



# つらな衝突

和田 浩二

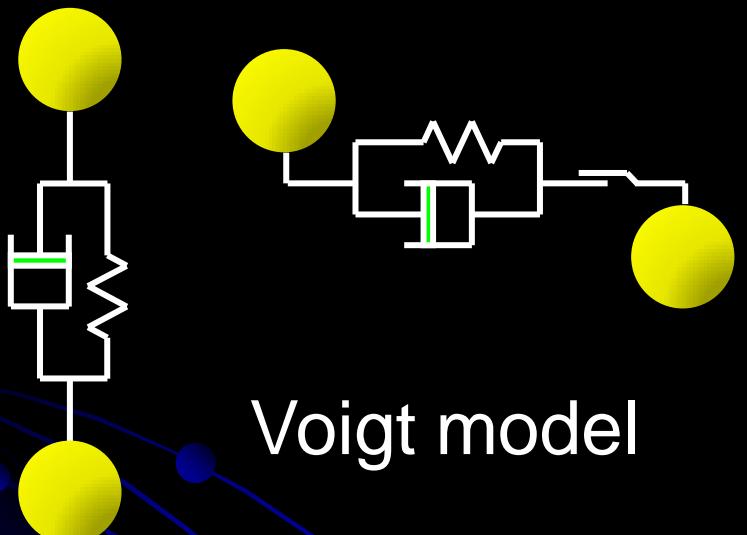
千葉工業大学惑星探査研究センター

北京大学天体物理科学研究所

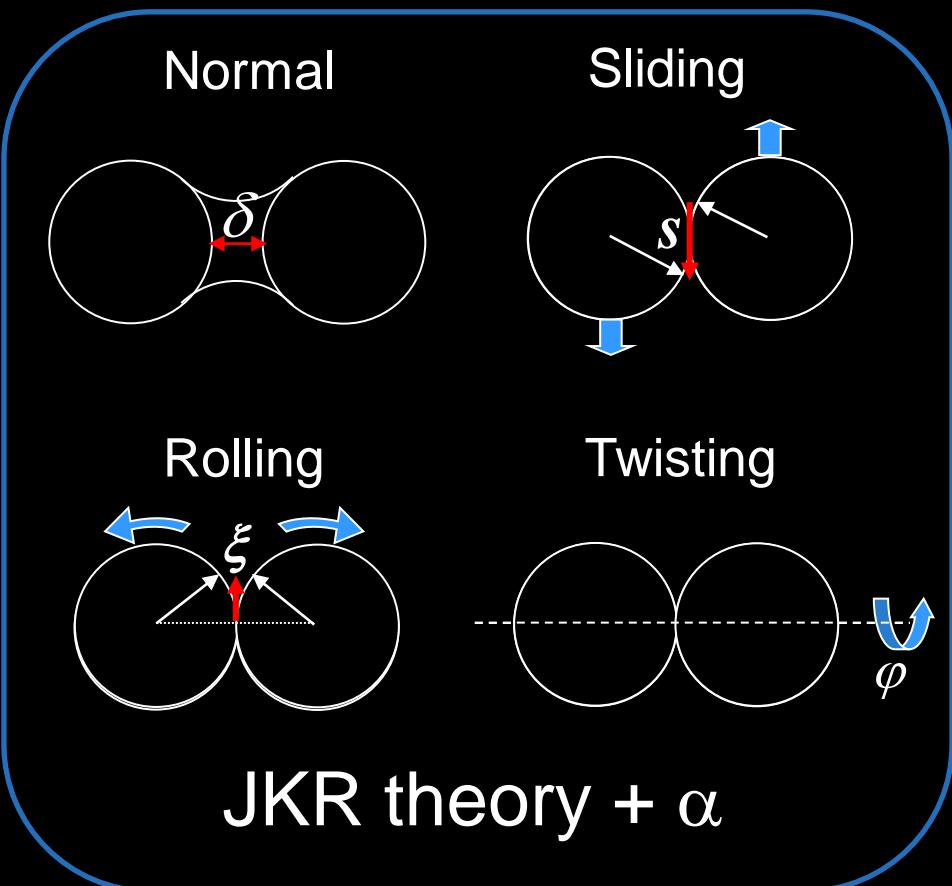
京大宇宙学系創成科学研究所

# 粒の衝突

接触粒子間相互作用 + 個々の粒子の運動を計算

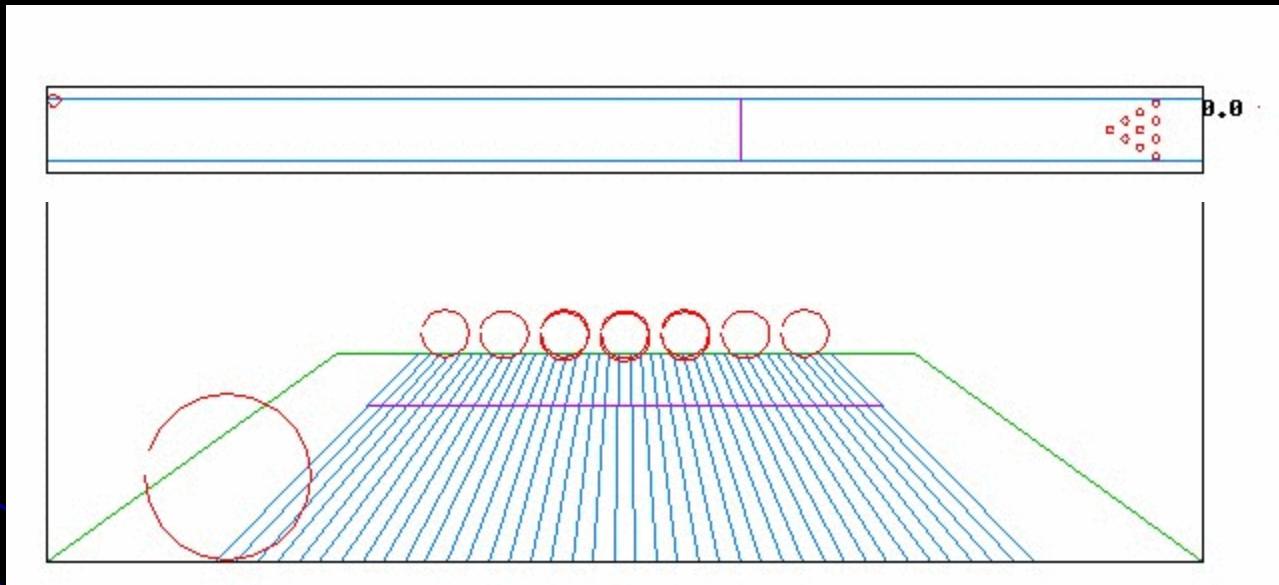


Voigt model

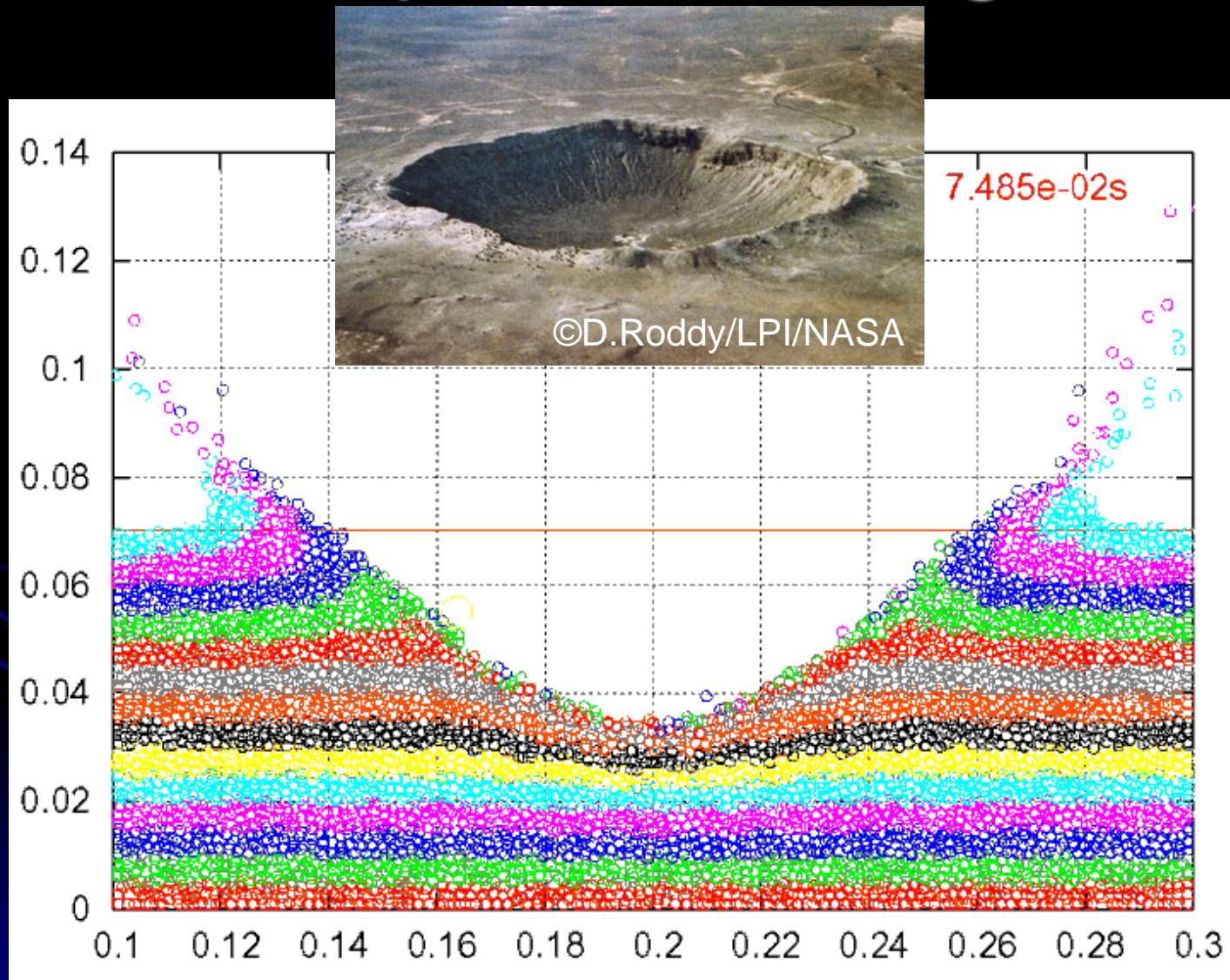


# 粒の衝突

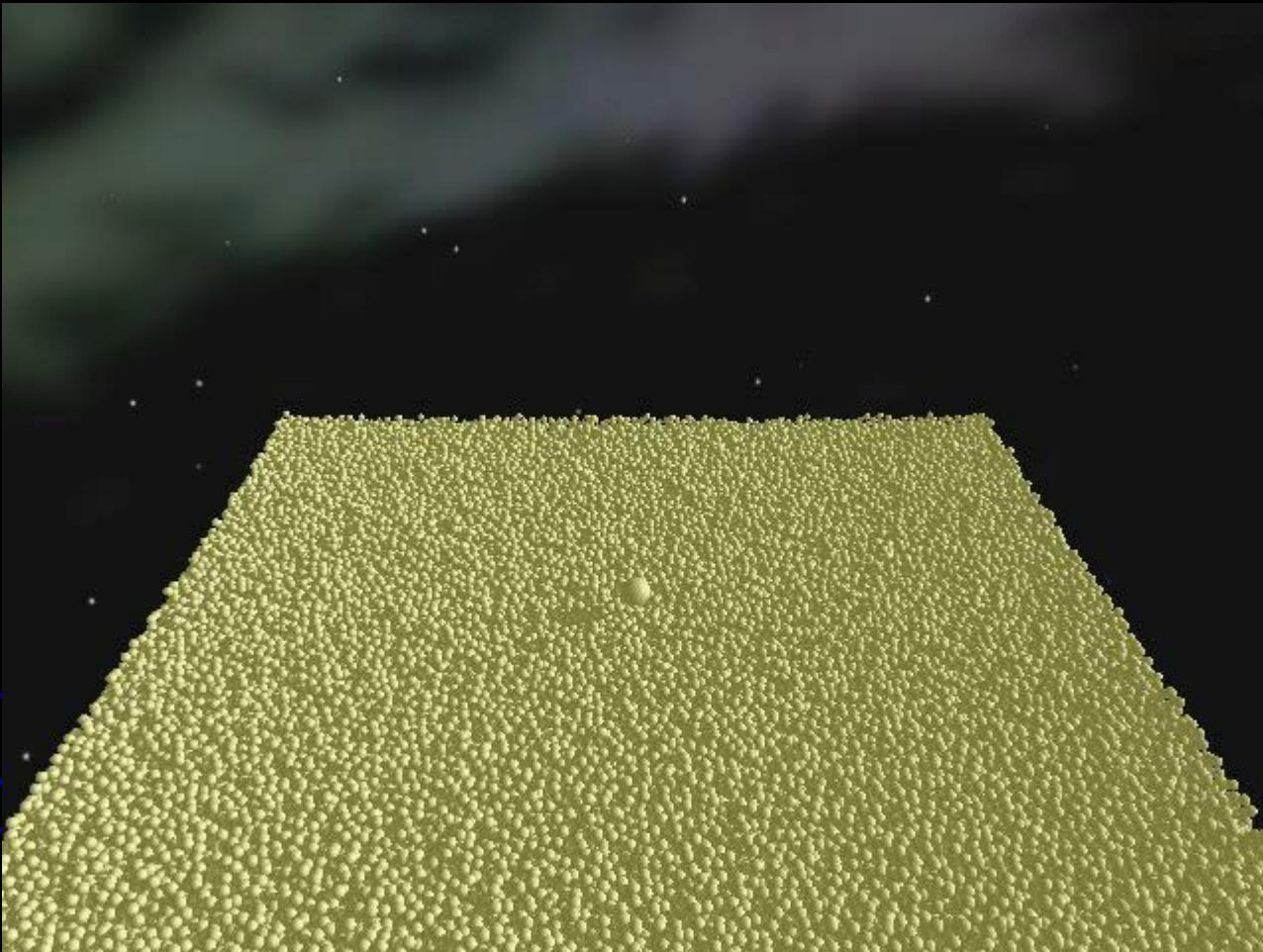
接触粒子間相互作用 + 個々の粒子の運動を計算



# Impact cratering



# Impact cratering



CG by Dr. T. Takeda, NAOJ

# Impact cratering



CG by Dr. T. Takeda, NAOJ

# Dust aggregate collisions

0.4 m/s



9 m/s



50 m/s



Ice aggregates,  $N = 1024$

offset collision

# Background

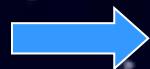
Collisional growth of dust  
( $< \mu\text{m}$ )



Planetesimal formation  
( $> \text{km}$ )

Structure evolution of dust aggregates in protoplanetary disks

When and how are aggregates compressed and/or disrupted ?

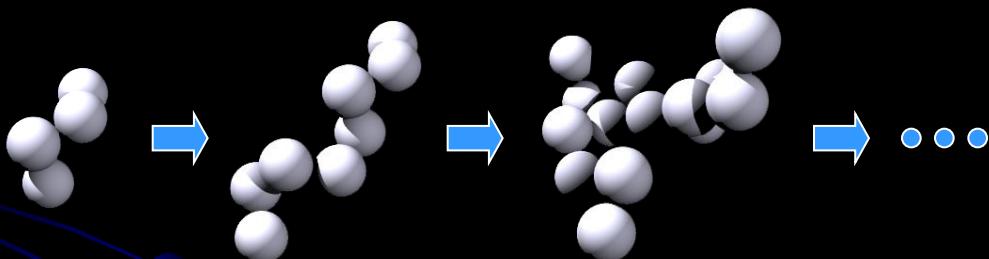


Numerical simulation of dust aggregate collisions!

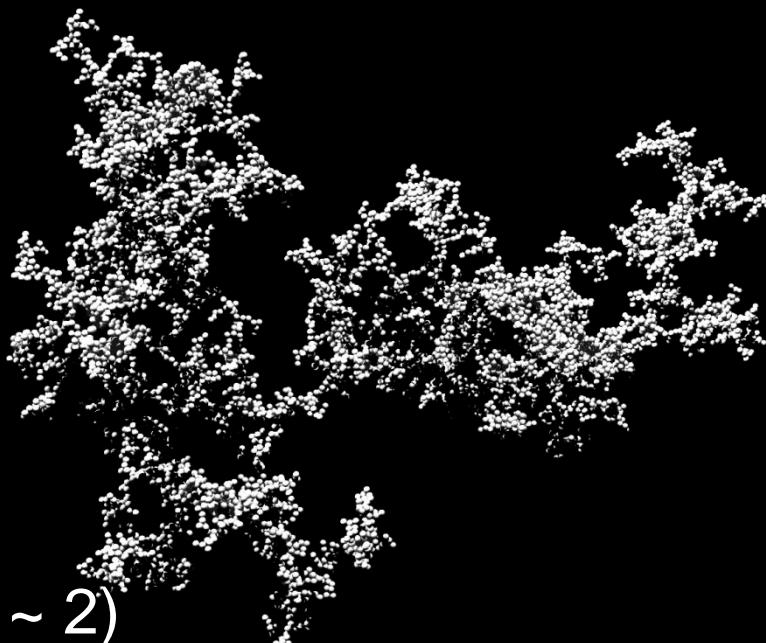
# Ballistic Cluster-Cluster Aggregation (BCCA)

- ✓ In the early growth stage, **undeformed** BCCAs are formed because of their low collision velocity (< mm/s)

- A series of hit-and sticks of comparable aggregates



- **Fluffy** structure (fractal dimension < ~ 2)



How are the BCCA structures compressed ?

Dominik & Tielens 1997;  
Wada et al. 2007, 2008; Suyama et al. 2008

# Background

Collision velocity of dust  
in protoplanetary disks      < several 10 m/s

e.g., <  $\sim$ 50 m/s (Hayashi model, without turbulence)



## Is it possible for dust to grow through collisions ?

Maybe possible in head-on collisions

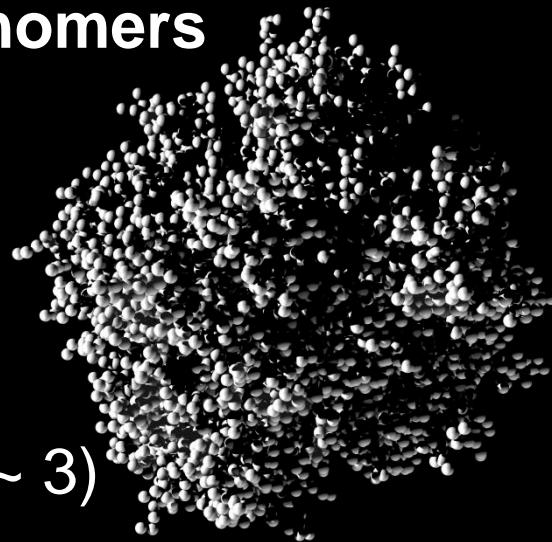
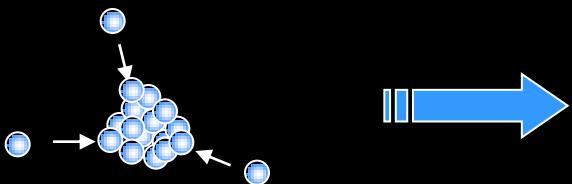
Experimental: Blum & Wurm 2000, Wurm et al. 2005

Numerical: Dominik & Tielens 1997, Wada et al. 2008

## What if in offset collisions ?

# Ballistic Particle-Cluster Aggregation (BPCA)

- Formed by one-by-one sticking of monomers



- Compact structure (fractal dimension  $\sim 3$ )

Dust is expected to be compact

- at high velocity collisions causing their disruption

Collisions of BPCA clusters

→ implication for growth and disruption of dust

Wada et al. 2009, Paszun & Dominik 2009

# Objective

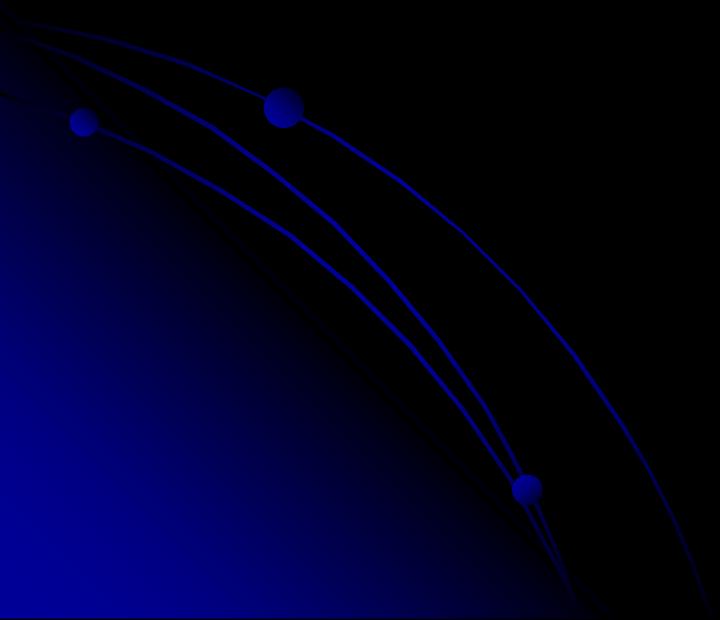
To construct a macroscopic model of aggregate structure evolution by numerical simulations of aggregate collisions

## Collisions of BCCA & BPCA clusters

- Compression process (BCCAs)  
Gyration radius → scaling law  
圧縮アグリゲイトのフラクタル次元 = ~ 2.5
- Growth and Disruption process (BPCAs)  
Number of particles in largest fragments  
→ growth efficiency  
氷アグリゲイトの破壊臨界速度 = ~ 50 m/s



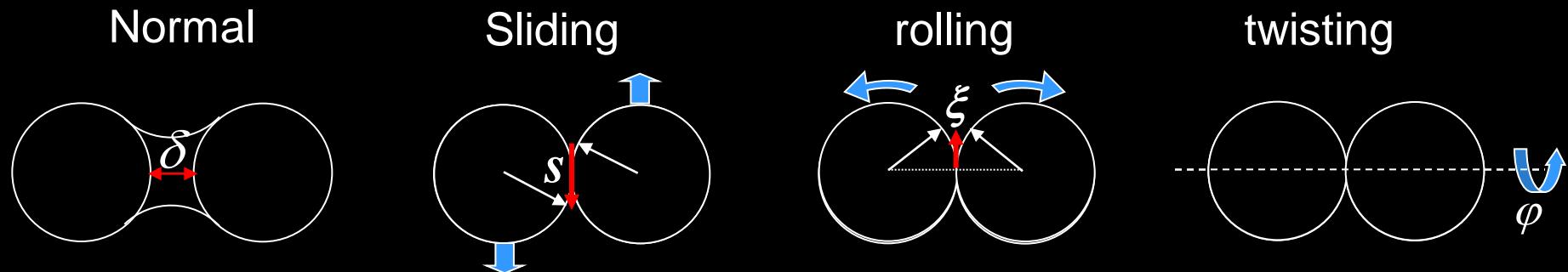
# Simulation Method



# Grain interaction model

Johnson, Kendall and Roberts (1971); Johnson (1987); Chokshi et al. (1993)  
 Dominik and Tielens (1995,96); Wada et al. (2007)

## Elastic spheres having surface energy



Contact & Separation  
 $s, \xi, \phi >$  critical displacements }  $\rightarrow$  Energy dissipation

$E_{\text{break}}$ : Energy to break a contact

$E_{\text{roll}}$ : Energy to roll a pair of gains by 90°

# Previous study

## Dominik and Tielens (1997)

Each grain motion is directly calculated,  
taking into account particle interactions

DUST AGGREGATE COLLISIONS  
(c) 1996  
C. DOMINIK and A. TIELENS

TYPE: CLUSTER-CLUSTER  
MATERIAL: ICE  
SIZES: 1E-5 .. 1E-5 CM

✓ modeling grain interactions seriously

Limitations:  
D&T "recipe"

- 2-D, Head-on collision
- $\sim n_k E_{\text{roll}}$  → Max. compression
- Small size (40+40 grains)
- $> 10 n_k E_{\text{break}}$  → Catastrophic disruption
- Initial structure: only 1 type

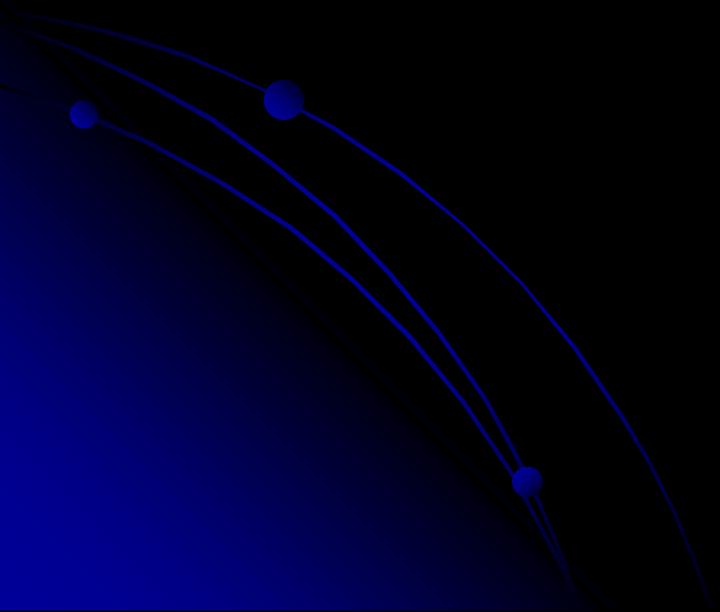
$E_{\text{roll}}$  : Energy to roll a grain by 90°

$E_{\text{break}}$  : Energy to break a contact

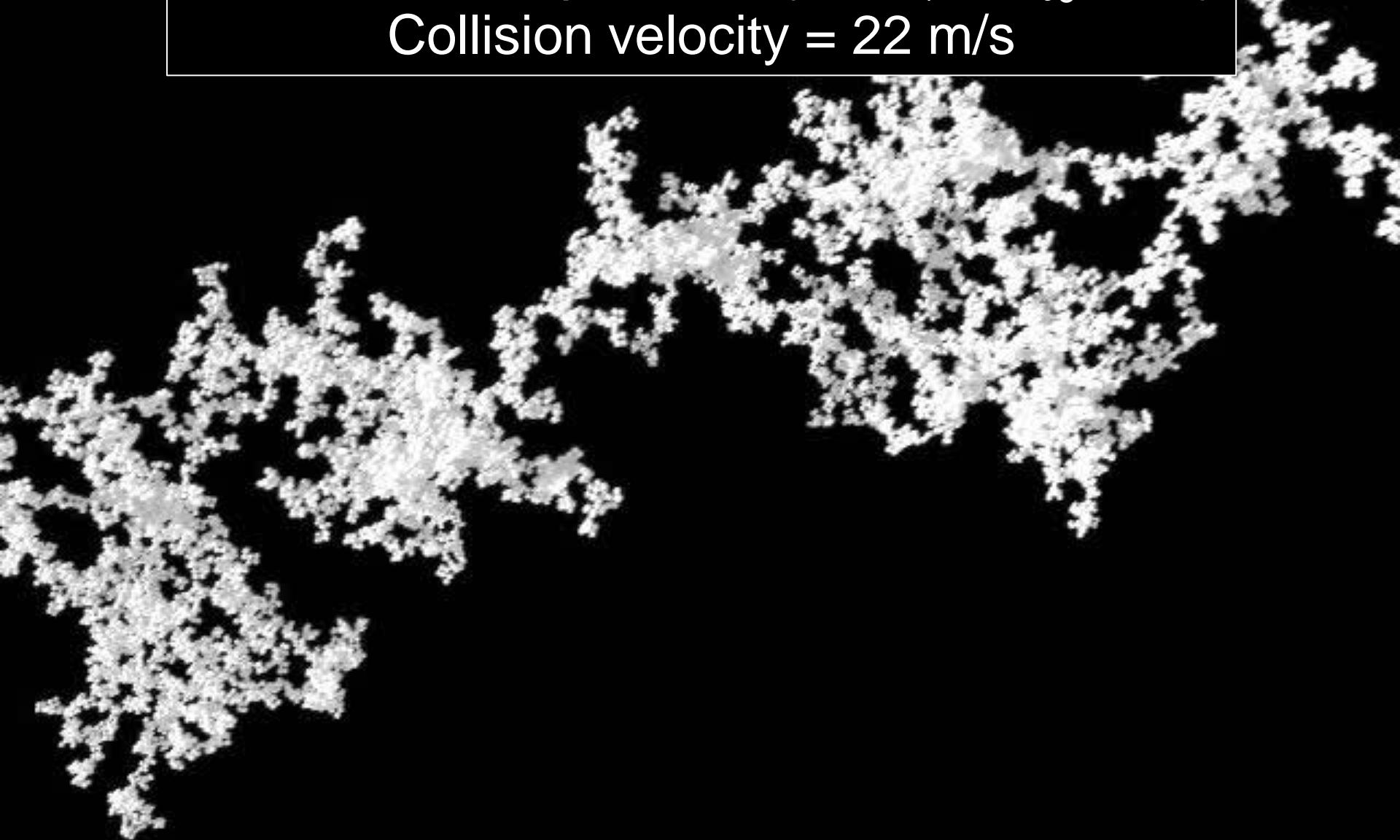
$n_k$  : Number of contacts in initial aggregates

# Collisions between BCCA clusters

: Compression process

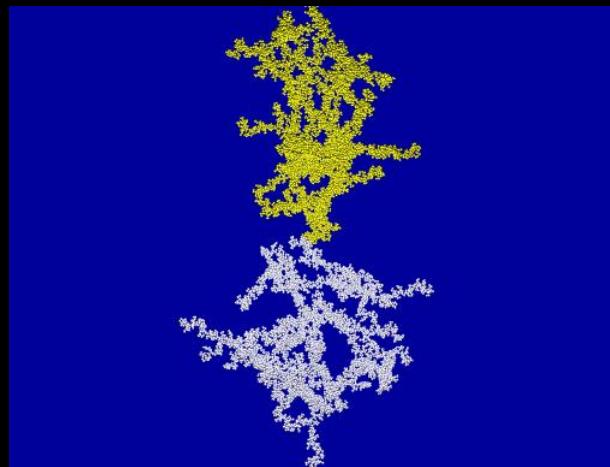
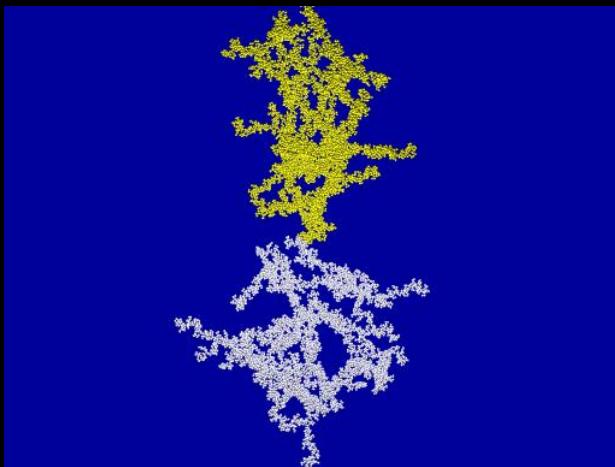
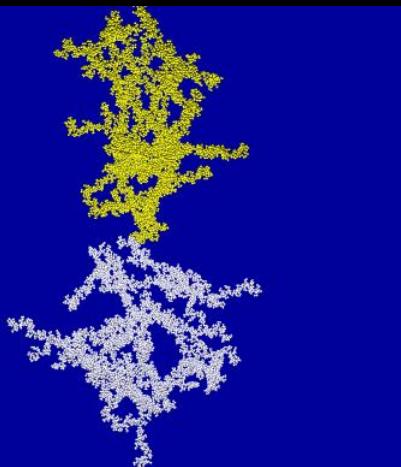


A collision of BCCAs  
8192+8192 ice particles ( $r=0.1\mu\text{m}$ ,  $\xi_c = 8\text{\AA}$ )  
Collision velocity = 22 m/s



# Example of simulations

**Ice, 8192 + 8192,  $\xi_{\text{crit}} = 8 \text{ \AA}$**



$$E_{\text{impact}} \sim 0.7 E_{\text{roll}}$$

$$V_{\text{impact}} = 0.2 \text{ m/s}$$

$$E_{\text{impact}} \sim 0.3 n_k E_{\text{roll}}$$

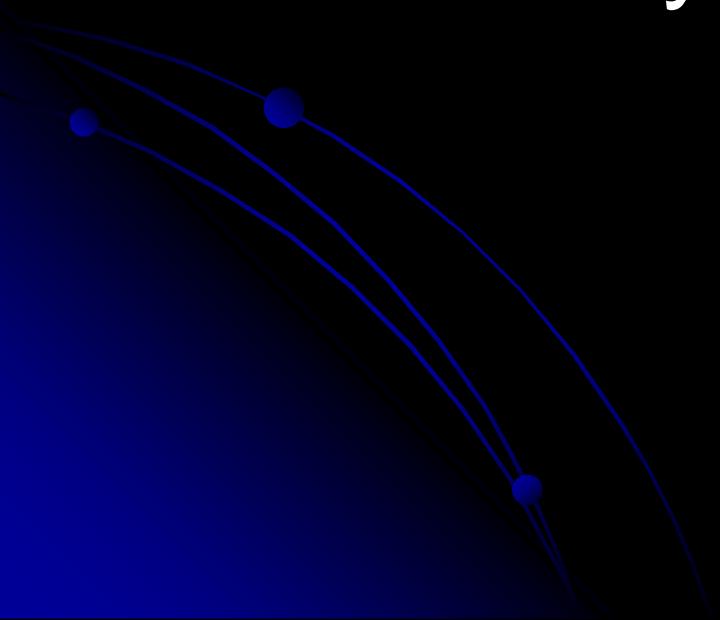
$$V_{\text{impact}} = 17 \text{ m/s}$$

$$E_{\text{impact}} \sim 13 n_k E_{\text{break}}$$

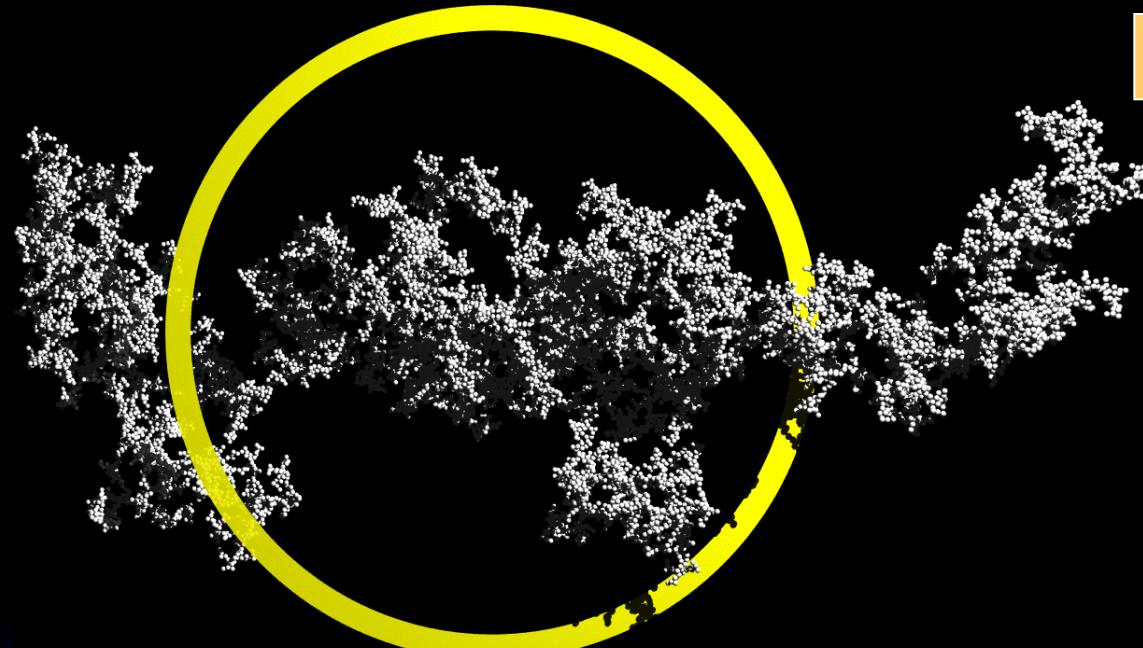
$$V_{\text{impact}} = 39 \text{ m/s}$$



# Numerical Results on Gyration Radius



# Gyration radius $r_g$ : compression process



**Ice, 8192 + 8192,  $\xi_{\text{crit}} = 8 \text{ \AA}$**

$$r_g = \sqrt{\frac{1}{N} \sum_i |x_i - x_g|^2}$$

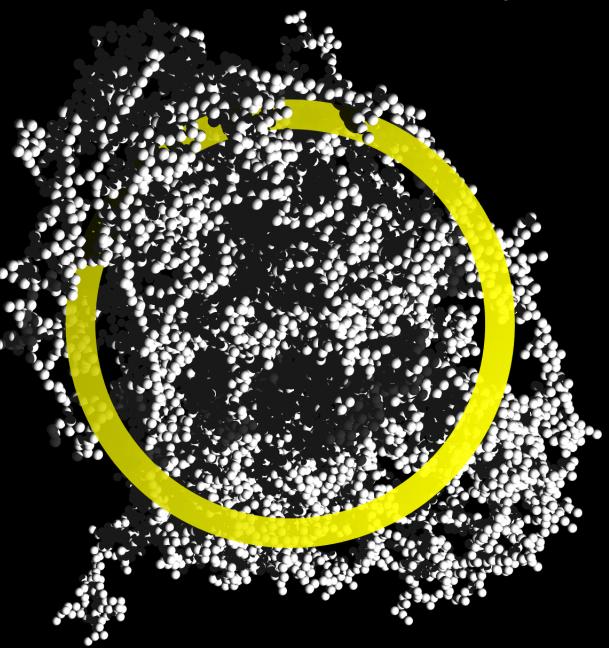
$x_g$ : center of mass

$$E_{\text{impact}} \sim 0.01 E_{\text{roll}}$$

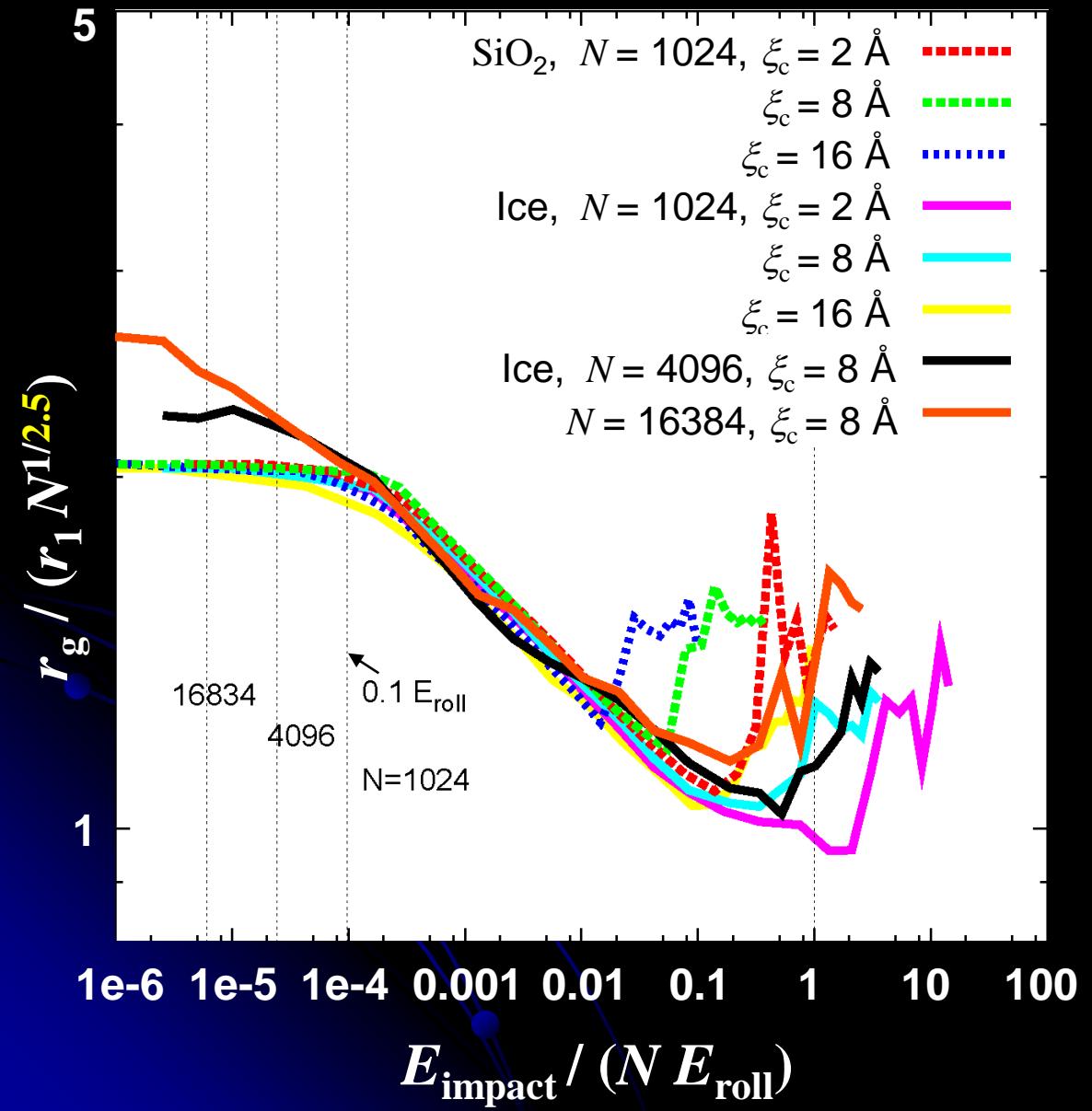
Impact velocity: 0.024 m/s

$$E_{\text{impact}} \sim 0.19 N E_{\text{roll}}$$

Impact velocity: 13 m/s

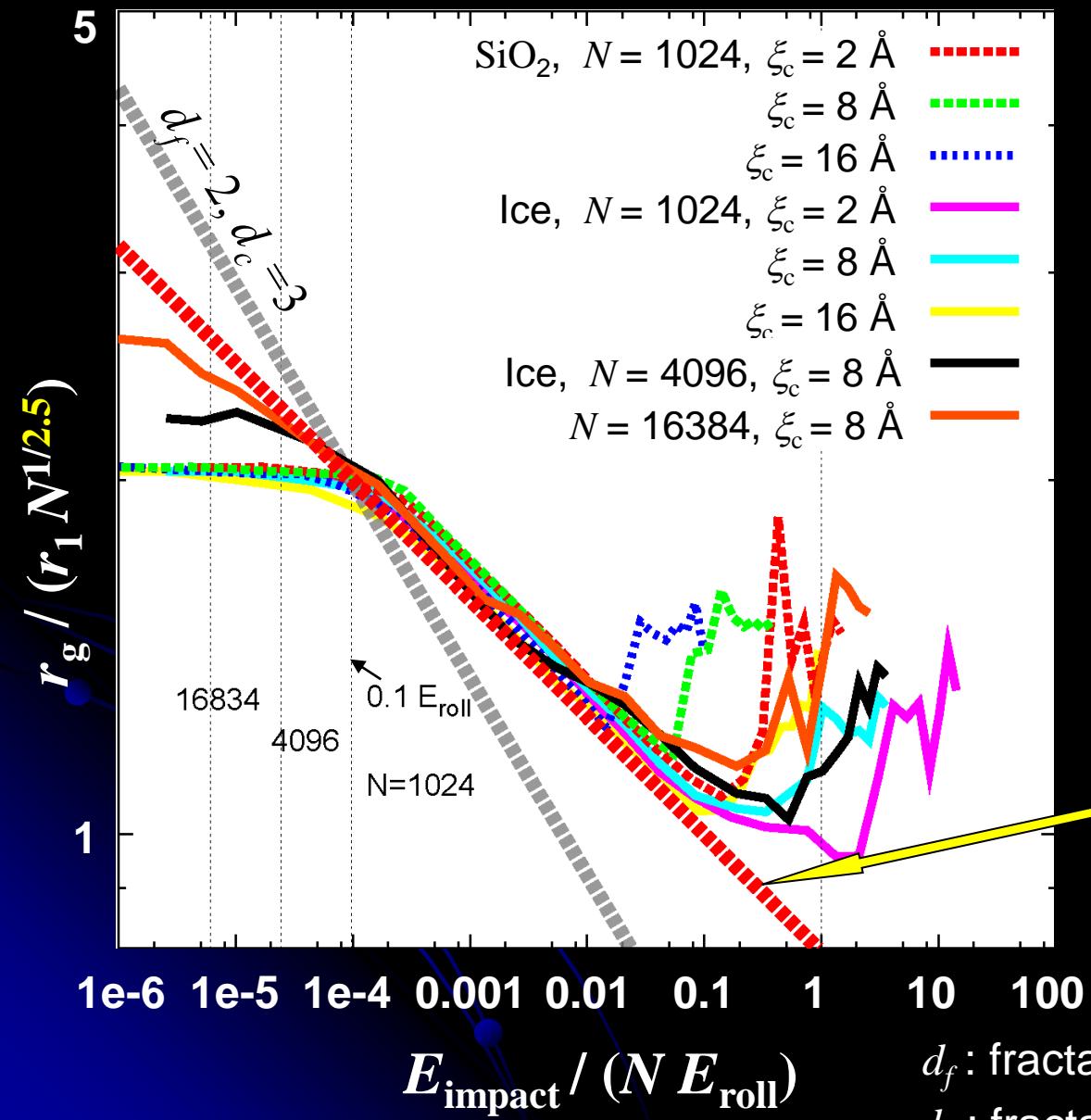


# Gyration radius $r_g$ : compression process



- ✓ Scaled by  $E_{\text{impact}} / (N E_{\text{roll}})$
- ✓  $r_g$  is normalized by  $r_1 N^{\frac{1}{2.5}}$

# Gyration radius $r_g$ : compression process

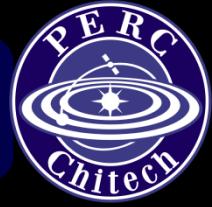


- ✓ Scaled by  $E_{\text{impact}} / (N E_{\text{roll}})$
- ✓  $r_g$  is normalized by  $r_1 N^{1/2.5}$
- ✓ Not fully compressed

$$\frac{r_g}{r_1 N^{1/2.5}} \approx 0.8 \left( \frac{E_{\text{impact}}}{N E_{\text{roll}}} \right)^{-0.1}$$

$d_f$ : fractal dimension of BCCA  
 $d_c$ : fractal dimension of max. compression

# Successive collisions in a BCCA mode

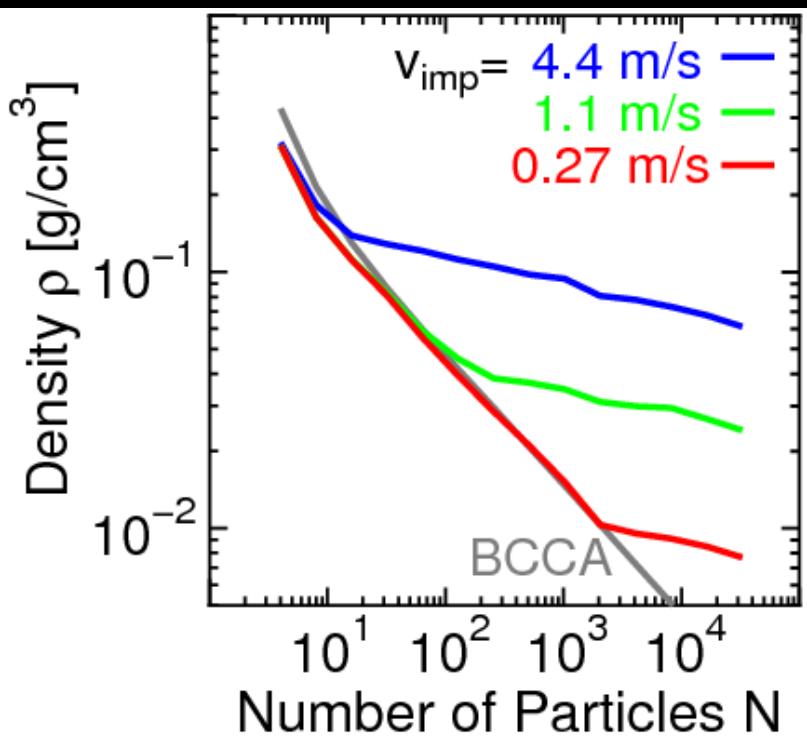


Suyama et al. 2008

- ✓ Fractal dimension ~2.5
- ✓ Decrease in density



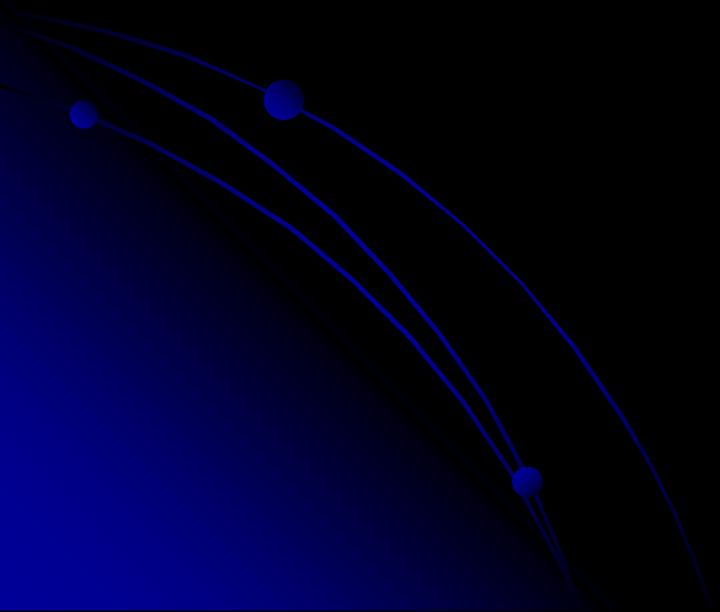
CG by Dr. T. Takeda, 4D2Uproject, NAOJ



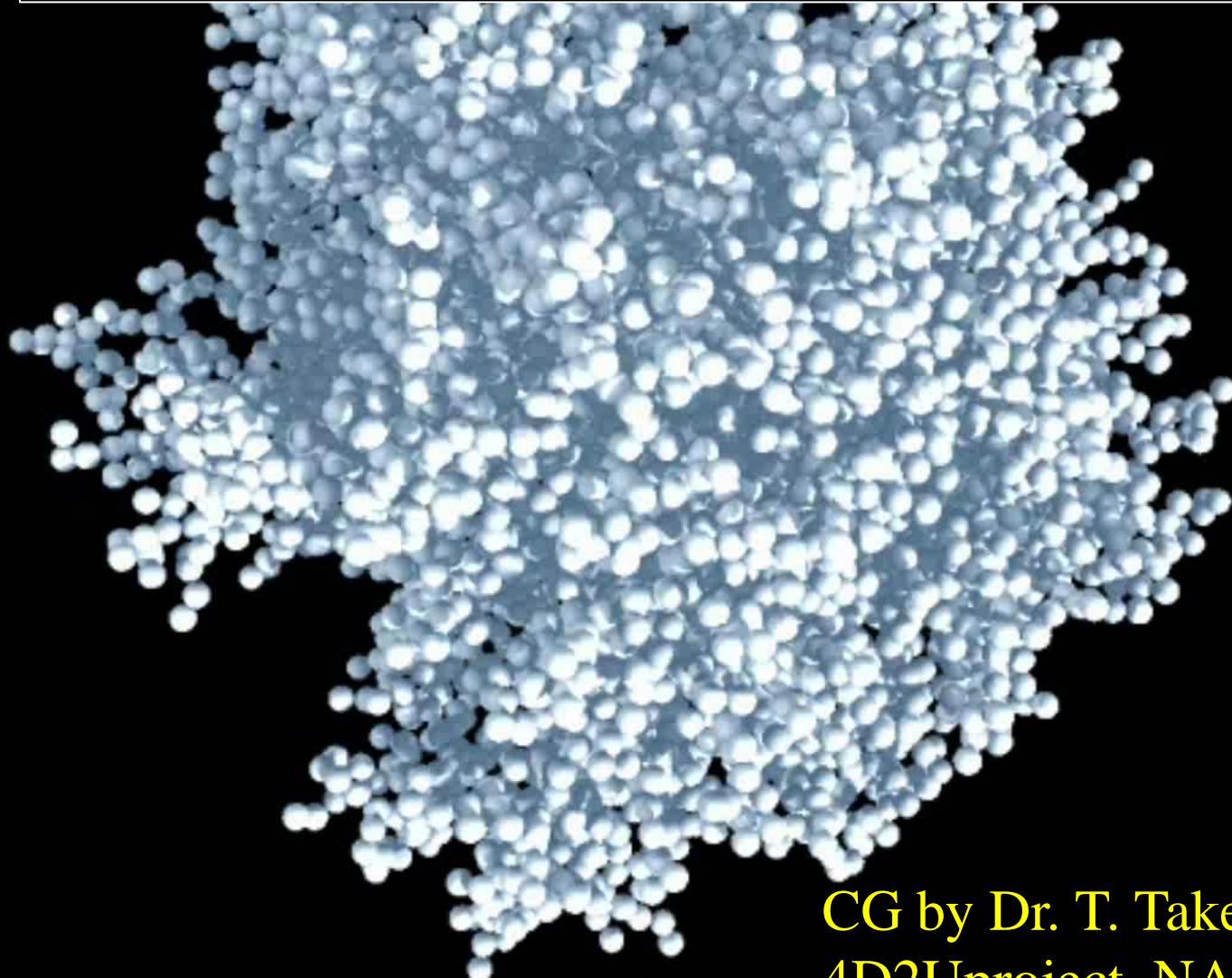


# Collisions between BPCA clusters

: Growth and Disruption process



A collision of BPCAs  
8000+8000 ice particles ( $r=0.1\mu\text{m}$ ,  $\xi_c = 8\text{\AA}$ )  
Collision velocity = 57 m/s



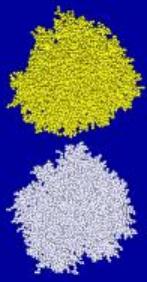
CG by Dr. T. Takeda,  
4D2Uproject, NAOJ

# Collisions of BPCA clusters

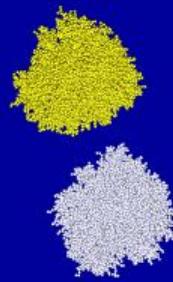
$N=8000+8000$ , ice,  $\xi_c = 8\text{\AA}$ ,  $v_{\text{imp}} = 70 \text{ m/s}$  ( $E_{\text{imp}} = 42 N E_{\text{break}}$ )



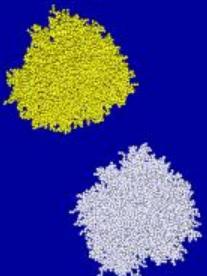
$b = 0$



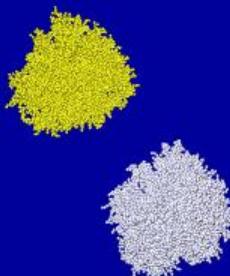
$b = 0.39$



$b = 0.69$

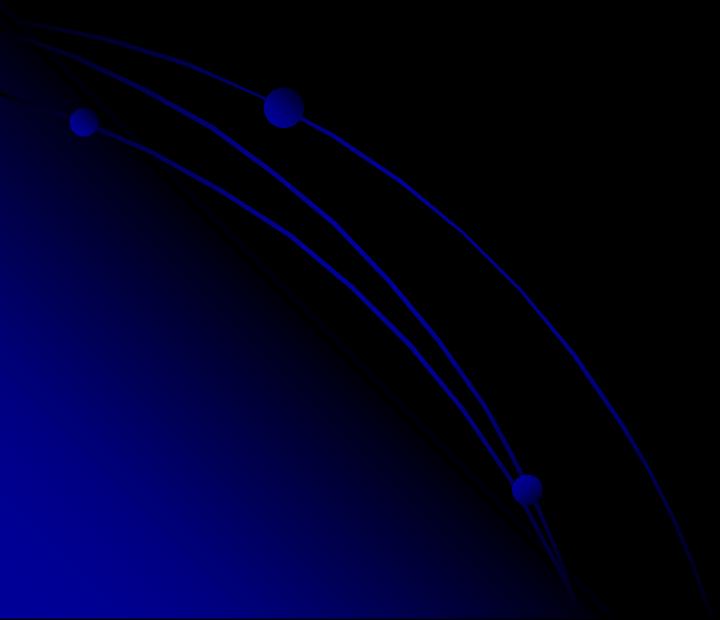


$b = 1.00$

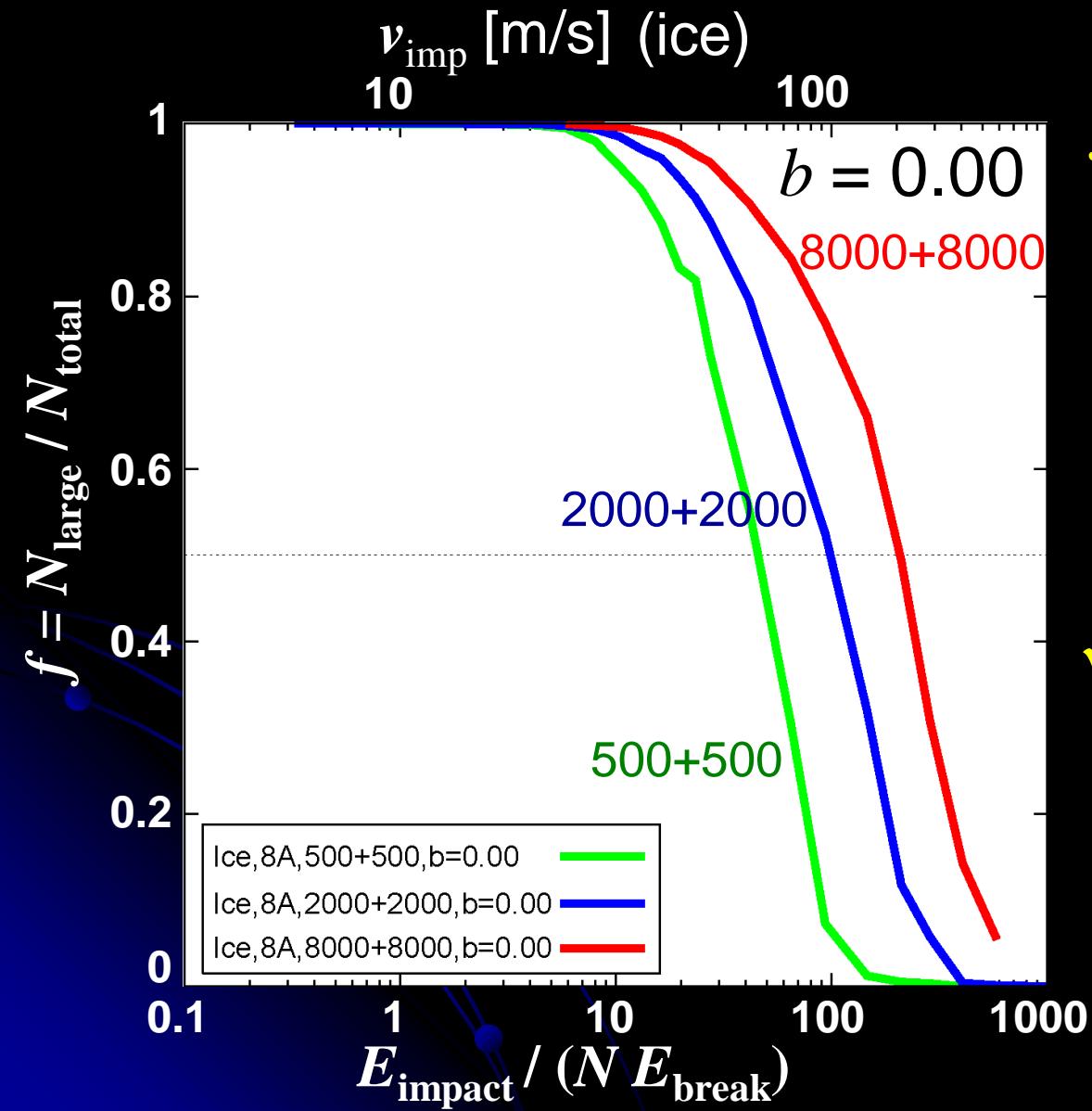




# Growth Efficiency For Collisions of BPCAs



# Largest fragment mass $N_{\text{large}}$ : growth efficiency



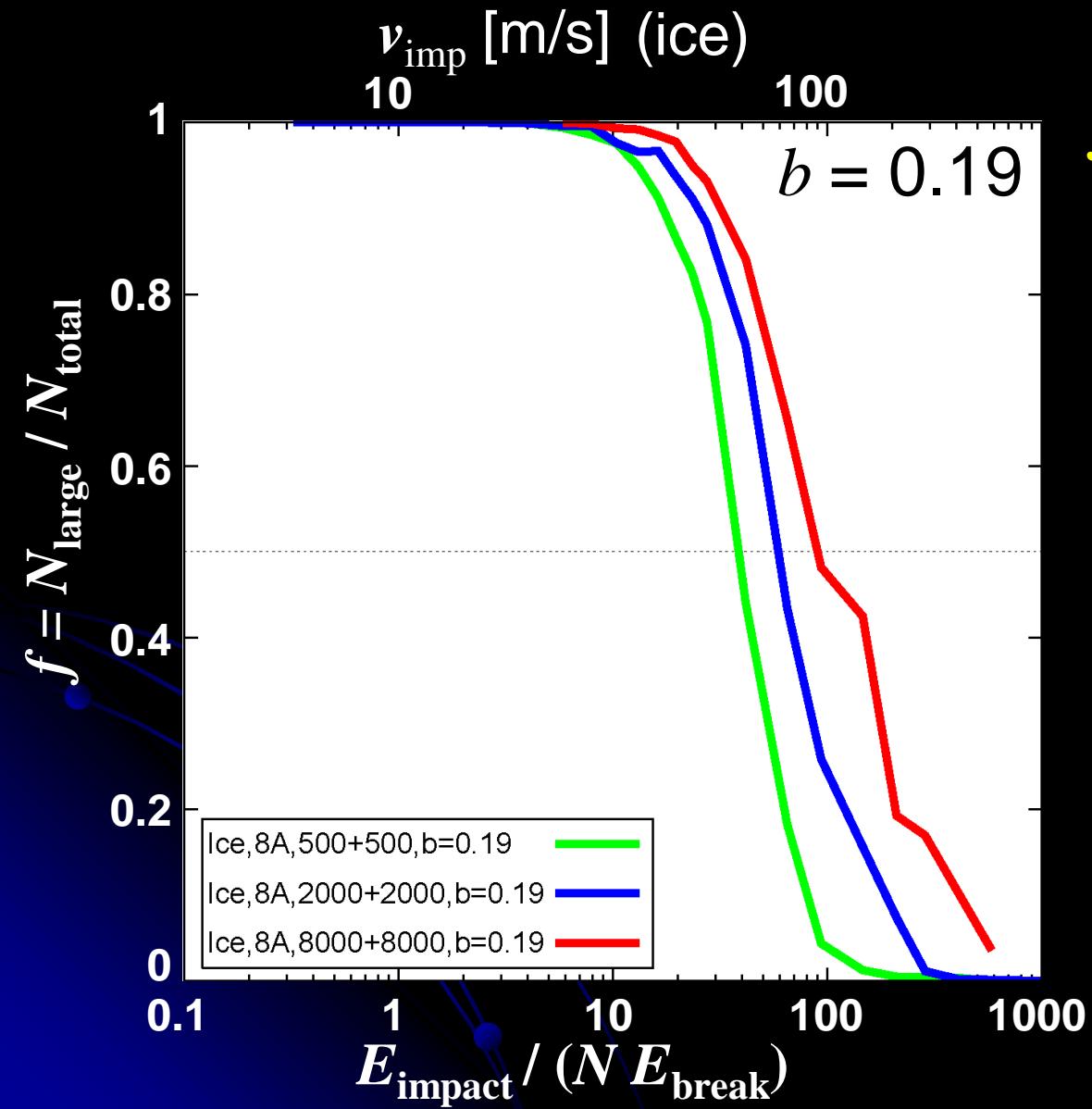
$$f \equiv N_{\text{large}} / N_{\text{total}}$$

: growth efficiency

$$\begin{cases} f > 0.5 \rightarrow + \text{growth} \\ f < 0.5 \rightarrow - \text{growth} \end{cases}$$

✓ dependent on  $N$

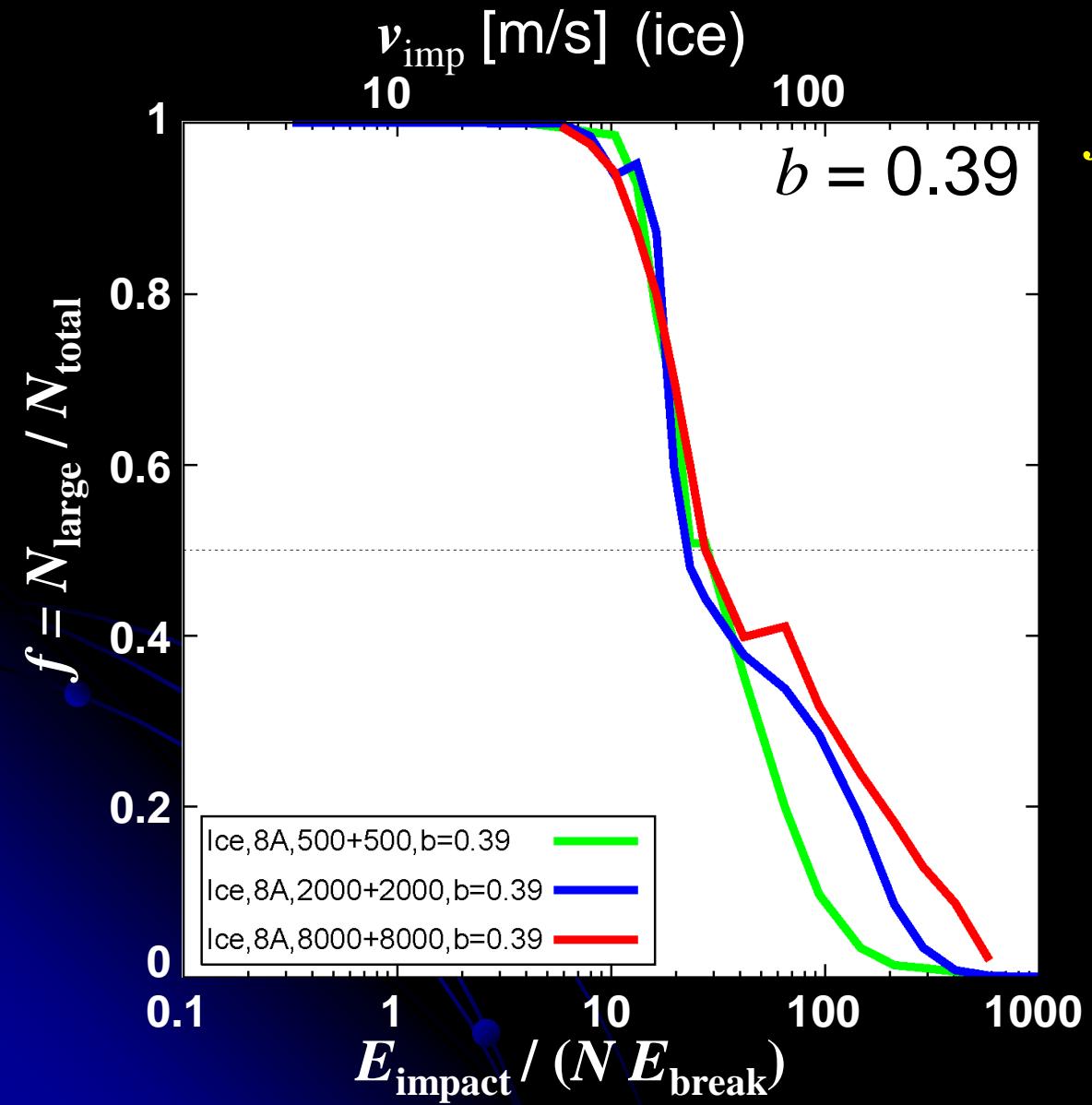
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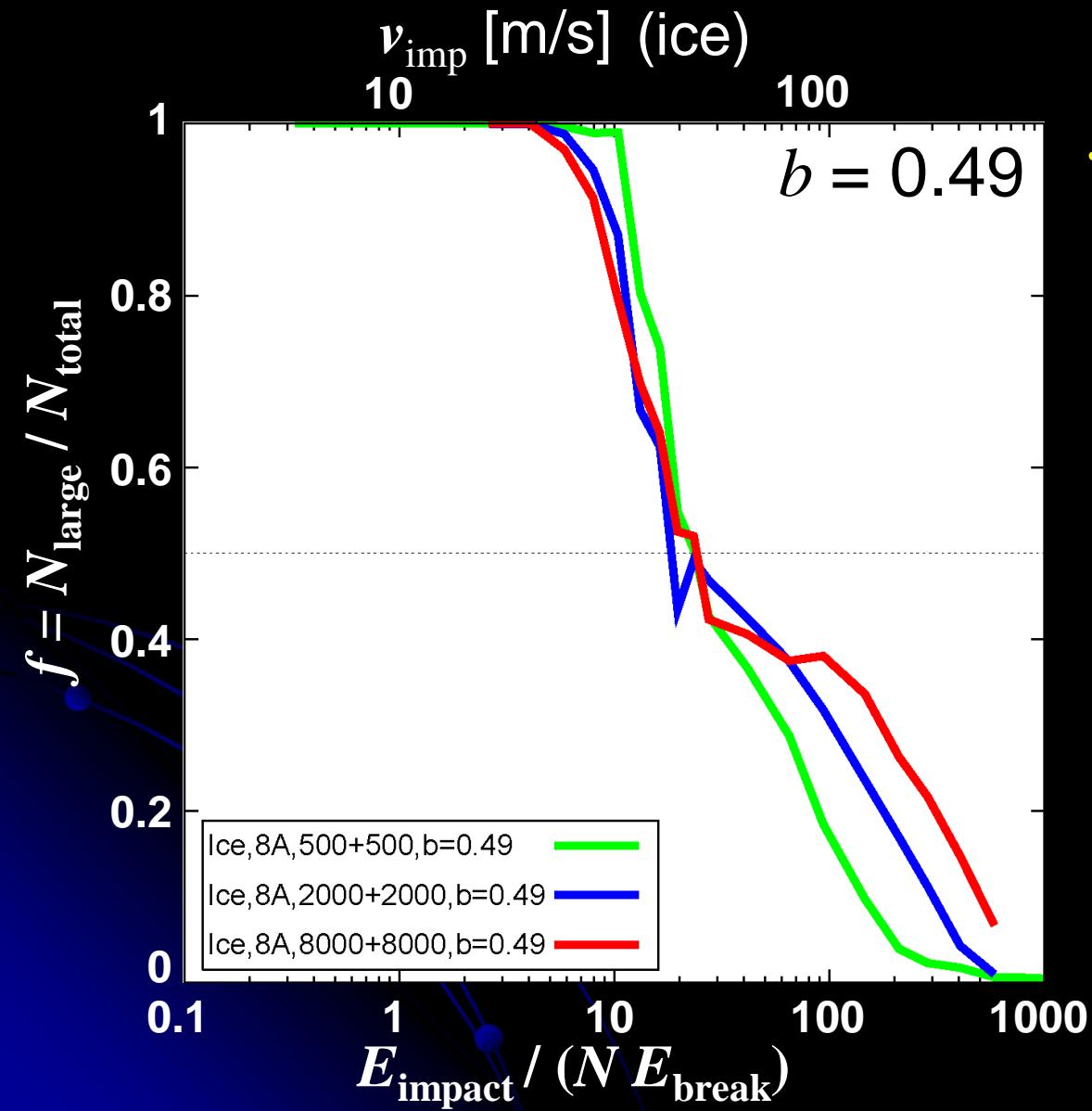
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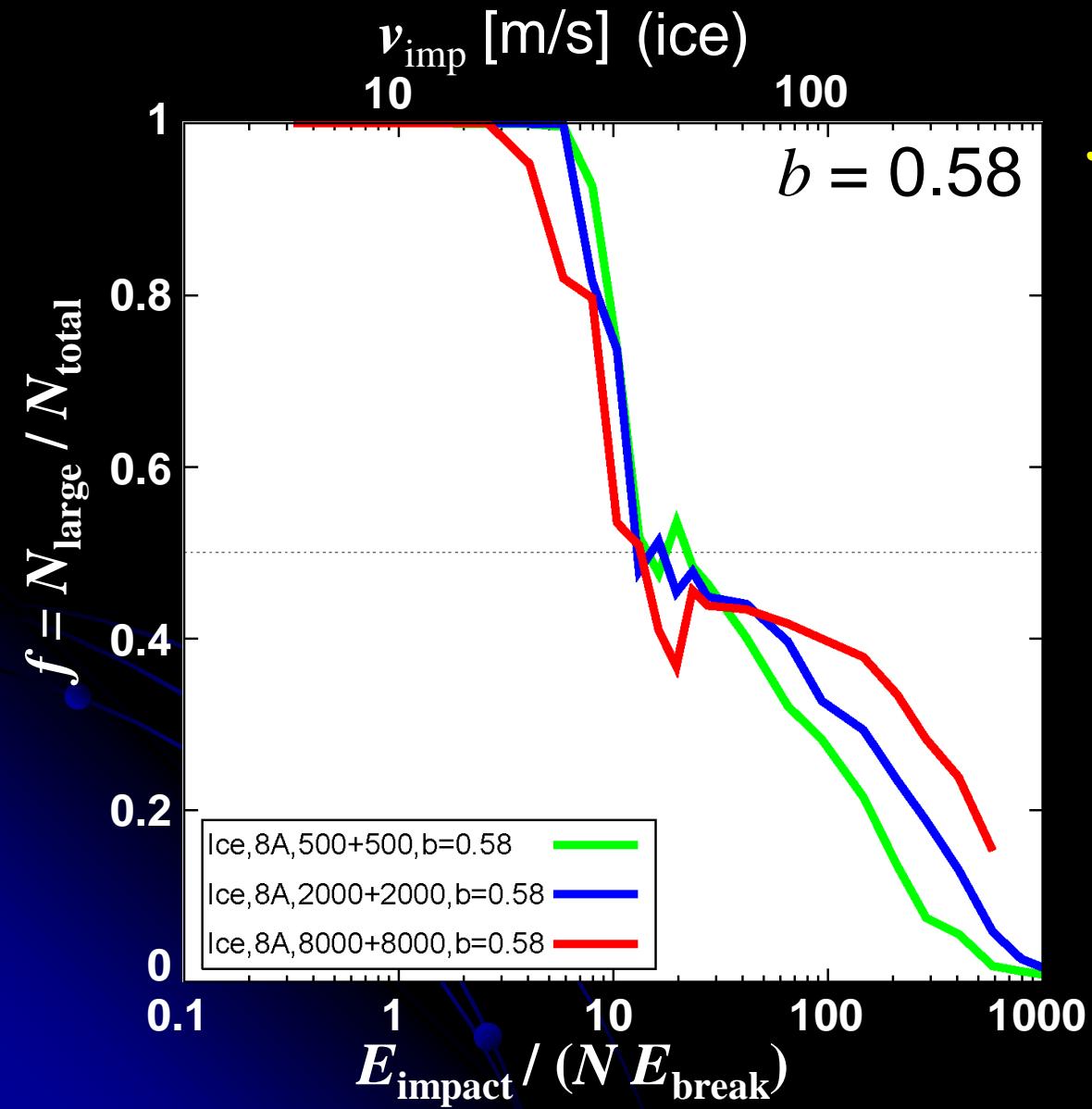
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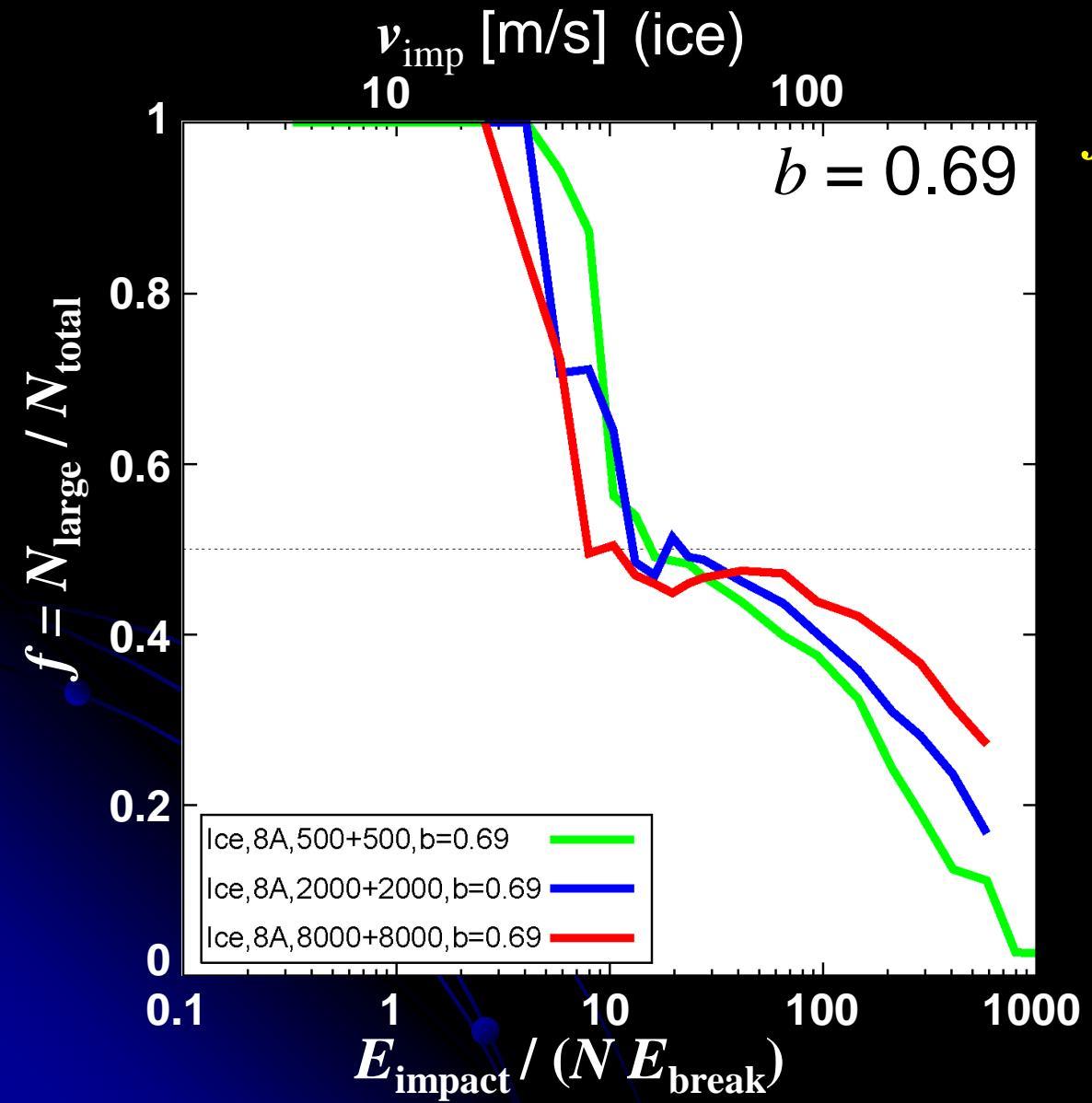
$\begin{cases} f > 0.5 \rightarrow + \text{growth} \\ f < 0.5 \rightarrow - \text{growth} \end{cases}$

# Largest fragment mass $N_{\text{large}}$ : growth efficiency



$f \equiv N_{\text{large}} / N_{\text{total}}$   
: growth efficiency  
 $\left\{ \begin{array}{l} f > 0.5 \rightarrow + \text{growth} \\ f < 0.5 \rightarrow - \text{growth} \end{array} \right.$

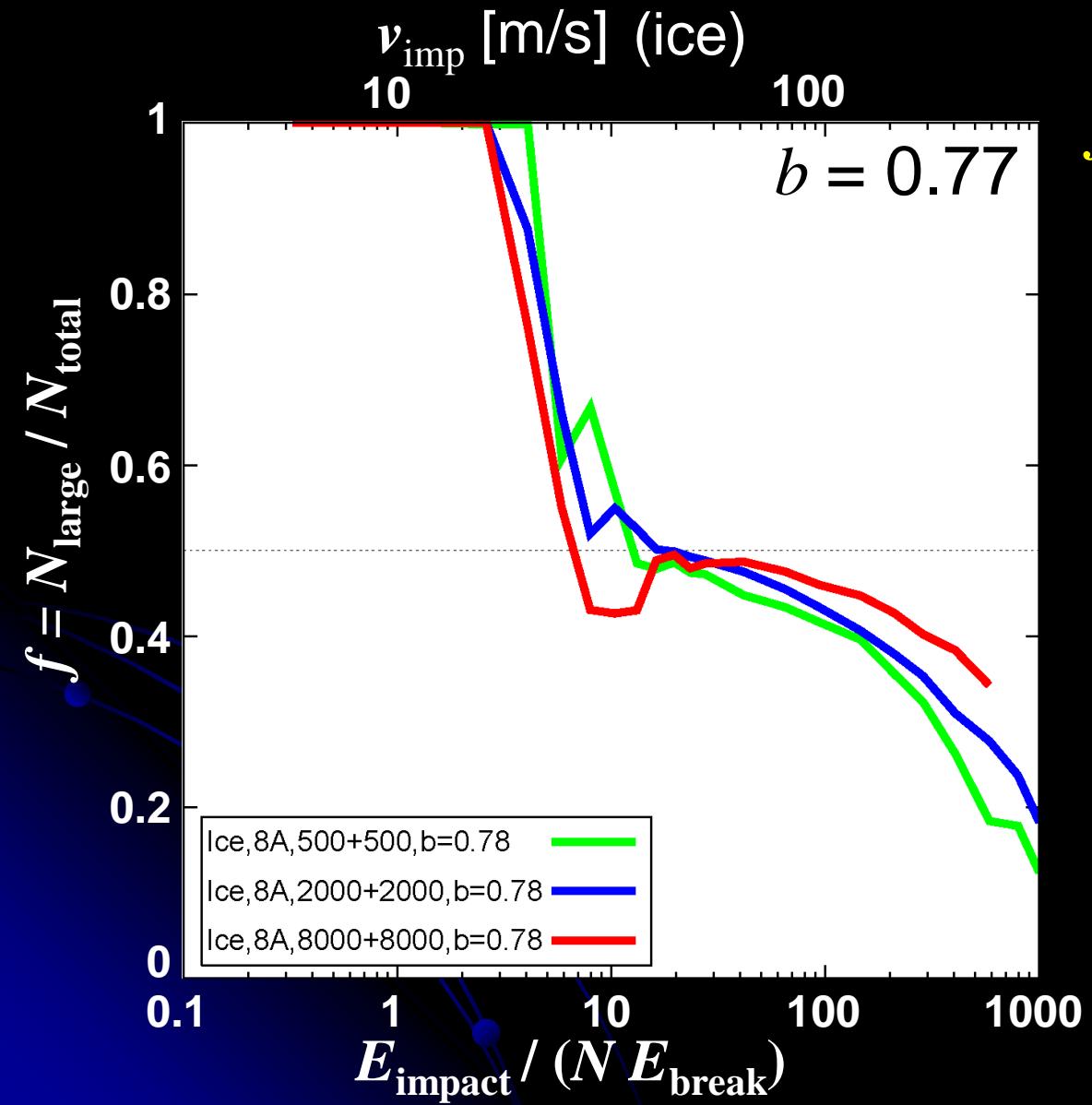
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$f \equiv N_{\text{large}} / N_{\text{total}}$   
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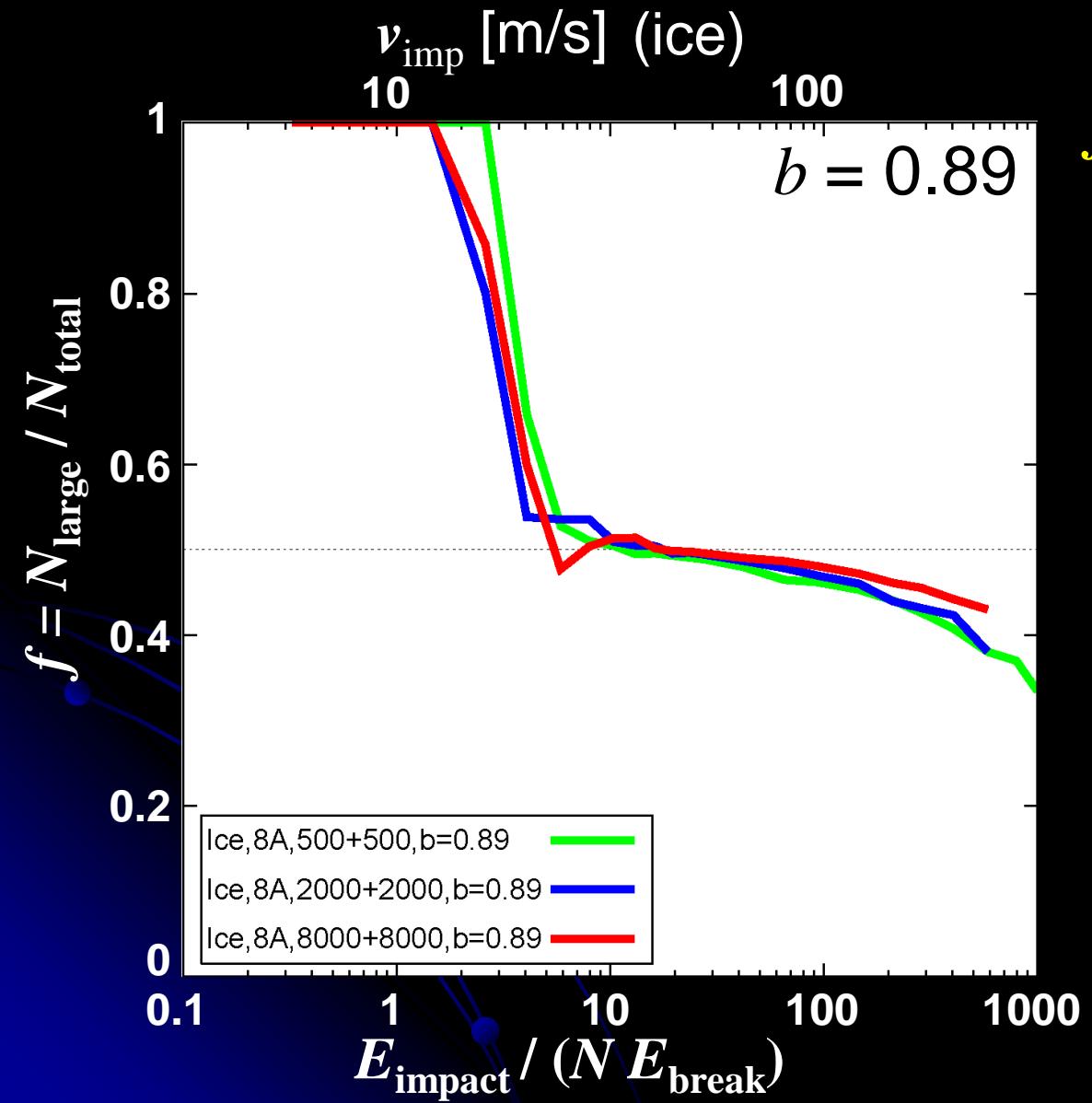
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# Largest fragment mass $N_{\text{large}}$ : growth efficiency



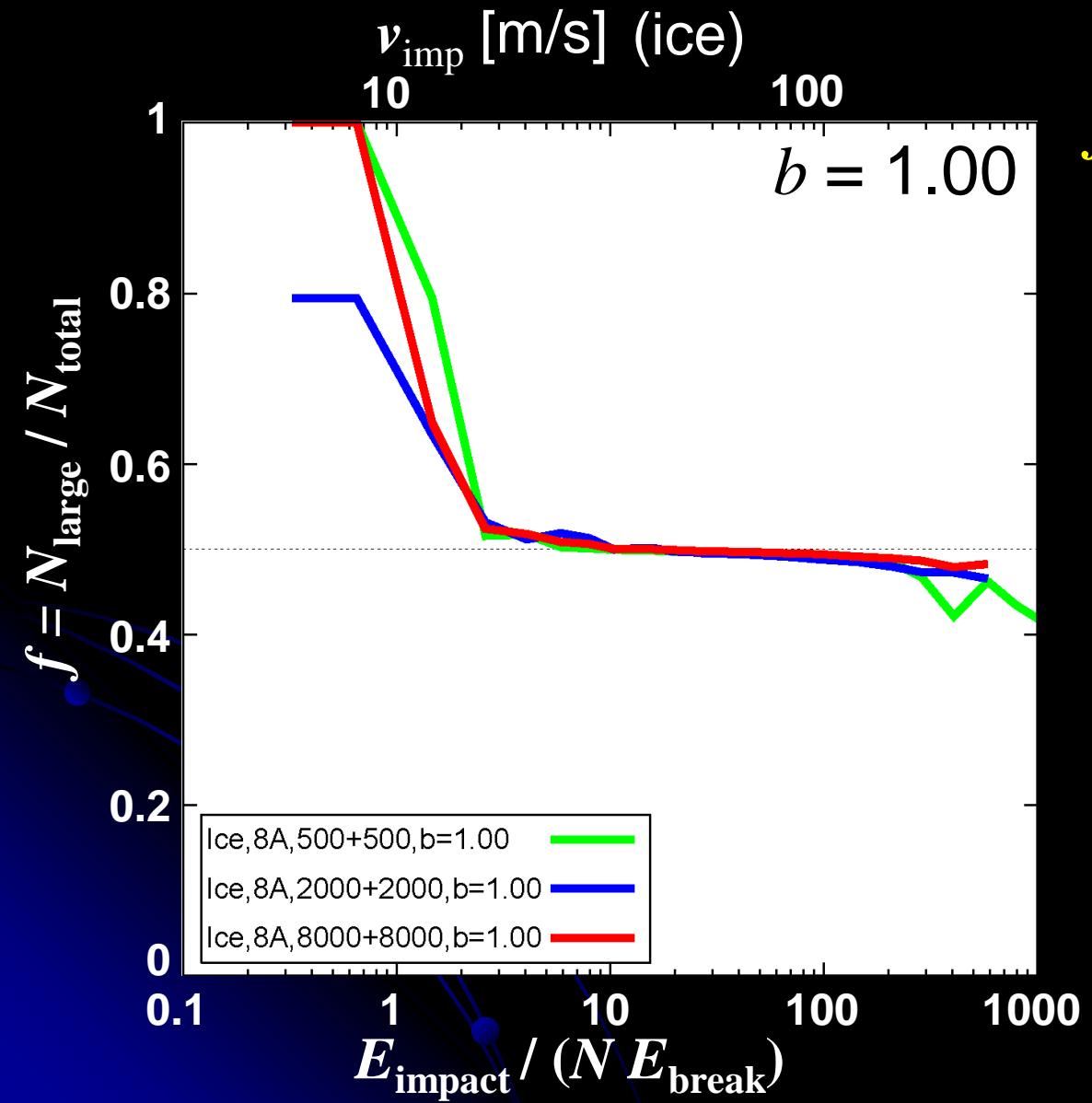
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$f \equiv N_{\text{large}} / N_{\text{total}}$   
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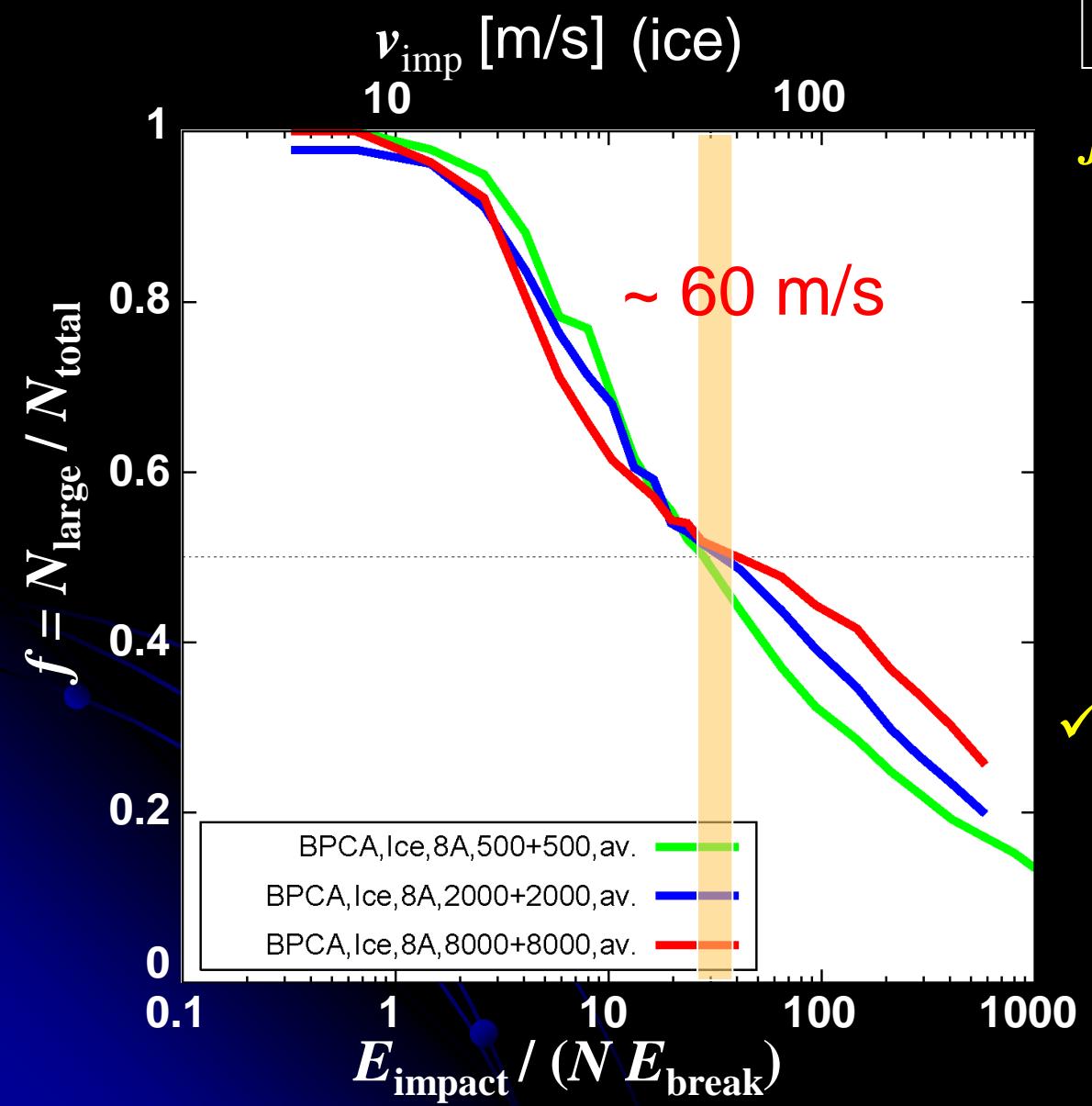
# Largest fragment mass $N_{\text{large}}$ : growth efficiency



$f \equiv N_{\text{large}} / N_{\text{total}}$   
: growth efficiency  
 $\left\{ \begin{array}{l} f > 0.5 \rightarrow + \text{growth} \\ f < 0.5 \rightarrow - \text{growth} \end{array} \right.$

✓ Offset collisions  
↓  
independent of  $N$

# Growth efficiency averaged



Averaged for  $b^2$

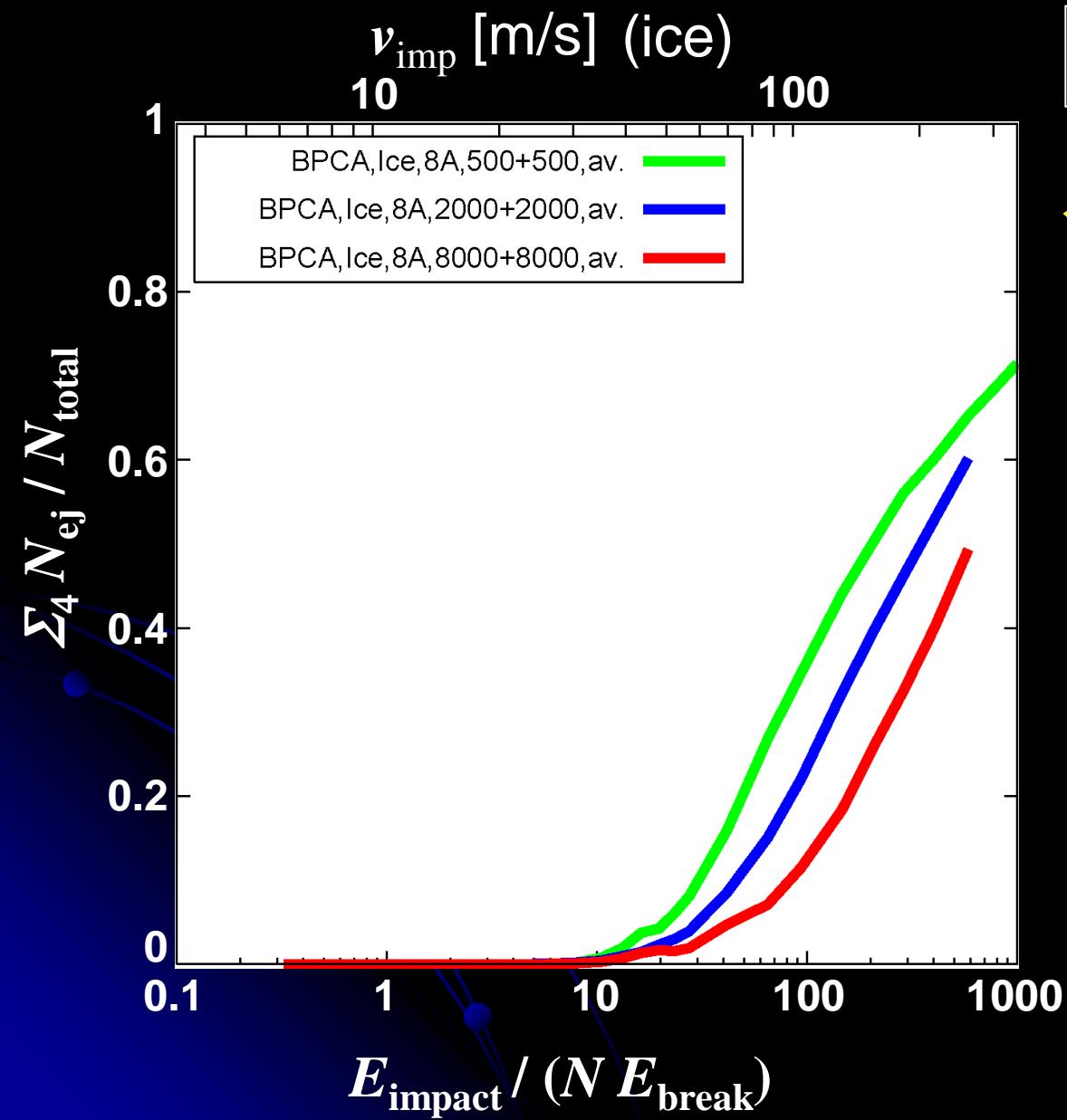
$$f \equiv N_{\text{large}} / N_{\text{total}}$$

: growth efficiency

$$\begin{cases} f > 0.5 \rightarrow + \text{growth} \\ f < 0.5 \rightarrow - \text{growth} \end{cases}$$

✓ small dependence on  $N$

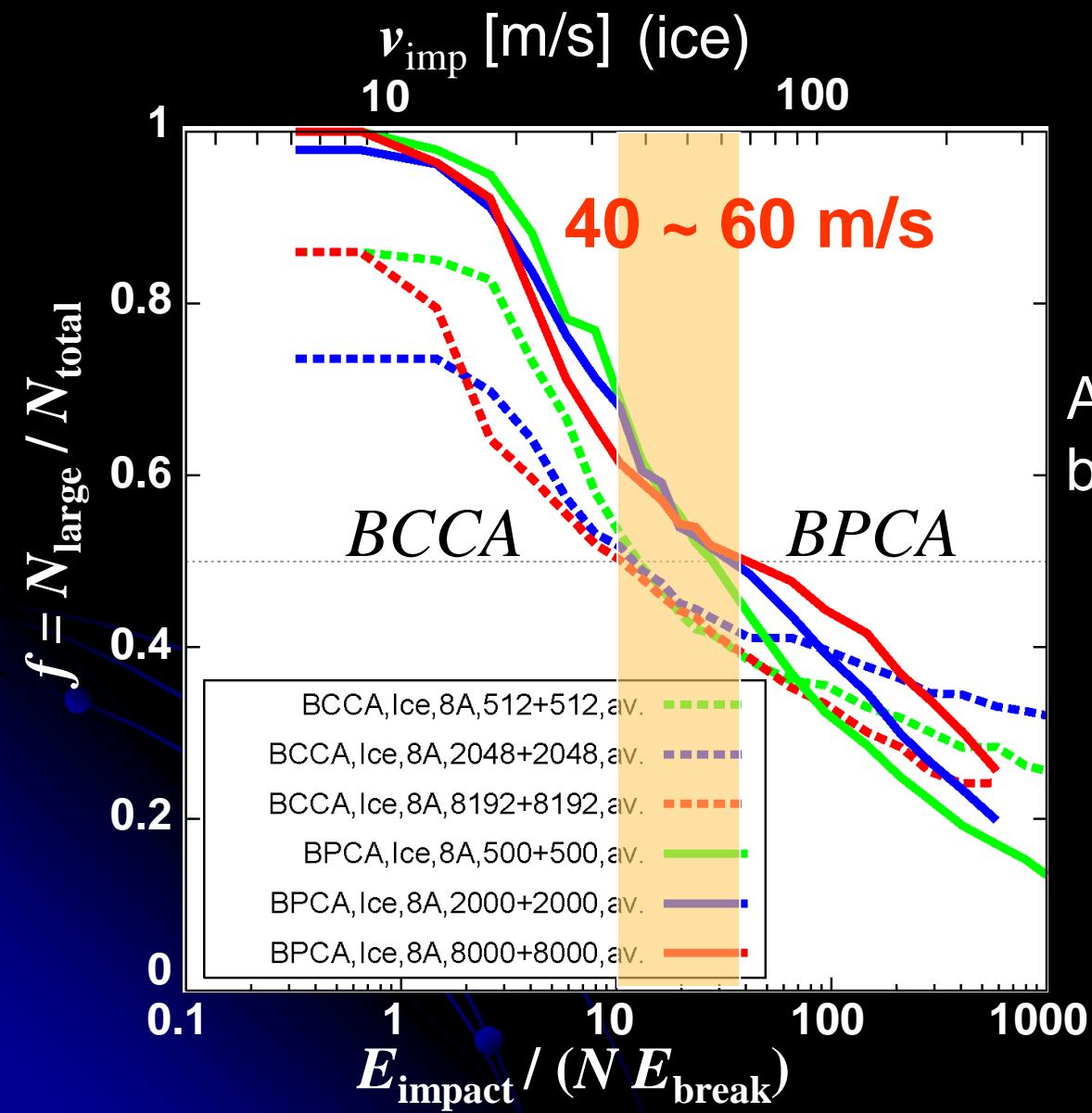
# Amount of ejecta mass: $\Sigma_4 N_{ej}$ , averaged



Averaged over  $b^2$

✓ dependent on  $N$   
The larger aggregates,  
the smaller amount of ejecta.

# Averaged growth efficiency : BCCA & BPCA



Averaged over  $b^2$

Actual dust structure:  
between BCCA and BPCA

# Summary and Implications

- Dust aggregates remain fluffy (fractal dimension  $\sim 2.5$ ) .

Very fluffy planetesimals could be formed !?

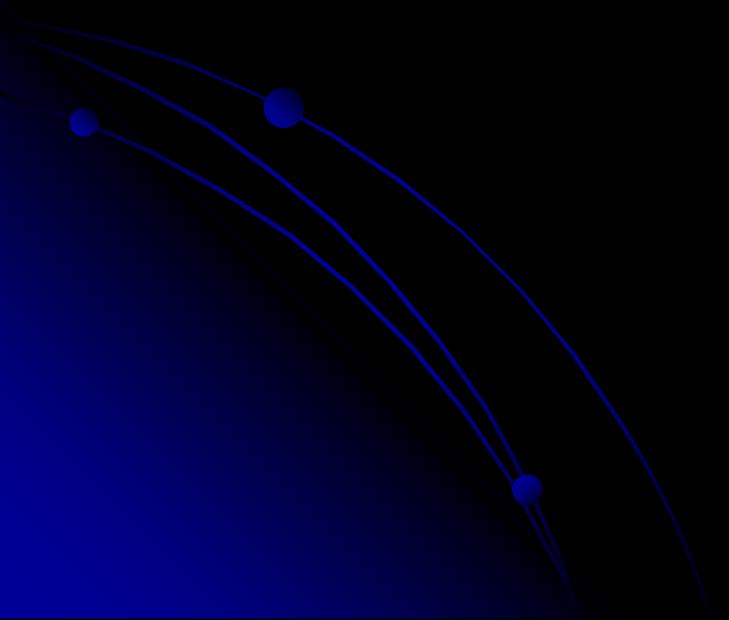
Other processes to compress aggregates are necessary.

- Icy aggregates can grow at collision velocity  $< 60 \text{ m/s}$ .

Planetesimals can be formed through collisions of dust.



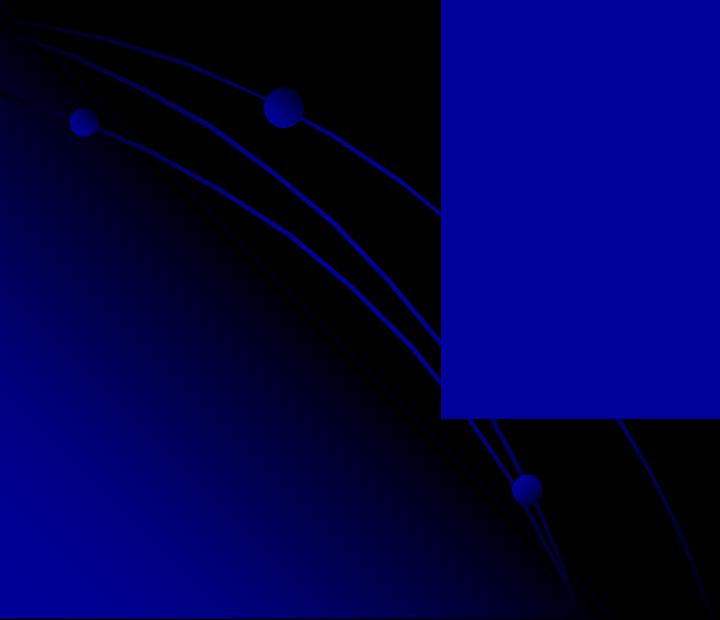
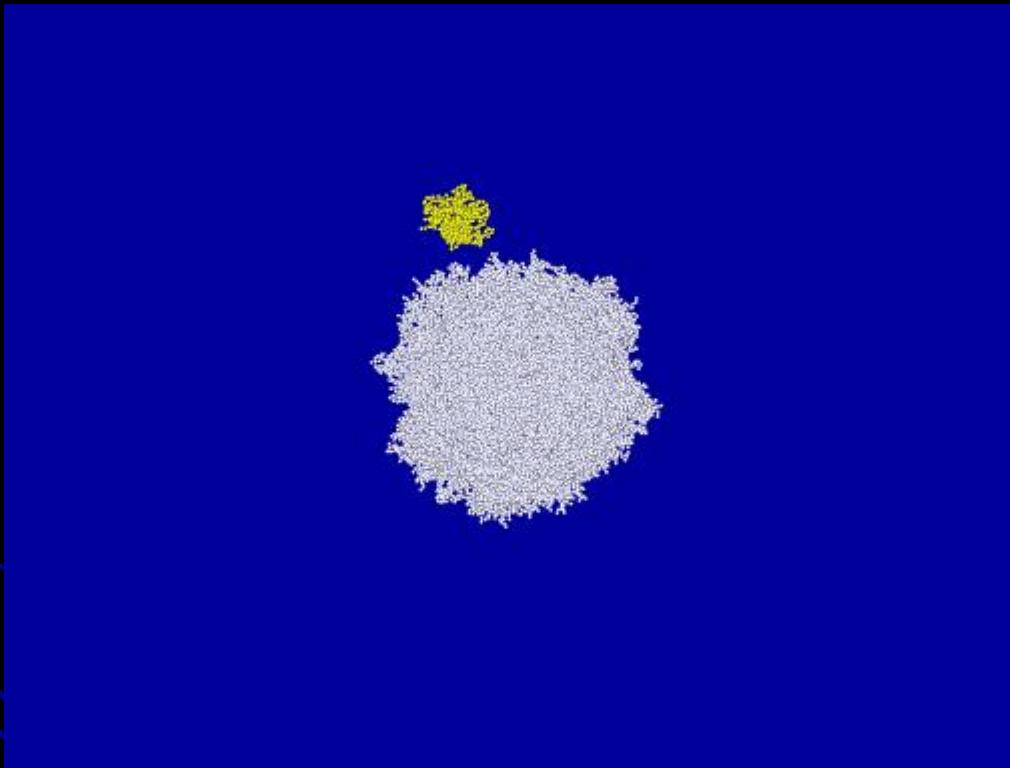
# What's next?



# Collisions between different sized aggregates

BPCA,  $N = 32000 + 500$ , ice,  $\xi_c = 8\text{\AA}$ ,  $u_{\text{col}} = 70 \text{ m/s}$

$$b = 0.39$$



# Bouncing problem

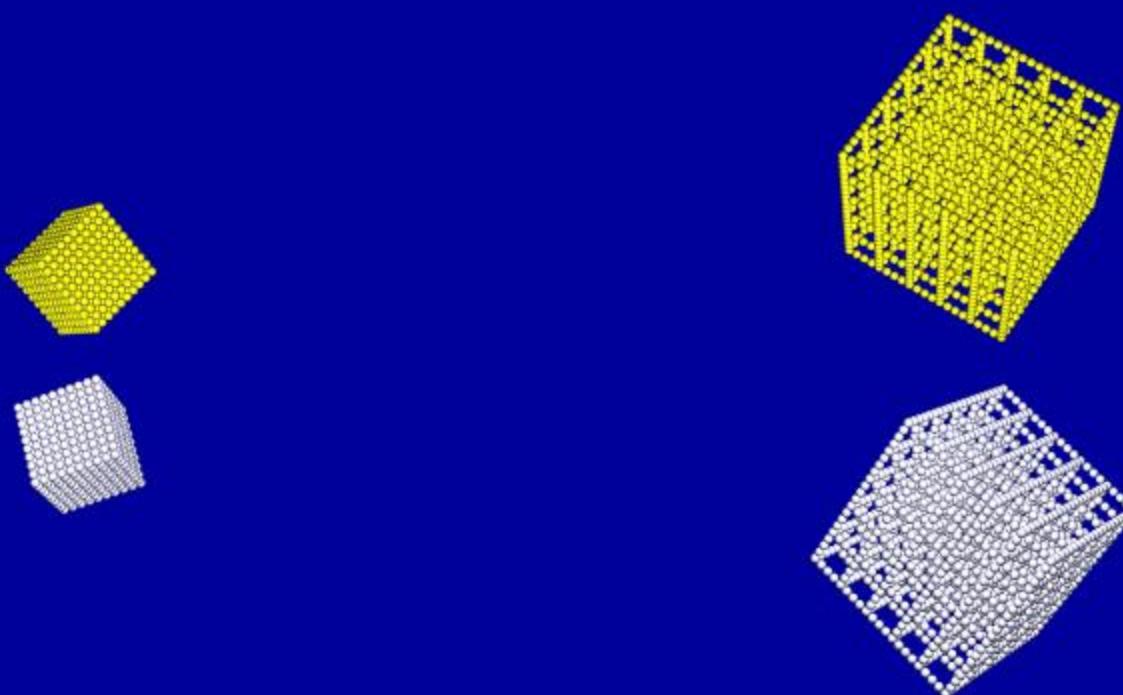
“Bouncing” prevents dust from growing

In experiments: Bouncing at  $u_{\text{col}} < \sim 1 \text{ m/s}$



Blum & Münch 1993; Blum and Wurm 2008; Güttler et al. 2009

In our simulation: No bouncing for coordination number < 6



# What's next?

焼結の影響

非球形粒子の影響

粒子のサイズ分布の影響

粒子間相互作用モデルの改良・検証

静的圧縮の効果

帶電の影響

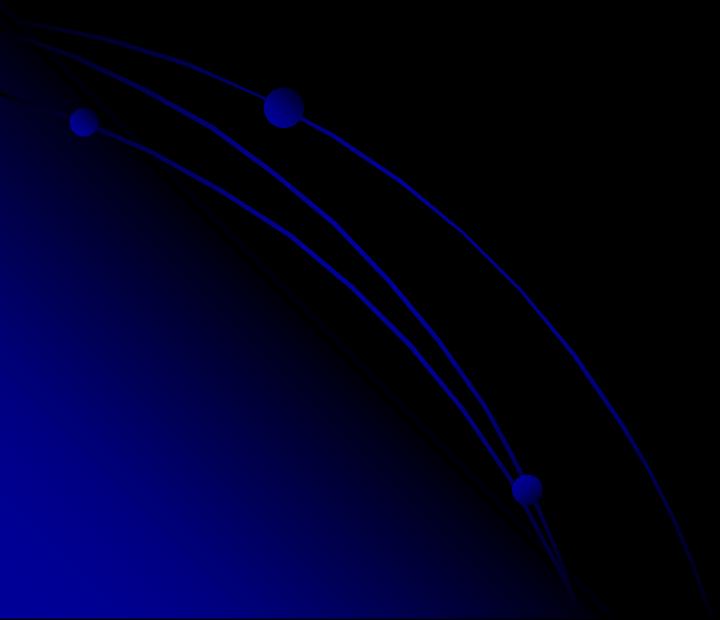
破片のサイズ分布・構造

彗星・小惑星の表層進化

衝突クレーター



ありがとうございました



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