

# Planetary Growth with Fragmentation and Gas Drag



seit 1558

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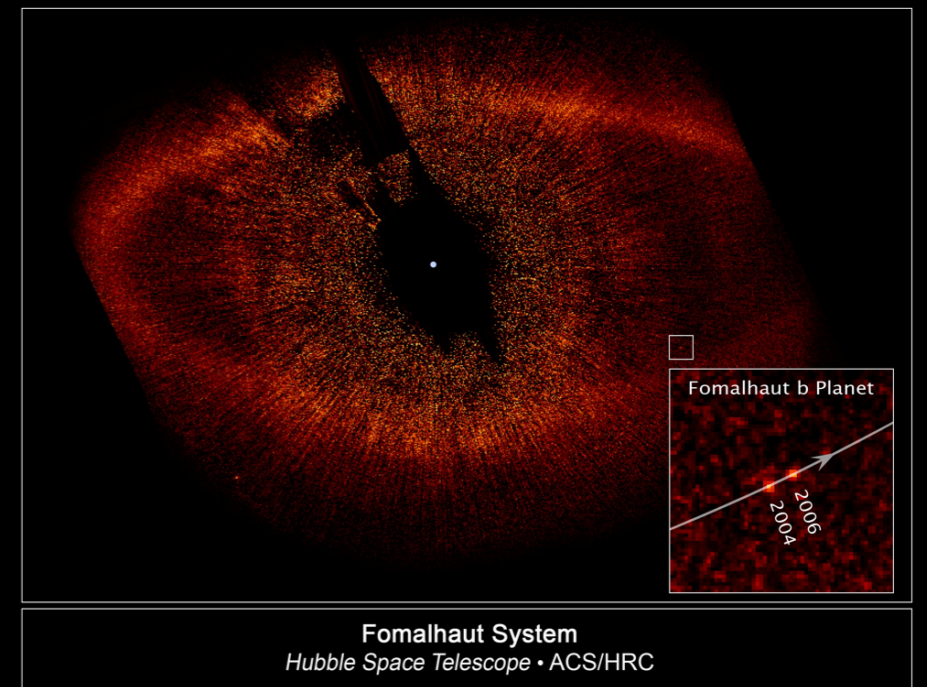


# contents

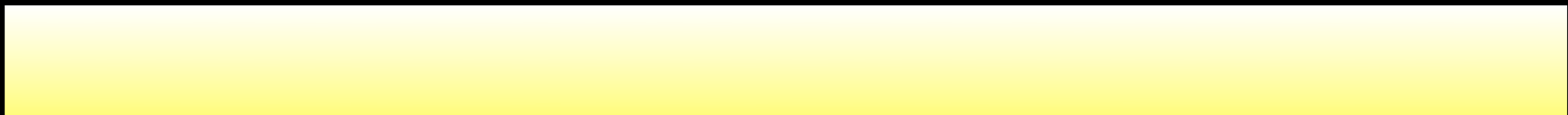
- Introduction
- Embryo Growth
- Final Embryo Mass
- Discussion

# Fragmentation

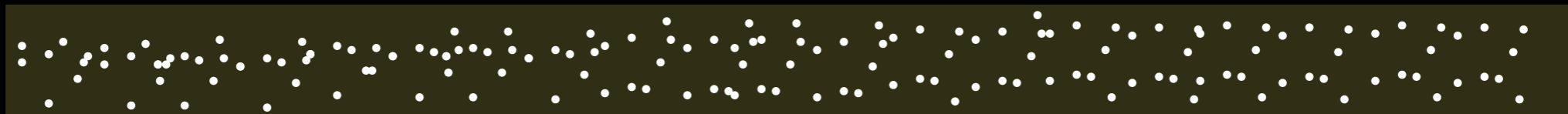
- Asteroids, Edgeworth-Kuiper belt
  - Family
  - Size distribution
- Debris disks



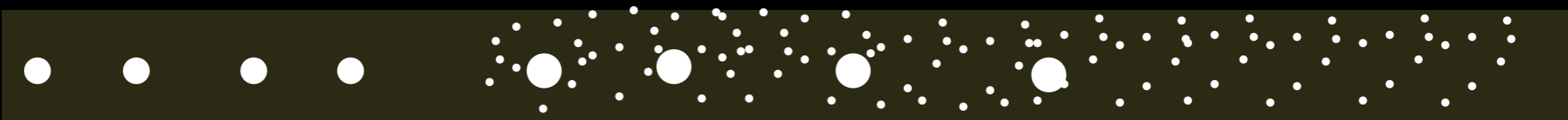
# Standard Model



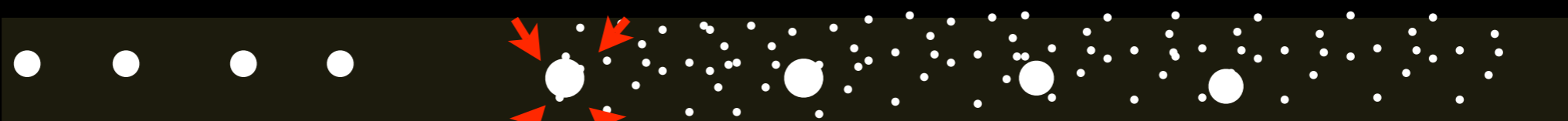
$10^{5-6}$ yr



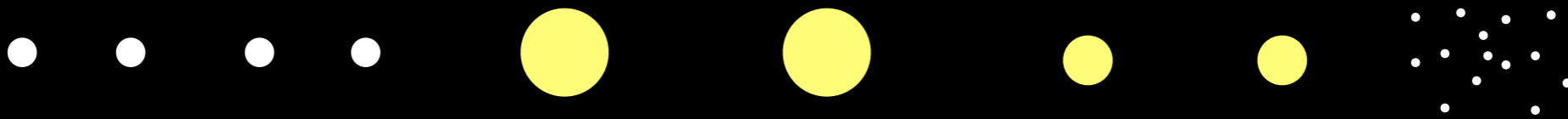
$10^{5-7}$ yr



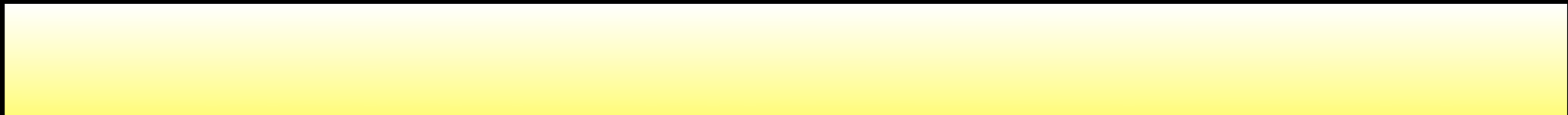
$10^{6-8}$ yr



$10^9$ yr



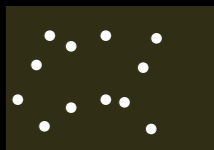
# Standard Model



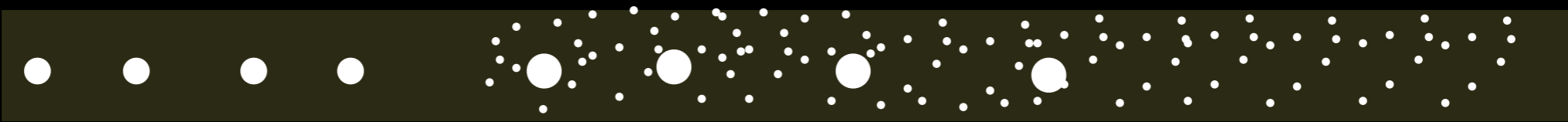
$10^{5-6}$ yr



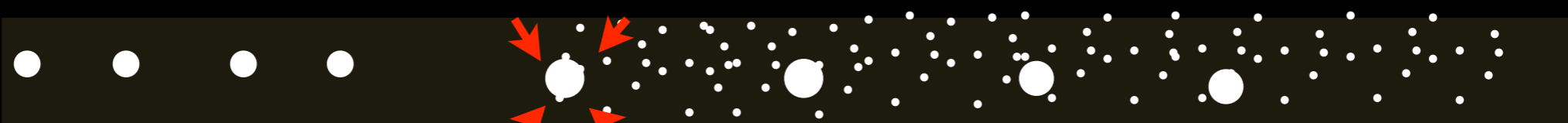
# Planetesimals



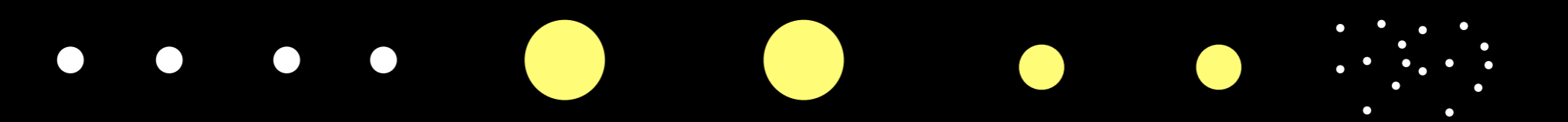
$10^{5-7}$ yr



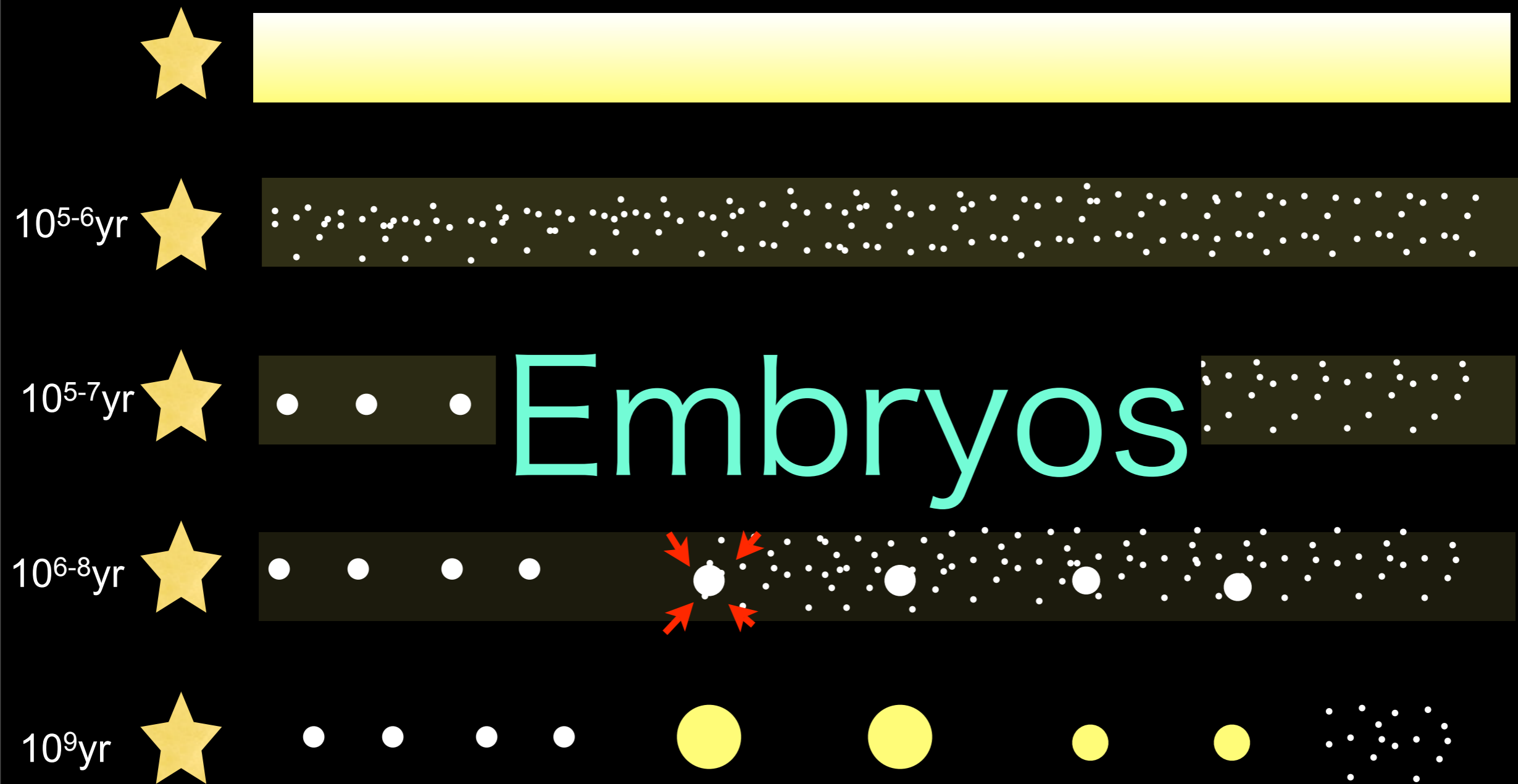
$10^{6-8}$ yr



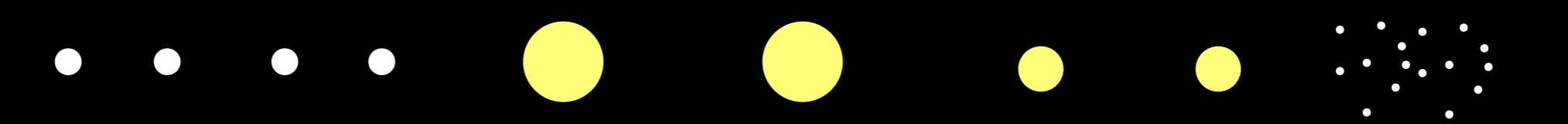
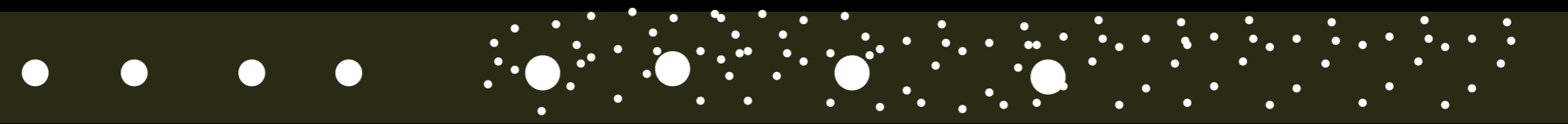
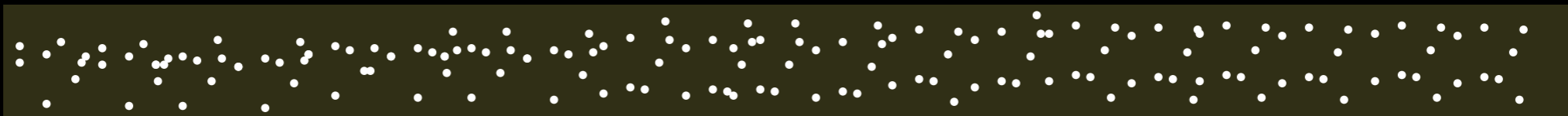
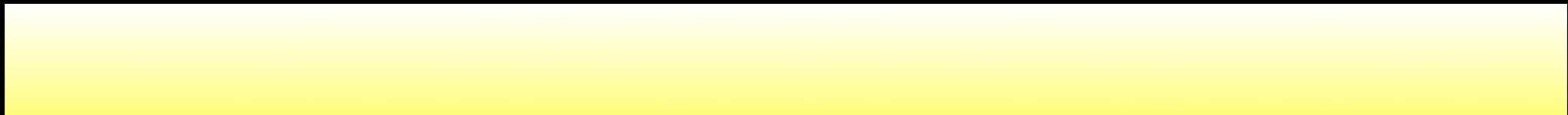
$10^9$ yr



# Standard Model



# Standard Model



$10^{5-6}$ yr

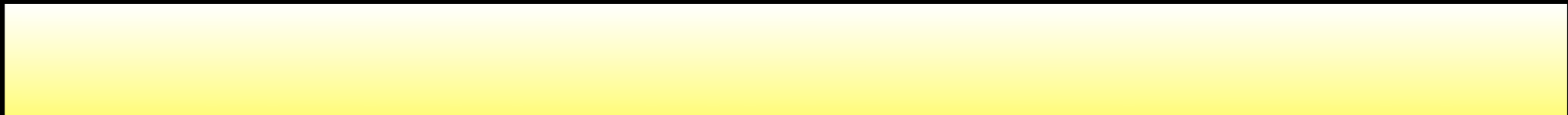
$10^{5-7}$ yr

$10^{6-8}$ yr

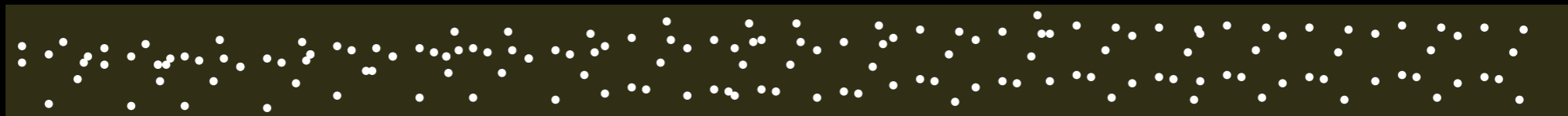
$10^9$ yr

Gas Accretion

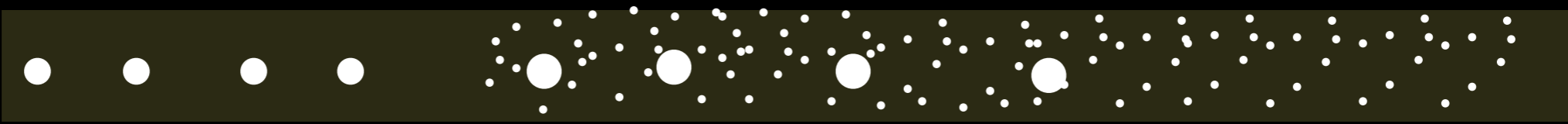
# Standard Model



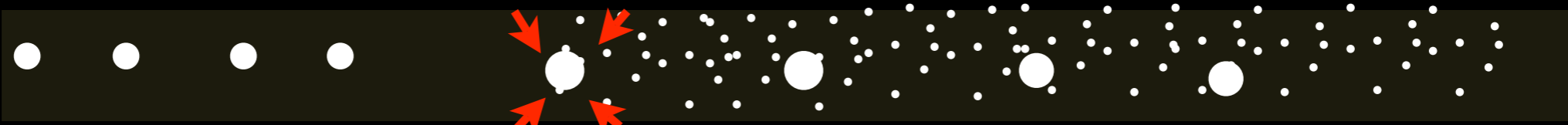
$10^{5-6}$ yr



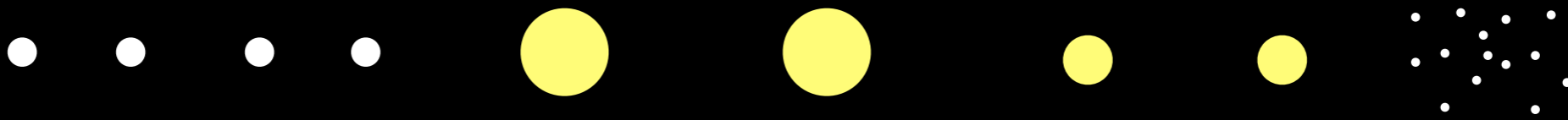
$10^{5-7}$ yr



$10^{6-8}$ yr

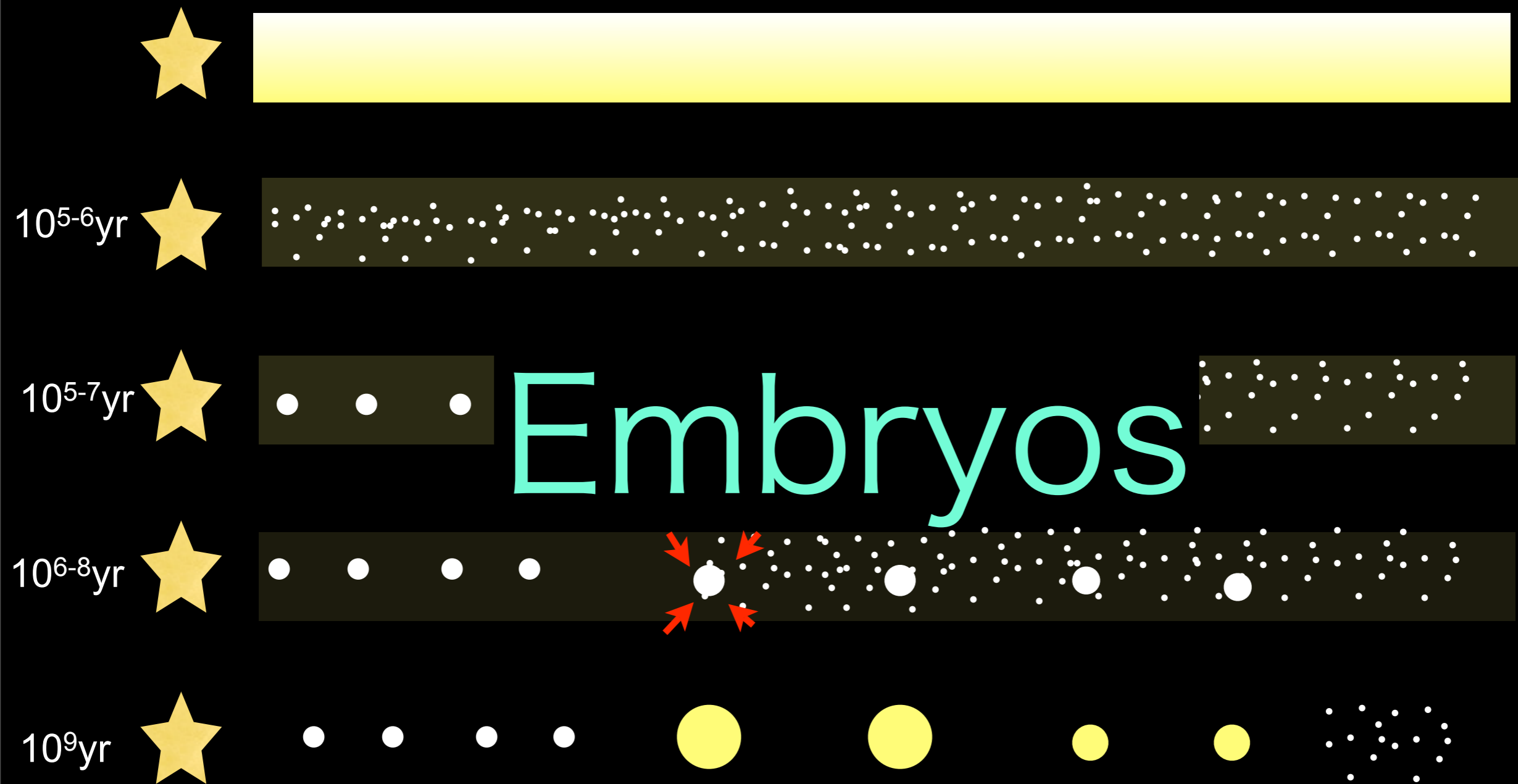


$10^9$ yr





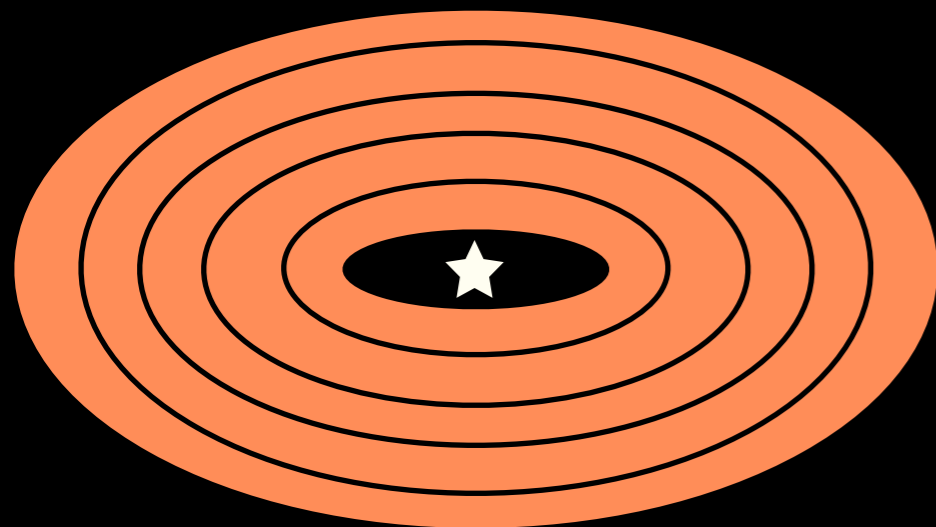
# Standard Model



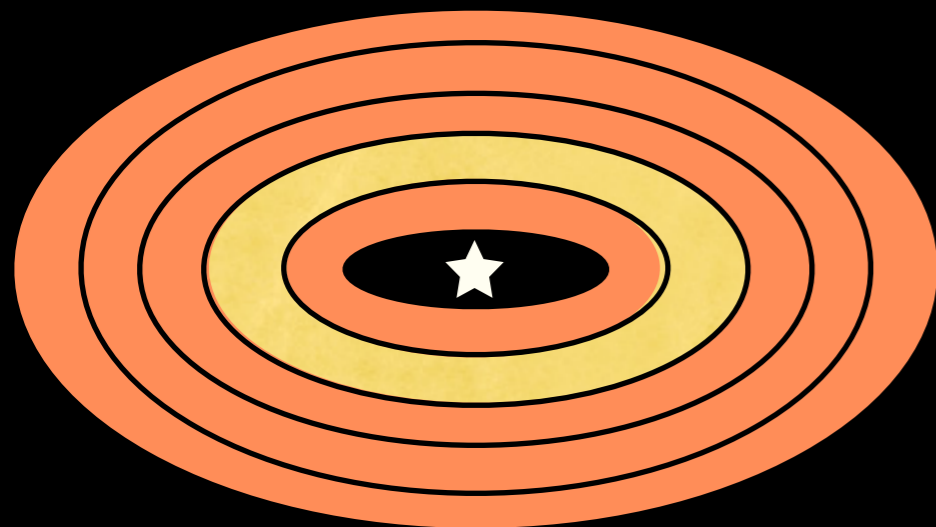
# Embryo Growth with Fragmentation

- Planetary embryos grows by accretion with planetesimals.
- Massive embryos induce distractive collisions between planetesimals.
- Fragmentation reduces the final embryo mass.

# Calculation Model

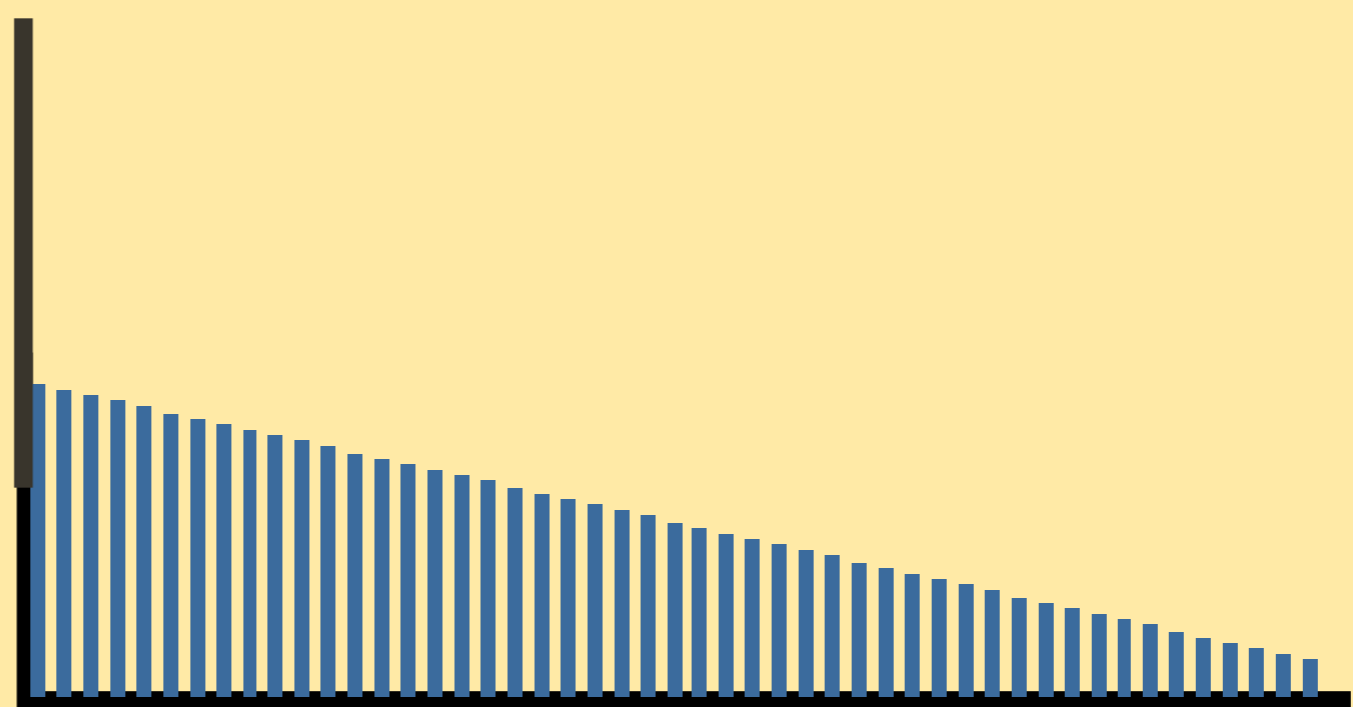


# Calculation Model

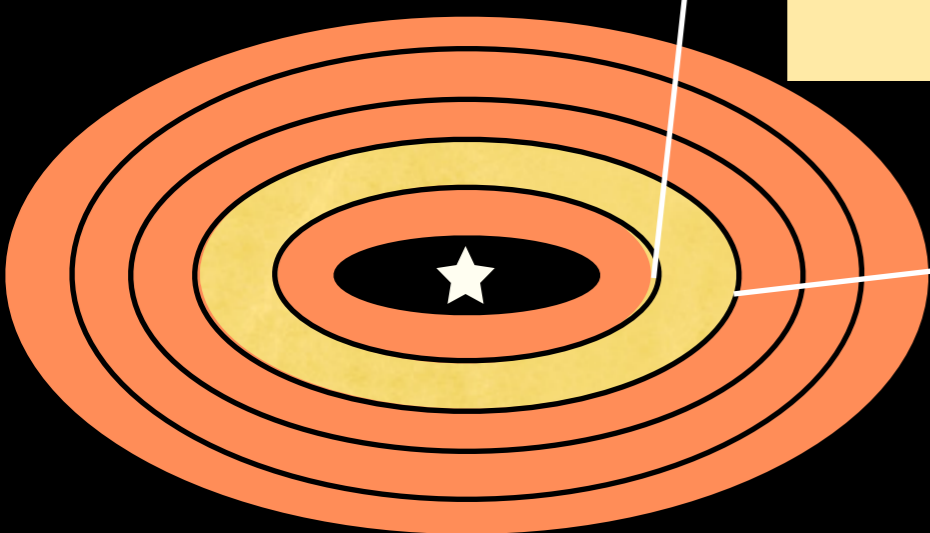


# Calculation Model

Number

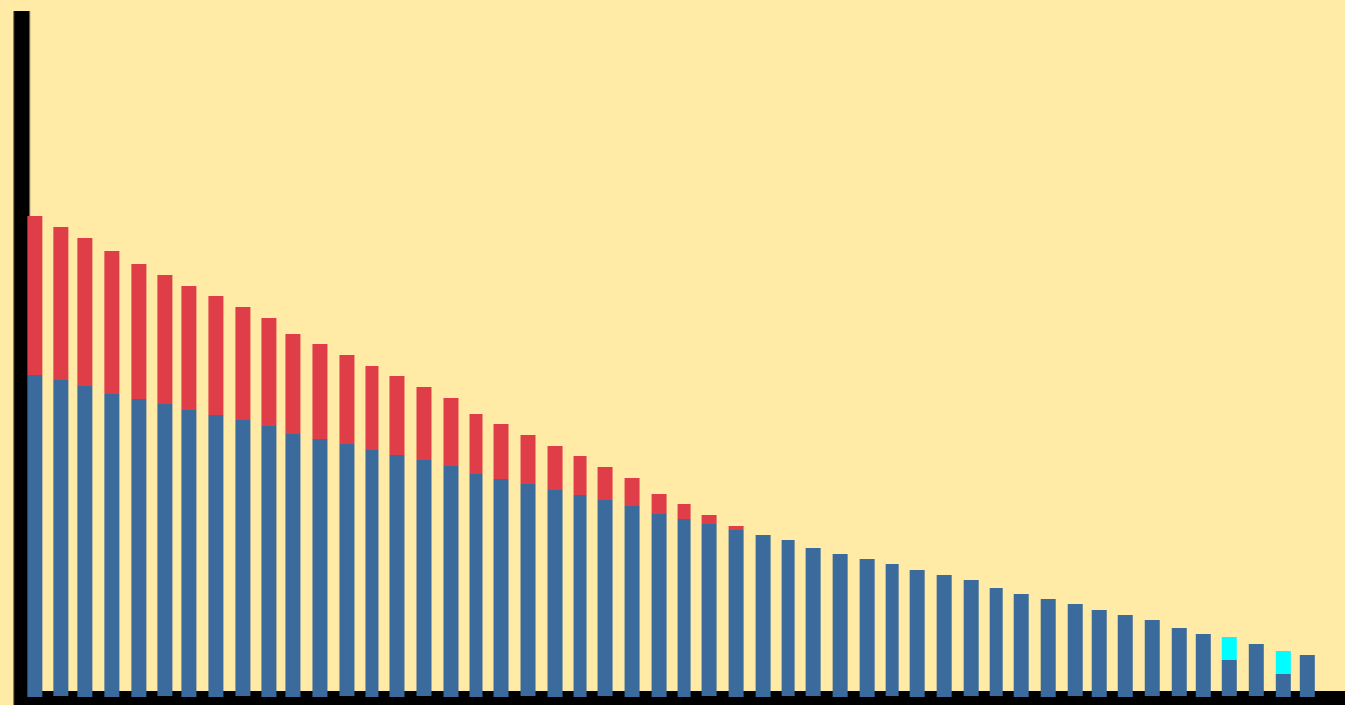


mass

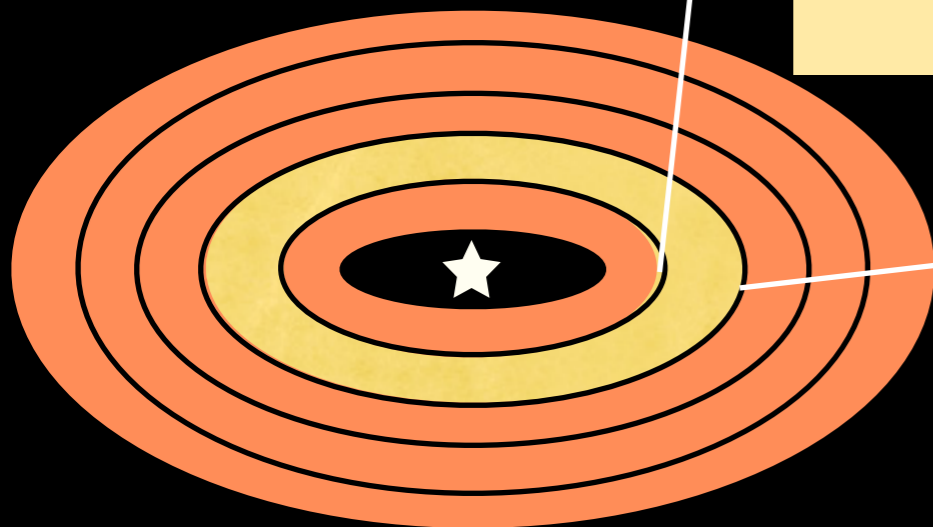


# Calculation Model

Number



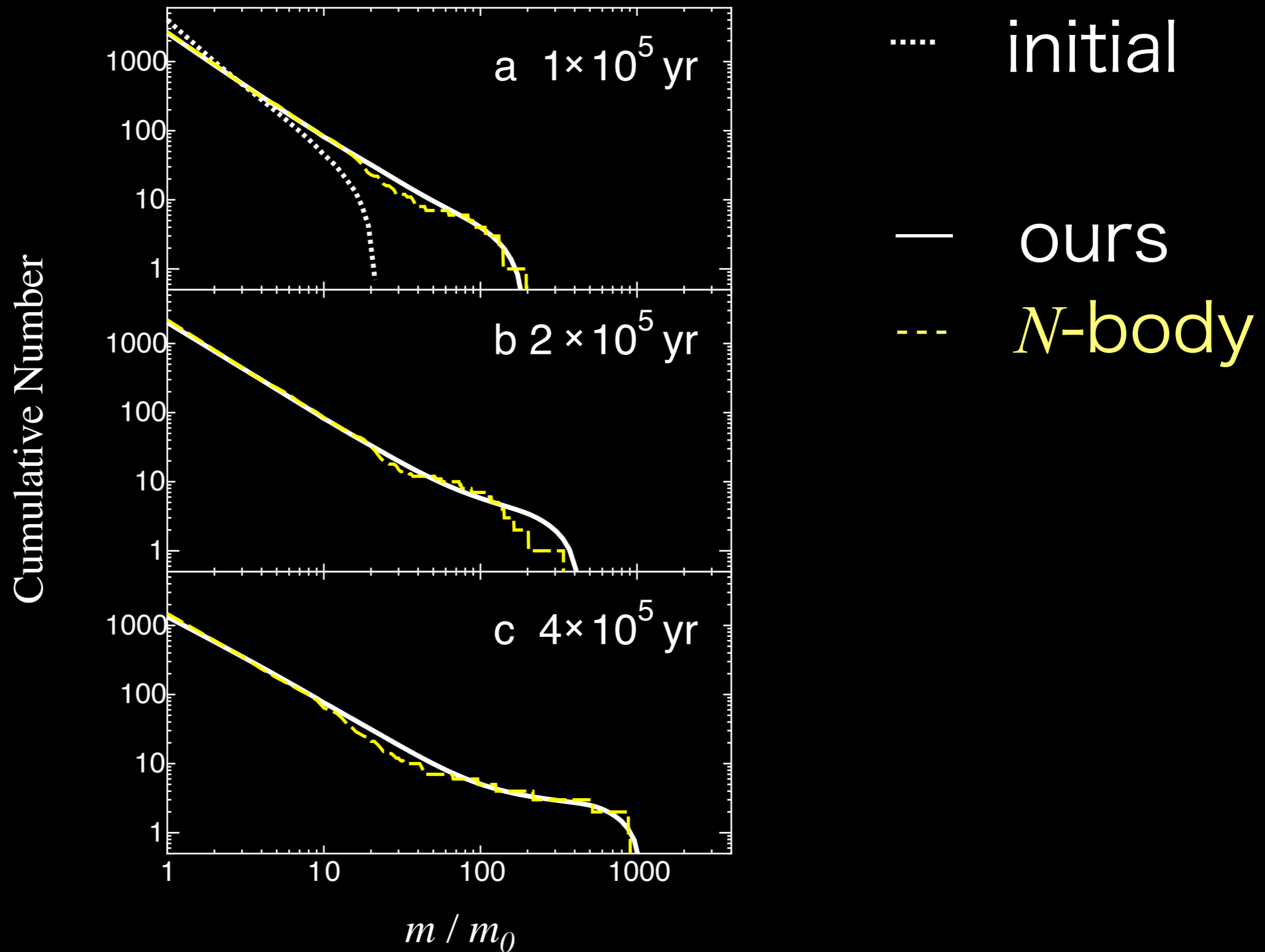
mass



# $N$ -Body Simulation

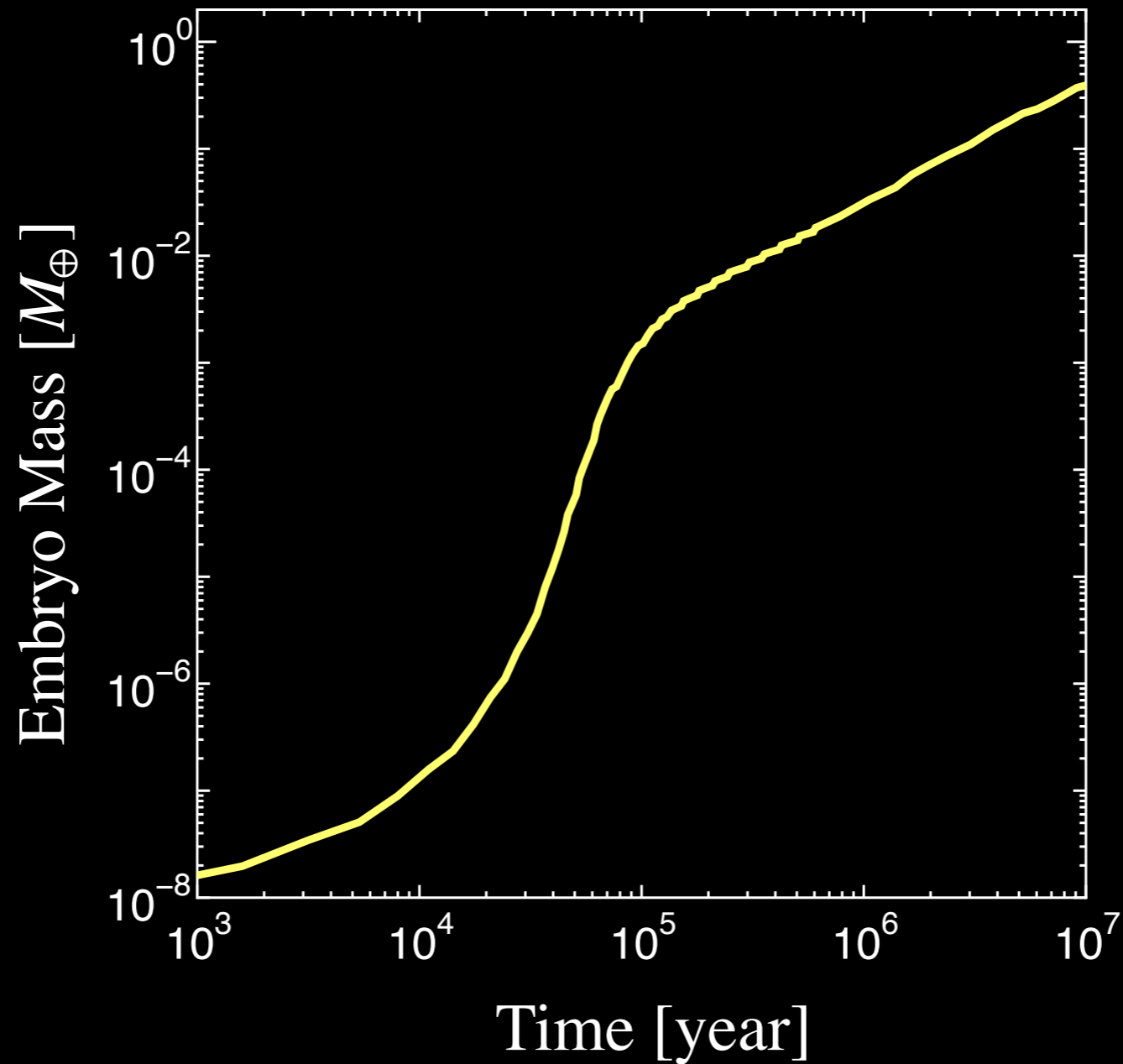
- Direct  $N$ -body simulation is most reliable for the embryo growth.
- If fragmentation is neglected.
- Comparison with  $N$ -body simulation for the case without fragmentation to validate our simulation.

# Validation



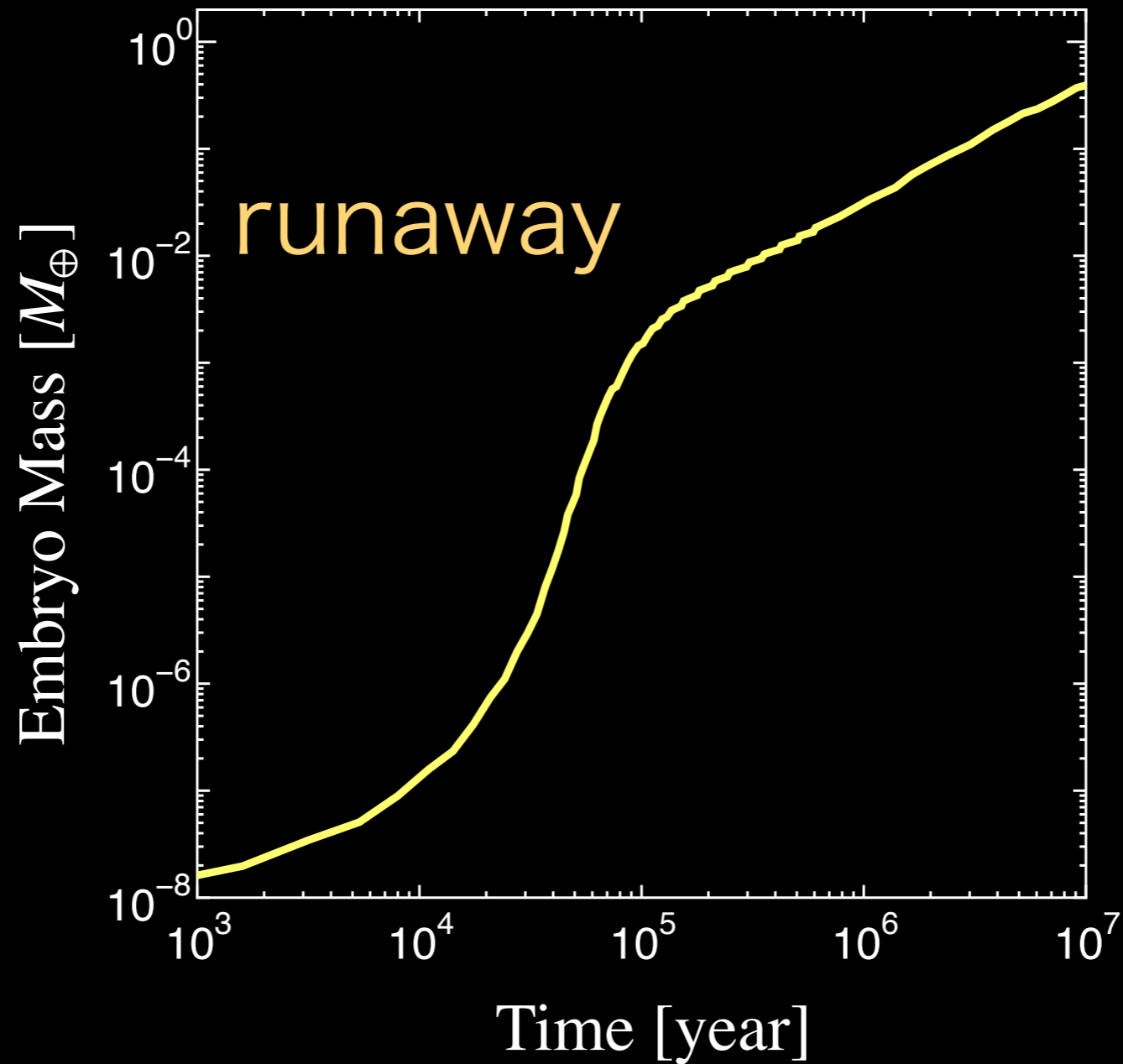


# Embryo Growth without Fragmentation



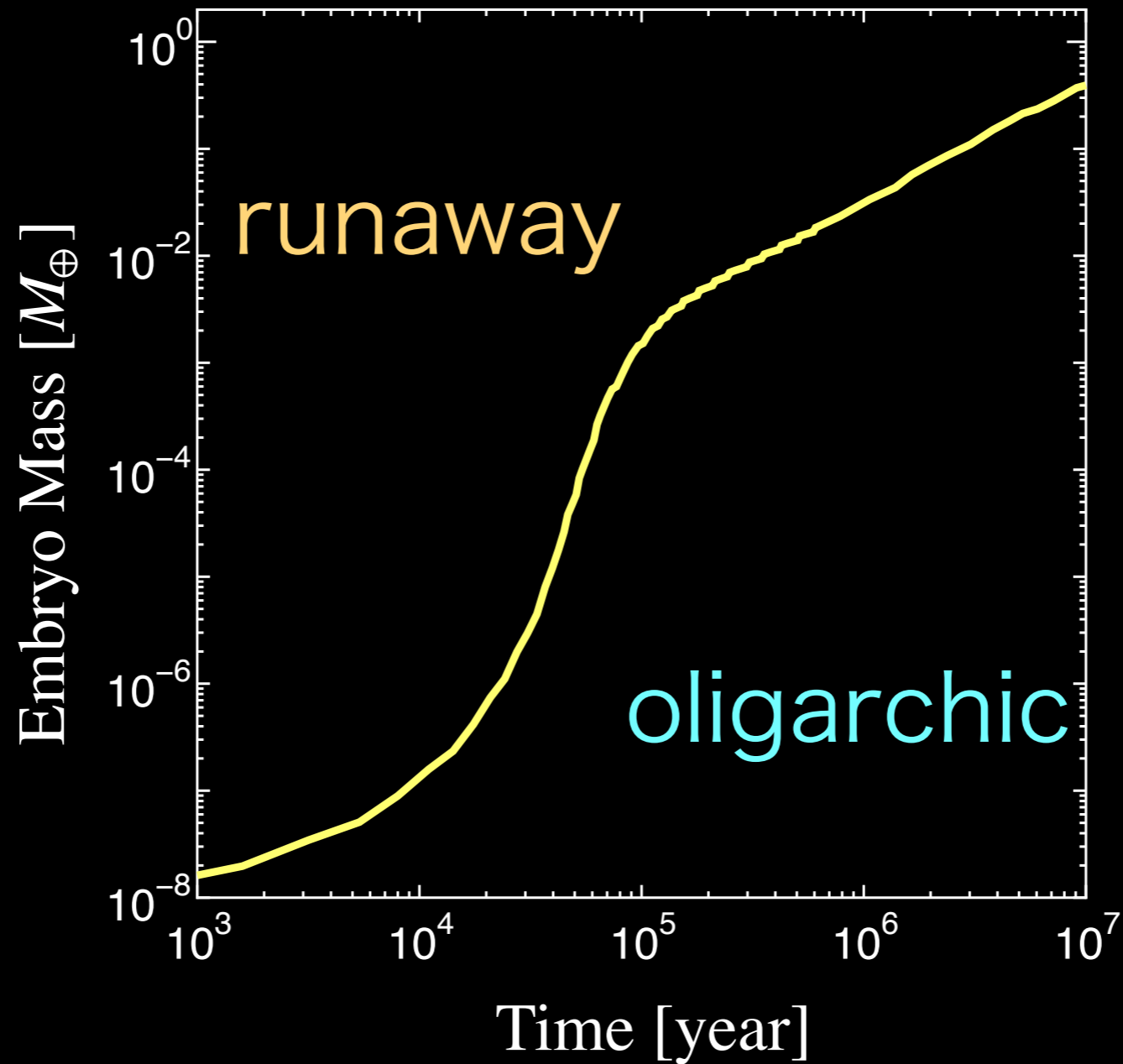
at 3.2AU  
MMSN

# Embryo Growth without Fragmentation



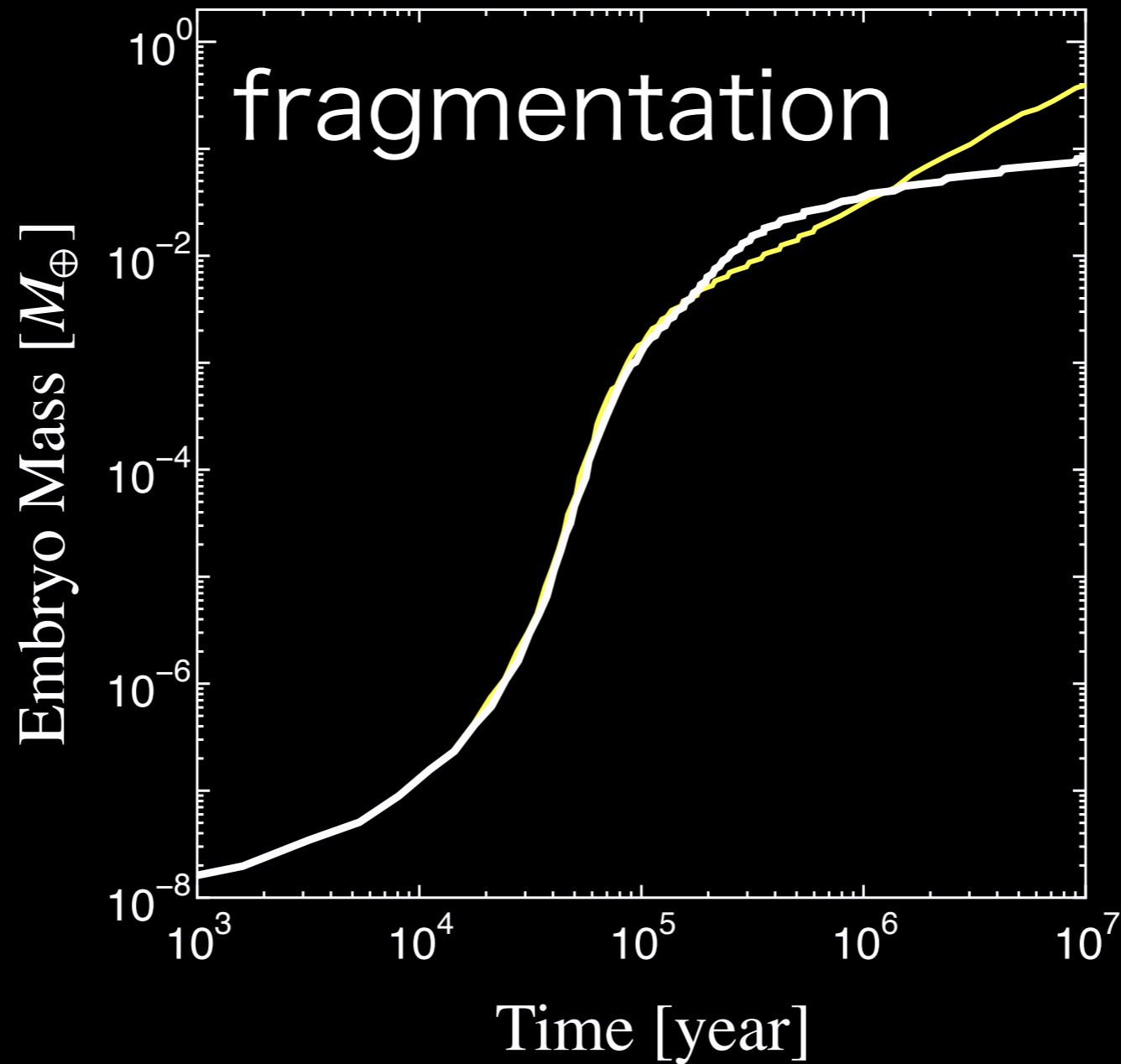
at 3.2AU  
MMSN

# Embryo Growth without Fragmentation



at 3.2AU  
MMSN

# Embryo Growth



no frag.

at 3.2AU  
MMSN

# Analysis

Embryo

Fragments

Planetesimals



mass

# Analysis

Embryo

collision cascade

Fragments

Planetesimals



mass

# Analysis

Embryo

collision cascade

Fragments



Planetesimals



mass

# Analysis

Embryo

collision cascade

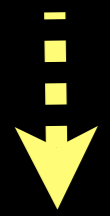
Fragments



Planetesimals



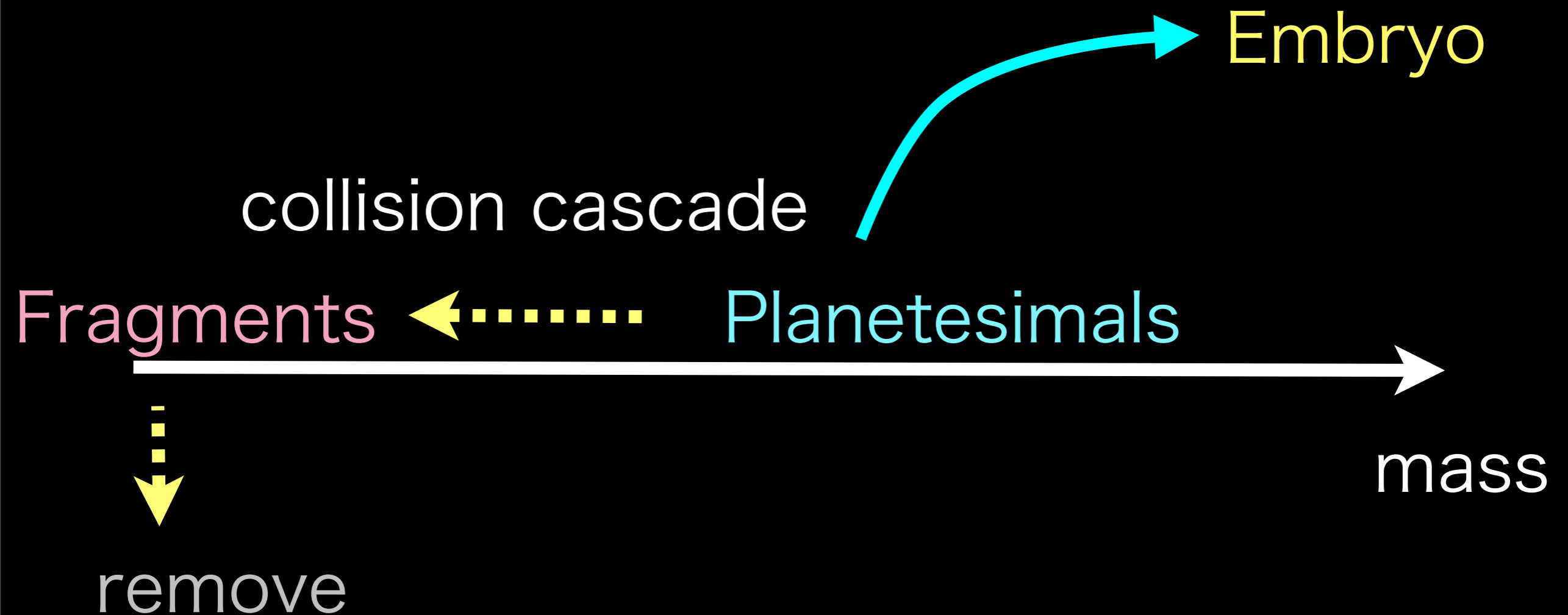
mass



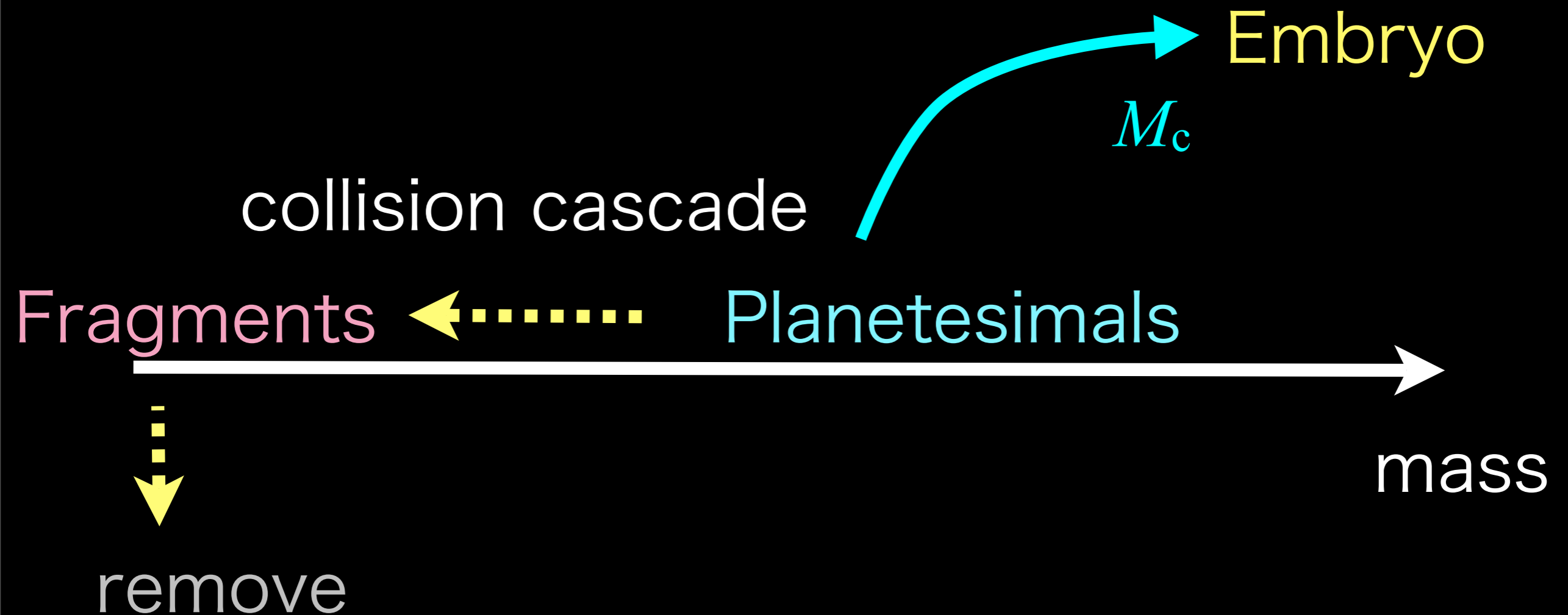
remove



# Analysis



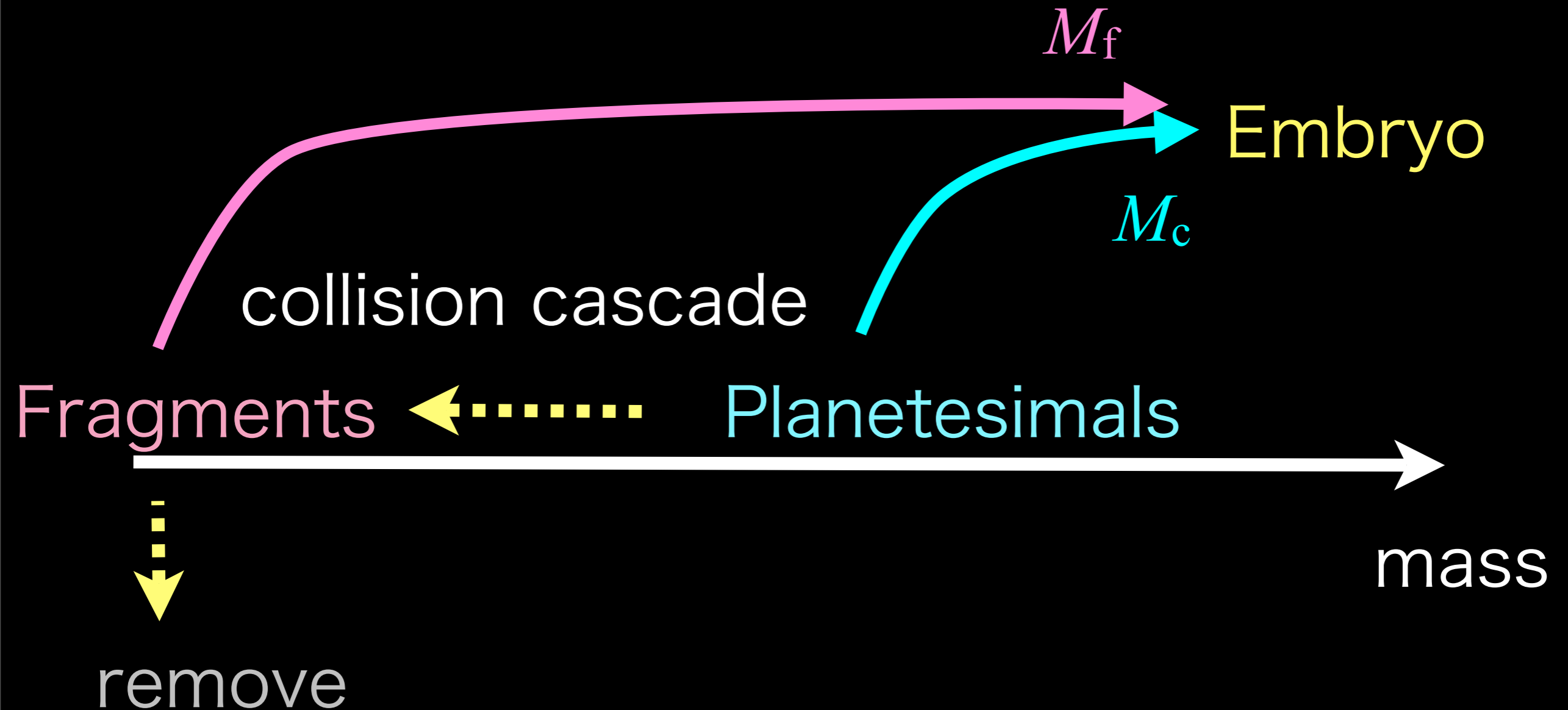
# Analysis



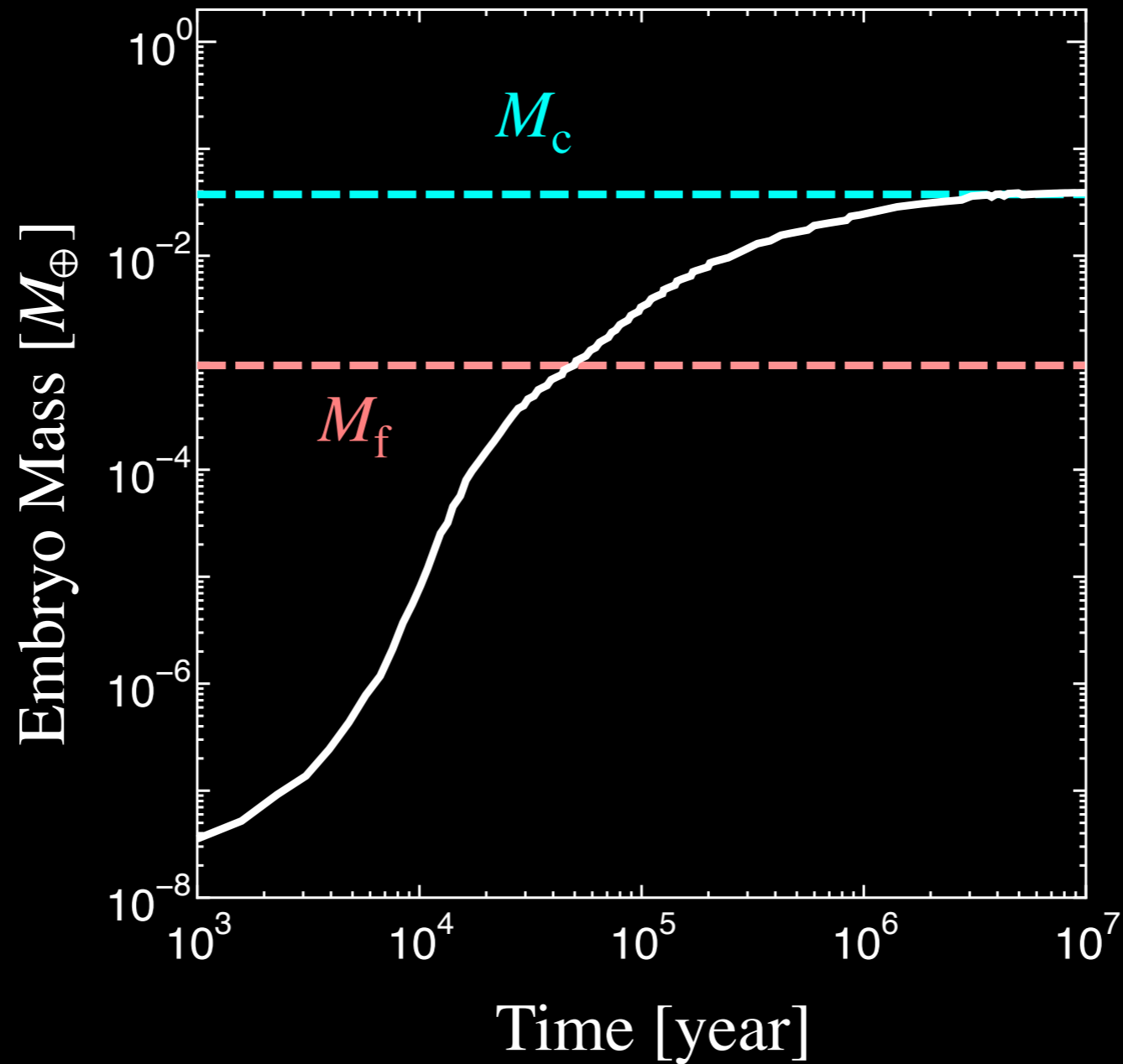
# Analysis



# Analysis

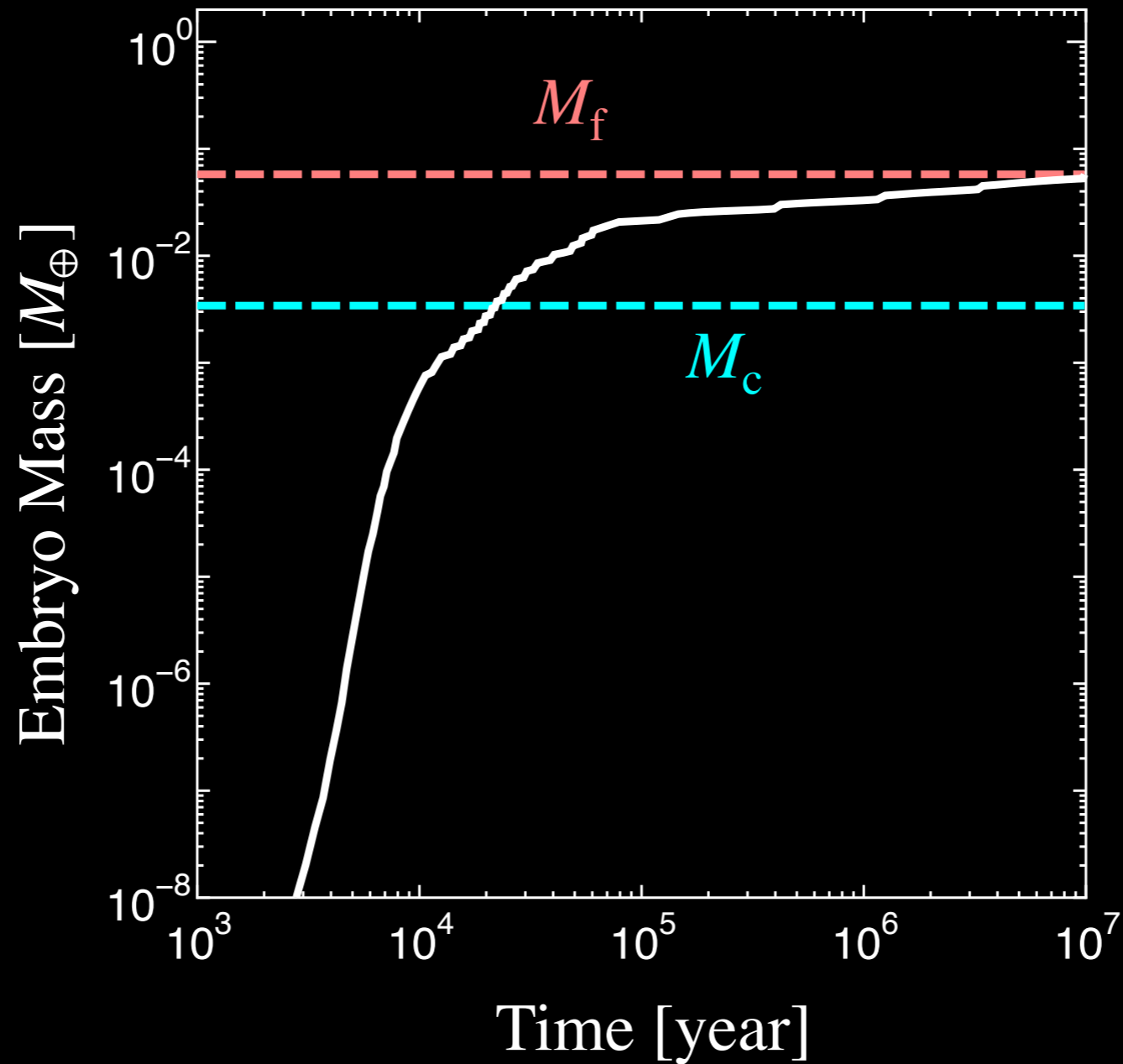


# Final Embryo Mass



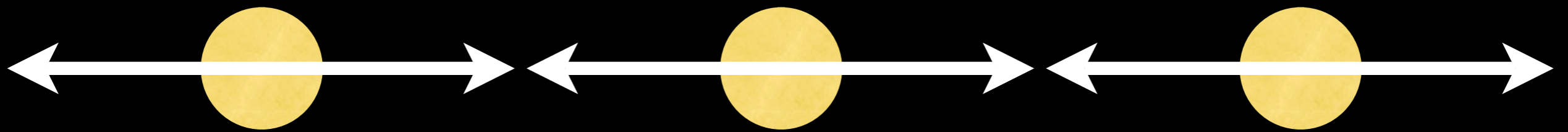
$r_0 = 10$  km  
at 1 AU  
MMSN

# Final Embryo mass



$r_0 = 1$  km  
at 3.2 AU  
MMSN

# Isolation Mass



$$M_{\text{iso}} = 2\pi ab\Sigma$$

$a$ : distance

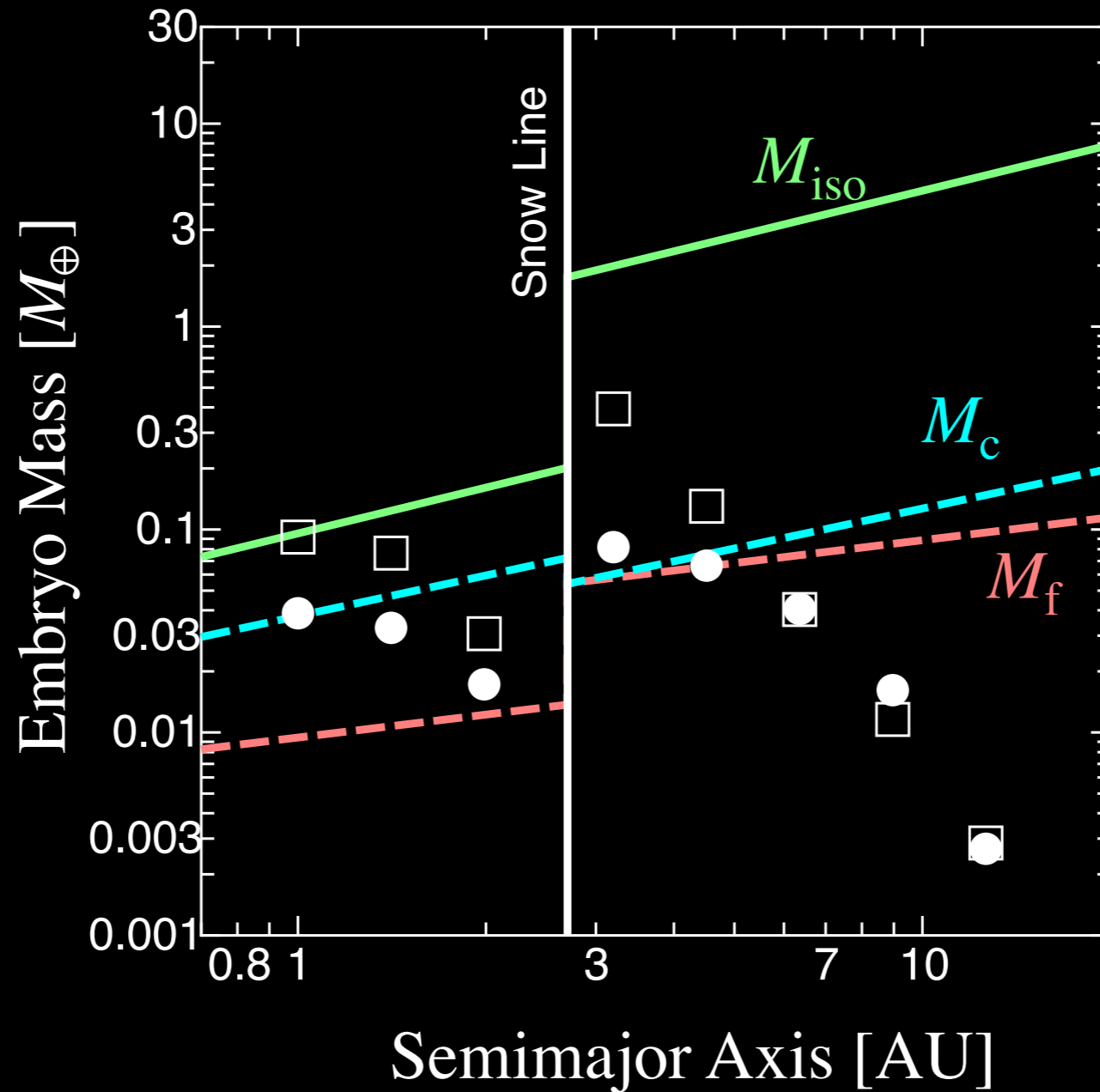
$b$ : separation

$\Sigma$ : surface density

# Distance

Sim. in  $10^7$  yr

Frag.  
● Yes  
□ No

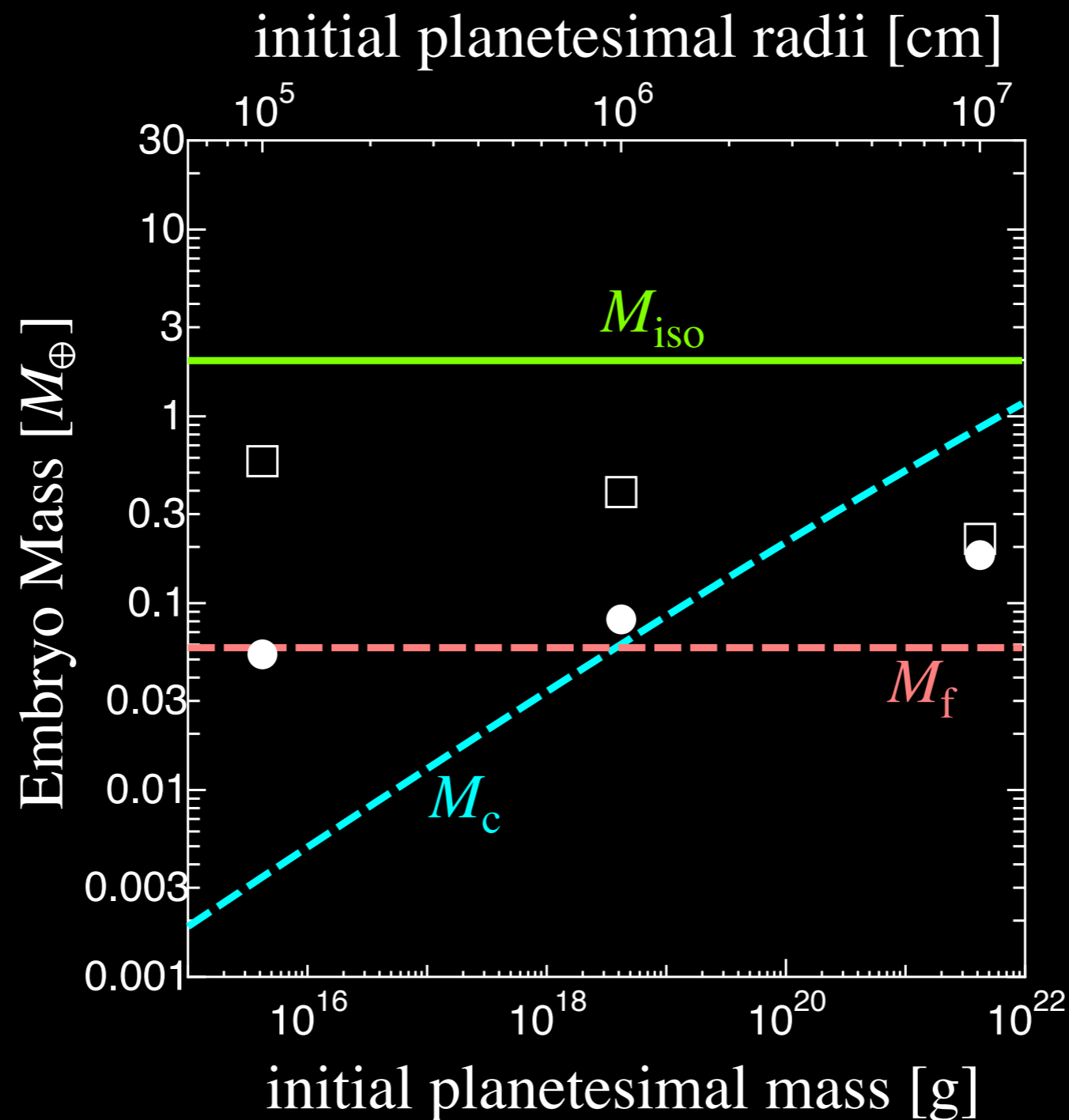


$r_0 = 10$  km

MMSN

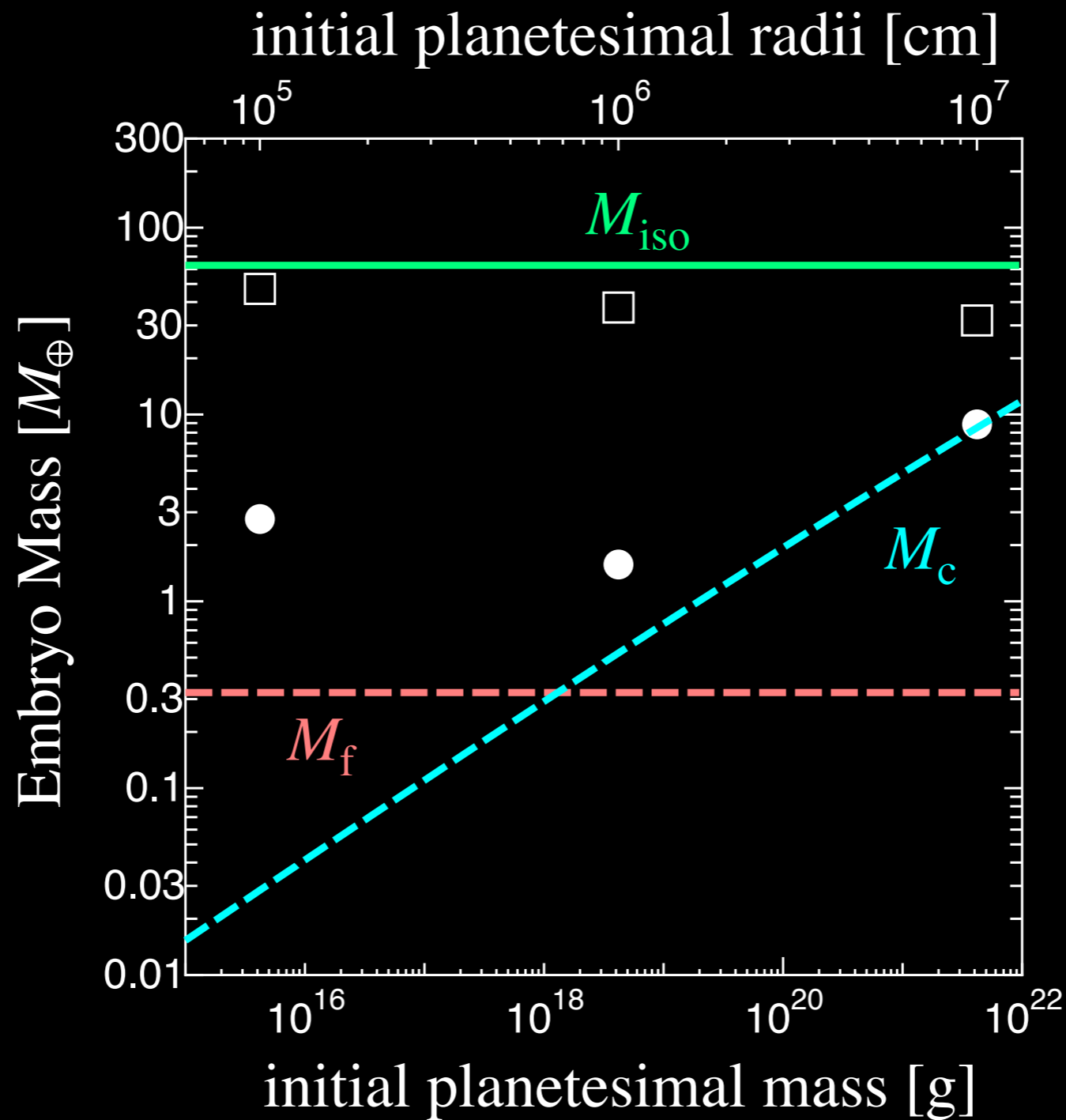


# Initial Planetesimal



$10^7$  yr  
at 3.2AU  
MMSN

# Massive Disk



$10^7$  yr

at 3.2AU

10MMSN

# Conclusion

- The final embryo mass is much smaller than the isolation mass.
- Our analytical formulae are consistent with the final mass.
- Embryo mass reaches the critical core mass at 3-4AU for  $r_0 > 100$  km and  $> 10$ MMSN