Dynamics of the Atlantic meridional overturning circulation and Southern Ocean in an ocean model of intermediate complexity

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## Outline

#### 1. Introduction

2. Model

3. Solutions

4. Summary

# Background

McCreary et al. 2016. Dynamics of the Atlantic meridional overturning circulation and Southern Ocean.... Prog. Oceanogr. http://dx.doi.org/10.1016/j.pocean. 2016.01.001.

## "Great Conveyor"



#### (IPCC)



#### Meridional overturning streamfunctions:

#### Southern Ocean

#### Atlantic



Saenko & WJ Merryfield (2005).

▶ "Deep" and "Bottom" cells.

## MOC (cont'd)

What is the meridional overturning circulation (MOC)?

- Near-surface water flows poleward, getting denser (colder or saltier or both);
- sinks to great depths;
- gets less dense by internal diffusion and comes back to the sea surface or dynamically upwells to the sea surface and gets less dense by surface flux.

For the deeper cell, diffusion is critical. For the upper cell, probably it's not.

# Upwelling in the Southern Ocean



Speer et al. (2000)

- What determines the location and strength of the sinking?
- What determines the location and strength of the upwelling?

For the upper cell: How do the SO winds affect/control the MOC strength? What do mesoscale eddies do?

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 Eddy compensation: Eddy-induced transport opposing Ekman drift.



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- Eddy saturation of *M*?: Stronger winds, weaker response.

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- Eddy saturation of *M*?: Stronger winds, weaker response.
- (Eddy saturation of ACC strength?)

## Full OGCM



Saenko & WJ Merryfield (2005). Two cells.  $_{^{7/29}}$ 

# Zonally-averaged models



Stocker & Wright (1991)

## Box models



Gnanadesikan (1999) Needs empirical parameterizations and scalings.



### Various models

- ► OGCMs are too complex.
- Zonally-averaged models are still too complex and probably missing important dynamics.
- Box models are missing important dynamics.

Layer model



thermocline + intermediate = upper layer
deep + bottom = lower layer

Layer model



- Understand dynamics;
- Understand the dynamics behind the empirical parameterizations;
- Replace scalings with more precise formulae;
- Propose new formulae.

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Governing equations Start from the standard  $1\frac{1}{2}$ -layer model:

$$oldsymbol{u}_t + foldsymbol{k} imes oldsymbol{u} = -g'oldsymbol{
abla}h + oldsymbol{ abla}/h, \ h_t + oldsymbol{
abla} \cdot (holdsymbol{u}) = w_{
m e}$$

Time average:

$$f\mathbf{k} \times \overline{\mathbf{u}} = -g' \nabla \overline{h} + \tilde{\boldsymbol{\tau}} / \overline{h},$$
$$\nabla \cdot (\overline{h}\overline{\mathbf{u}}) + (\overline{h'\mathbf{u}'}) = \overline{w_{e}}.$$

GM parameterization:

$$\overline{h}\boldsymbol{u}^* \equiv \overline{h'\boldsymbol{u}'} = -\kappa_{\rm GM}\boldsymbol{\nabla}\overline{h}.$$

Governing equations (2) "Residual" velocity:  $\hat{u} \equiv \overline{u} + u^*$ . Continuity eq. is simply

 $\boldsymbol{\nabla}\cdot(\overline{h}\hat{\boldsymbol{u}})=\overline{w_{\mathrm{e}}}.$ 

Momentum eq. becomes

$$\begin{aligned} f\boldsymbol{k} \times \overline{h}\hat{\boldsymbol{u}} &= -g'\boldsymbol{\nabla}P + \tilde{\boldsymbol{\tau}} - f\boldsymbol{k} \times \kappa_{_{\mathrm{GM}}}\boldsymbol{\nabla}\overline{h} \\ &= -g'\boldsymbol{\nabla}P + \tilde{\boldsymbol{\tau}} - f\boldsymbol{k} \times \frac{\kappa_{_{\mathrm{GM}}}}{g'\overline{h}} \left(\tilde{\boldsymbol{\tau}} - f\boldsymbol{k} \times \overline{h}\overline{\boldsymbol{u}}\right) \\ &= -g'\boldsymbol{\nabla}P + \tilde{\boldsymbol{\tau}} - \frac{\nu}{f}\boldsymbol{k} \times \tilde{\boldsymbol{\tau}} - \nu\overline{h}\hat{\boldsymbol{u}} + \nu\overline{h}\boldsymbol{u}^*, \end{aligned}$$

where 
$$P \equiv g' \overline{h}^2 / 2$$
 and  $\nu \equiv \kappa_{_{GM}} f^2 / (g' \overline{h})$ .

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#### Governing equations (3) Finally,

$$f \mathbf{k} imes \mathbf{U} pprox -g' \mathbf{\nabla} P - \nu \mathbf{U} + \boldsymbol{\tau},$$
  
 $\mathbf{\nabla} \cdot \mathbf{U} = w_{e},$ 

where  $\boldsymbol{U} \equiv \overline{h\boldsymbol{u}} = \overline{h}\hat{\boldsymbol{u}}$  and  $P \equiv g'\overline{h}^2/2$ .  $\boldsymbol{U}$  is the "residual" transport and  $\nu \equiv \kappa_{\text{GM}} f^2/(g'\overline{h}) = \text{const.}$ 

$$w_{\rm e} = \begin{cases} -\gamma'(\overline{h} - h_{\rm m}) & \text{where } \overline{h} < h_{\rm m}: \text{``mixed layer'',} \\ -\gamma(\overline{h} - h_{\rm n}) & \text{at } y = y_{\rm n}: \text{``sinking'',} \\ w_{\rm d} & \text{elsewhere: diff. upwelling.} \end{cases}$$

We consider the limit  $\gamma, \gamma' \to \infty$ .

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# Model configuration



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### Numerical solution



### Atlantic: Interior solution

#### North of $y_a$ in the interior, the Sverdrup solution

$$P = P_{e} - \frac{f^{2}}{\beta} \int_{0}^{x} \mathrm{d}x \left(\frac{\tau^{x}}{f}\right)_{y}$$

is an excellent approximation.



### Atlantic: Constraints

$$P = \mathbf{P_e} - \frac{f^2}{\beta} \int_0^x dx \left(\frac{\tau^x}{f}\right)_y$$
$$\mathcal{M} = \frac{P_e - P_n}{f(y_n)}$$

Remember that  $P = g' \overline{h}^2 / 2$ .  $\implies$  If  $P_e$  is known, everything is determined.

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South of  $y_a$ , a zonally-uniform solution exists:

$$-fV = -\nu U + \tau^x, \quad fU = -P_y, \quad V_y = 0$$

because  $w_e = 0$ .

$$V = \mathcal{M}/L = \text{const.}, \quad U = \frac{f}{\nu} \left( \frac{\tau^x}{f} + \frac{\mathcal{M}}{L} \right),$$
$$P = \mathbf{P}_{\mathsf{a}} + \int_{y}^{y_{\mathsf{a}}} dy \, \frac{f^2}{\nu} \left( \frac{\tau^x}{f} + \frac{\mathcal{M}}{L} \right).$$

How to determine  $\mathcal{M}$  (or *V*) in the SO? Note that

$$U = -rac{P_y}{f} = -rac{g'}{f}\overline{h}\,\overline{h}_y = rac{g'}{f}\overline{h}rac{V^*}{\kappa_{_{\mathrm{GM}}}} = rac{f}{
u}V^*.$$

Therefore

$$V = \frac{\nu}{f}U - \frac{\tau^x}{f} = V^* - \frac{\tau^x}{f}$$

as expected!

 $h_y$  can be discontinuous at y'. We in fact included  $\rho_y$  and parameterized  $V^*$  due to mixed-layer (submesoscale) eddies. But we concluded  $V^* \simeq 0$  when  $h_{\rm m}$  is small.

Therefore,  $V = \mathcal{M}/L \simeq -\tau^x/f$ at y'.  $h_{y}$  can be discontinuous at y'. We in fact

included  $\rho_y$  and parameterized  $V^*$  due to mixed-layer (submesoscale) eddies. But we concluded  $V^* \simeq 0$  when  $h_m$  is small.

## Southern Ocean: Outcrop Is y' fixed?

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## Southern Ocean: Outcrop Is y' fixed? No!



Some authors fix y', depriving the system of one deg. of freedom  $\rightarrow$  letting  $V^*$  a free parameter instead!

Southern Ocean: Constraints So, y' is a free parameter in the SO solution.  $y' \Rightarrow \mathcal{M}/L = -\tau^x(y')/f(y')$  $\Rightarrow q' h_m^2/2 = \overline{P(q')}$  $P = P_{a} + \int_{u}^{y_{a}} dy \frac{f^{2}}{\nu} \left(\frac{\tau^{x}}{f} + \frac{\mathcal{M}}{L}\right)$  $\Rightarrow P_a$ .

Then, the solution is determined:

$$V = \mathcal{M}/L = \text{const.}, \quad U(y) = \frac{f}{\nu} \left(\frac{\tau^x}{f} + \frac{\mathcal{M}}{L}\right),$$
$$P(y) = P_a + \int_y^{y_a} dy \, \frac{f^2}{\nu} \left(\frac{\tau^x}{f} + \frac{\mathcal{M}}{L}\right).$$

# Zonal boundary layer



Solve for the zonal boundary layer.

# Zonal boundary layer



Solve for the zonal boundary layer. After a lot of algebra,  $P_{e} - P_{a} = \Pi(\nu, \mathcal{M}, \tau^{x}(y_{a}), \tau^{x}_{y}(y_{a}^{+}), \tau^{x}_{yy}(y_{a}^{+})).$ 

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## Integral constraints

- Sinking:  $\mathcal{M} = F(P_e)$ .
- Upwelling:  $\mathcal{M} = -L \tau^x(y')/f(y')$ .
- Outcrop:  $y' = Y[P_a, \mathcal{M}, \nu, \tau^x(y)].$
- ► Zon. bndry layer:  $P_{e} - P_{a} = \Pi(\nu, \mathcal{M}, \tau^{x}(y_{a}), \tau^{x}_{y}(y_{a}^{+}), \tau^{x}_{yy}(y_{a}^{+}))$

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 $\Rightarrow \mathcal{M}, y', P_{e} = \text{func. of } [\tau^{x}(y), \nu, L].$ 

# Impacts of $\nu$



• Location of outcrop (y').

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## Impacts of $\nu$



- ► Location of outcrop (*y*′).
- Outcrop determines *M*.
   *M* decreases only because outcrop shifts southward.



#### • Location of outcrop (y').

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- ► Location of outcrop (*y*′).
- ► "Eddy compensation": At y',  $\mathcal{M} \approx -\tau^x/f$ ,  $V^* \approx 0$ . But, at  $y_a$ ,  $|\tau^x/f| > \mathcal{M}$ , the difference being  $LV^*$ .



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► "Strength of ACC":  

$$\overline{U}^{x} = -\overline{P}_{y}^{x}/f = (\tau^{x} - |f|\mathcal{M}/L)/\nu.$$



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- ► "Eddy compensation": At y',  $\mathcal{M} \approx -\tau^x/f$ ,  $V^* \approx 0$ . But, at  $y_a$ ,  $|\tau^x/f| > \mathcal{M}$ , the difference being  $LV^*$ .
- ► "Strength of ACC":  $\overline{U}^x = -\overline{P}^x_y/f = (\tau^x - |f|\mathcal{M}/L)/\nu.$
- "Eddy saturation": If  $\nu \propto (\tau^x)^n, \dots$

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## Summary

#### • $\mathcal{M} = \text{Ekman drift at } y'$ .

• "Eddy compensation" =  $V_{ek}(y_a) - V_{ek}(y')$ .

► V\* (eddy-induced transport) weakens M through poleward shift of y'.

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- $\mathcal{M} = \text{Ekman drift at } y'$ .
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  - ► V\* (eddy-induced transport) weakens M through poleward shift of y'.
- ► The ACC strength depends weakly on *τ* primarily because of *M*.
- "Eddy saturation" can be parameterized by  $\nu \propto \tau^{\alpha}$ .

# Extra slides

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### Parameterization of sinking

- Present study:  $w_e = -\gamma (P P_n)$  $\Rightarrow \mathcal{M} = (P_e - P_n)/f.$
- A box ocean: M ≈ 0.8P<sub>e</sub>/f (Schloesser et al. 2014).

Generally,  $P_a$  is smaller in the latter.  $\Rightarrow$  larger  $\mathcal{M}$  (y' shifting north) and smaller U in ACC (smaller pressure gradient across ACC).