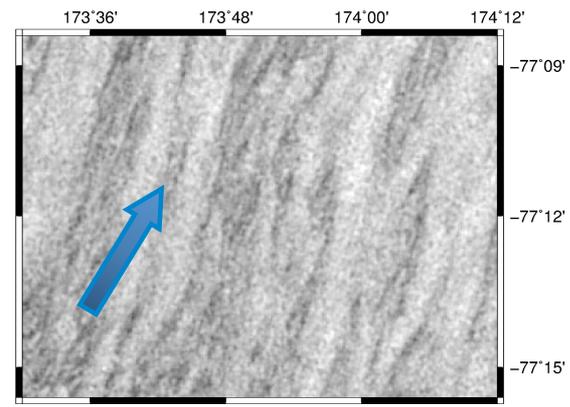
< coast ~ 13 km >



< 13 km ~ 25 km >



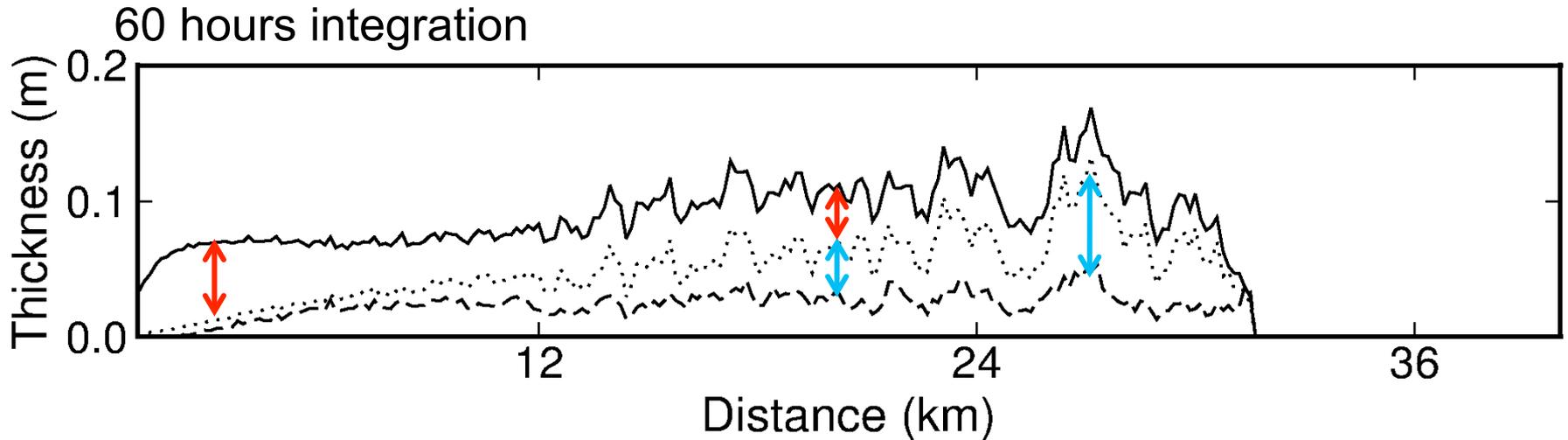
< 25 km ~ 38 km >



Modeled streaks are almost identical to the satellite image

Effective thermal ice thickness in the active frazil polynya

Thermal ice thickness \propto (net air-sea heat flux)⁻¹



- A. Solid: Equivalent ice thickness corresponds to total ice mass (incl. under water frazil)
- B. Dotted: y-averaged effective ice thickness (weighted integ. of ice mass near the surface)
- C. Dashed: simulated thermal ice thickness calculated from net heat loss in the model

A-B: Effect of downward turbulent transport of frazil

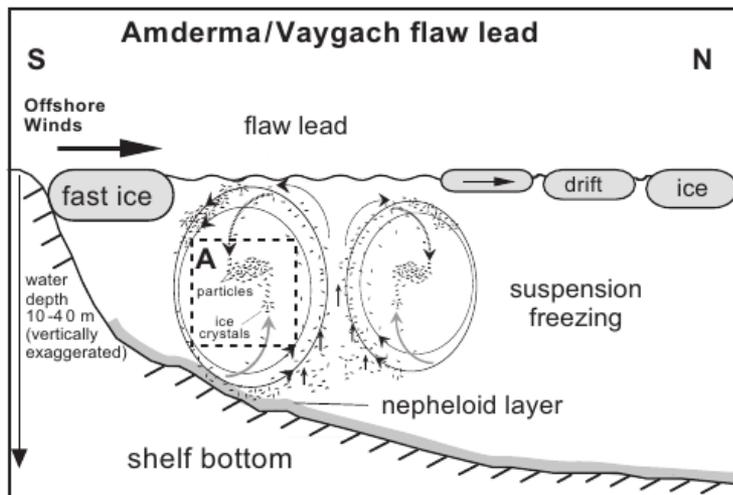
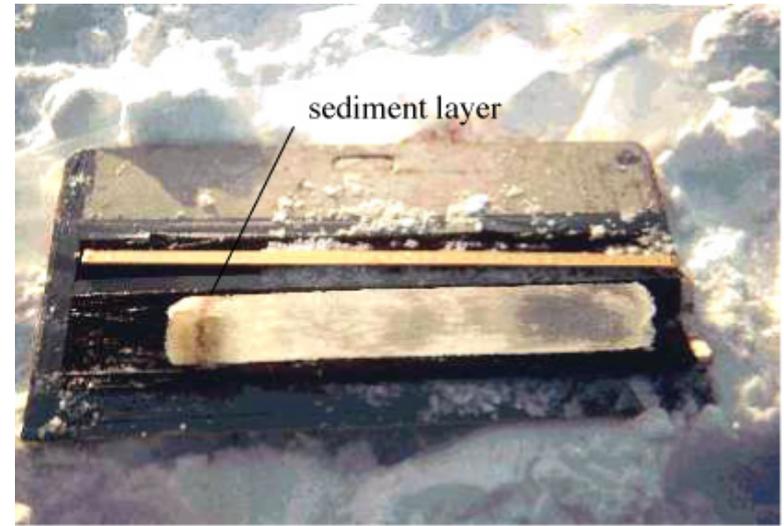
B-C: Effect of streak-structure formation

Both **turbulent transport (initial stage/near shore)** and **streak-structure (later stage/near ice edge)** contribute to the higher net ice production in the active polynya under strong wind

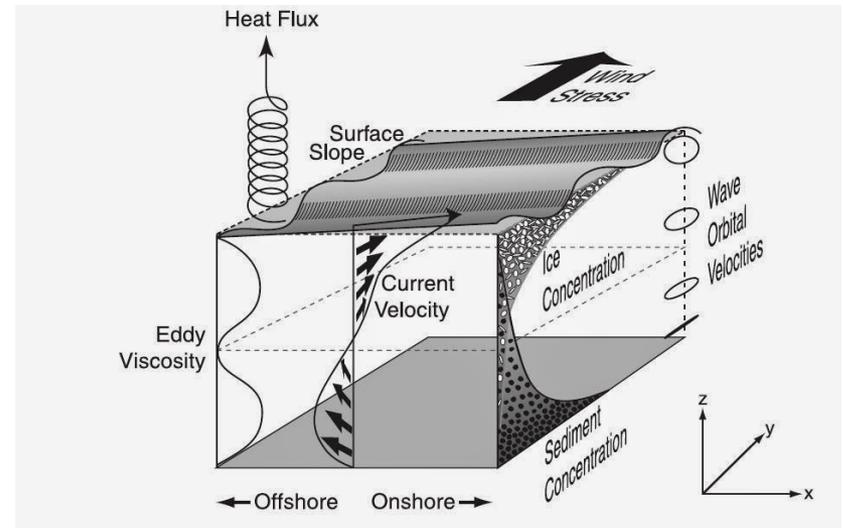
The simulated thermal thickness (< 5 cm) is quantitatively consistent with satellite (MODIS) brightness temperature in the active polynya

Sediments in Sea ice

- Sea ice (sometimes) contains a lot of **small grain sediments**
 - ✓ Surface albedo decline, can enhance melting.
 - ✓ Transport of trace elements, important on **ocean bio-geochemistry**.
- Possible origins of sediments in sea ice:
 - ✓ Dust from continents (fallen with snows).
 - ✓ **Suspended from ocean floor and entrained** (Nurnberg et al., 1994)



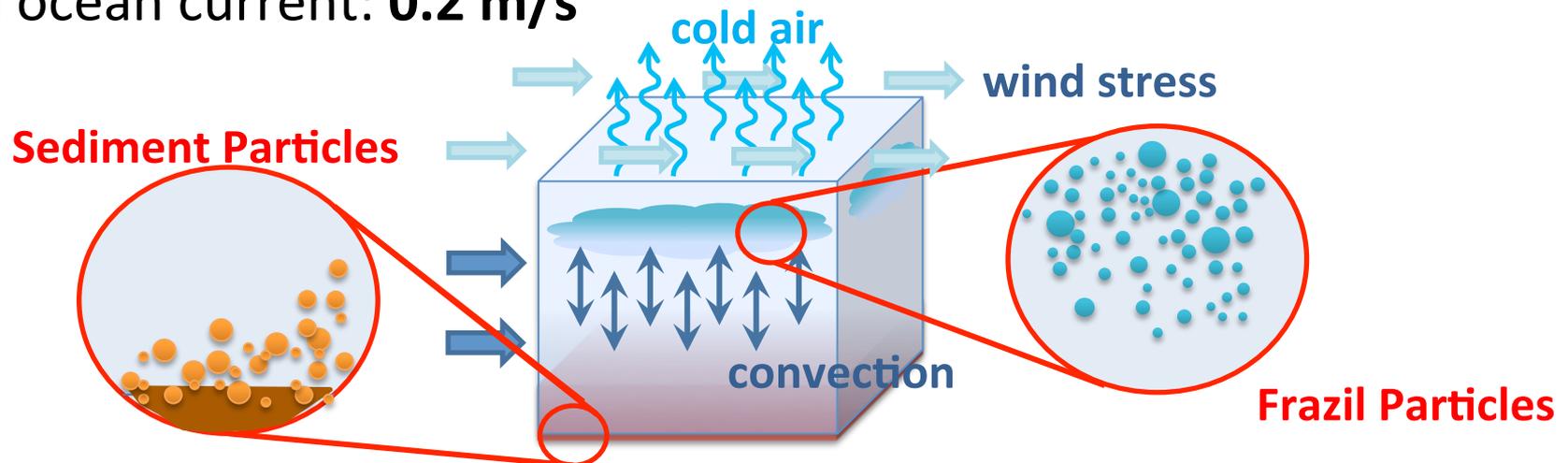
Dethlef and Kuhlmann (2009)



Sherwood et al. (2009)

A simple idealized experiment

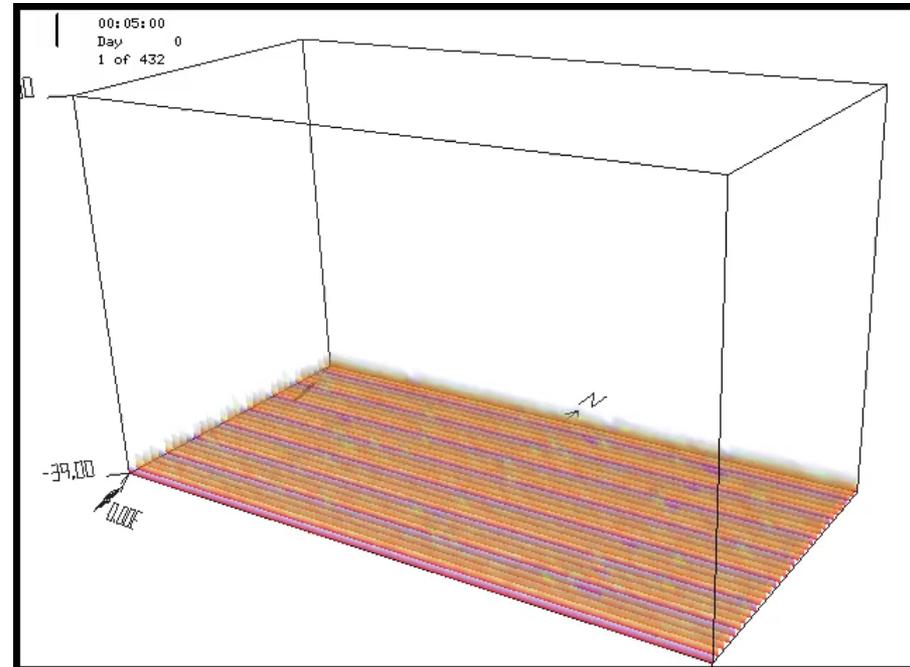
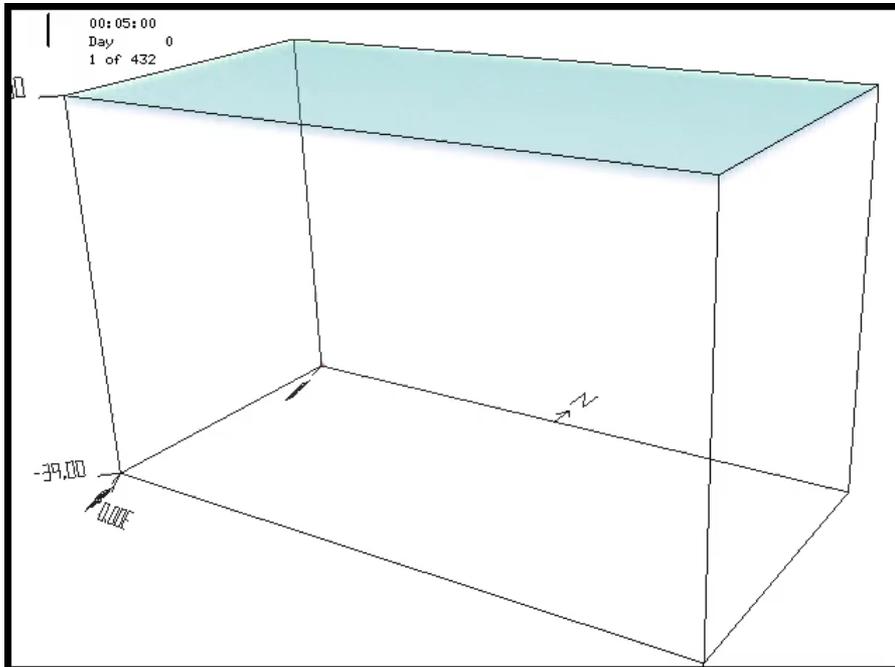
- Ocean component: kinaco (nonhydrostatic, Matsumura and Hasumi, 2008)
+ **Lagrangian frazil ice component** (developed in the present study)
- Domain: 64m x 32m x 40m, horizontally periodic boundaries.
- Resolution: 1m x 1m x 1m
- Subgrid-model: Smagorinsky-type LES, C is reduced at $z < 10\text{m}$
- Initial condition: $\theta = -1.6^\circ\text{C}$, $S = 30\text{psu}$ uniform
- Air temperature: -20°C (Up to $\sim 730\text{ W/m}^2$ heat flux at the open water)
- Wind forcing: **5 m/s**
- Initial ocean current: **0.2 m/s**



Results

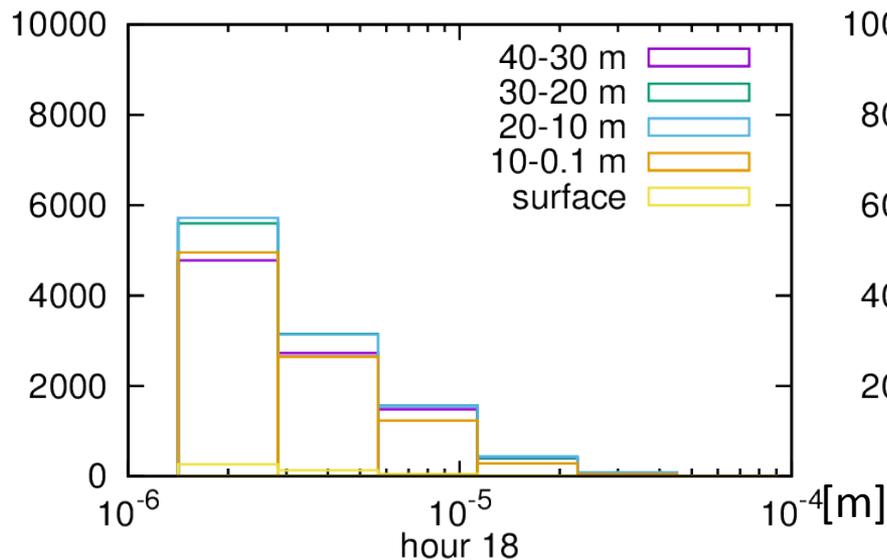
L) Frazil distribution (log scale, blue 10^{-2} kg/m³ -- red 10^2 kg/m³)

R) Sediment distribution

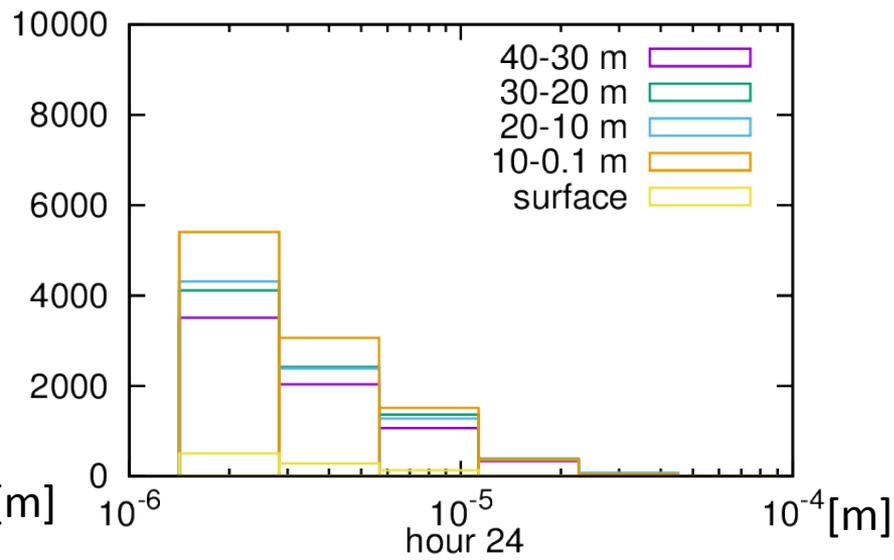


Histogram (categorized by ocean layer/diameter)

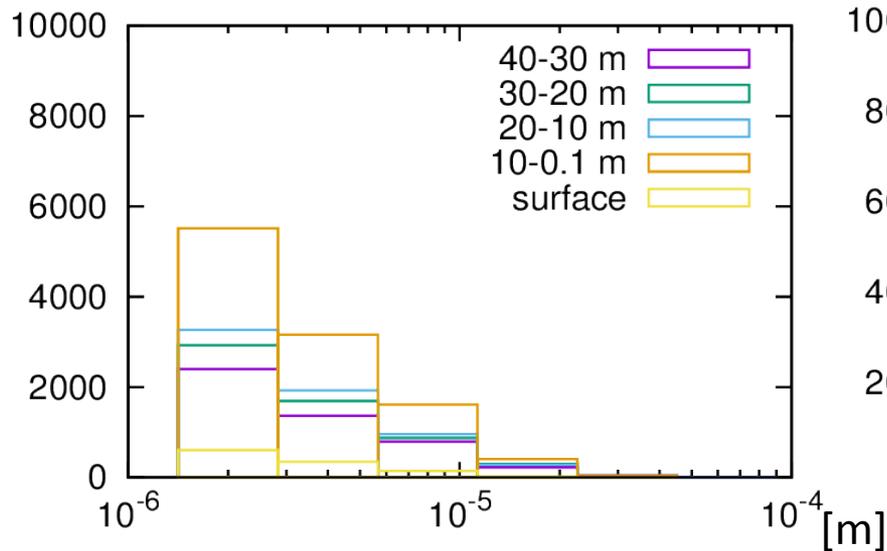
hour 06



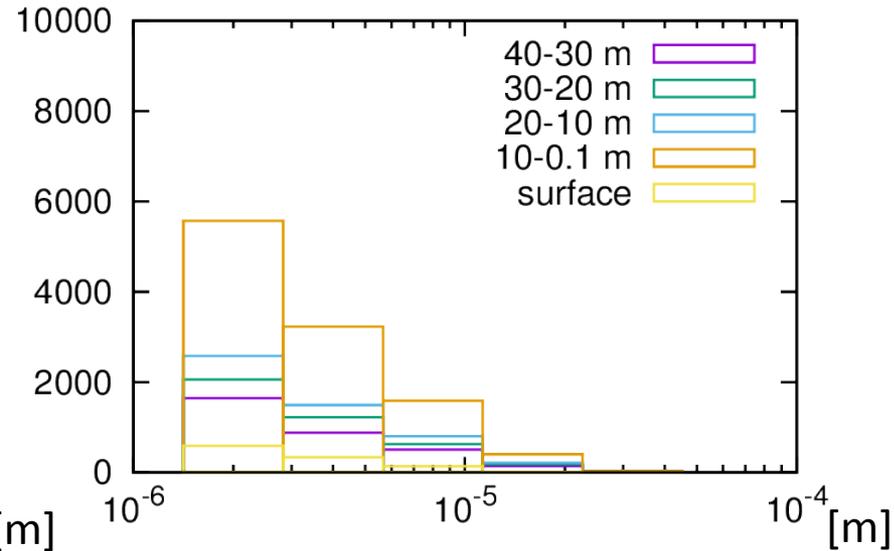
hour 12



hour 18



hour 24



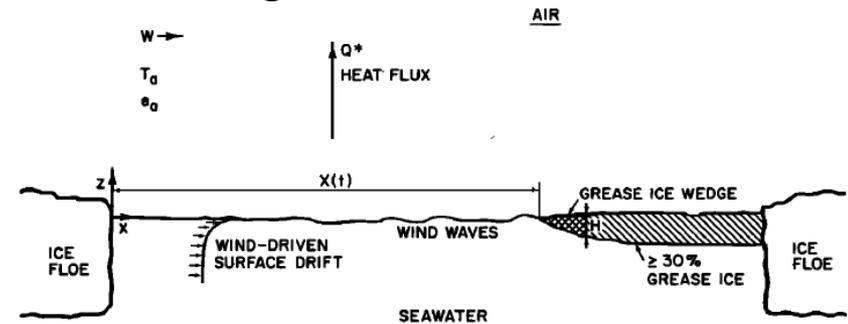
Suspension of sediments > 20 μ m is rare, consistent with observation

Summary

- A new modeling framework of **frazil ice/grease ice** by using **online Lagrangian particle tracking** is developed
- Modeled Lagrangian particle is treated as a cluster of many crystals
- Simulate thermodynamic grows of each particles
- Parameterize buoyant rise velocity, turbulent diffusion, enhanced molecular viscosity, insulating effects etc.
- **Successfully simulate the behavior of underwater frazil ice and their transition to the surface grease ice cover**
 - ✓ Vertical motion of underwater frazil ice induce **latent heat transport**
 - ✓ **Potential supercooling is realized** due to the freezing point decline with depth
 - ✓ Frazil ice model retains open water relatively longer periods and hence net heat loss is increased compared with solid ice model (**~30% greater ice production in the initial 24h**)
- Large domain polynya experiments represents streak-like structure of grease ice
- **Sediment entrainment** is a key topic of the future works

Future works

- More precise treatment of **crystal size spectrum**:
 - ✓ Very sensitive to the grows/melt rate and rise velocity
 - ✓ Should be investigated by direct observation.
- In-situ supercooling state:
 - ✓ Relaxed in a single time step (1sec.) in the present model.
 - ✓ Up to O(10) mK supercooling is observed in reality.
 - ✓ What is seeding nuclei? How many?
- **Consolidation**:
 - ✓ Transit to **solid ice (columnar grows)** when frazil volume fraction in the grease ice layer becomes sufficiently high ($\sim 30\%$).
 - ✓ Essential to the polynya opening/closing and refreezing of leads.



- Coupled with **wave dynamics model**
 - ✓ Simulate pancake ice formation
 - ✓ Frazil streaks induced by Langmuir circulation

Bauer and Martine (1983)n