

サイズ分布のある粒子からなる ダストアグリゲイトの衝突シミュレーション

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Background

Collisional growth of dust
($< \mu\text{m}$)



Planetesimal formation
($> \text{km}$)

Structure evolution of dust aggregates in protoplanetary disks:

- ✓ When and how are aggregates compressed and/or disrupted ?
- ✓ Can dust aggregates grow through collisions?



Numerical simulation of dust aggregate collisions!

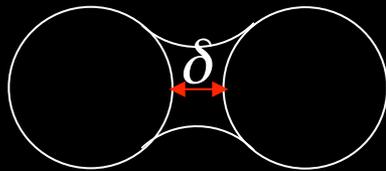
Grain interaction model

Johnson, Kendall and Roberts (1971)
 Johnson (1987), Chokshi et al. (1993)
 Dominik and Tielens (1995,96)
 Wada et al. (2007)

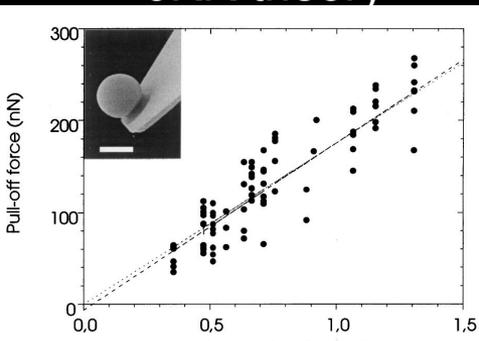


Elastic spheres having surface energy

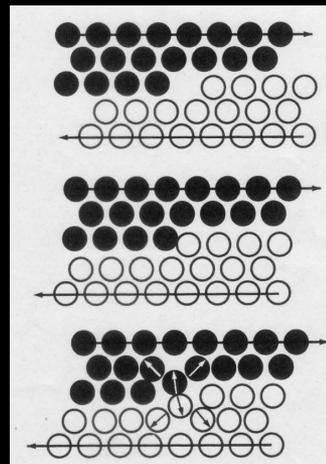
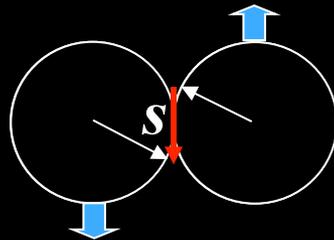
Normal



JKR theory

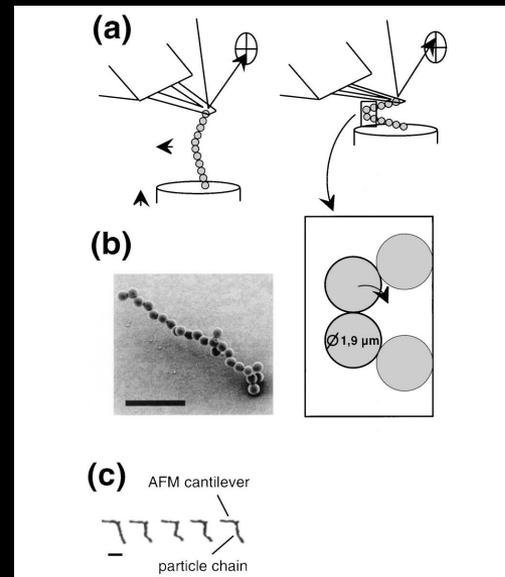
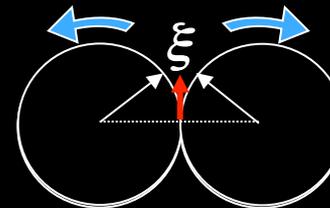


Sliding



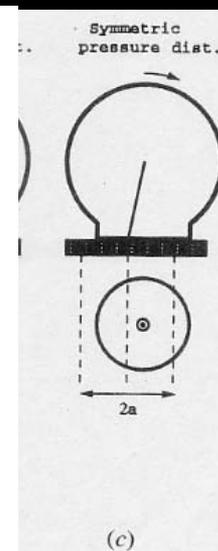
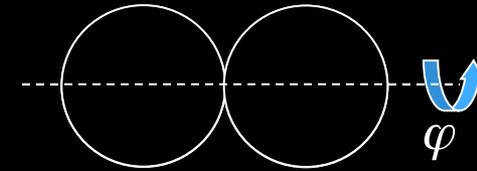
(Dominik & Tielens 1996)

rolling



(Heim et al. 1999)

twisting



(Dominik & Tielens 1995)

Critical sticking velocity:
 exp. ~ 10 × theo. !?
 (Poppe et al. 2000)

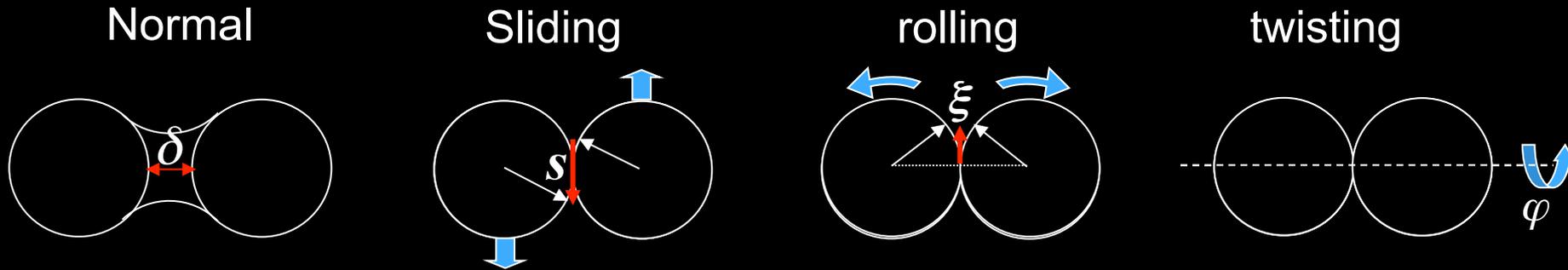
JKR and rolling resistance have been tested with experiments using ~1 μm SiO₂ particles. (Heim et al. 1999; Poppe et al. 2000; Blum & Wurm 2000)

Grain interaction model

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Elastic spheres having surface energy



Contact & Separation

$s, \xi, \varphi >$ critical displacements

→ Energy dissipation

- Critical slide $s_{crit} \sim 1.5 \text{ \AA}$ (for 0.2 \mu m quartz)
- Critical roll $\xi_{crit} \sim 2 \text{ \AA}$ (or $\sim 30 \text{ \AA}$ (Heim et al., 1999))
- Critical twist $\varphi_{crit} \sim 1^\circ$

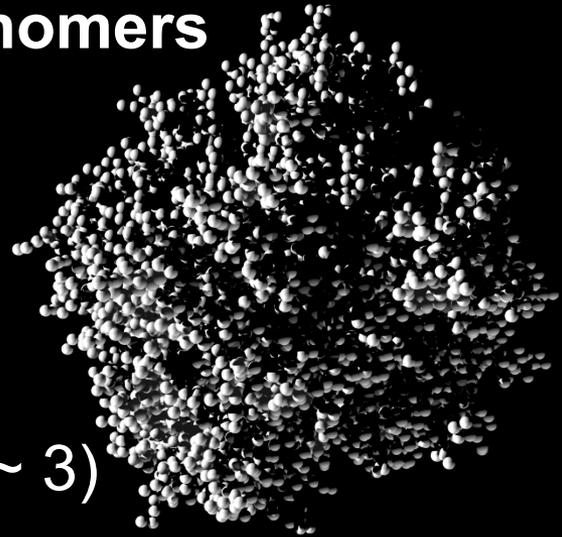
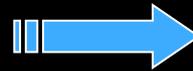
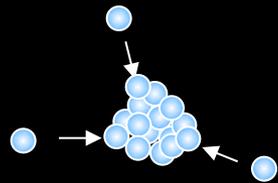
E_{break} : Energy to break a contact

E_{roll} : Energy to roll a pair of grains by 90°

Ballistic Particle-Cluster Aggregation (BPCA)



- Formed by one-by-one sticking of monomers



- **Compact** structure (fractal dimension ~ 3)

Dust is expected to be compact

- at high velocity collisions causing their disruption

Collisions of BPCA clusters

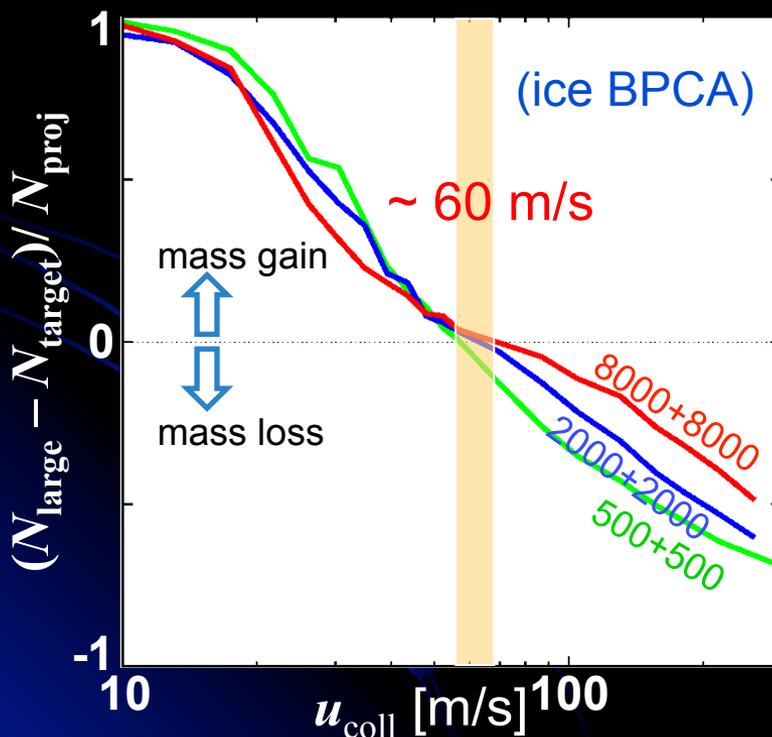
→ implication for growth and disruption of dust

Motivation

Collision velocity of dust in protoplanetary disks < several 10 m/s !
 e.g., < ~ 50 m/s (Hayashi model, without turbulence)



Is it possible for dust to grow through collisions ?



Possible for ice dust aggregates composed of particles with the same radius of $0.1 \mu\text{m}$

But for silicate dust?

$$u_{\text{coll}} \text{ for silicate} = 0.1 \times u_{\text{coll}} \text{ for ice}$$

What if size-distribution of constituent particles?

Particle size-distribution



Interstellar dust grains:

$$r = \sim 0.025 - 0.25 \mu\text{m}$$

Power-law with an exponent of -3.3 to -3.6

from interstellar extinction (Mathis, Rumpl, & Nordsieck 1977)

Interaction b/w different-sized particles

- Connections become strong for small particles.

Critical collision velocity for sticking of two monomers

$$\frac{1}{2} \mu v_c^2 = E_{break} = 1.5 F_c \delta_c \propto R^{\frac{4}{3}}$$



$$v_c \sim \sqrt{\frac{F_c \delta_c}{\mu}} \propto R^{-\frac{5}{6}}$$

v_c increases with decreasing reduced radius R .

μ : Reduced mass, F_c : Separation force, δ_c : Compression (separation) length

- But small particles make aggregates weak?

Energy for catastrophic disruption $E_c \sim 10 n_k E_{break} \propto n_k R^{4/3}$

n_k : Number of contacts



$$\frac{E_{c,L}}{E_{c,S}} \sim \frac{2 \times R_L^{4/3}}{4 \times R_S^{4/3}} \approx 10 \left(\frac{R_L / R_S}{10} \right)^{4/3}$$

Objective



Do collisions of aggregates composed of particles with a size distribution encourage dust growth?

Simulations of collisions between BPCAs composed of **particles with various size distributions**.



✓ Growth efficiency: $f = (M_{\text{large}} - M_{\text{target}}) / M_{\text{proj}}$

Critical collision velocity for disruption of aggregates

$$u_{\text{coll}} \text{ at } f = 0$$

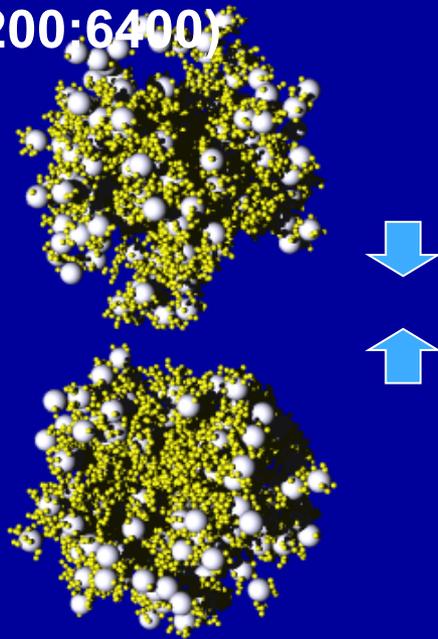
Initial Conditions and Parameters

Head-on collisions of BPCA clusters with the same size

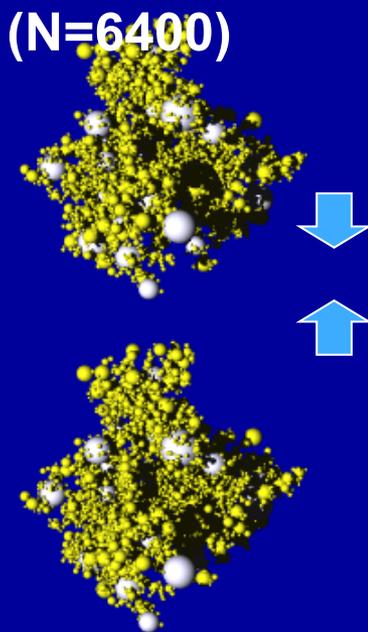
- Particle size distribution $n(r)dr \propto r^{-3.5} dr$

- $r = 0.1\mu\text{m} \times 100, 0.025\mu\text{m} \times 3200$ (binary: total mass = 0.1×150)
- $r = 0.1\mu\text{m} \times 200, 0.025\mu\text{m} \times 6400$ (binary: total mass = 0.1×300)
- $r = 0.2 - 0.025\mu\text{m}, N=6600$ (continuous: total mass = 0.1×201.6)

Bimodal (200:6400)



Continuous (N=6400)



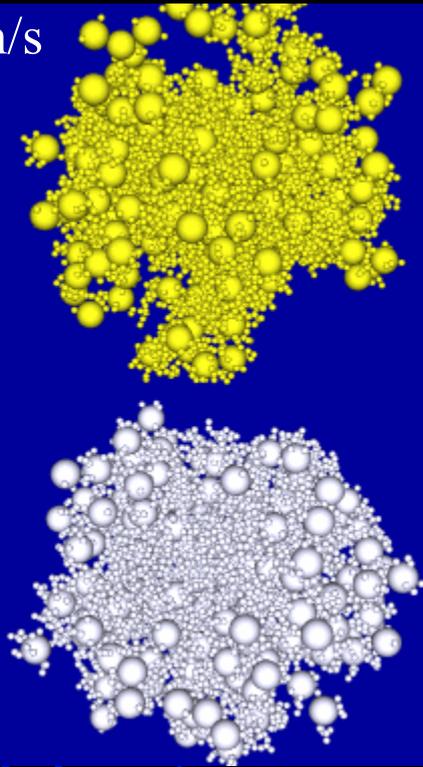
✓ Ice ($E = 7.0 \cdot 10^{10}$ Pa, $\nu = 0.25$, $\gamma = 100$ mJ/m²), critical rolling displace. $\xi_{\text{crit}} = 8\text{\AA}$

✓ Collision velocity $u_{\text{coll}} = 20 - 700$ m/s

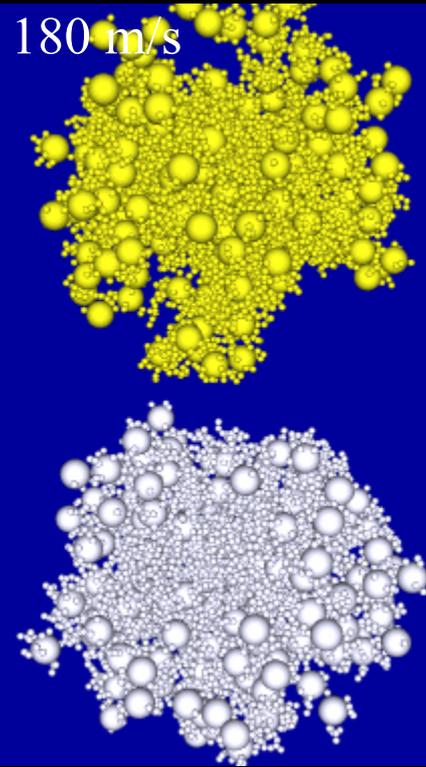
Examples of simulations

- $r=0.1\mu\text{m}\times 200$, $0.025\mu\text{m}\times 6400$ (binary: total mass= 0.1×300)

$u_{\text{coll}} = 55.3 \text{ m/s}$



$u_{\text{coll}} = 180 \text{ m/s}$



No.11

8000 : 8000

$b = 0$

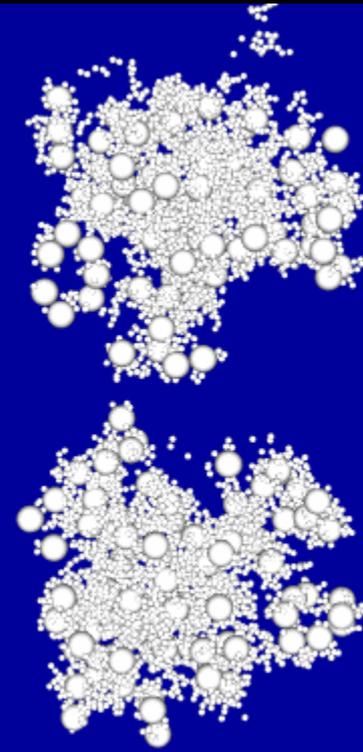
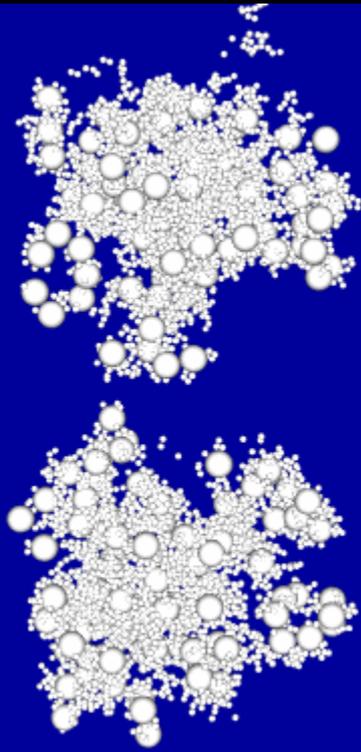


$u_{\text{coll}} = 52 \text{ m/s}$

No.20

Examples of simulations

- $r=0.1\mu\text{m}\times 200$, $0.025\mu\text{m}\times 6400$ (binary: total mass= 0.1×300)



No.11

8000 : 8000

$b = 0$



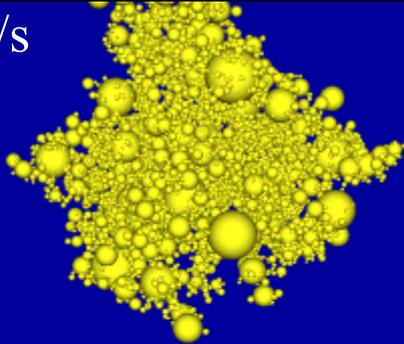
$u_{\text{coll}} = 52 \text{ m/s}$

No.20

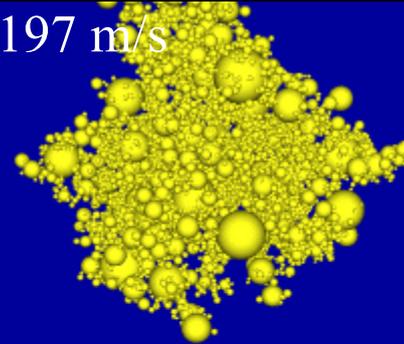
Examples of simulations

- $r=0.2\mu\text{m} - 0.025\mu\text{m}$ $N=6600$ (continuous: total mass= 0.1×201.6)

$u_{\text{coll}} = 49.3 \text{ m/s}$



$u_{\text{coll}} = 197 \text{ m/s}$



No.09

8000 : 8000

$b = 0$



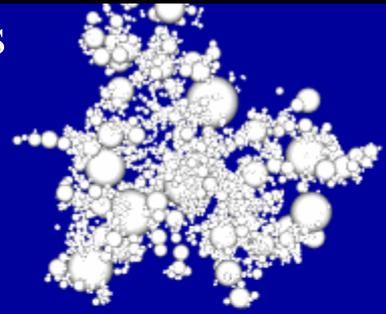
$u_{\text{coll}} = 52 \text{ m/s}$

No.15

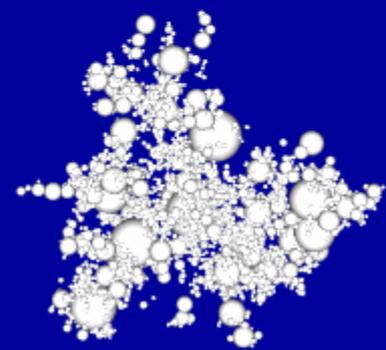
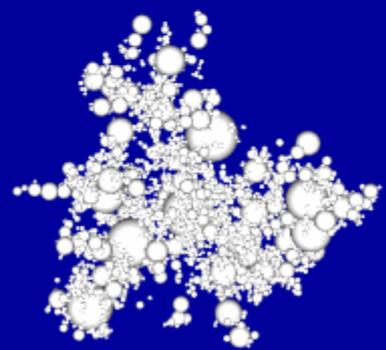
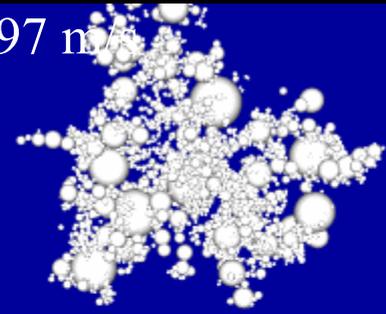
Examples of simulations

• $r=0.2\mu\text{m} - 0.025\mu\text{m}$ $N=6600$ (continuous: total mass= 0.1×201.6)

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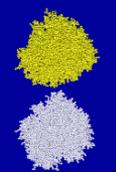


$u_{\text{coll}} = 197 \text{ m/s}$



No.09

8000 : 8000
 $b = 0$



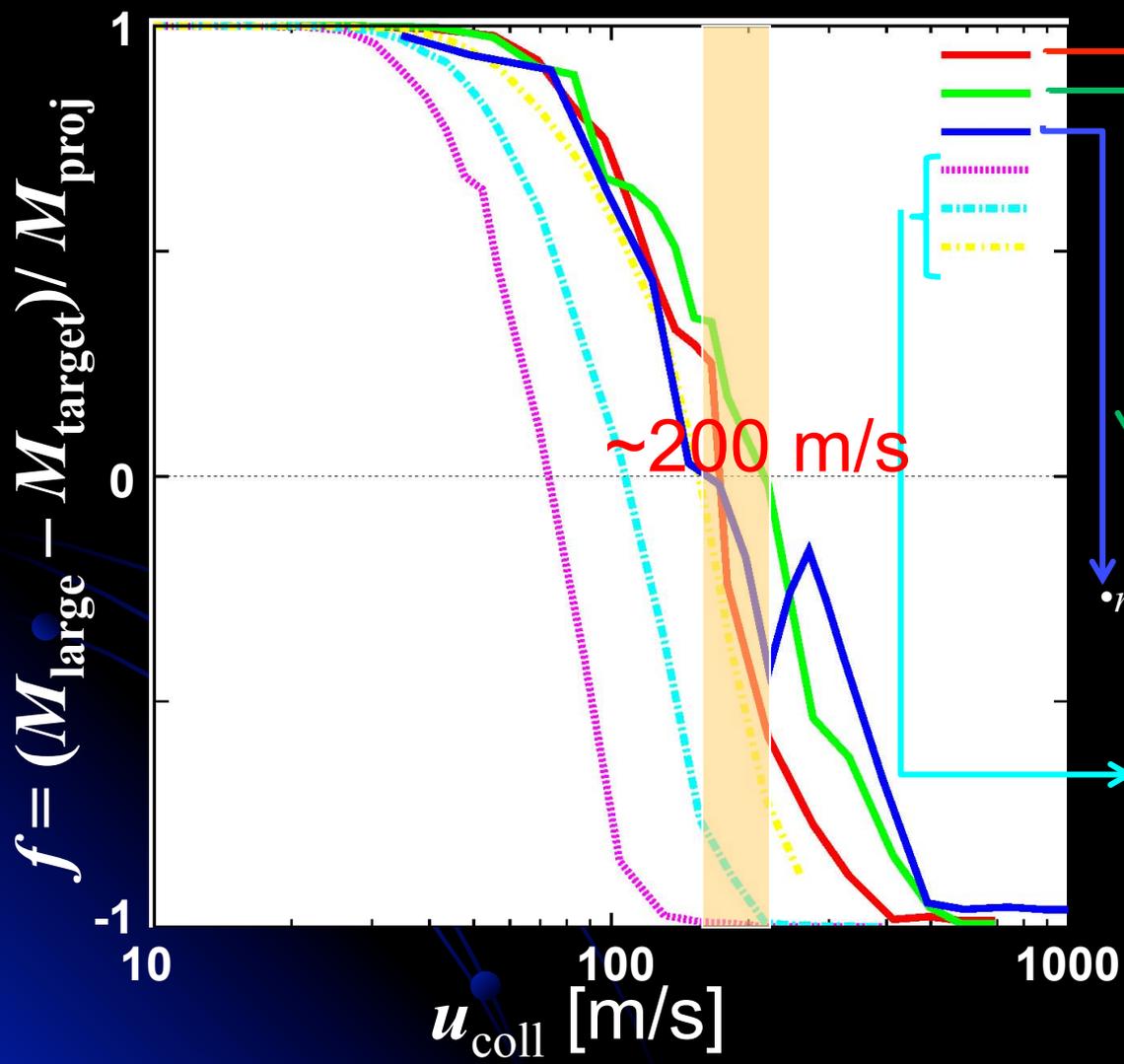
$u_{\text{coll}} = 52 \text{ m/s}$

No.15

Growth efficiency

(ice)

$$f \equiv (M_{\text{large}} - M_{\text{target}}) / M_{\text{proj}}$$



growth efficiency

- $f > 0 \rightarrow$ mass gain
- $f < 0 \rightarrow$ mass loss

• $r=0.1\mu\text{m} \times 100, 0.025\mu\text{m} \times 3200$
(binary: 150+150)

• $r=0.1\mu\text{m} \times 200, 0.025\mu\text{m} \times 6400$
(binary: 300+300)

• $r=0.2\mu\text{m} - 0.025\mu\text{m}, N=6600$
(continuous: 201.6+206.1)

- BPCA (500+500)
- BPCA(2000+2000)
- BPCA(8000+8000)



Summary and Implication

Simulations of collisions of **aggregates composed of particles with a size distribution**

- Particle size distribution leads to large growth efficiency.
➔ encouraging dust growth and planetesimal formation

- The critical collision velocity $u_{\text{coll,crit}}$ is unchanged?

$u_{\text{coll,crit}}$ for ice ~ 200 m/s

$u_{\text{coll,crit}}$ for silicate = $0.1 \times u_{\text{coll,crit}}$ for ice ~ 20 m/s

Cautious! These $u_{\text{coll,crit}}$ are for head-on collisions.

Offset collisions must be investigated.

Can dust grow through collisions?