

# Structure of Moist Convection in Planetary Atmospheres

Kensuke Nakajima

[kensuke@geo.kyushu-u.ac.jp](mailto:kensuke@geo.kyushu-u.ac.jp)

6<sup>th</sup> CPS Planetary School, Kobe, Japan

7 January 2010

# Outline

- Introduction
  - Examples of clouds in planetary atmospheres
- Short summary on clouds
  - Elements on convective instability
  - Elements on cloud microphysics
- Condensation and buoyancy
- Classification of convective clouds in planetary atmospheres
- Roles of cloud convection

# PRECAUTION

I will discuss some thermodynamics, but , re-examine the content carefully if you become interested in it.

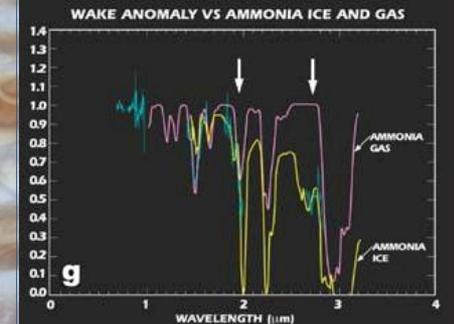
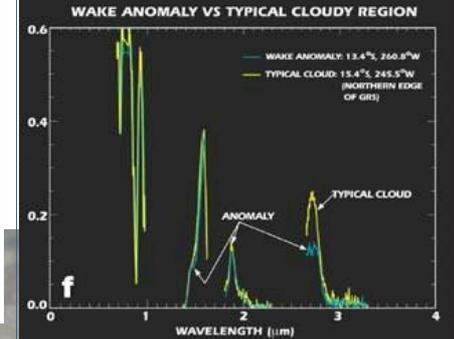
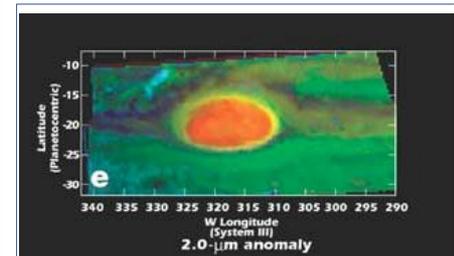
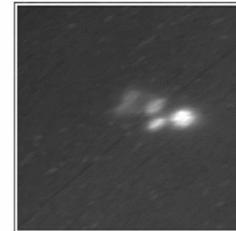
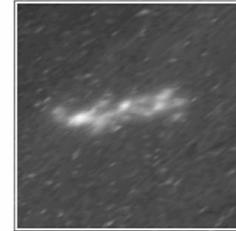
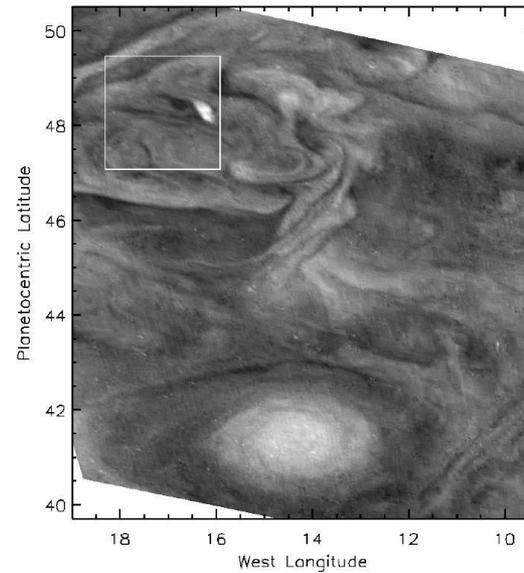
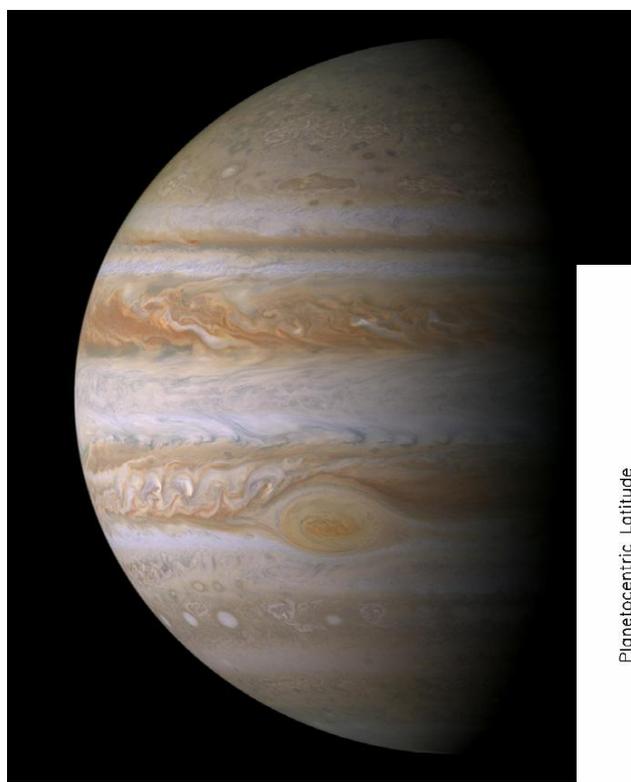
In 1988 Yutaka Abe said to me :

*“If you want to use something as a tool for research, you have to understand it to the extent in which you can use it even in your dream (while sleeping)”.*

My knowledge on thermodynamics is far from that state.

# Examples of clouds in planetary atmospheres

# Jovian Thunderstorm



Baines et al(2002)

# Saturnian Thunderstorm

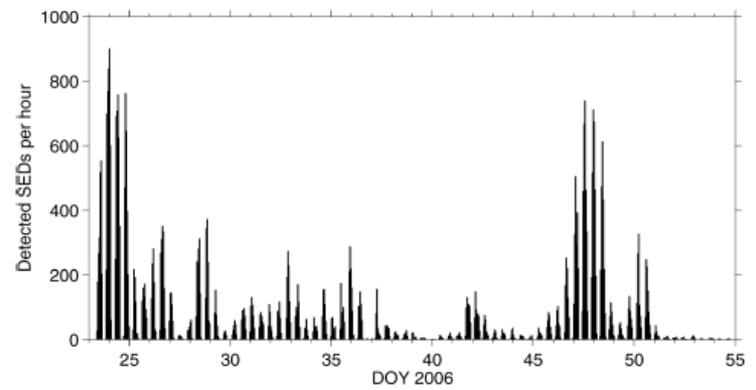


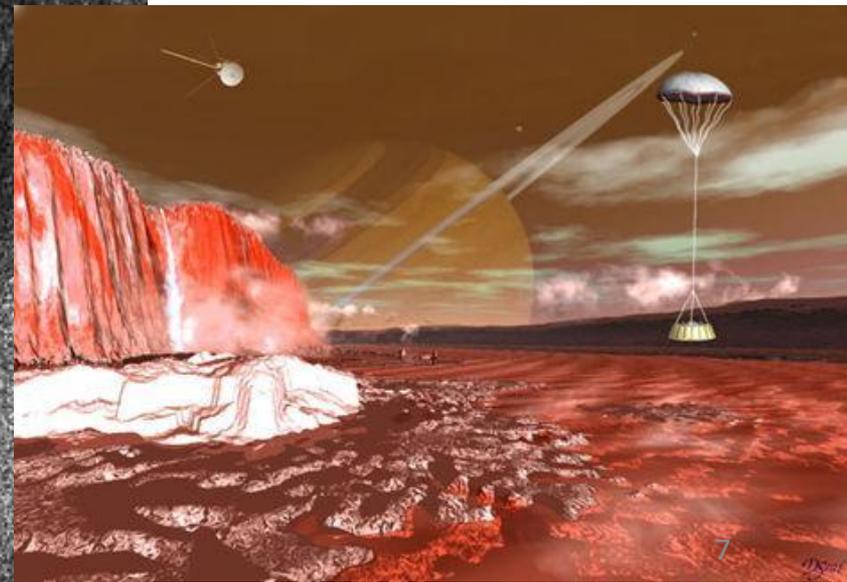
Fig. 2. Number of recorded SEDs per hour as a function of time for storm E in early 2006.

Fischer et al(2007)

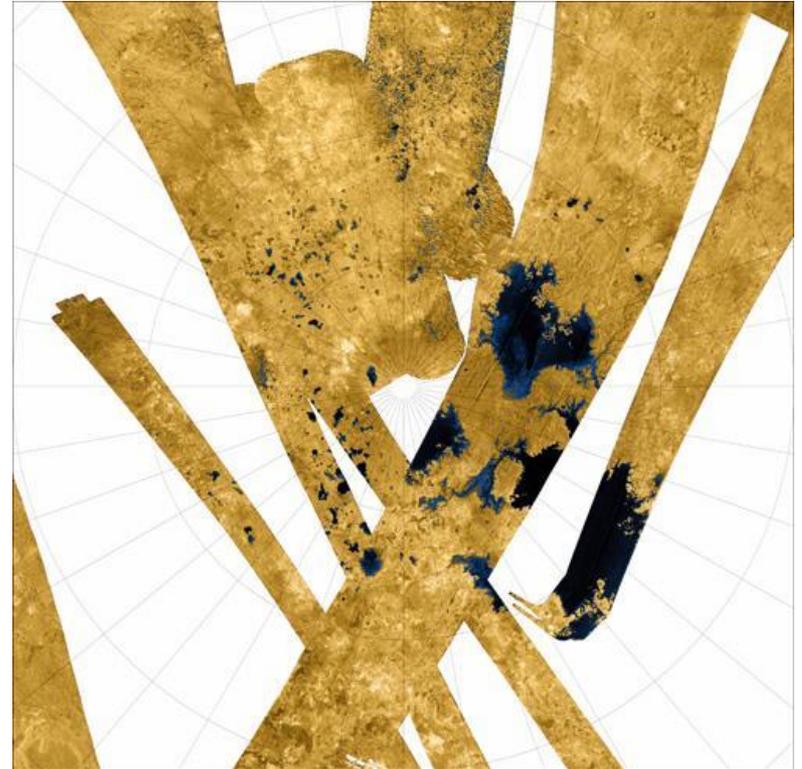
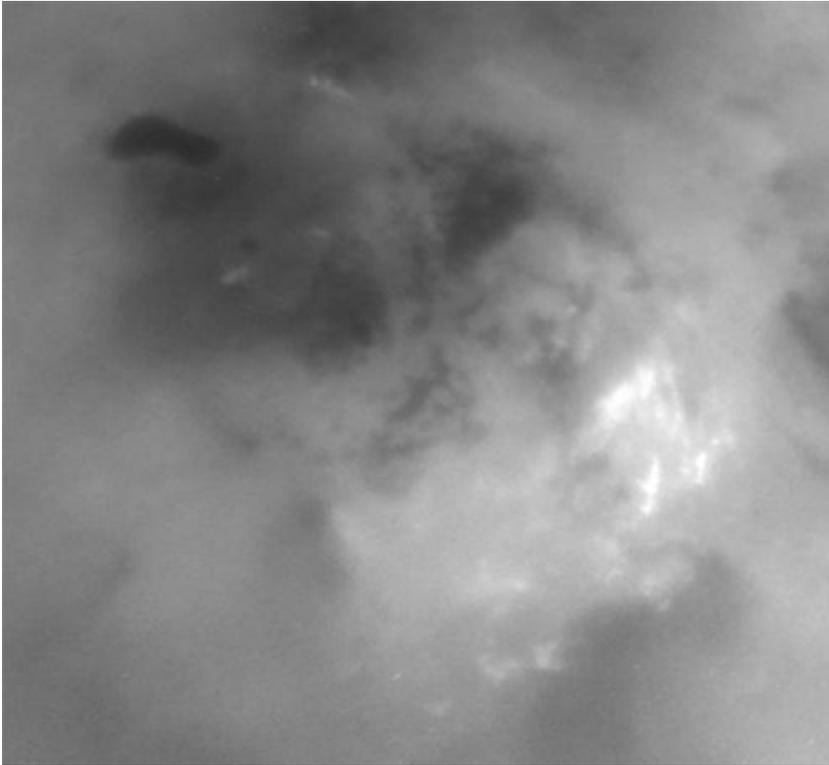
# Titan's lower atmosphere revealed by Cassini/Huygens



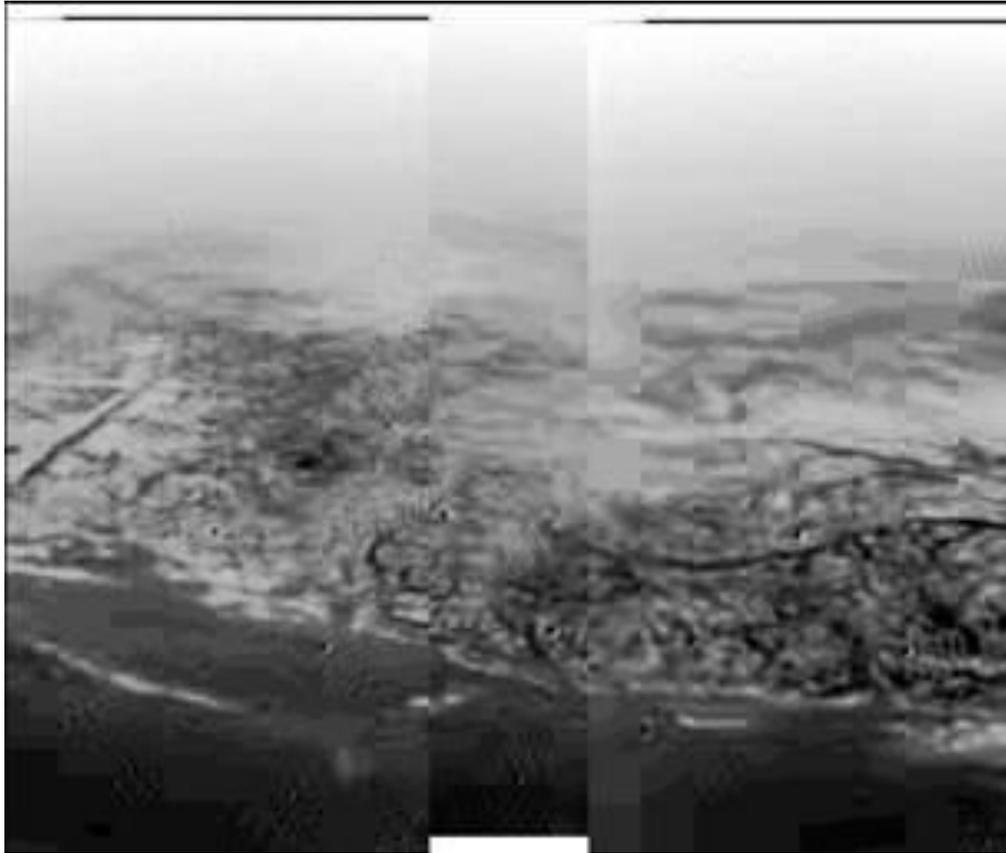
Surface was not Ocean  
but Desert-like.



# Convective cloud and Lakes



# Signature of liquid (Huygens)



River-like feature



Methane "steam" from heated soil at the landing site

# Mars: clouds of H<sub>2</sub>O, CO<sub>2</sub>, Dusts

Mars • Global Dust Storm



June 26, 2001



September 4, 2001

**Hubble Space Telescope • WFPC2**

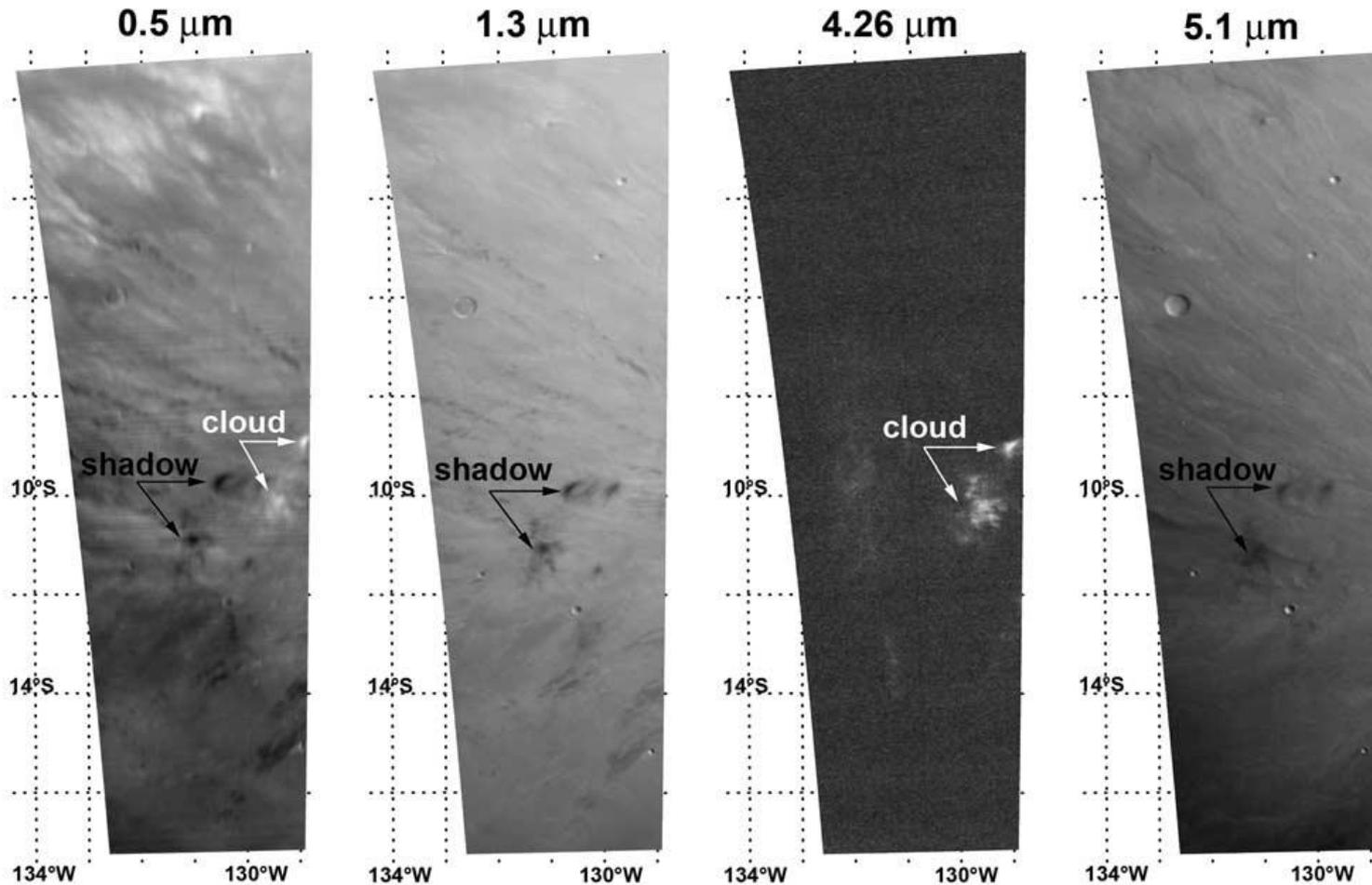
NASA, J. Bell (Cornell), M. Wolff (SSI), and the Hubble Heritage Team (STScI/AURA) • STScI-PRC01-31

# Cirrus-like water ice cloud in Martian atmosphere



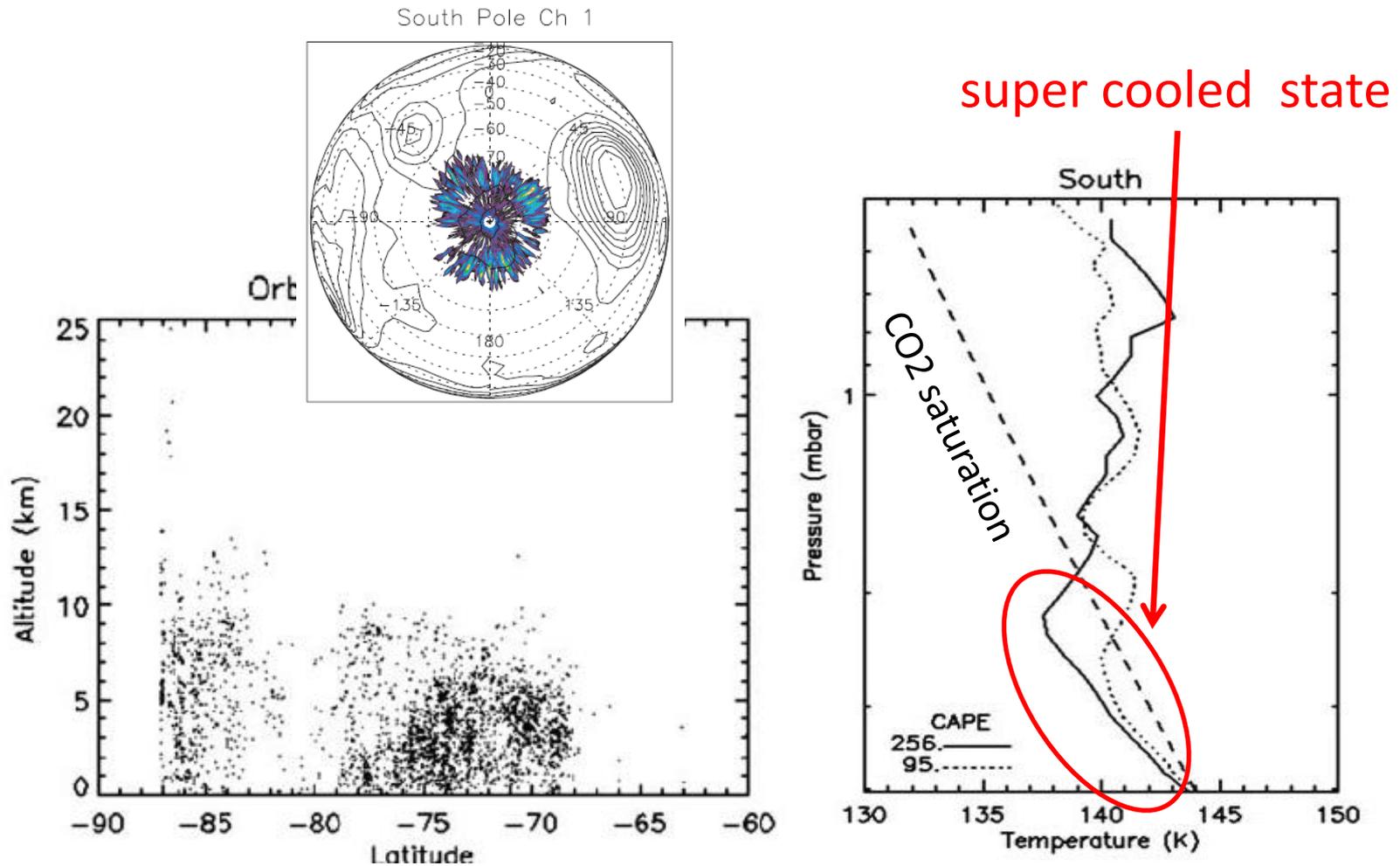
<http://marsprogram.jpl.nasa.gov/MPF/science/clouds.html>

# High altitude (80km) CO<sub>2</sub> clouds observed by OMEGA (Mars Express)



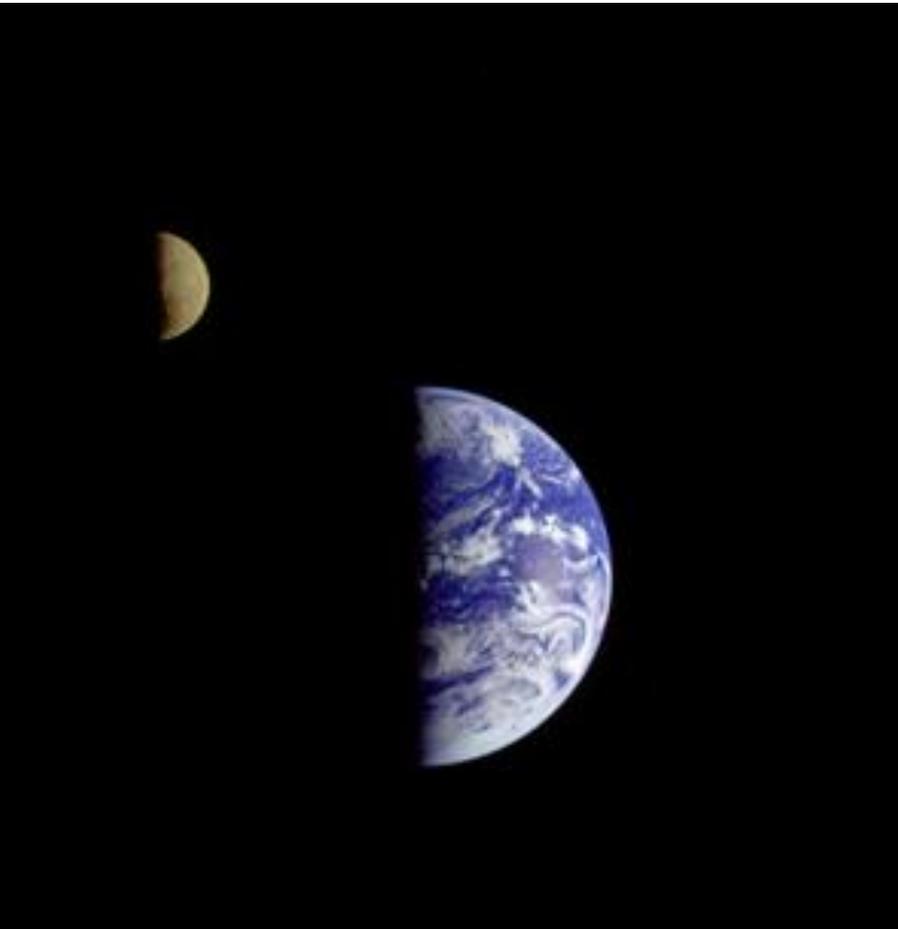
Montmessin et al (2007)

# CO2 “Convective clouds” in Martian south polar region



# Earth's water clouds

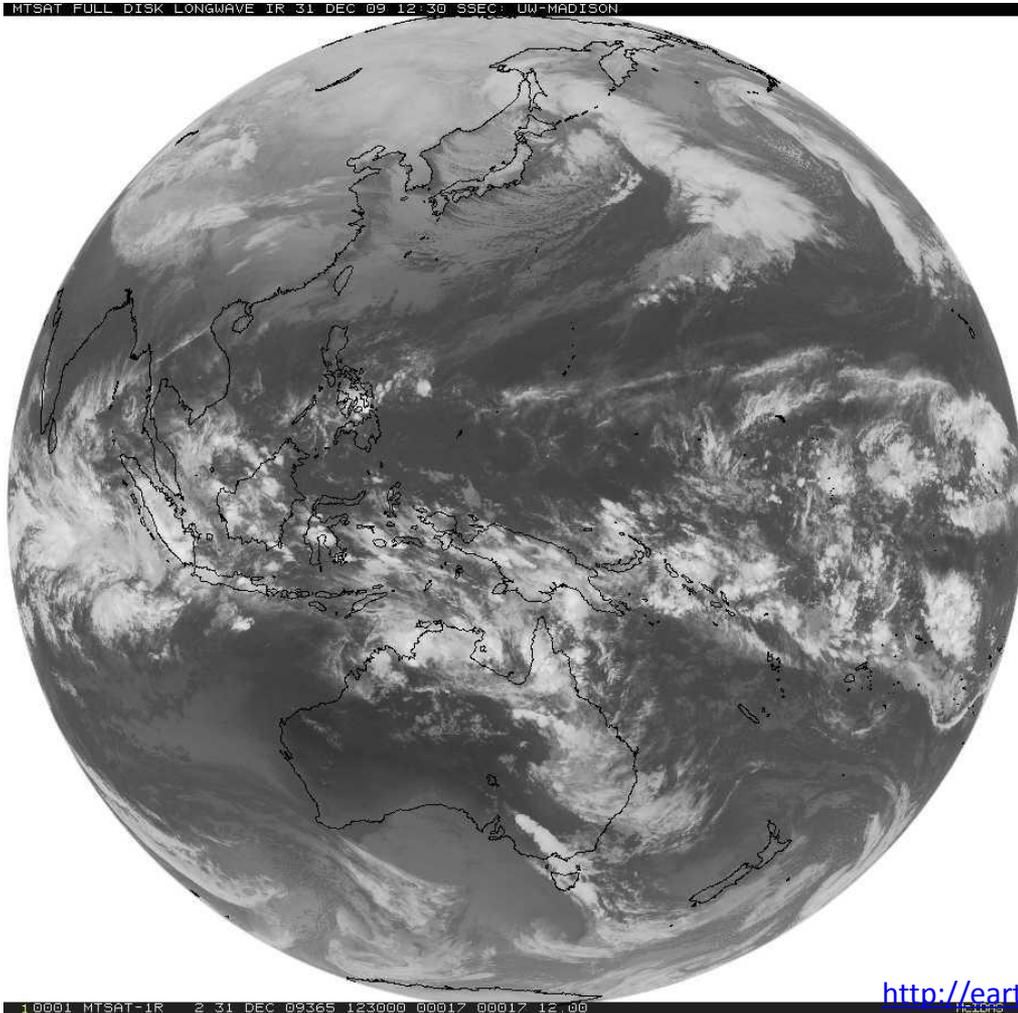
The only place where we have detailed knowledge on clouds.



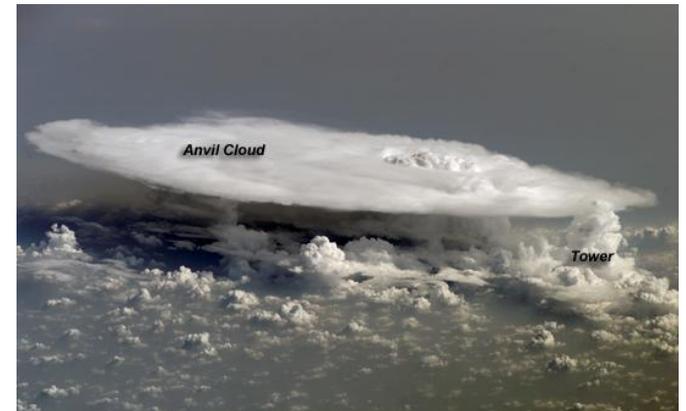
# Thunderclouds

from space: “clusters” of 100-1000km scale are seen.

Individual updraft:  $O(10\text{km})$

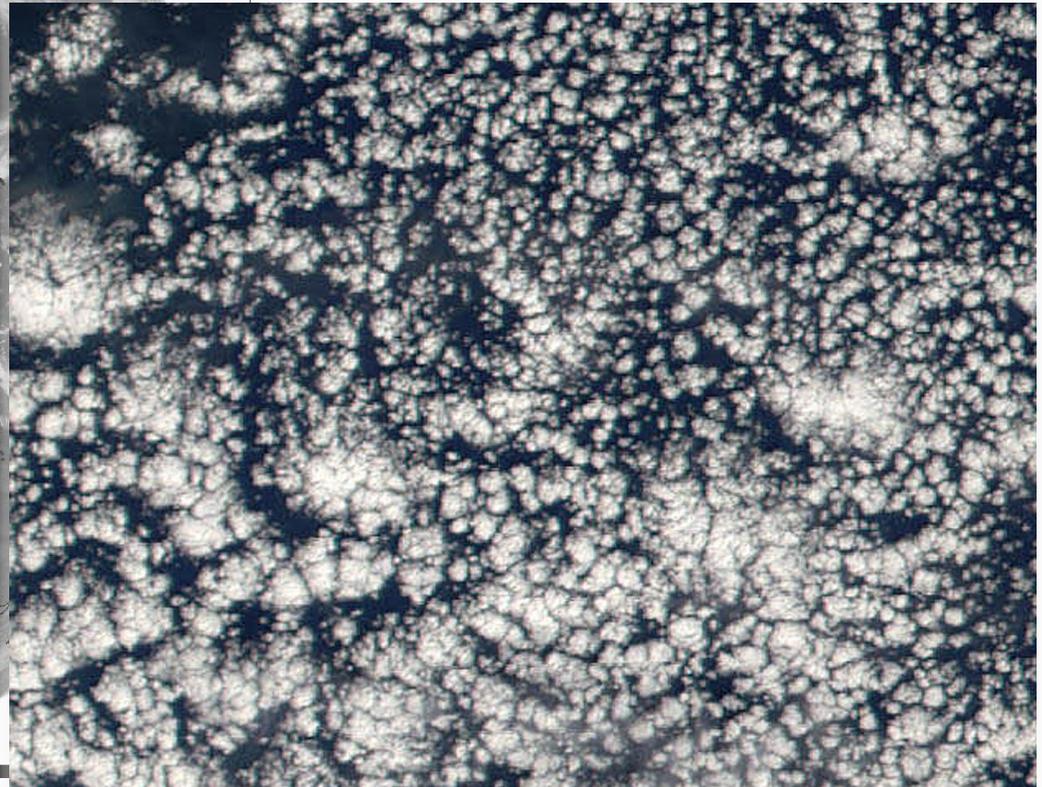
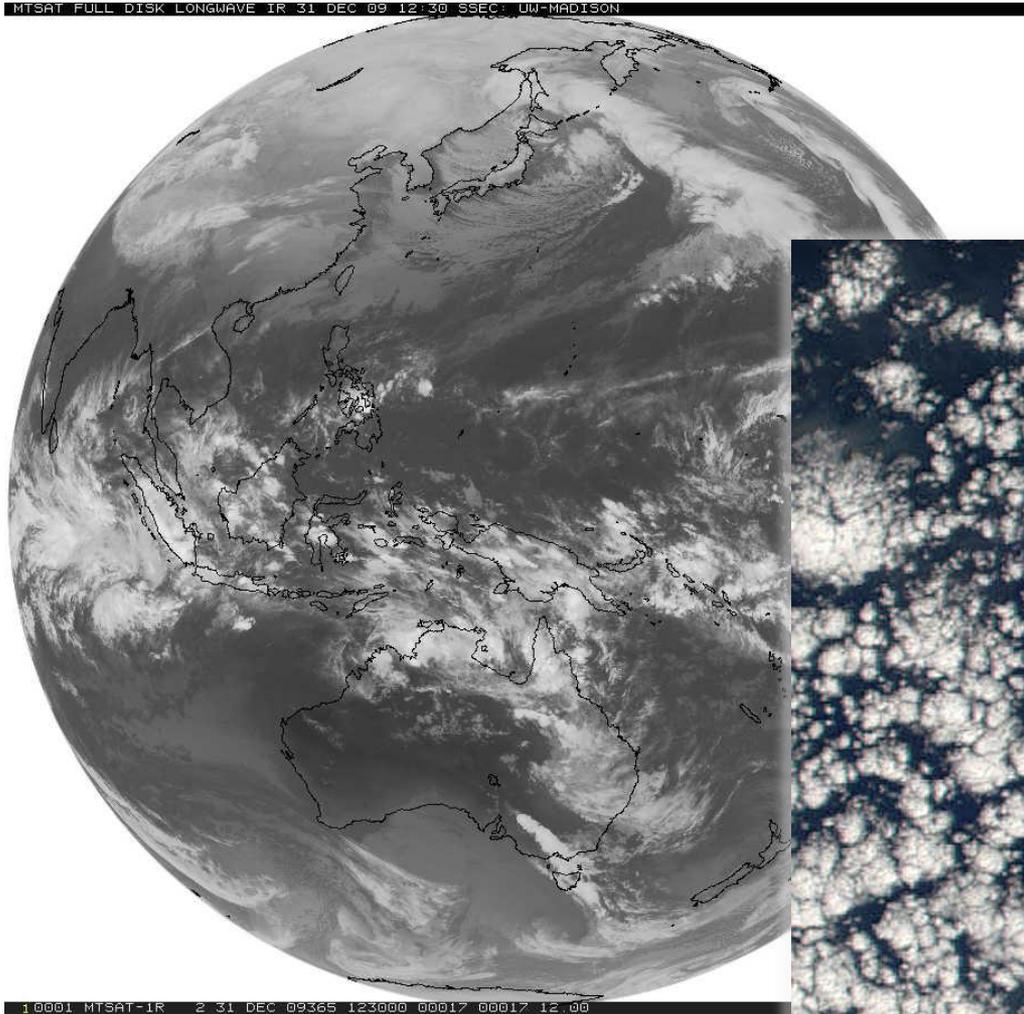


[http://en.wikipedia.org/wiki/Cumulonimbus\\_cloud](http://en.wikipedia.org/wiki/Cumulonimbus_cloud)

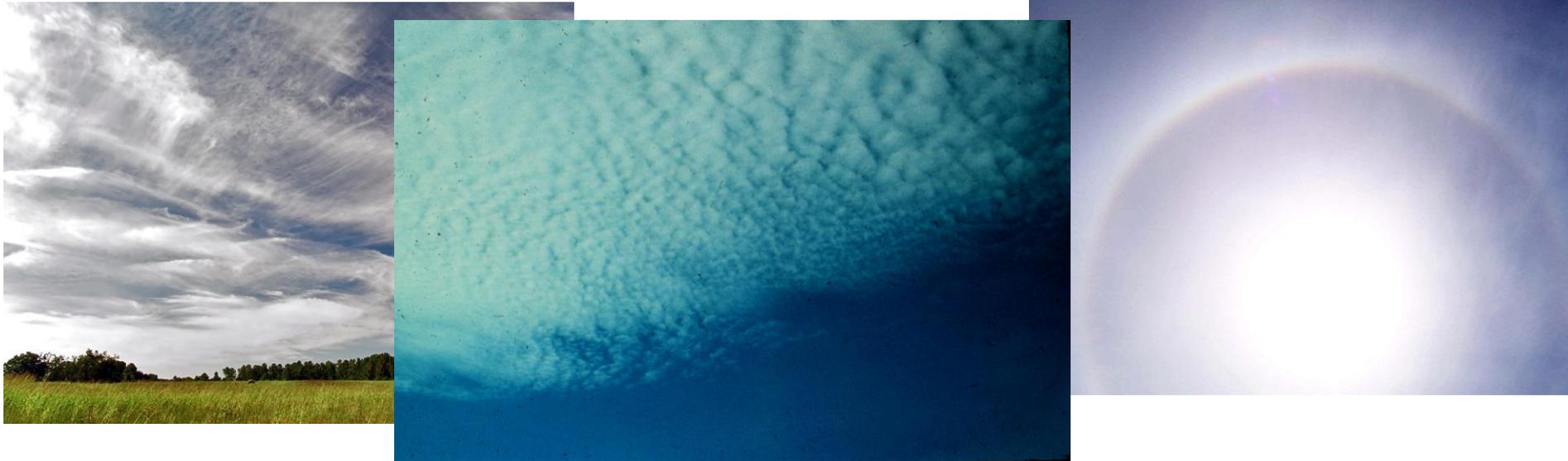


<http://earth.jsc.nasa.gov/sseop/EFS/images.pl?photo=ISS016-E-27426>

# smaller scale convective clouds



# Even Cirrus clouds have some convective character



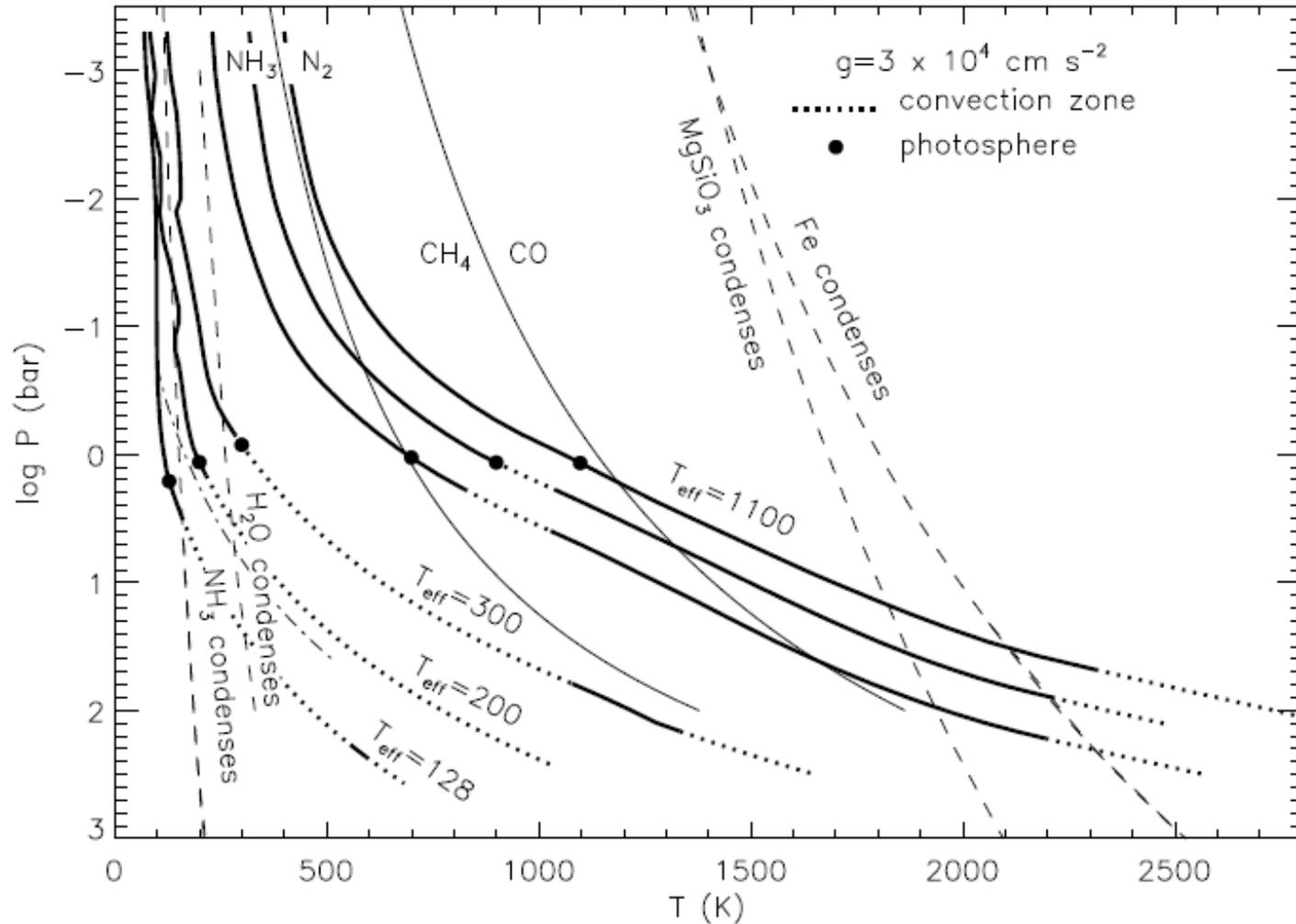
Apparently “stratiform” clouds in the atmospheres of other planets may well be more or less convective clouds.

[http://en.wikipedia.org/wiki/Cirrus\\_cloud](http://en.wikipedia.org/wiki/Cirrus_cloud)

[http://en.wikipedia.org/wiki/Cirrostratus\\_cloud](http://en.wikipedia.org/wiki/Cirrostratus_cloud)

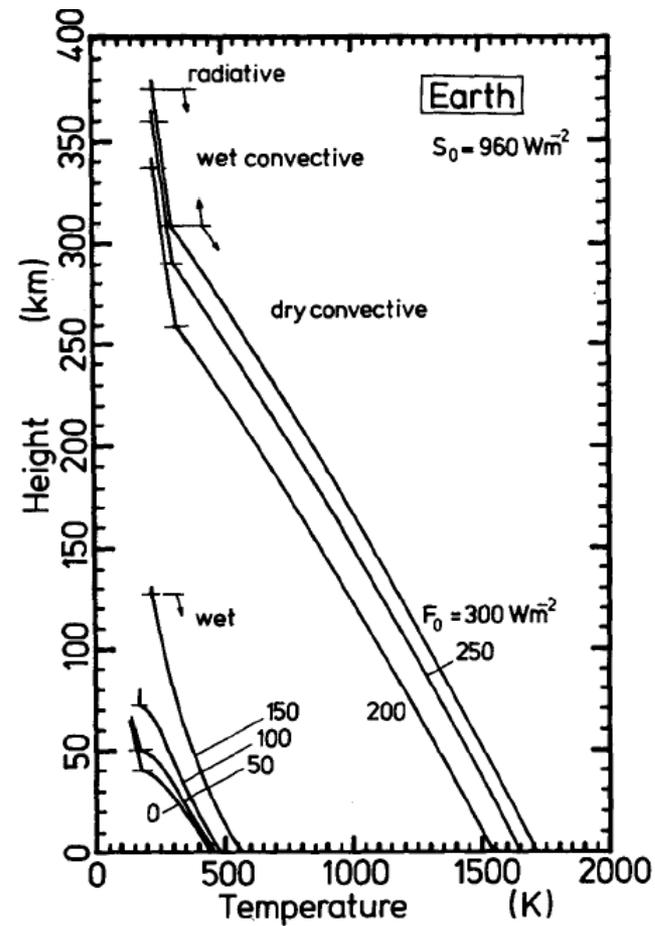
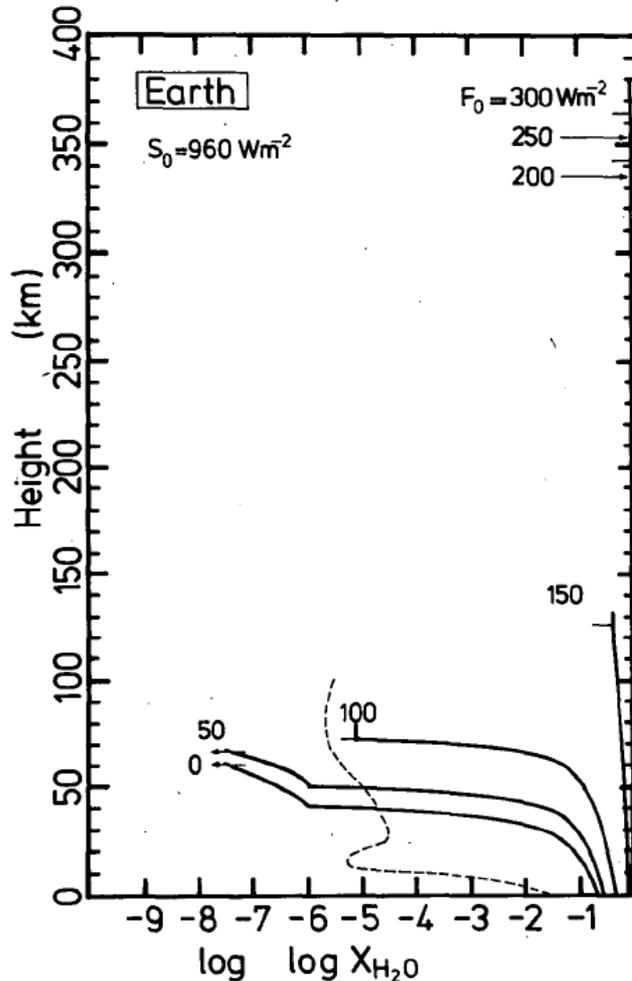
[http://en.wikipedia.org/wiki/Cirrocumulus\\_cloud](http://en.wikipedia.org/wiki/Cirrocumulus_cloud)

# possible iron and silicate clouds in “substellar” atmospheres



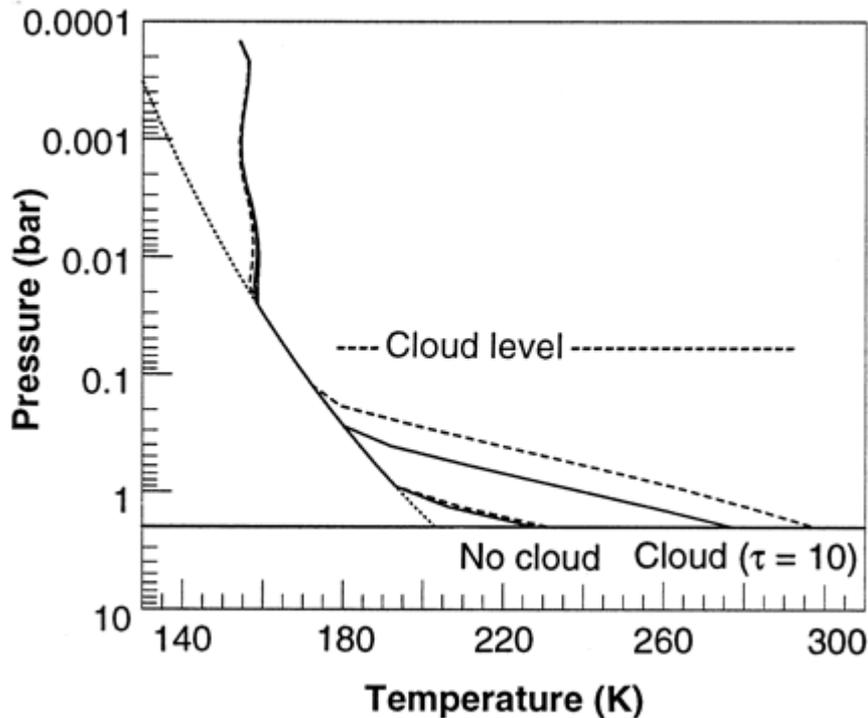
Clouds in the atmospheres  
long long ago...

# Almost pure water convection in the atmosphere of early Earth/Venus

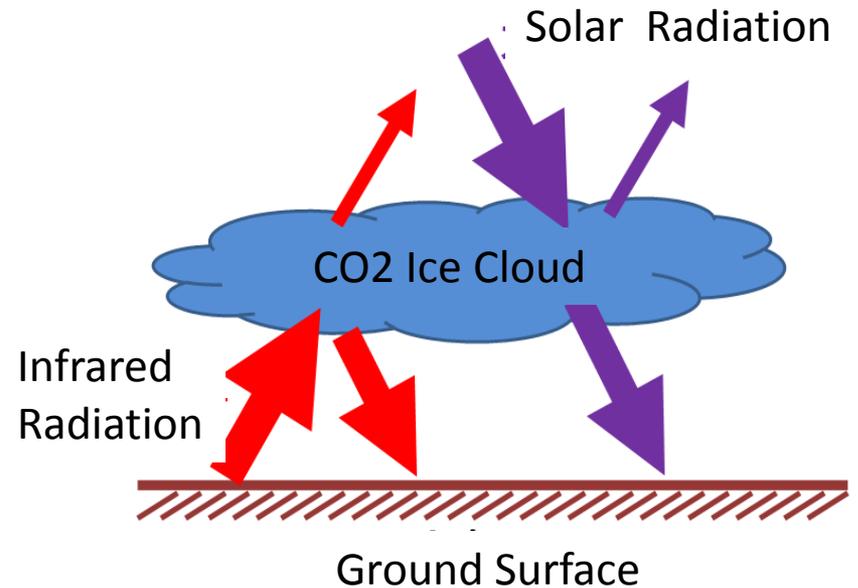


Abe and Matsui(1988)

# Thick CO<sub>2</sub> cloud in the atmosphere of Mars in its early history



Forget and Pierrehumbert (1997)

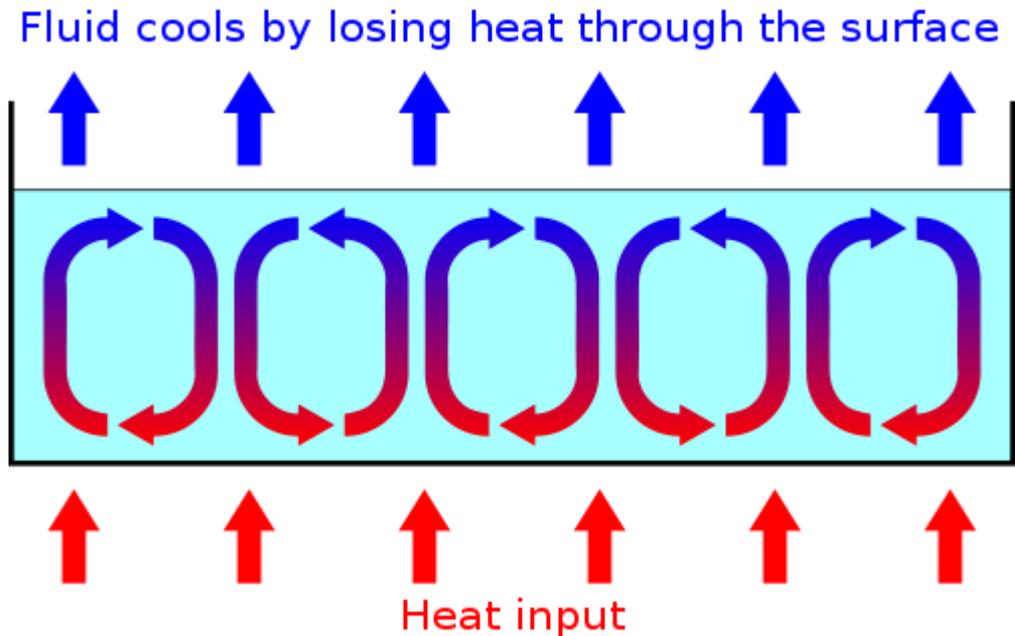
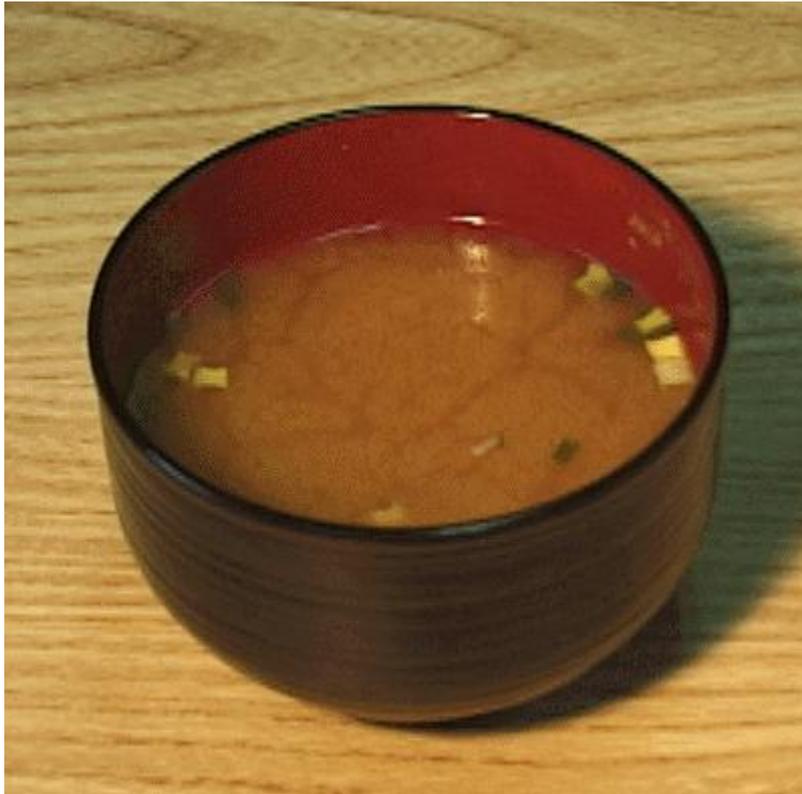


Pierrehumbert and Erlick(1998)

# Basics of moist convection

(the earth's clouds in mind)

# usual convection



[http://en.wikipedia.org/wiki/B%C3%A9nard\\_cells](http://en.wikipedia.org/wiki/B%C3%A9nard_cells)

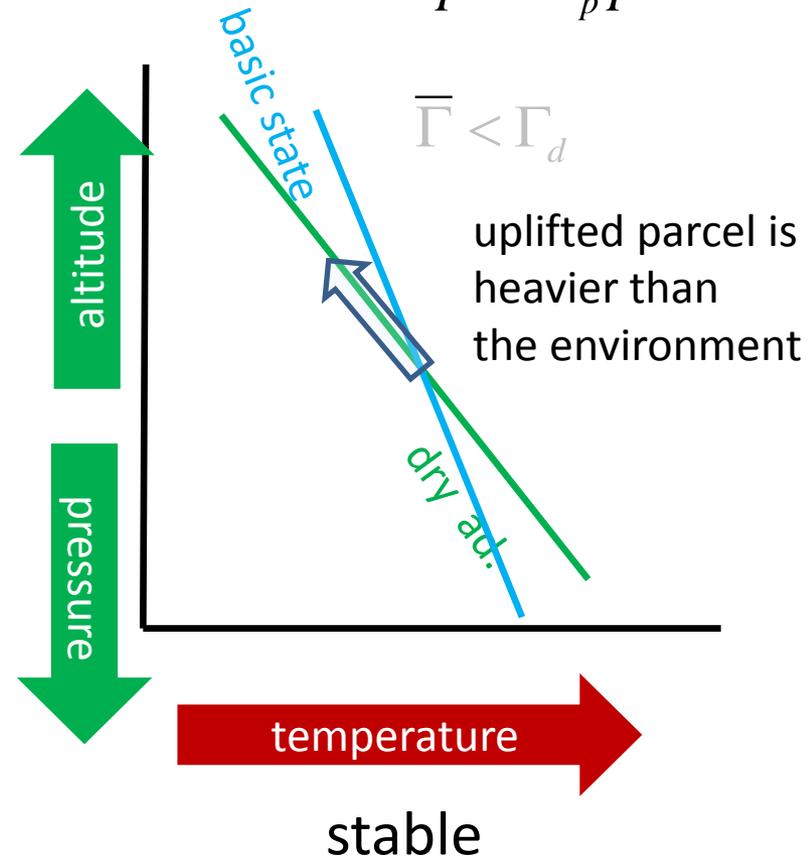
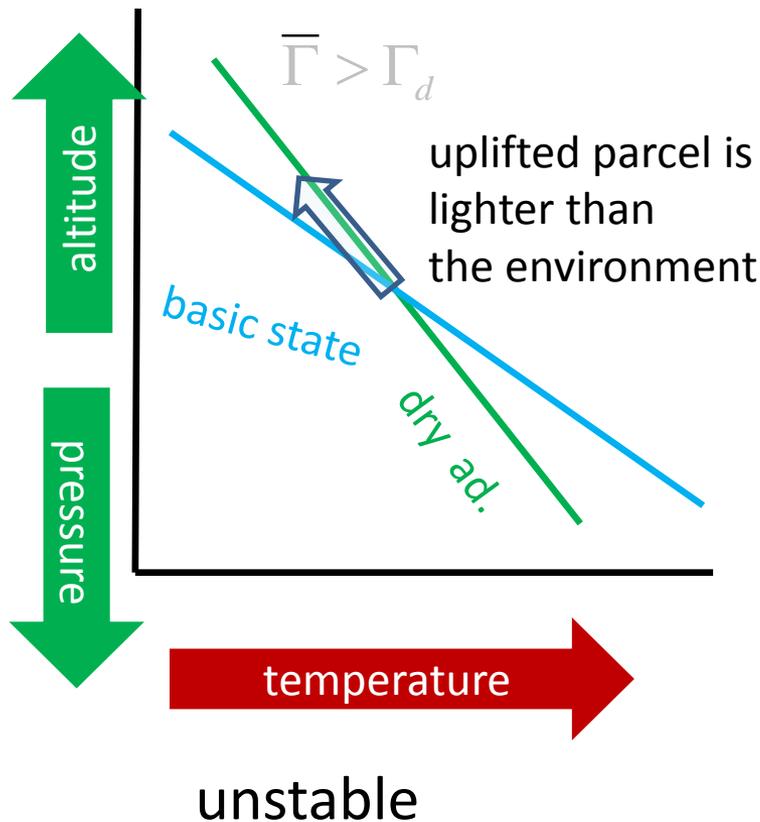
# condition of convective instability: dry adiabatic lapse rate

$$c_p dT - \alpha dp = 0$$

$$p = \rho RT$$

$$c_p dT - \frac{RT}{p} dp = 0$$

$$\frac{dT}{dp} = \frac{R_n T}{c_p p} \equiv \Gamma_d$$



# Moist adiabatic lapse rate

$$c_p dT - \alpha dp = d'Q$$

$$\varepsilon \equiv \mu_v / \mu_n$$

$$c_p dT - \frac{R_n T}{p} dp = -L dq$$

$$q = \varepsilon \cdot e_s / p$$

$$dq / q = de_s / e_s - dp / p$$

$$c_p dT - \frac{R_n T}{p} dp = -L q \left( \frac{L}{R_v T^2} \cdot dT - \frac{dp}{p} \right)$$

$$= L / (R_v T^2) \cdot dT - dp / p$$

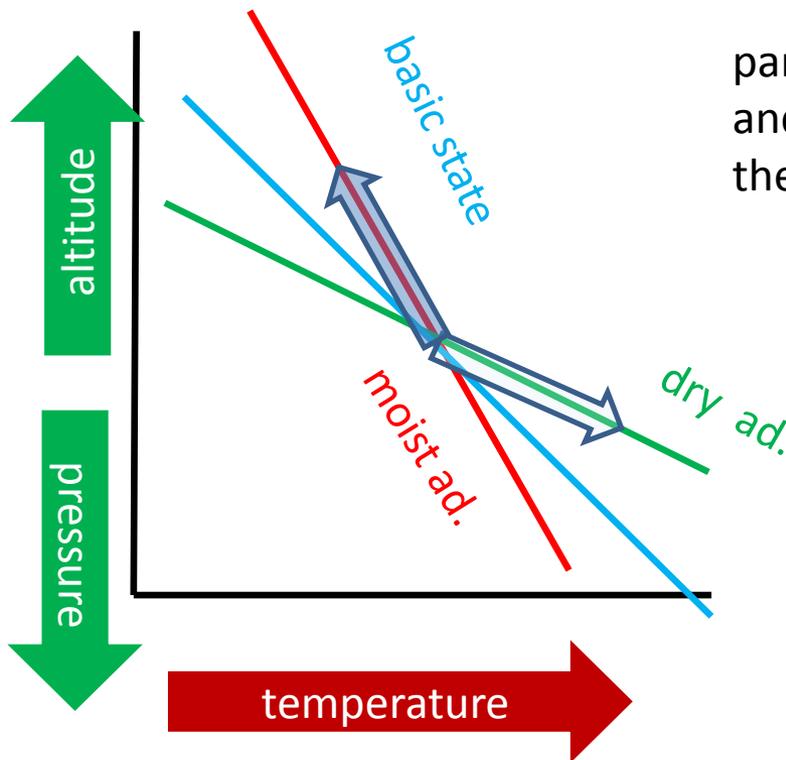
$$\left( c_p + \frac{L^2 q}{R_v T^2} \right) \cdot dT = (R_n T + L q) \cdot \frac{dp}{p}$$

$$\frac{dT}{dp} = \frac{R_n T}{c_p p} \cdot \left( 1 + \frac{L q}{R_n T} \right) \Bigg/ \left( 1 + \frac{L^2 q}{c_p R_v T^2} \right) = \Gamma_d \cdot \left( 1 + \frac{\varepsilon L e_s}{R_n T p} \right) \Bigg/ \left( 1 + \frac{\varepsilon^2 L^2 e_s}{c_p R_n T^2 p} \right)$$

# nonlinearity of moist convection

## (1) conditional instability

Asymmetry between upward and downward motion



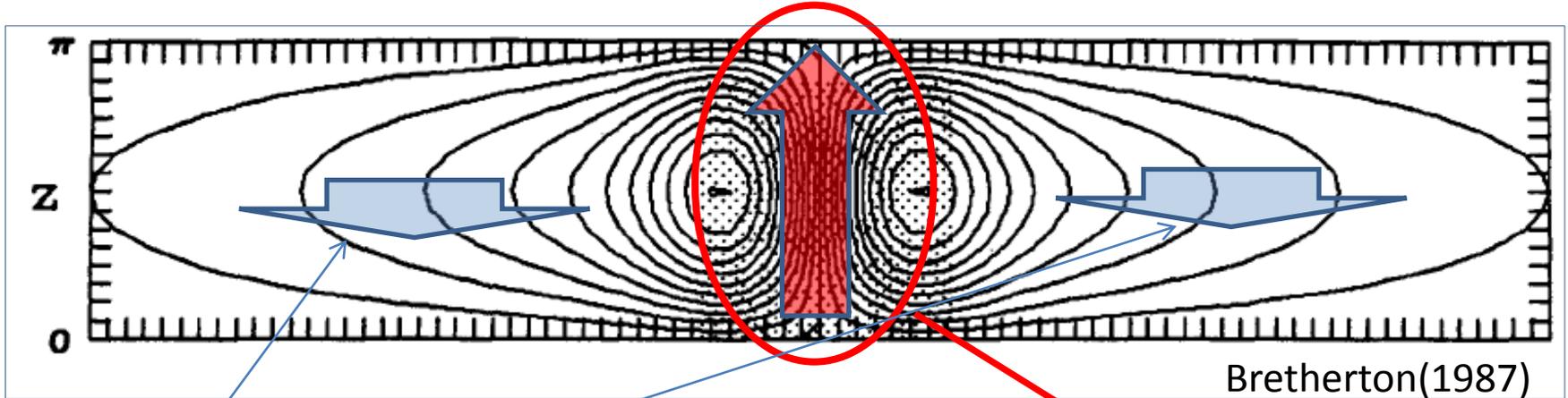
parcel moved upward is saturated and **lighter** than the environment, therefore **unstable**

parcel moved downward is unsaturated and **lighter** than the environment, therefore **stable**

N.B. Basic state is assumed to be just saturated and clear (no cloud particles to evaporate).

conditionally unstable

# Asymmetric structure with conditional instability



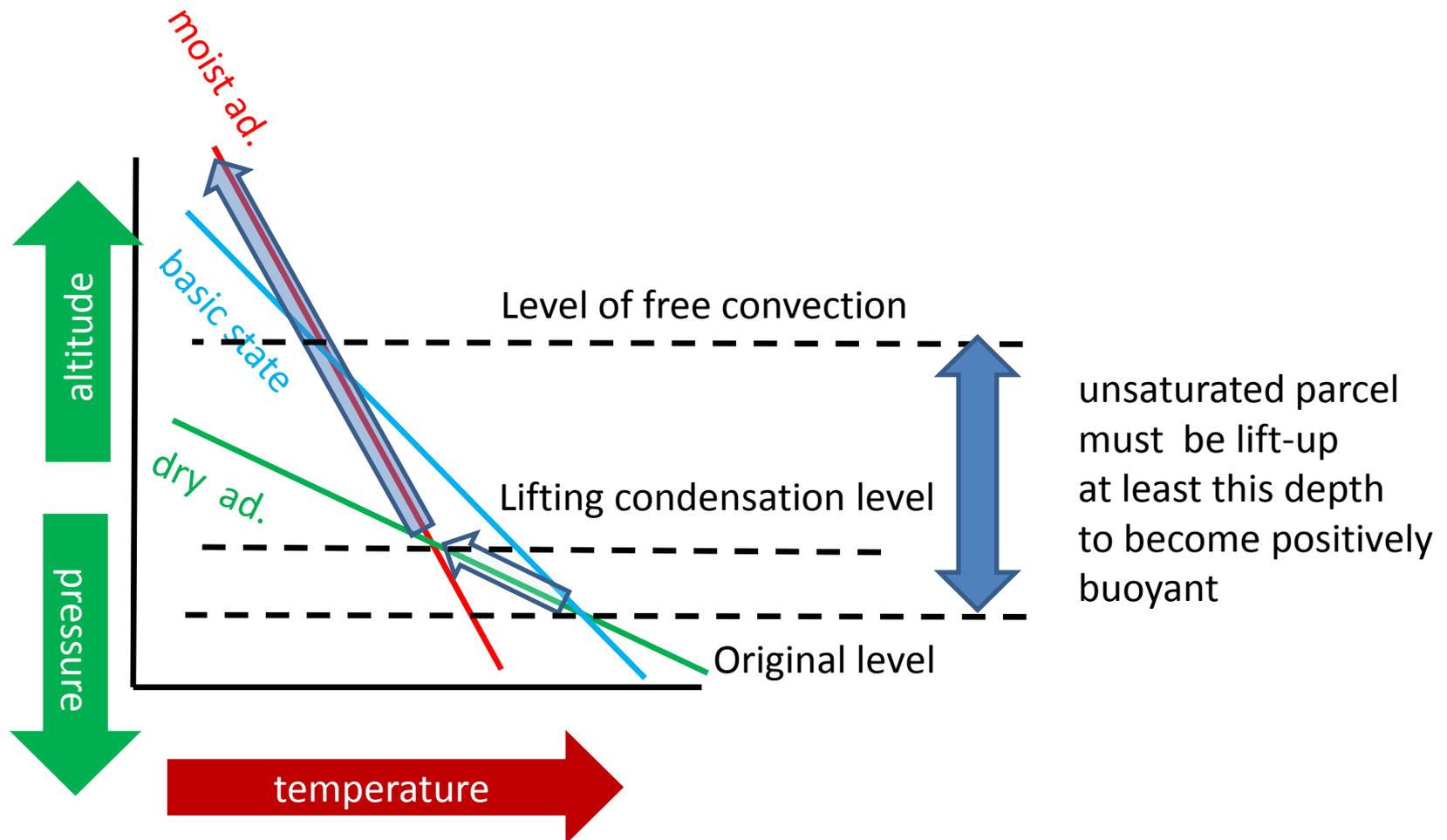
These weak downward motion are also very important.

- it heats the wide area through adiabatic compression.
- large scale horizontal motion is accompanying it!

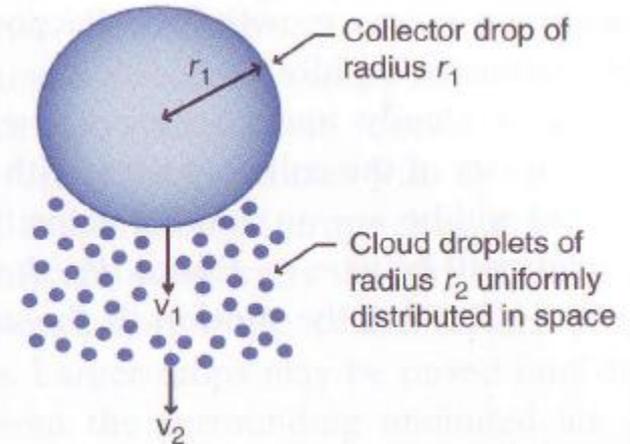
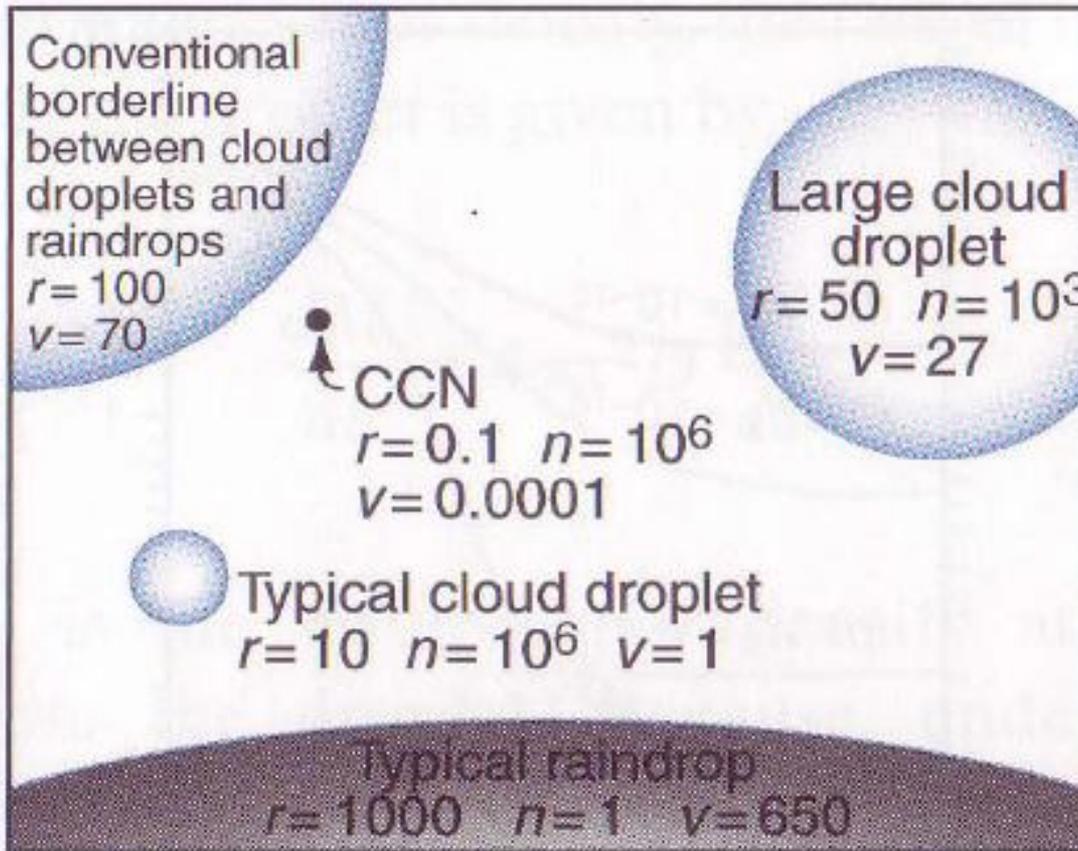


# nonlinearity of moist convection

## (2) potential instability



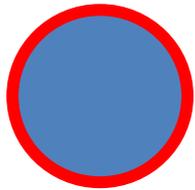
# Cloud microphysics: a long way from molecule to raindrop



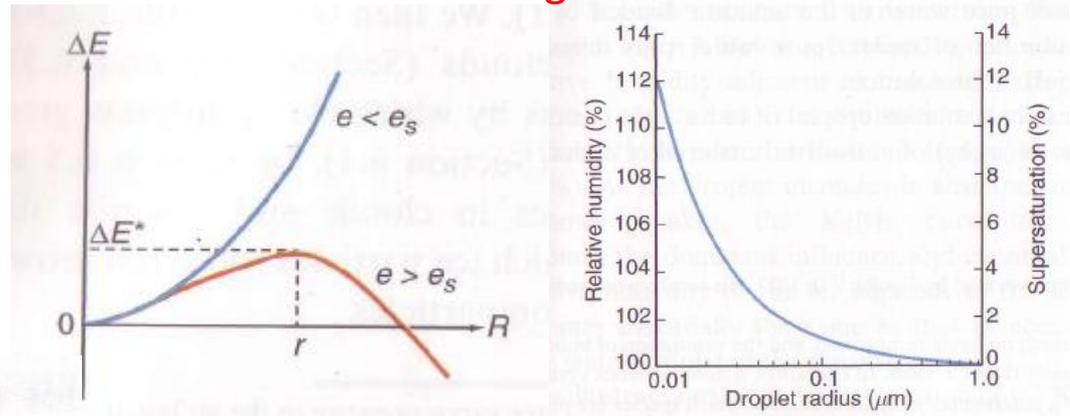
# Formation of cloud particle is difficult without “condensation nuclei”

$$E = E_{\text{volume}} + E_{\text{surface}}$$

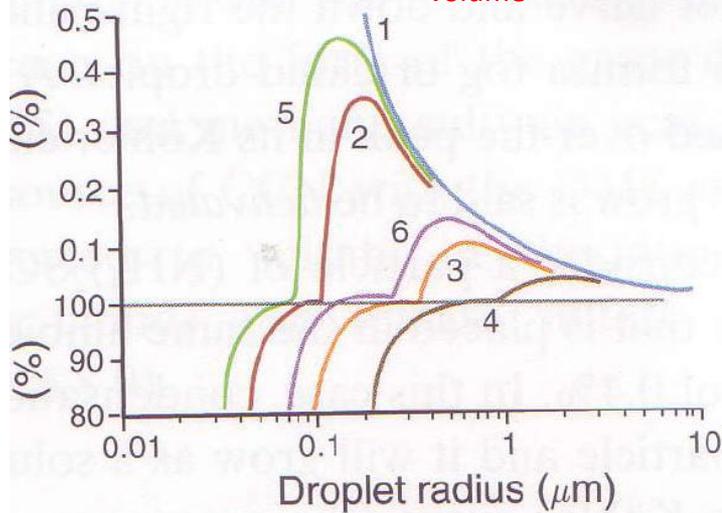
$$= (-) + (+)$$



With positive  $E$ , super saturation is necessary for condensation to begin.

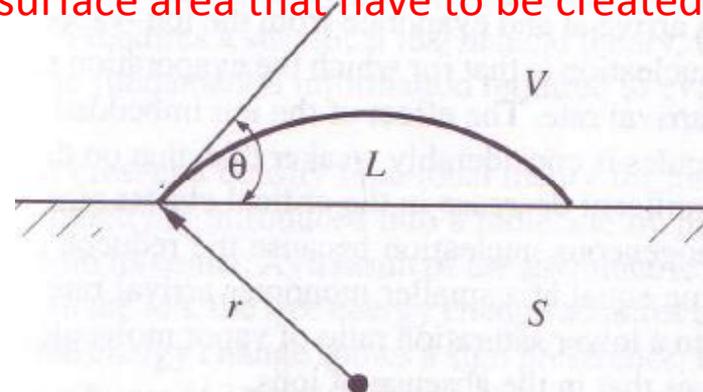


Solution lowers  $E_{\text{volume}}$



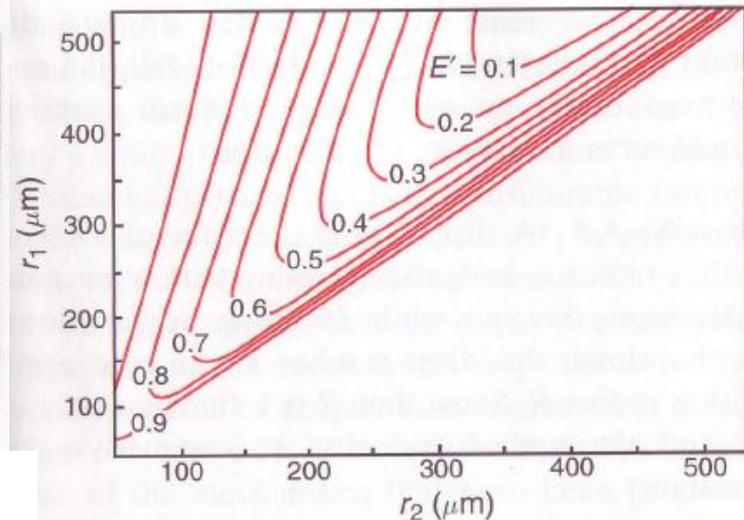
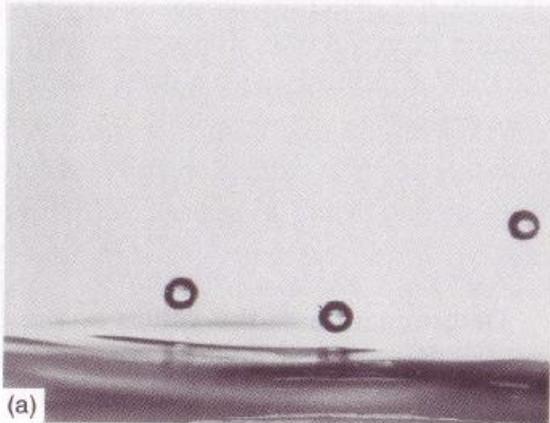
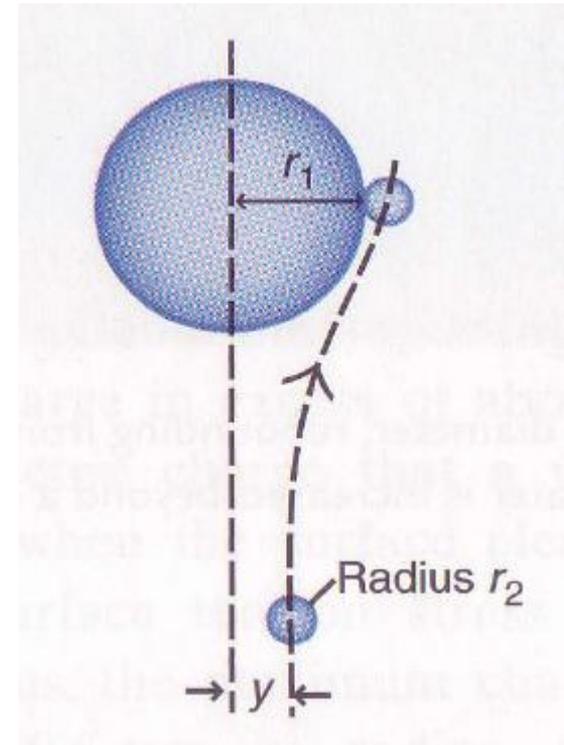
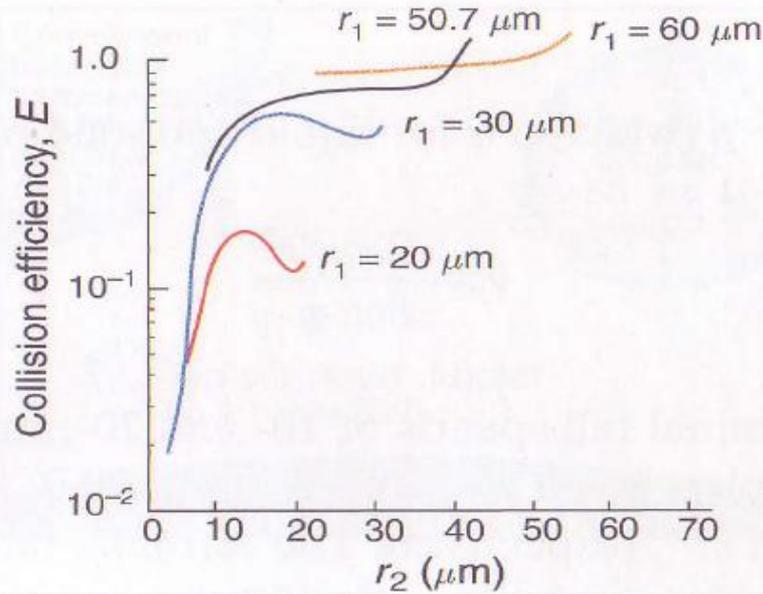
Wallace and Hobbs(2006)

condensation on CCN can reduce the surface area that have to be created.



Seinfeld and Pandis(1998)

# Collision Growth is not a “trivial” process



Wallace and Hobbs(2006)

# governing equations for numerical model of moist convection

## Fluid dynamics

$$\frac{dw}{dt} = -c_p \Theta_0 \frac{\partial \pi}{\partial x} + D(w),$$

$$\frac{dw}{dt} = -c_p \Theta_0 \frac{\partial \pi}{\partial z} + b + D(w).$$

$$b \equiv g \left( \frac{\theta}{\Theta_0} + \left( \frac{m_w}{m_w} - 1 \right) q_v - q_c - q_r \right)$$

$$\frac{\partial(\rho_0 u)}{\partial x} + \frac{\partial(\rho_0 w)}{\partial z} = 0$$

## Thermodynamics

$$\frac{d\theta}{dt} + w \frac{\partial \theta}{\partial z} = \frac{L}{c_p \Pi_0} (C - E_r) + D(\theta) + D(\Theta_0) + Q_{rad}$$

## Budget equations for condensable components

$$\frac{dq_v}{dt} = -C + E_r + D(q_v),$$

$$\frac{dq_c}{dt} = +C - P_{rc} + D(q_c),$$

$$\frac{dq_r}{dt} = +P_{rc} - E_r - \frac{1}{\rho_0} \frac{\partial}{\partial z} (\rho_0 V_T q_r) + D(q_r).$$

## Cloud micro physics

$$P_{rc} = P_{autoconv} + P_{collect}$$

$$P_{autoconv} = \frac{10^6 \rho_0 q_c^3}{60(2q_c + 2.66 \cdot 10^{-8} N_0 / \rho_0 D_0)^2}$$

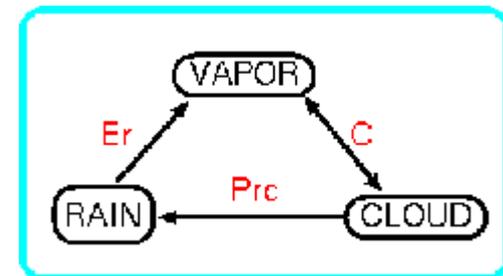
$$N_0 = 5.0 \cdot 10^7$$

$$D_0 = 0.366$$

$$V_T = 12.2 q_r^{1/8},$$

$$P_{collect} = 2.2 q_c (\rho_0 q_r)^{7/8},$$

$$E_r = 4.85 \cdot 10^{-2} (q_v^* - q_v) (\rho_0 q_r)^{0.65}$$



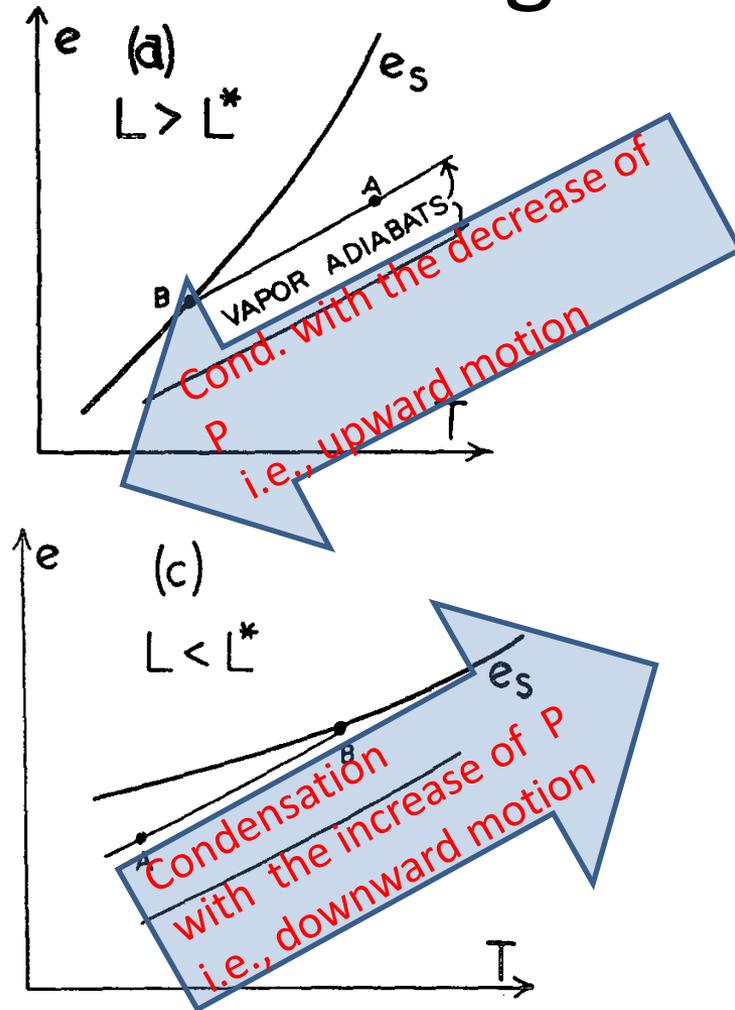
# Re-examination of moist convection

(planetary clouds in mind)

# Issues to be re-examined

- Condensable and non-condensable components can be different from *water vapor* and *air*.
  - Does condensation only in upward motion?
  - Condensable component may be heavier (i.e., having larger molecular weight) than non-condensable component.
- Large-degree of super-saturation may be necessary to begin condensation.
- Major component may condense.

# Sign of vertical motion resulting in condensation



$$\frac{de_s}{dT} = \frac{L}{\Delta v_v \cdot T} = \frac{L}{R_v T^2} e_s$$

$$\frac{de}{dT} = \frac{n_v}{n_n} \cdot \frac{dp}{dT} = \frac{n_v}{n_n} \cdot \frac{c_{pn}}{R_n} \frac{p}{T}$$

$$= \frac{c_{pn}}{R_n} \cdot \frac{e}{T} = \frac{L^*}{R_v T^2} e$$

$$L^* \equiv \frac{c_{pn}}{R_n} R_v T$$

McDonald(1964)

# Condensation occurs with upward motion for all planet

$$L > L^* \equiv \frac{C_{pn}}{R_n} R_v T \Leftrightarrow S^* > C_{pn}$$

substance	T[K]	S* [J/mol K]
H2O	270	168
NH3	250	92
CH4	100	86
C2H6	90	160
CO2(sublimation)	190	125
Fe	1800	200
MgSiO3	2000	225

$$S^* \equiv \frac{LR}{R_v T} = \frac{l}{T} > \frac{C_{pn} R}{R_n} = C_{pn}$$

$$C_{pn} \approx (2.5 \sim 3.5) R$$

$$\approx 20 \sim 30 [J / mol \cdot K]$$

Condensation occurs in upward motion in all (maybe) planetary atmospheres

# Effect of molecular weight on the density of saturated parcel

$$\rho = \rho_n + \rho_v = \frac{\mu_n p_n}{RT} + \frac{\mu_v p_v}{RT} = \frac{\mu p}{RT} \quad \mu \equiv \mu_n \frac{p_n}{p} + \mu_v \frac{p_v}{p}$$

$$\left(\frac{\rho'}{\rho}\right)_p = \left(\frac{\mu'}{\mu}\right)_p - \frac{T'}{T} = \left(\frac{T}{\mu} \left(\frac{d\mu}{dT}\right)_p - 1\right) \frac{T'}{T} \quad e_s = p \cdot \frac{\mu}{\mu_v} r_v^*$$

$$\left(\frac{d\mu}{dT}\right)_p = \frac{\mu_n}{p} \frac{d}{dT} (p - e_s) + \frac{\mu_v}{p} \frac{d}{dT} e_s = \frac{\mu_v - \mu_n}{p} \frac{d}{dT} e_s$$

$$= \frac{\mu_v - \mu_n}{p} \frac{L}{RT^2} e_s = (\mu_v - \mu_n) \frac{L}{RT^2} \frac{\mu}{\mu_v} r_v^* = \left(1 - \frac{\mu_n}{\mu_v}\right) \frac{L r_v^*}{RT^2} \mu$$

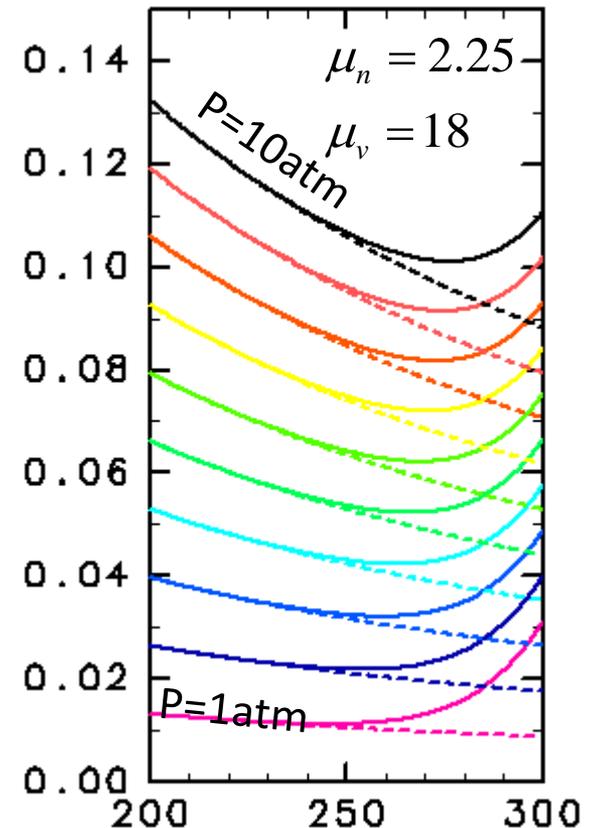
$$\frac{T}{\mu} \left(\frac{d\mu}{dT}\right)_p - 1 = \left(1 - \frac{\mu_n}{\mu_v}\right) \frac{L r_v^*}{RT} - 1$$

# Effect of molecular weight on the density of ascending parcel

$$\left(\frac{\rho'}{\rho}\right)_p = \left(\frac{\mu'}{\mu}\right)_p - \frac{T'}{T} = \left[ \left(1 - \frac{\mu_n}{\mu_v}\right) \cdot \frac{L}{RT} r_v^* - 1 \right] \cdot \frac{T'}{T}$$

If the condensable component is heavier than the non-condensable component, and its mixing ratio and/or the latent heat of condensation is large enough (i.e., the saturation vapor pressure depends strongly on the temperature), the ascending **warmer parcel is heavier** than the colder air in the environment!

Density of Jovian air saturated with water vapor

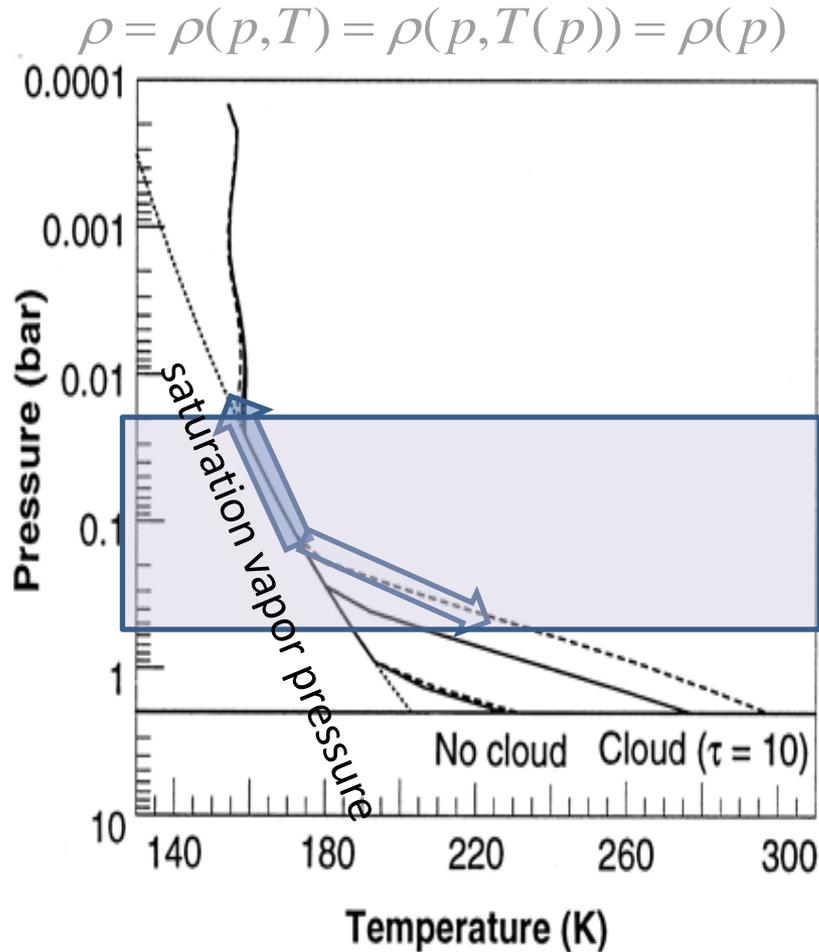


# The effect of molecular weight can be quite significant in Jovian planetary atmospheres

mixing ratios of condensable component						
	critical value	Jupiter	Saturn	Uranus	Neptune	solar system standard
H <sub>2</sub> O	0.057	?	?	?	?	0.015
NH <sub>3</sub>	0.104	0.004	0.002	?	?	0.002
CH <sub>4</sub>	0.112	(0.048)	(0.072)	0.368	0.24	0.006

Guillot (1995)

# major component condensation



Forget and Pierrehumbert(1997)

- P and T are constrained along saturation vapor pressure  $P=P(T)$ .
- In a plain view, the saturated layer is *neutral* because the fluid is *barotropic*, so that vorticity is conserved.
- Details of cloud microphysics could be critical.
  - The weight of cloud particles can significantly affect buoyancy.
  - Slight departure from saturation vapor pressure may affect buoyancy.
  - Cloud particles affects temperature change within downward motion.

Quicklook of moist convection  
numerically simulated in the condition  
of planetary atmospheres  
(more or less)

# The Earth



Plenty of water cloud.

Ocean covers 70%.

Water vapor is lighter than the dry air.

Nucleation is easy (We know it!).

# with full-set of cloud physics

Life cycle of individual convective cloud

The effect of cloud (e.g. temperature change) propagates as waves.

IT = 030

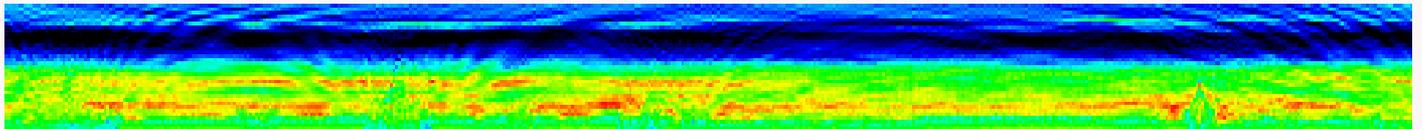
vertical  
velocity

$w$



temperature  
anomaly

$t$



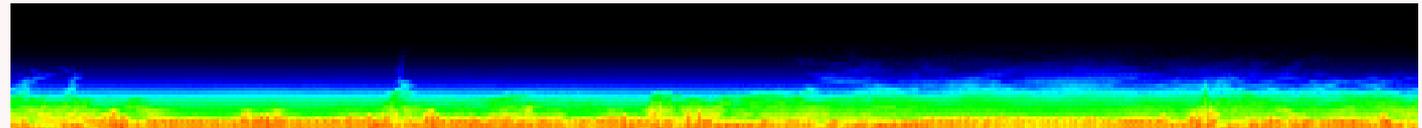
rain water  
mixing ratio

$r$

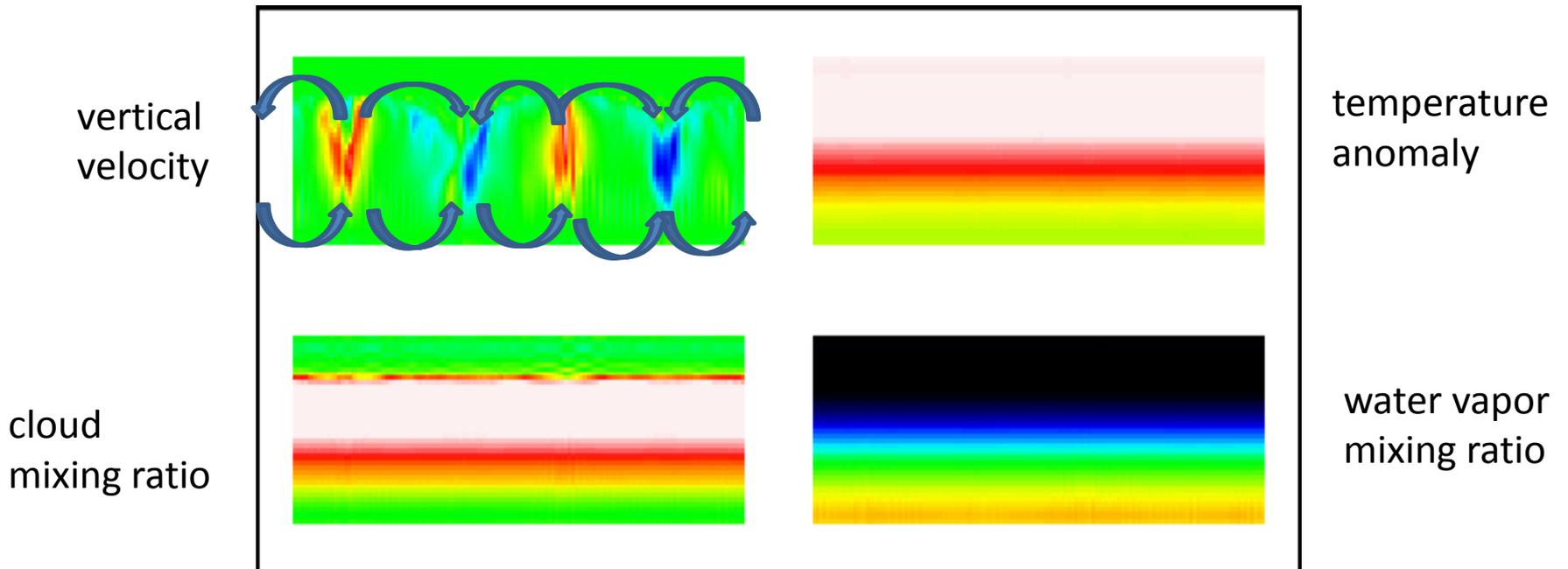


water vapor  
mixing ratio

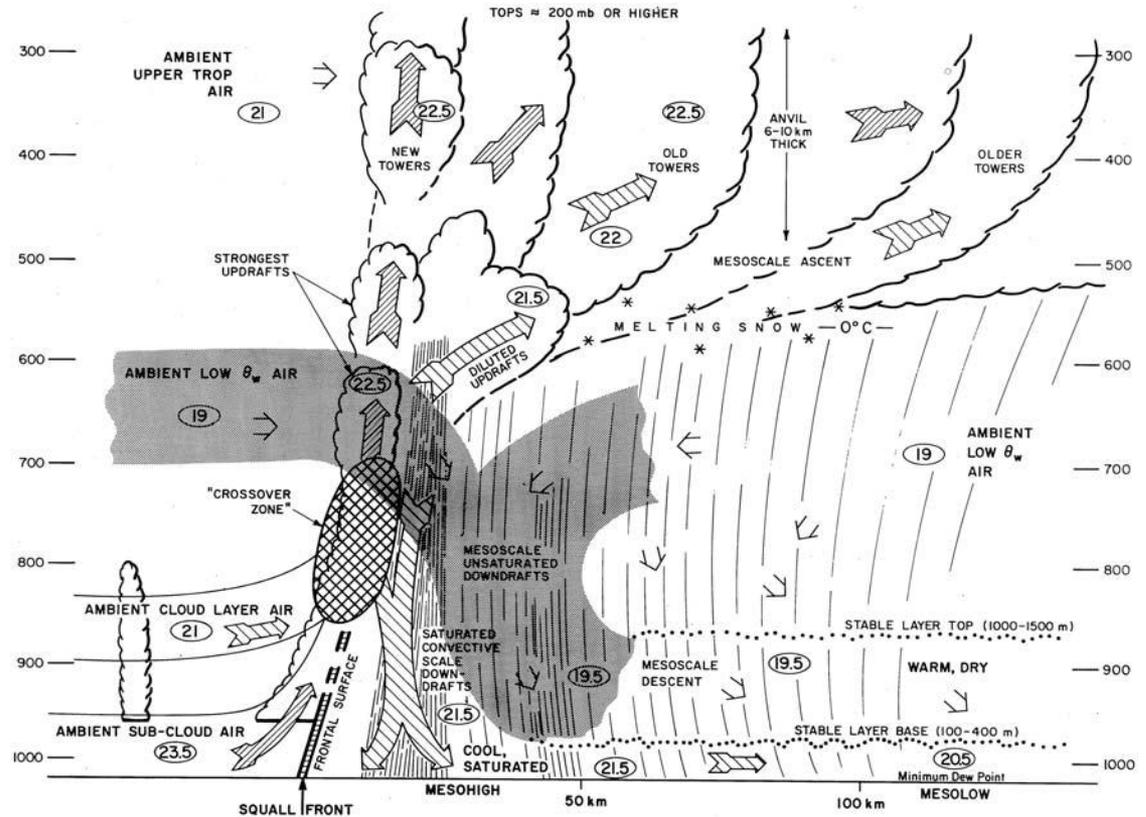
$q$



Without precipitation processes, moist convection is not very different from Bernard convection (Miso soup)

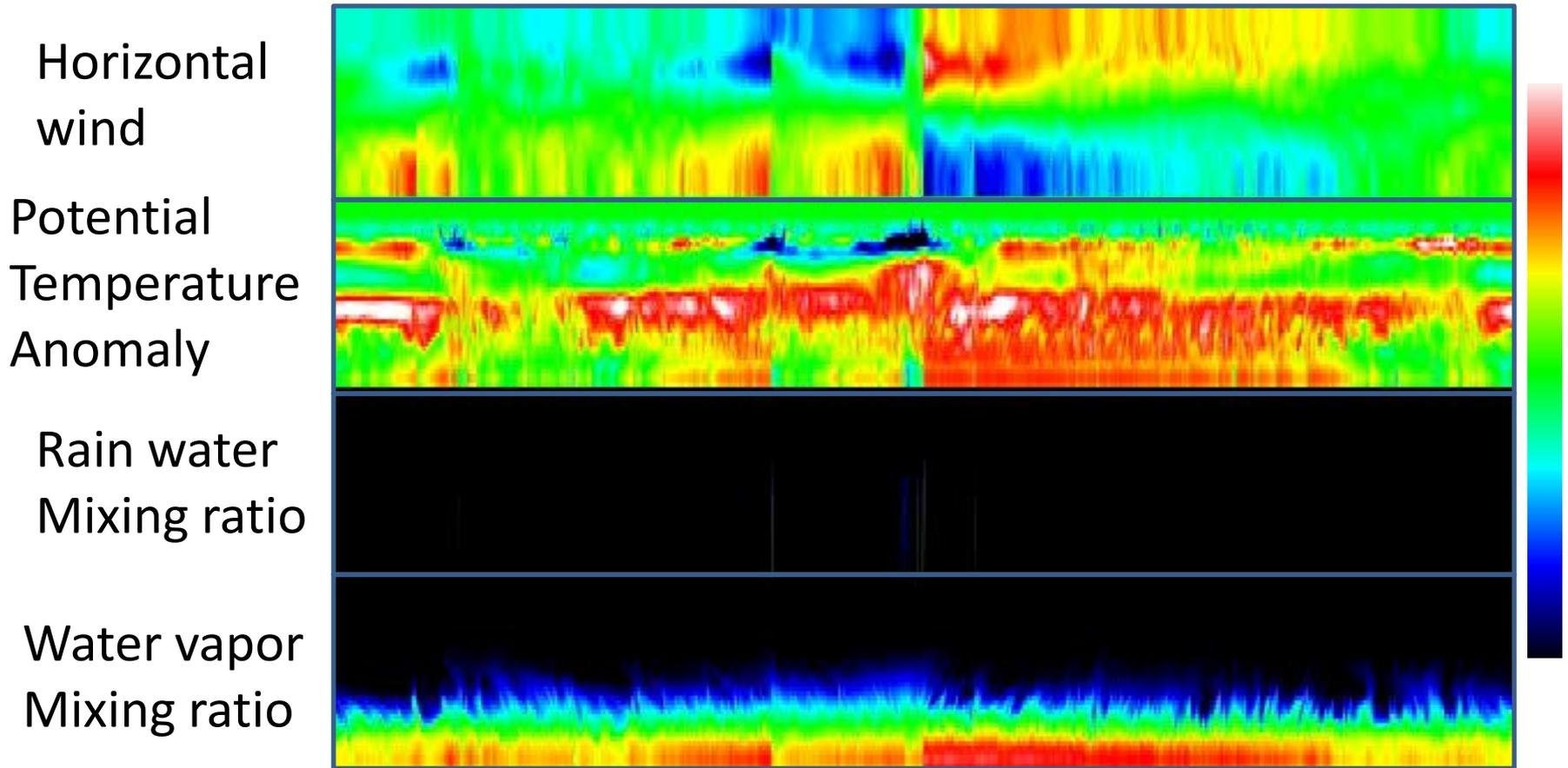


# Convective clouds tends to form as groups owing to the formation of rain



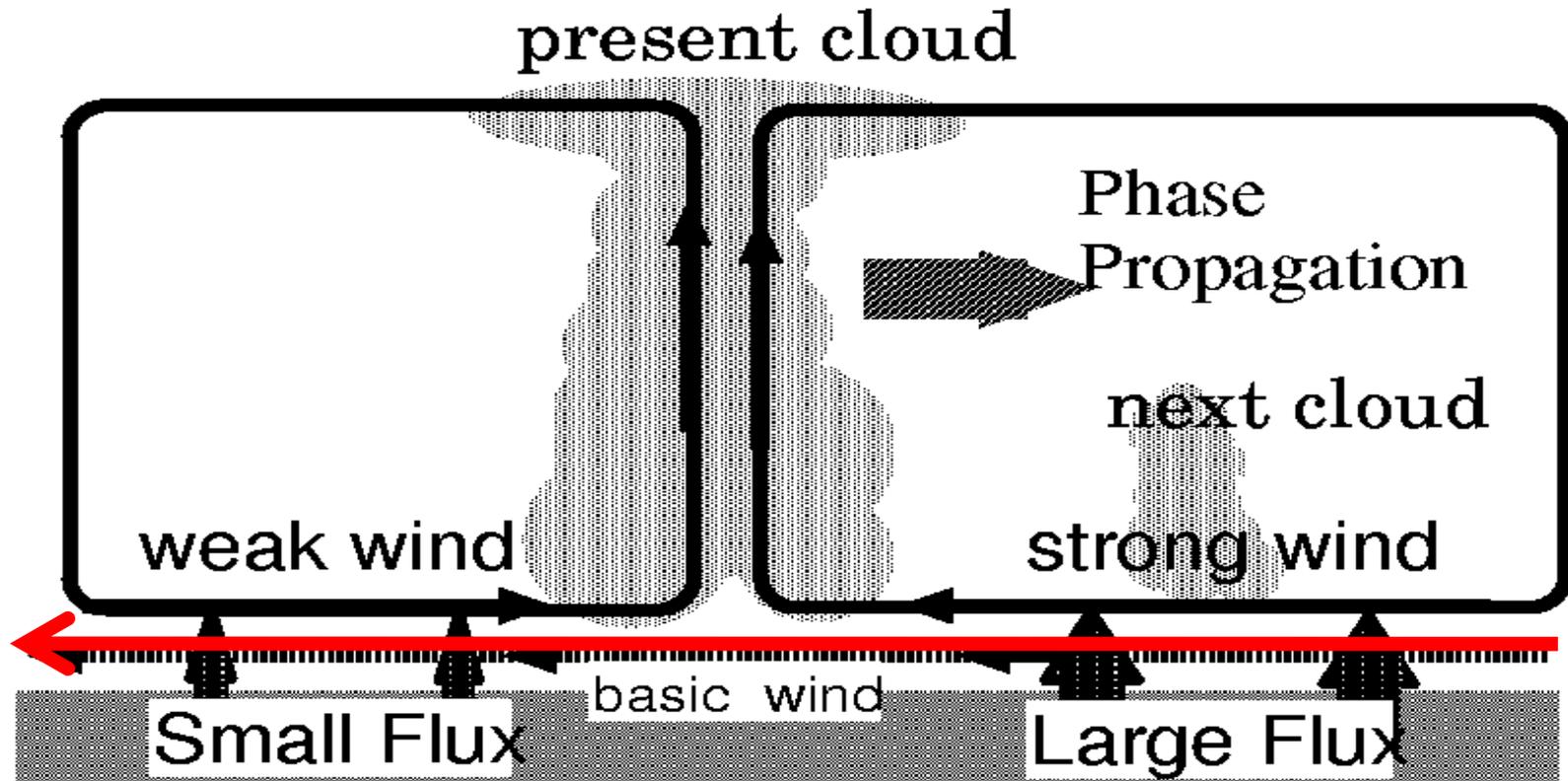
Tao and Moncrieff(2009)

# Horizontal scale of motion associated with cloud can have planetary scale.



domain : Zoomed from 65,536km to 128km

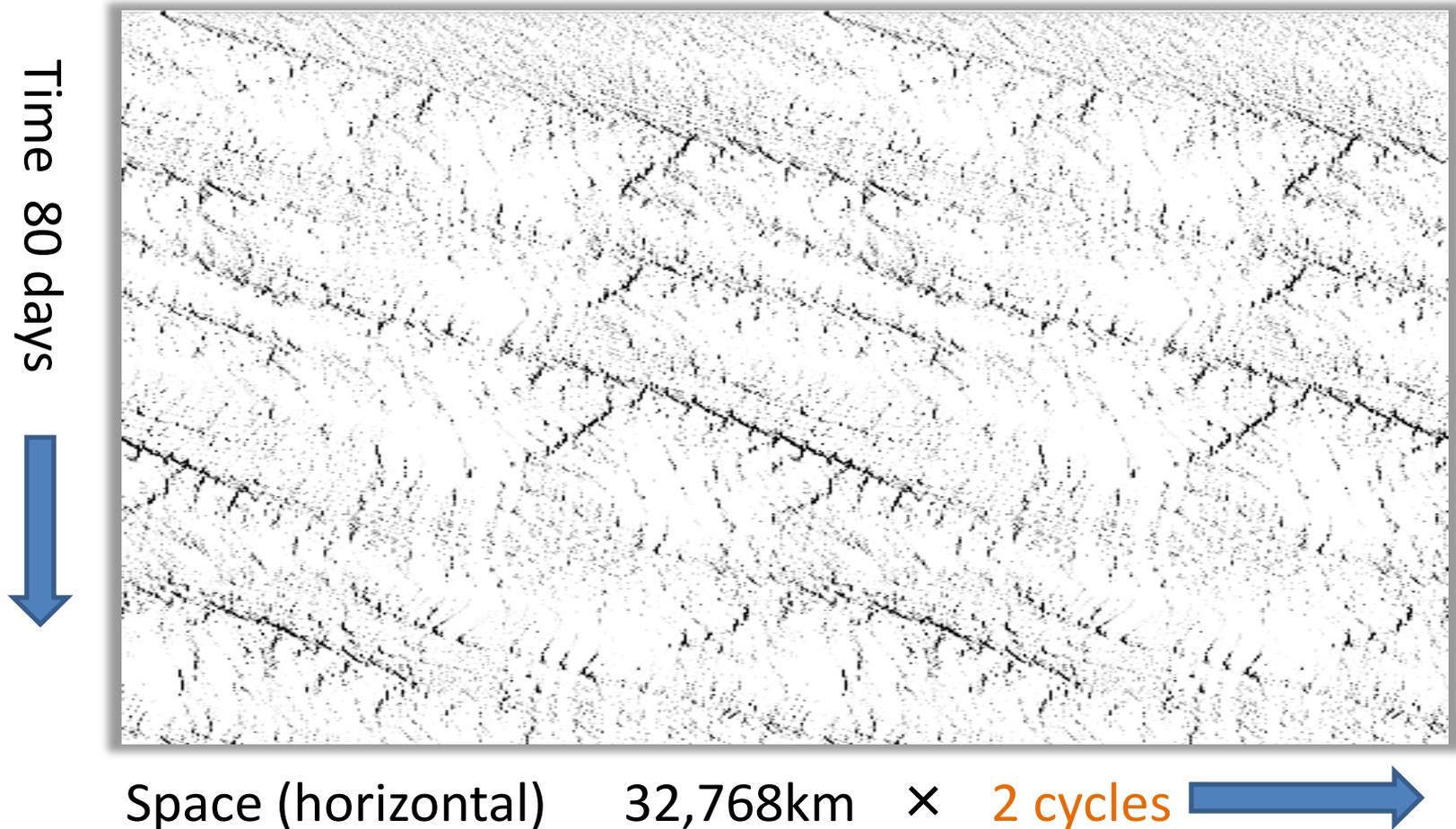
# wind-induced surface heat exchange



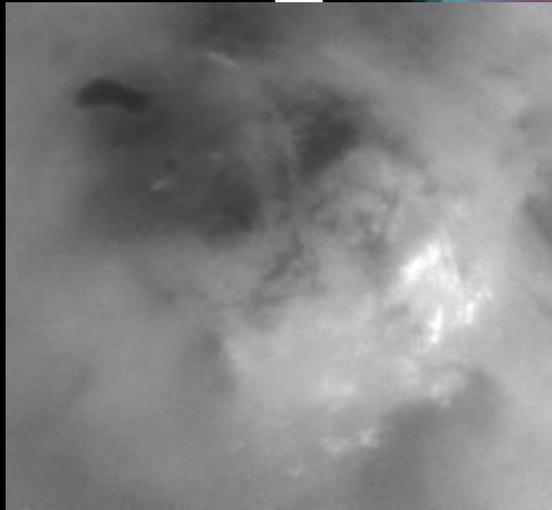
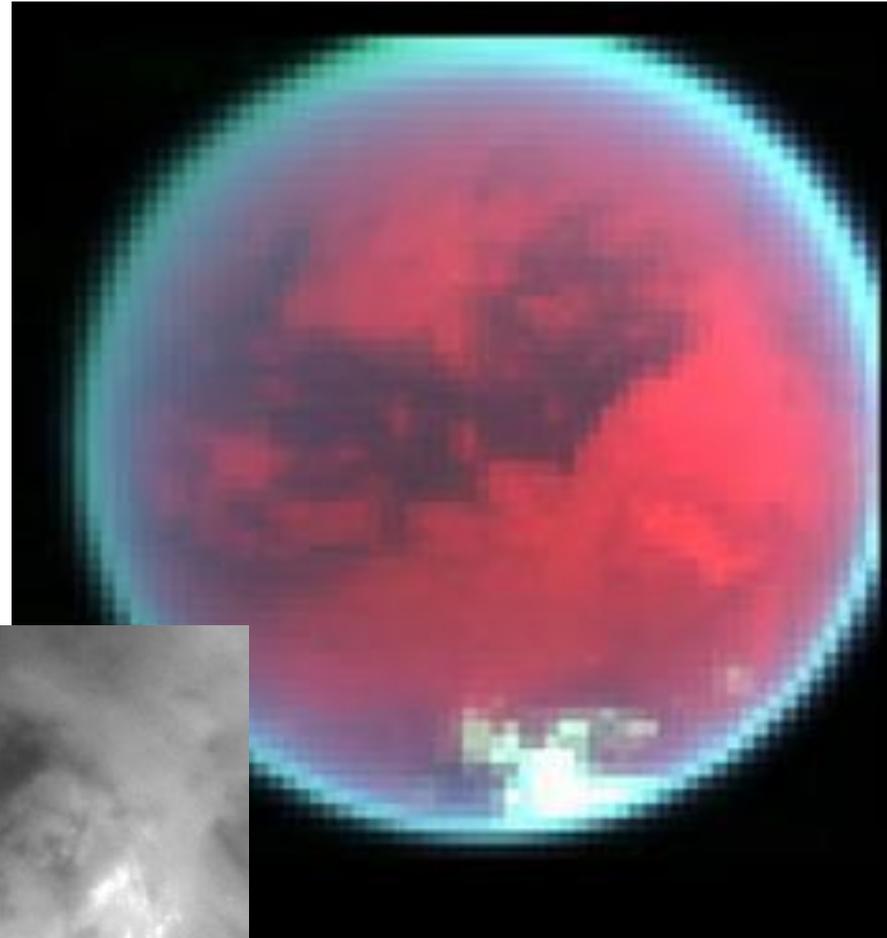
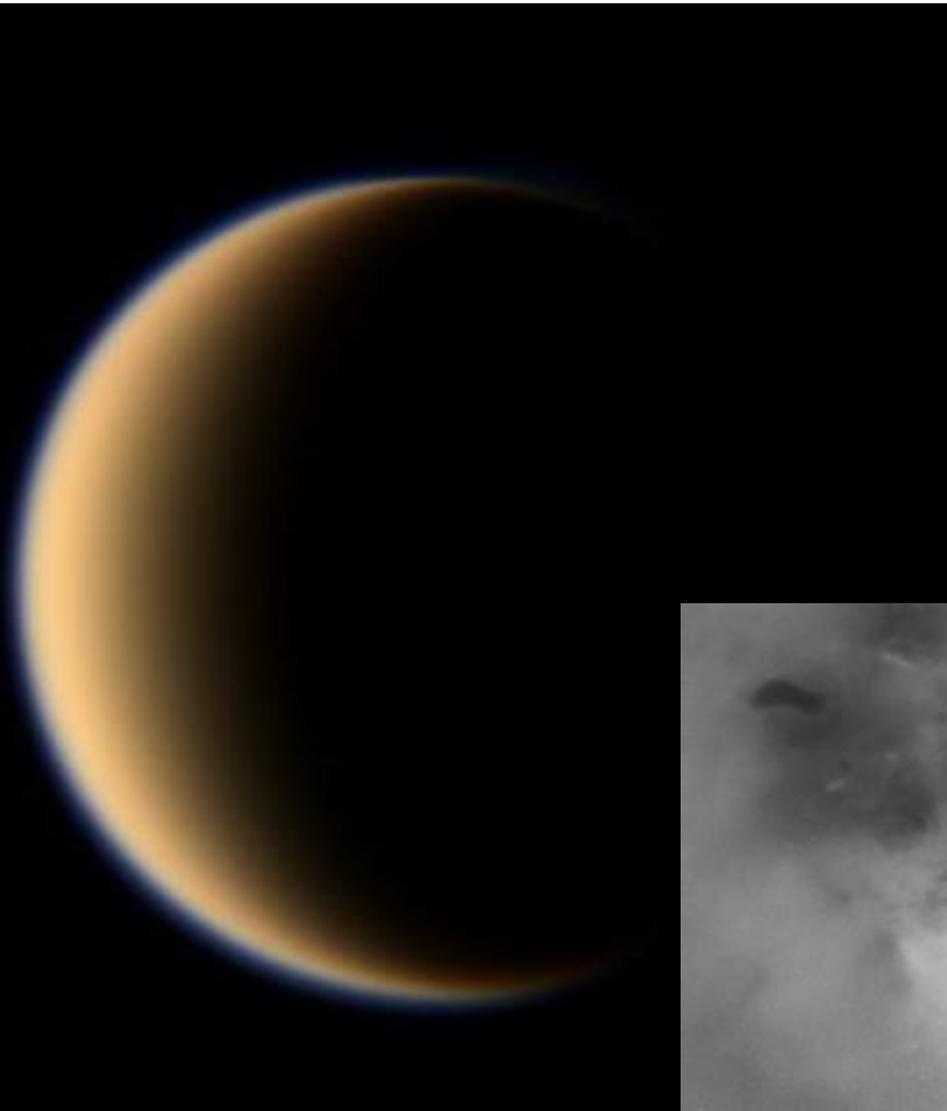
In the presence of **basic wind**, convective activity propagates by the asymmetry of surface flux.

# Organization affected by asymmetry of boundary condition

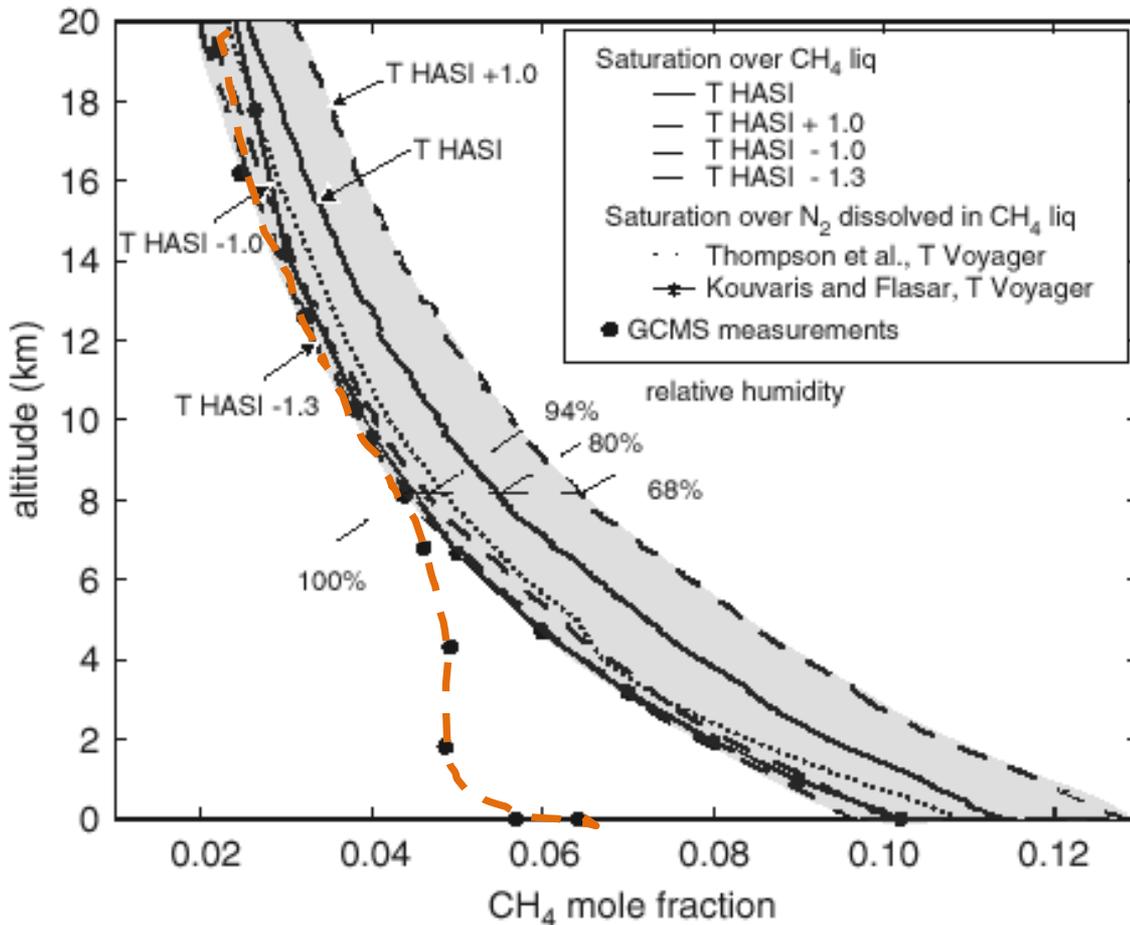
Rainfall intensity **propagating pattern is prominent.**



# Methane clouds on Titan



# Methane distribution in lower atmosphere of Titan



Atreya et al(2006)

saturated  
from 8-14 km.

significantly  
unsaturated  
below 8km.

Any convective  
cloud is possible?

Are there good aerosols?

How will be the  
methane "hydrology"  
like?

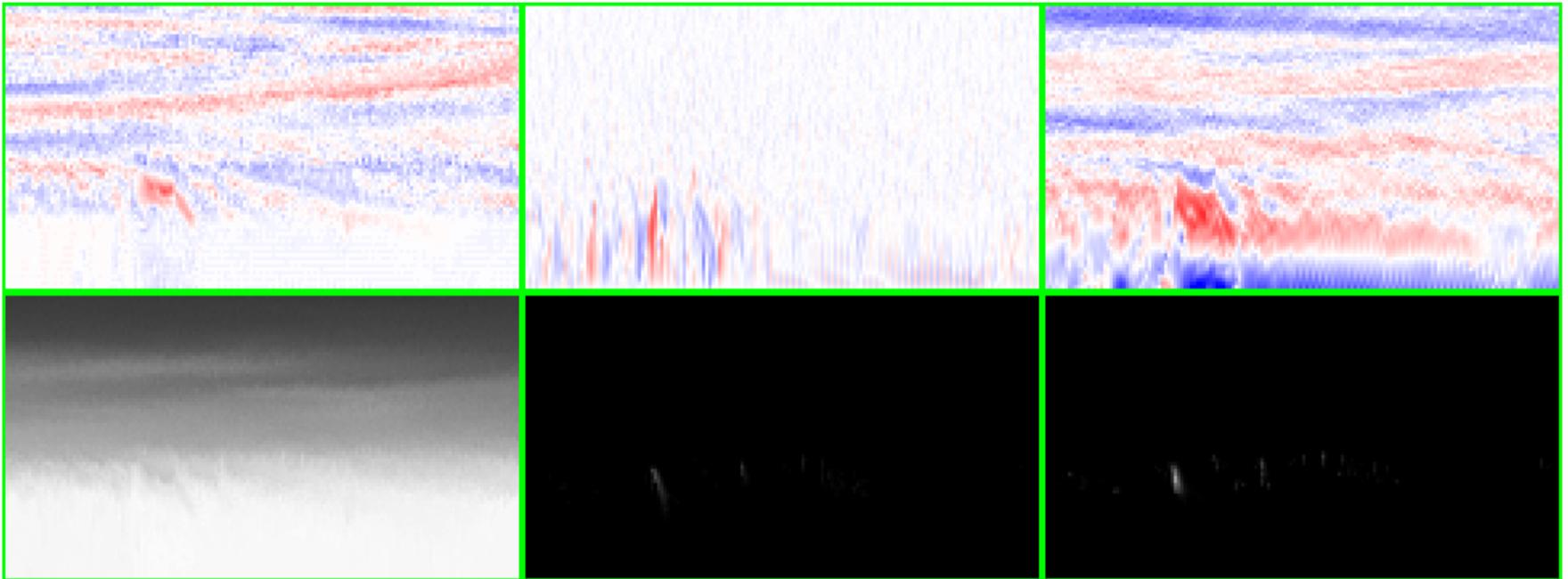
# simulated cloud

beginning of active convective cloud

temperature( $\pm 1\text{K}$ )

w( $\pm 4\text{m/s}$ )

u( $\pm 4\text{m/s}$ )



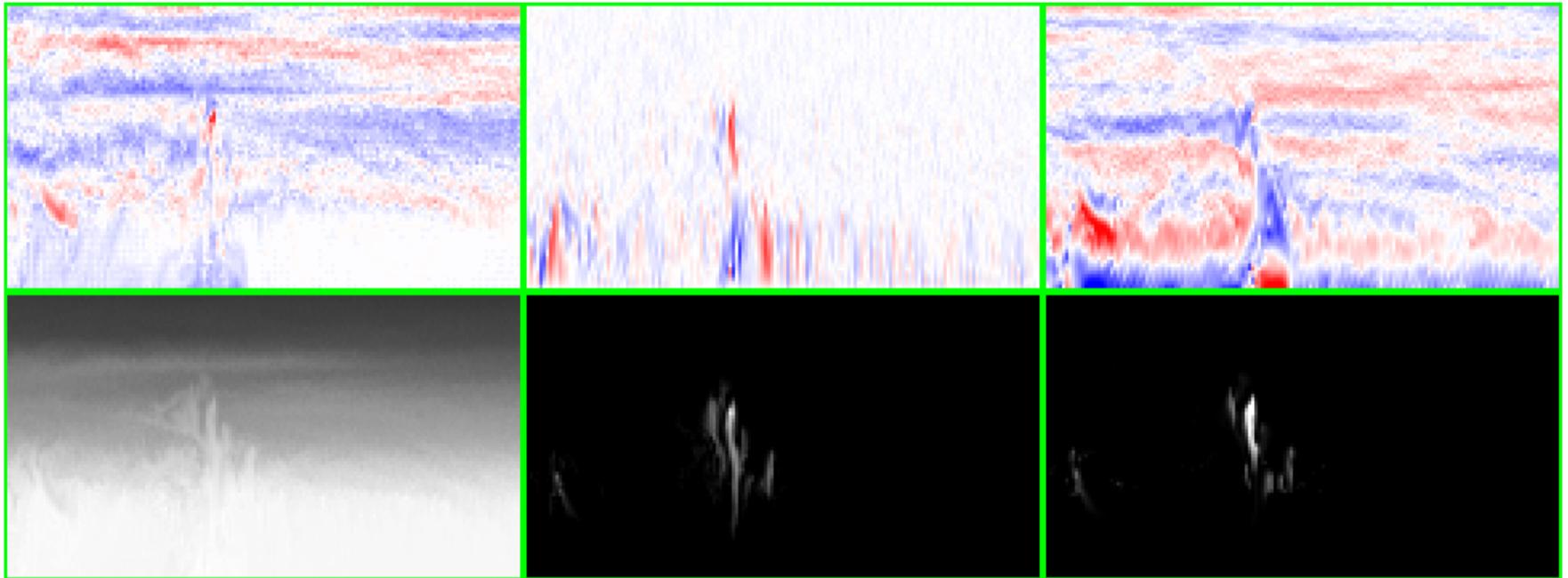
mixing ratio : vapor(0-0.03) rain(0-0.004) cloud(0-0.016)

横80km 縦20km

# 9hours later

- rainfall occurs, but mostly evaporates before reaching to the ground surface

temperature( $\pm 1\text{K}$ )       $w(\pm 4\text{m/s})$        $u(\pm 4\text{m/s})$



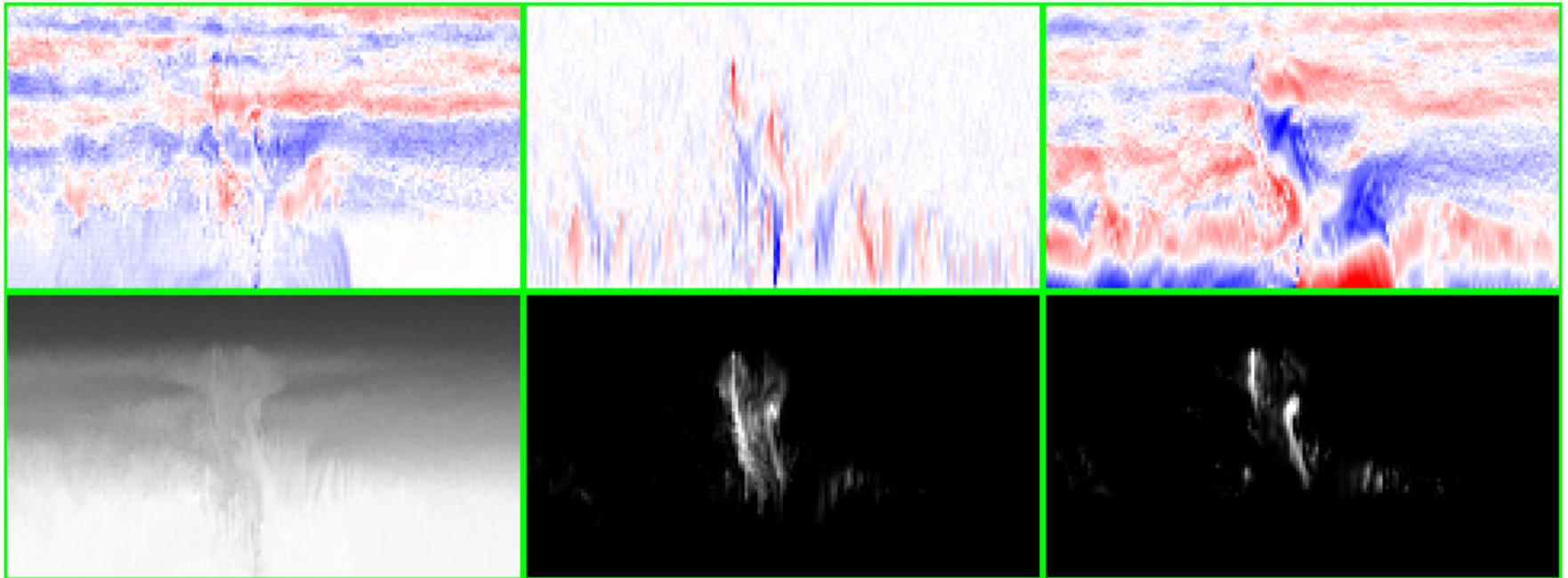
mixing ratio : vapor(0-0.03) rain(0-0.004) cloud(0-0.016)

横80km 縦20km<sup>52</sup>

# 14hours later

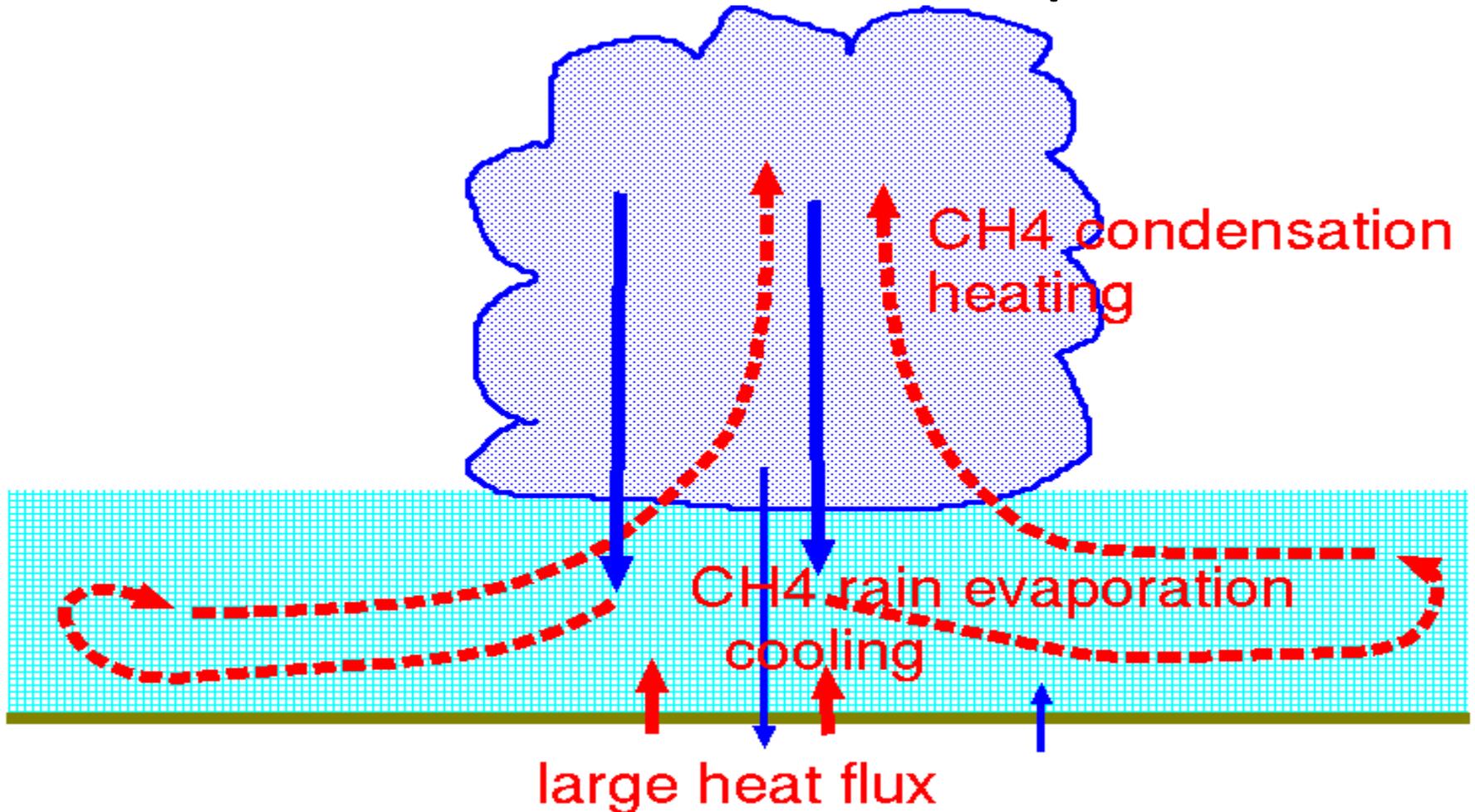
- cloud top is 16km. Cold pool near the surface resulting in successive cloud formation.

temperature( $\pm 1\text{K}$ )      w( $\pm 4\text{m/s}$ )      u( $\pm 4\text{m/s}$ )



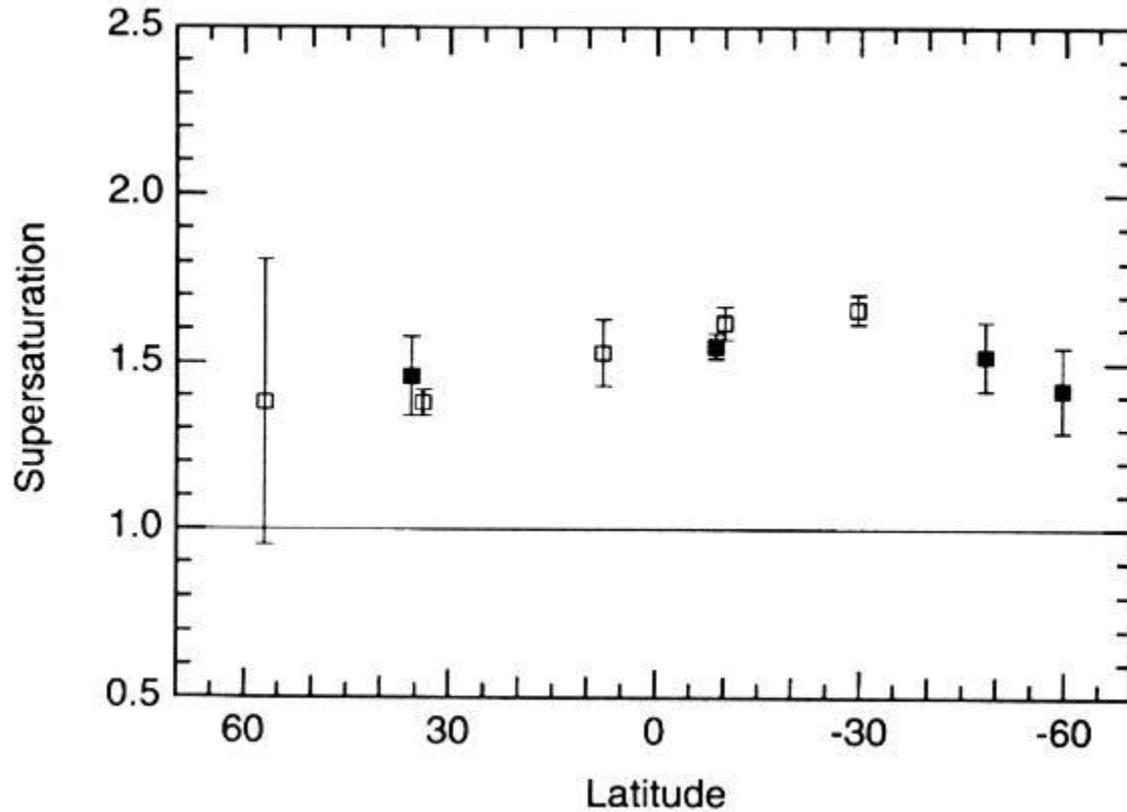
mixing ratio : vapor(0-0.03) rain(0-0.004) cloud(0-0.016)  
横80km 縦20km

# Possibly large contribution to vertical heat transport



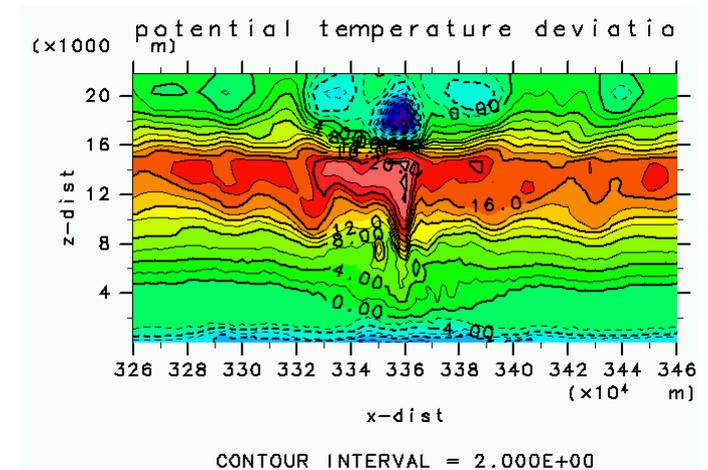
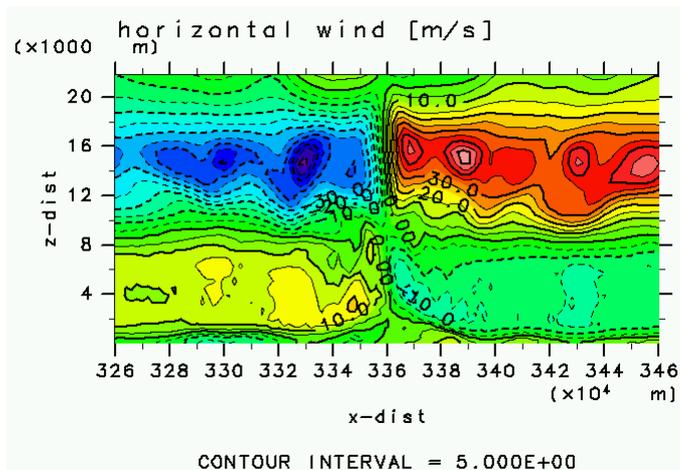
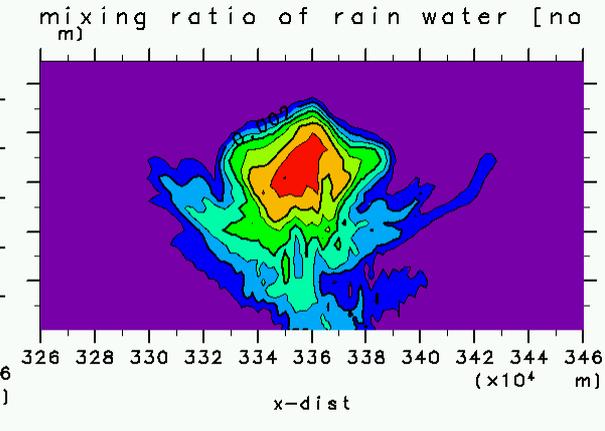
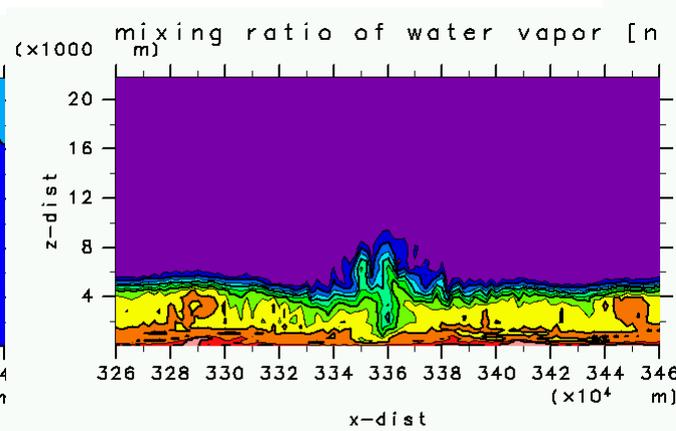
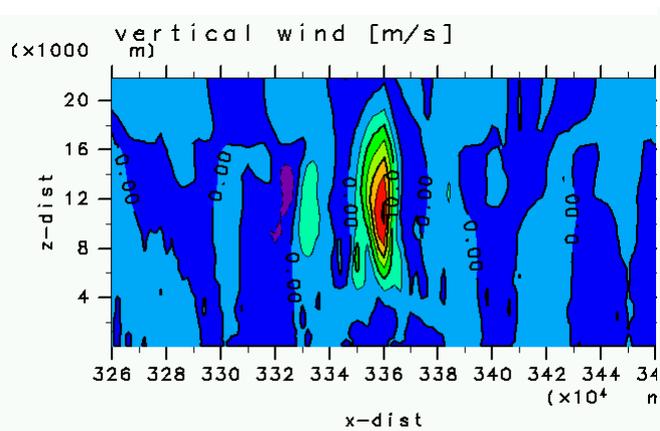
Precipitation and evaporation are weak.

# Large degree of super saturation at other part of the atmosphere?

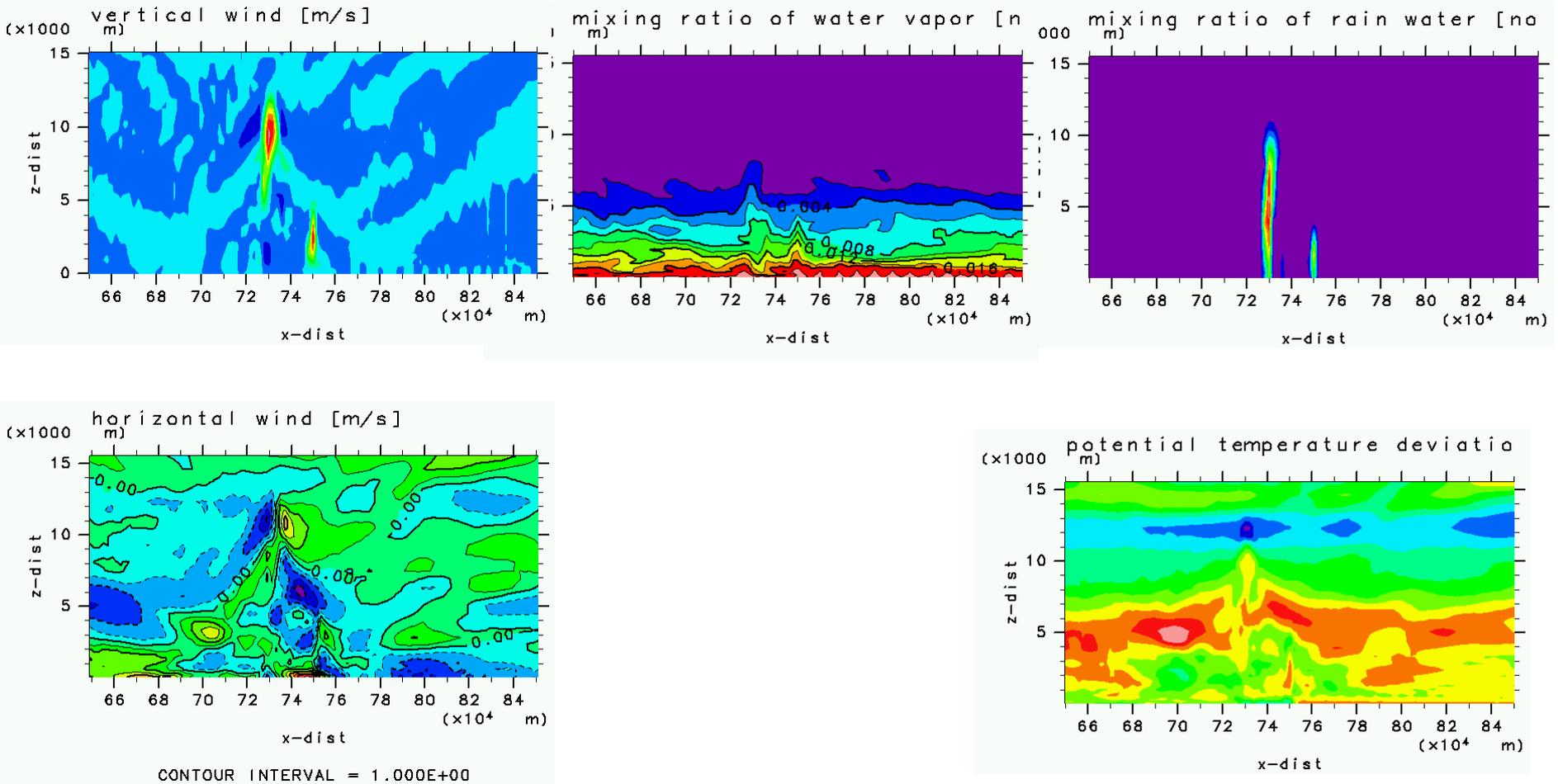


Flasar(1998)

# With large threshold for condensation (earth-like composition)



# Without threshold for condensation (earth-like composition)





# Jupiter

NH<sub>3</sub> condensation

H<sub>2</sub>S+NH<sub>3</sub> –NH<sub>4</sub>SH

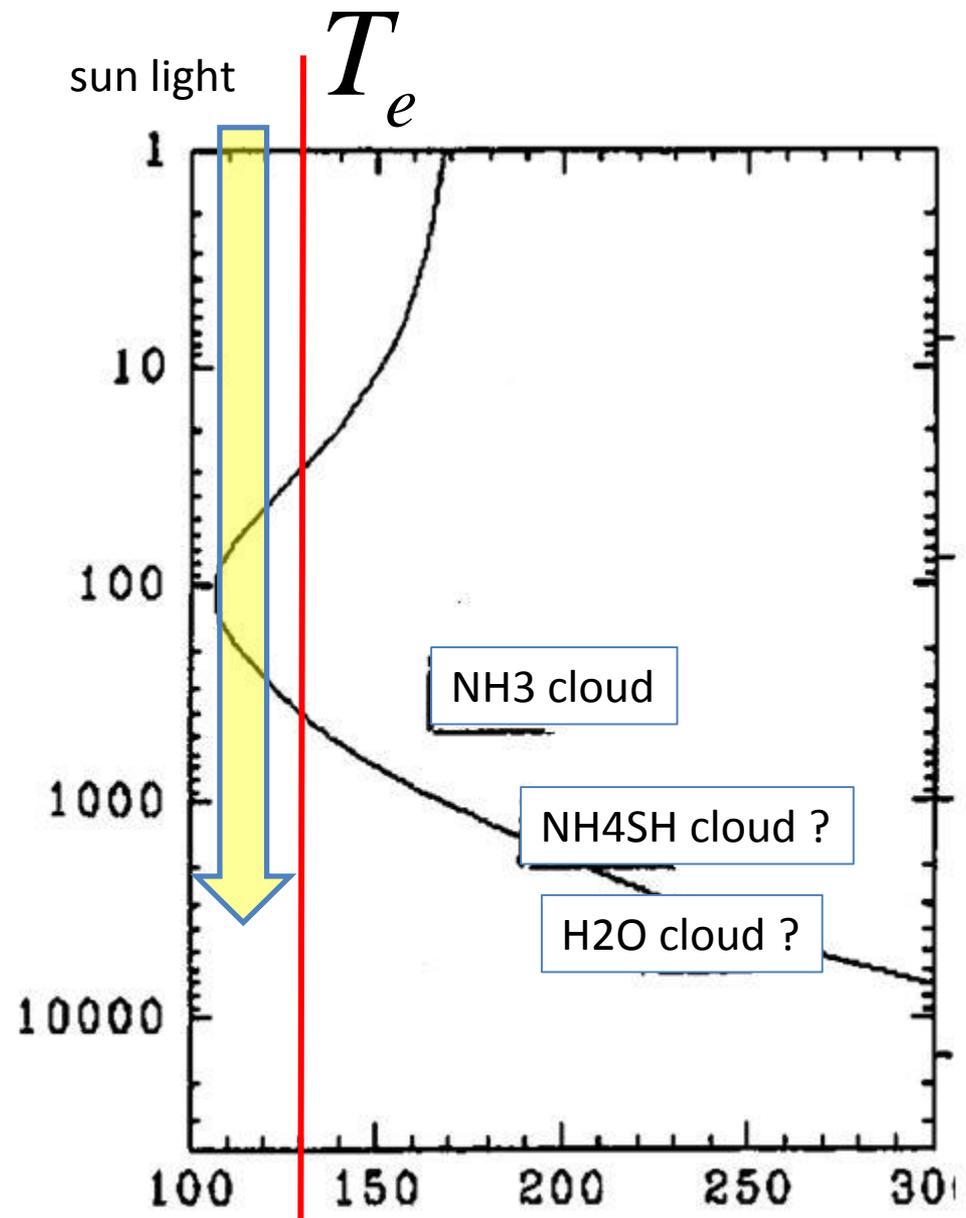
H<sub>2</sub>O condensation

(H<sub>2</sub>O NH<sub>3</sub> solution?)

Condensable components are heavier than the non-condensable component.

No oceans below.

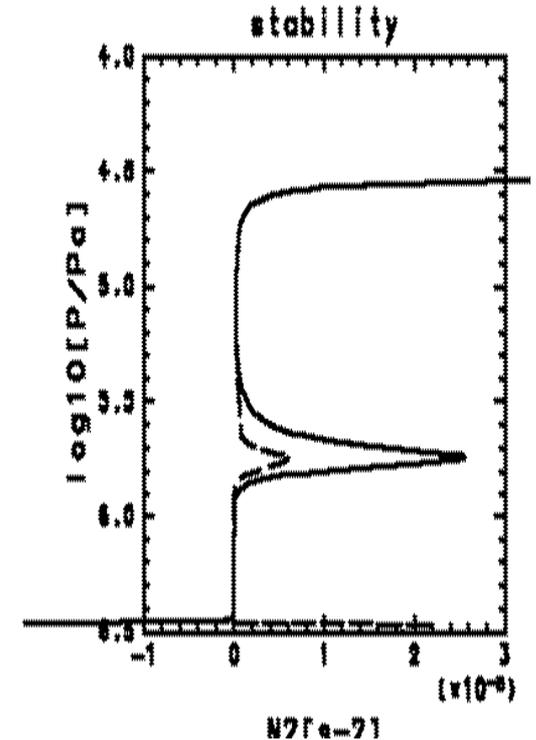
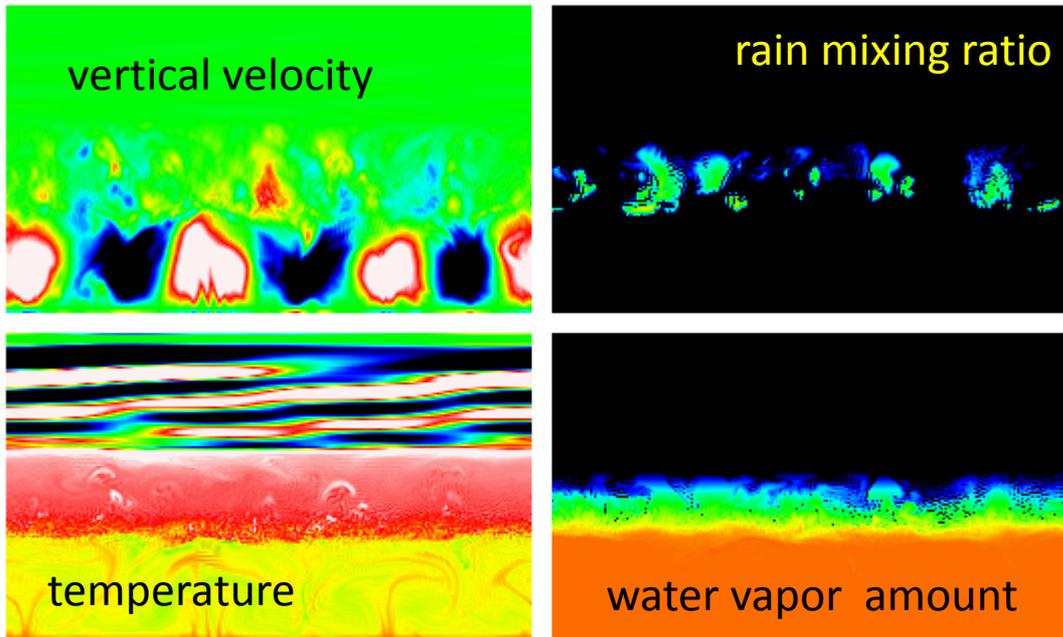
but heat from deep interior, indispensable to keep the atmosphere warm enough to allow active cloud processes.



Nakajima et al(1998)

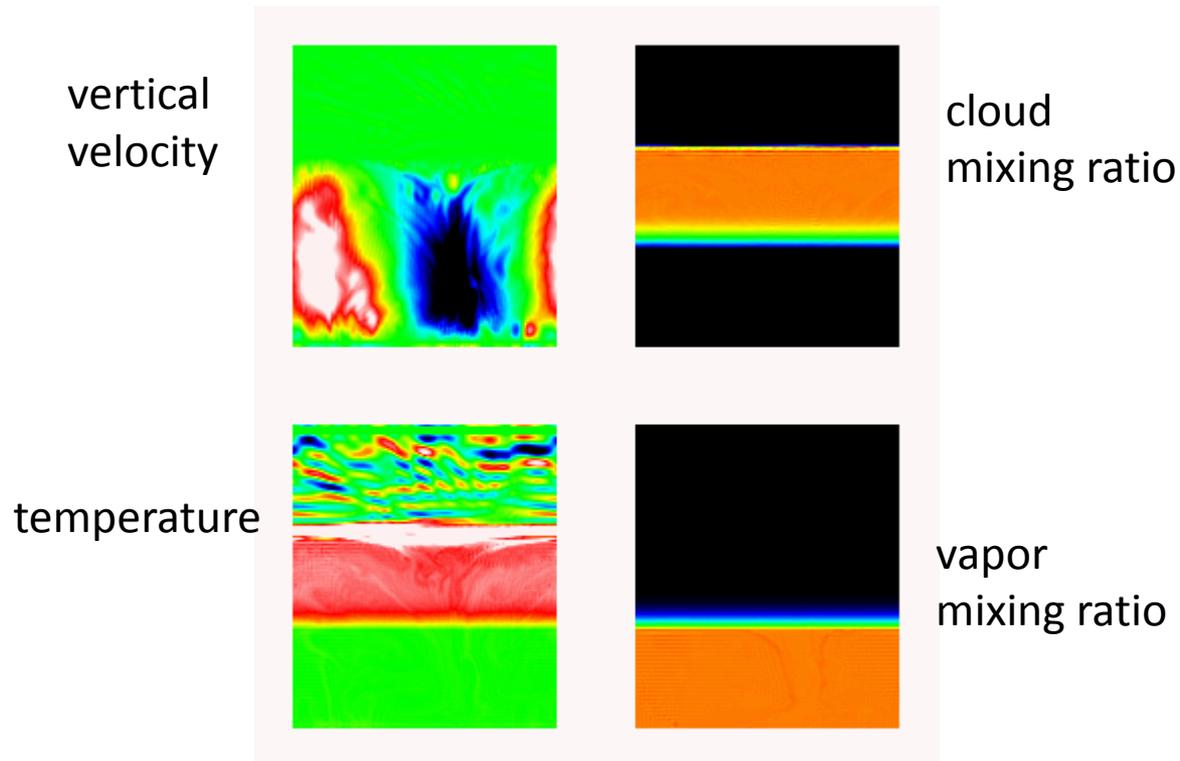
# Jupiter (with H2O only)

IT = 08



Static stability is dominated by the gradient of mean molecular weight

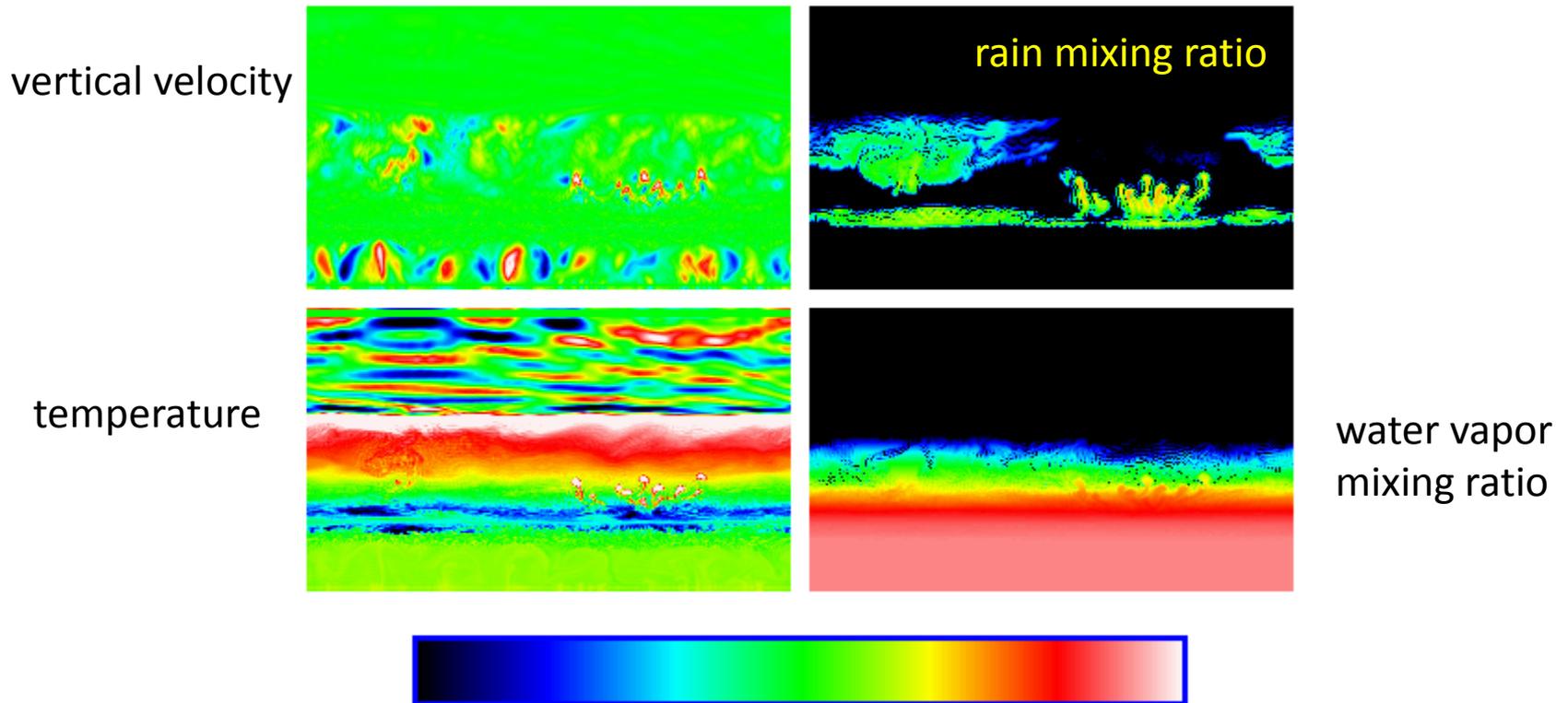
# Case with no cloud physics (no raindrop formation)



We have another cup of Miso soup.

# 10 times enhancement of H2O exceeding the positive buoyancy near the bottom domain

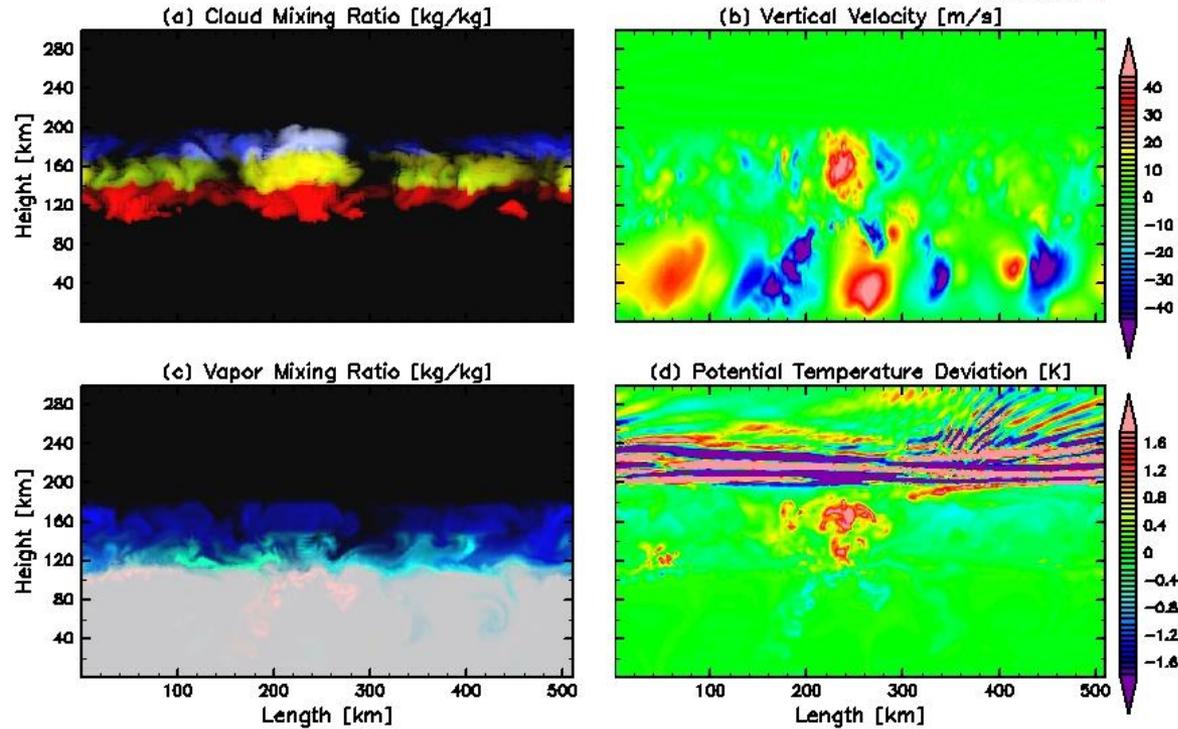
IT = 0



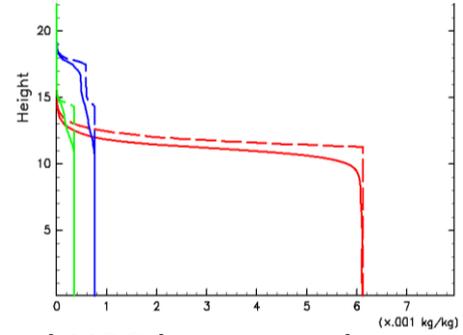
Layered cloud with super adiabatic lapse rate near the condensation level

# Convection with all of NH<sub>3</sub>, NH<sub>4</sub>SH, and H<sub>2</sub>O clouds Sugiyama et al (2009)

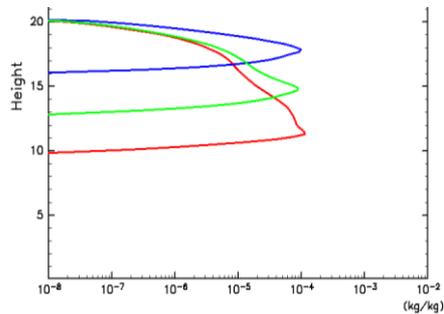
t = 1030000.0 s



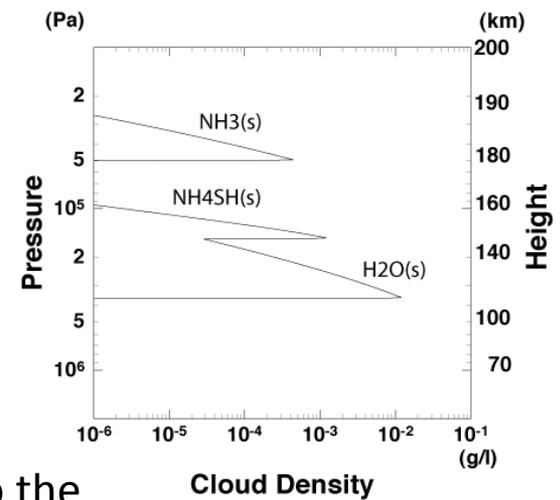
interaction among three cloud layers



NH<sub>3</sub> and H<sub>2</sub>S begin to decrease at H<sub>2</sub>O condensation level.

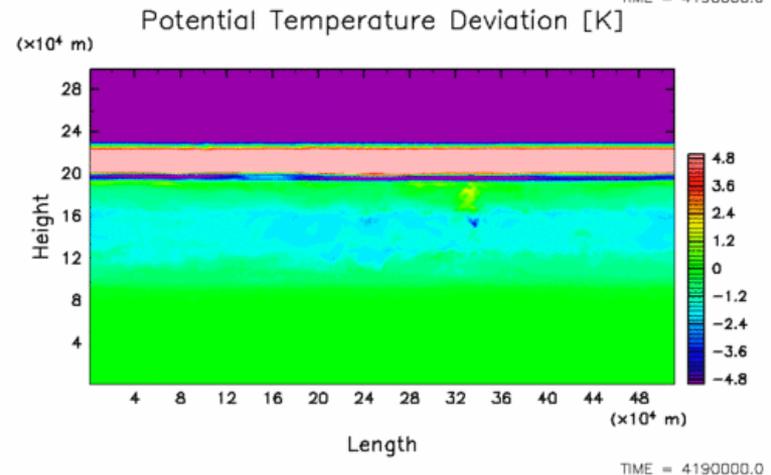
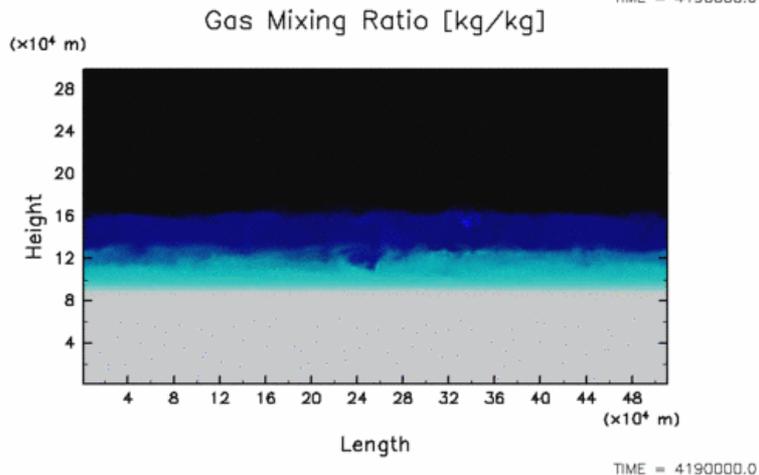
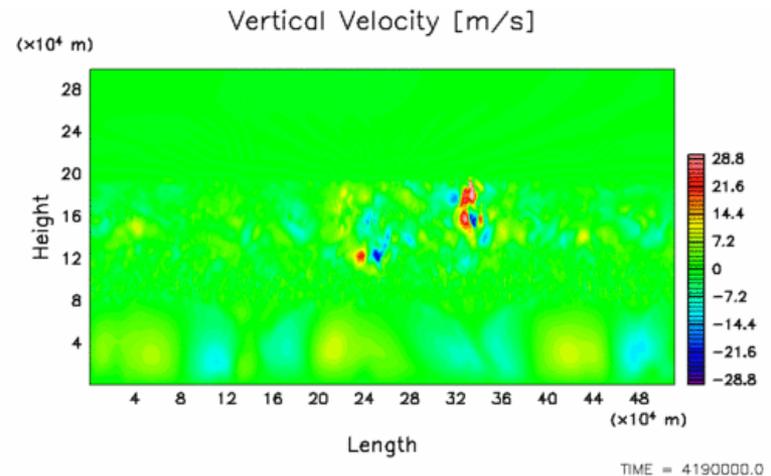
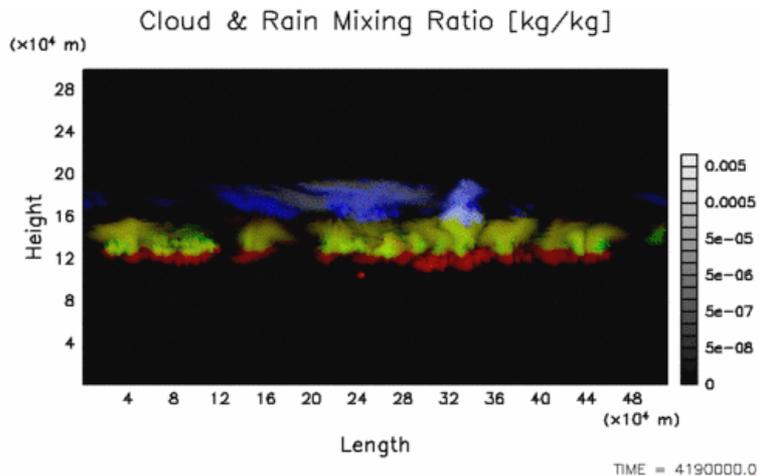


H<sub>2</sub>O cloud is transported to the top of NH<sub>3</sub> cloud.

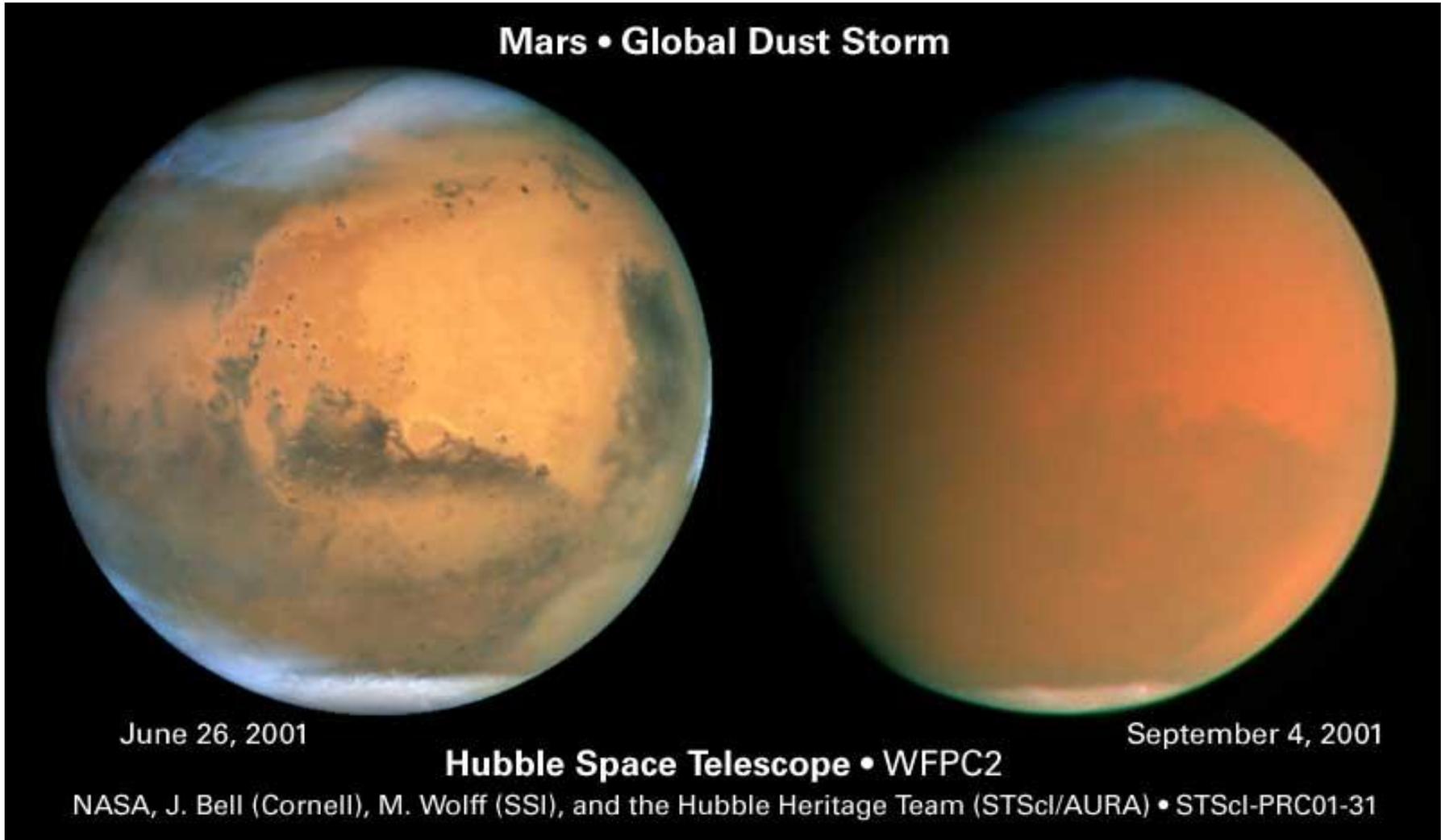


# Intermittency of cloud activity (see Sugiyama's poster)

Convection in the "active period" is quite vigorous!



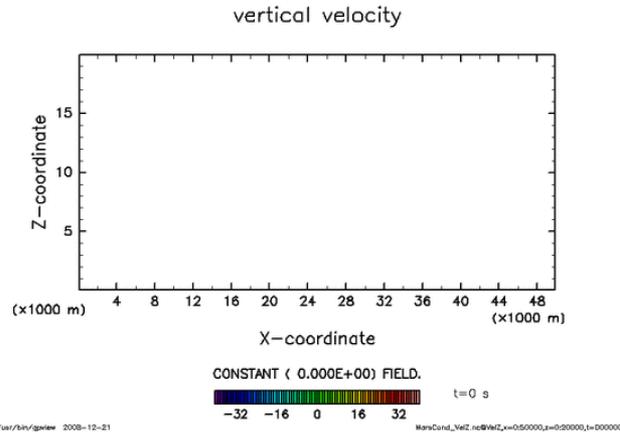
# Mars : condensation of major component (CO<sub>2</sub>)



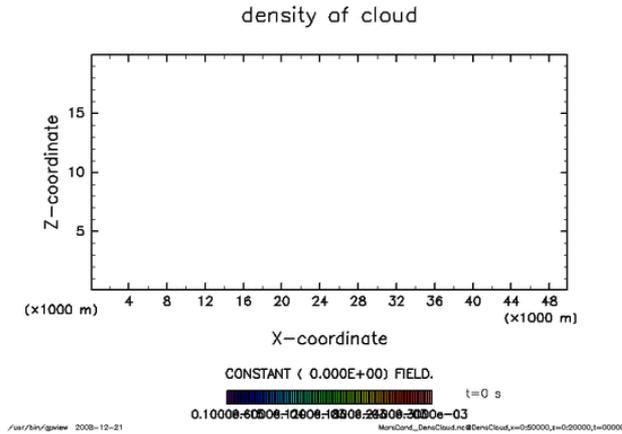
# CO2 cloud with condensation at S=135%

(See Yamashita's poster)

vertical velocity



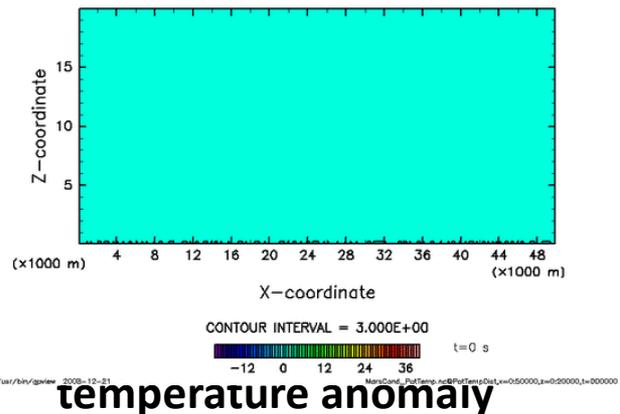
cloud density



weight of cloud is not included

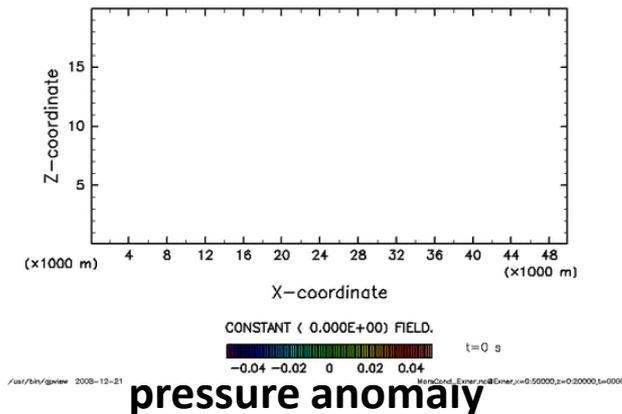
transient  
towe-like  
deep convection

disturbance of potential temperature



temperature anomaly

disturbance of Exner

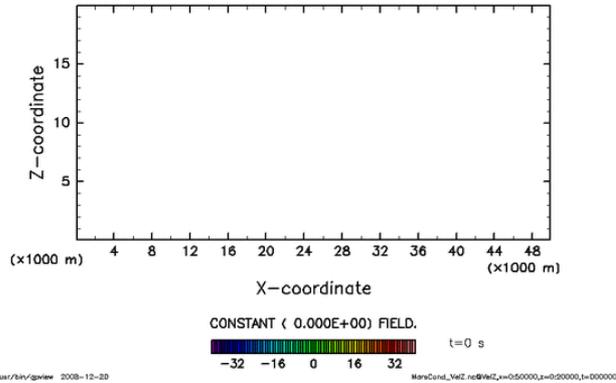


pressure anomaly

# CO2 cloud with condensation at S=100% (See Yamashita's poster)

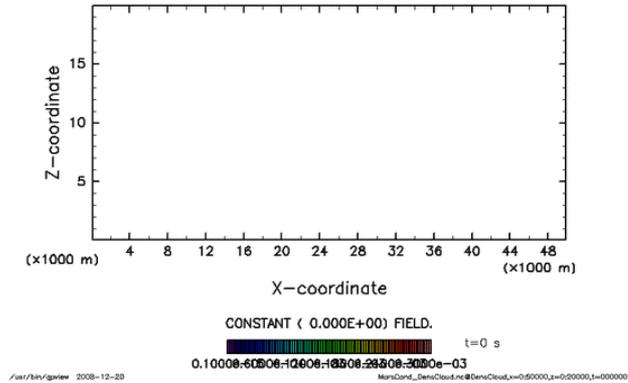
**vertical velocity**

vertical velocity



**cloud density**

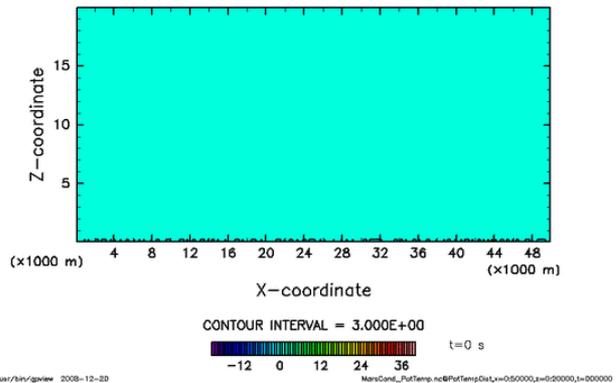
density of cloud



weight of cloud  
is not included

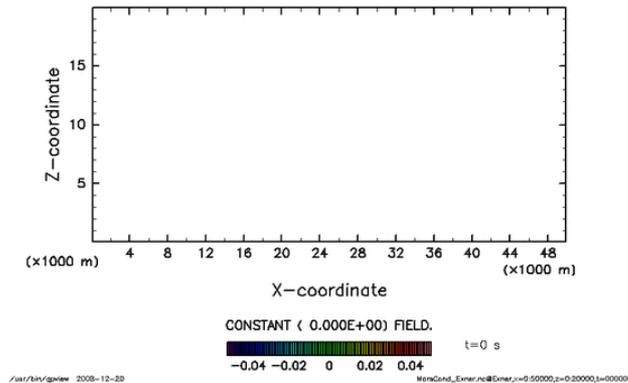
no tower-like  
convective cloud

disturbance of potential temperature



**temperature anomaly**

disturbance of Exner



**pressure anomaly**

Roles of moist convection  
in structure and dynamics  
and so on

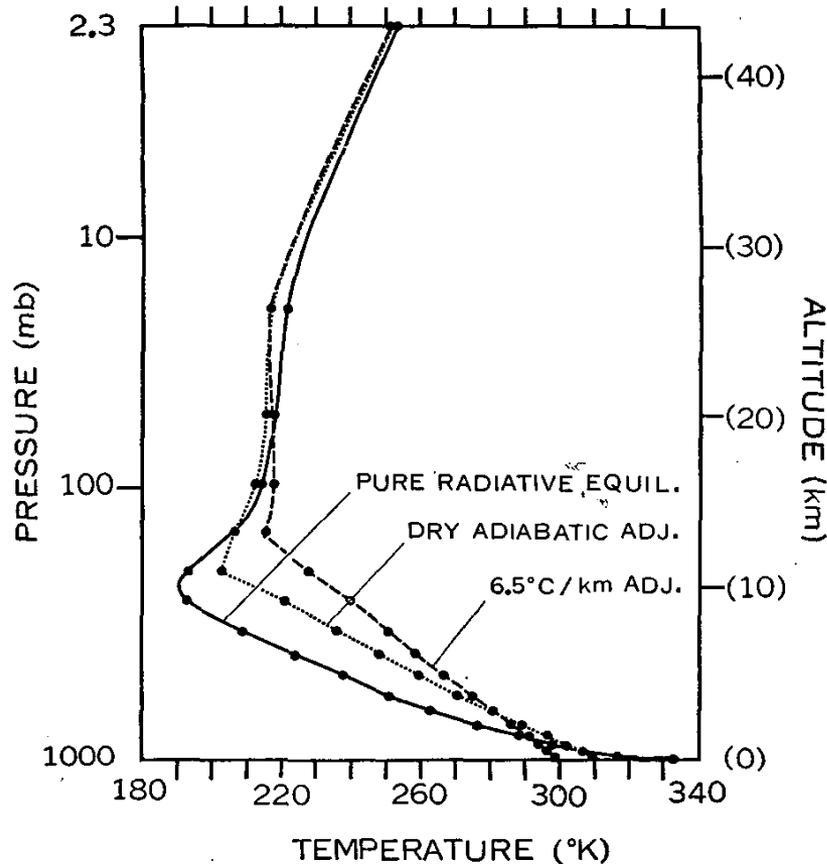
# Some examples

- Modification of atmospheric structure

$$\Gamma_m \neq \Gamma_d$$

- Latent heat transport
- Modification of thermodynamic efficiency of the atmospheric heat engine
- Enhancement of vertical coupling
  - land and the atmosphere (e.g. Titan seasonal cycle)
  - “sea” and the atmosphere ( e.g. El Nino of the earth)
- Interaction with large-scale flow (Jupiter?)
- Effects on climate through the modification of radiative heating/cooling.

# Modification of atmospheric structure

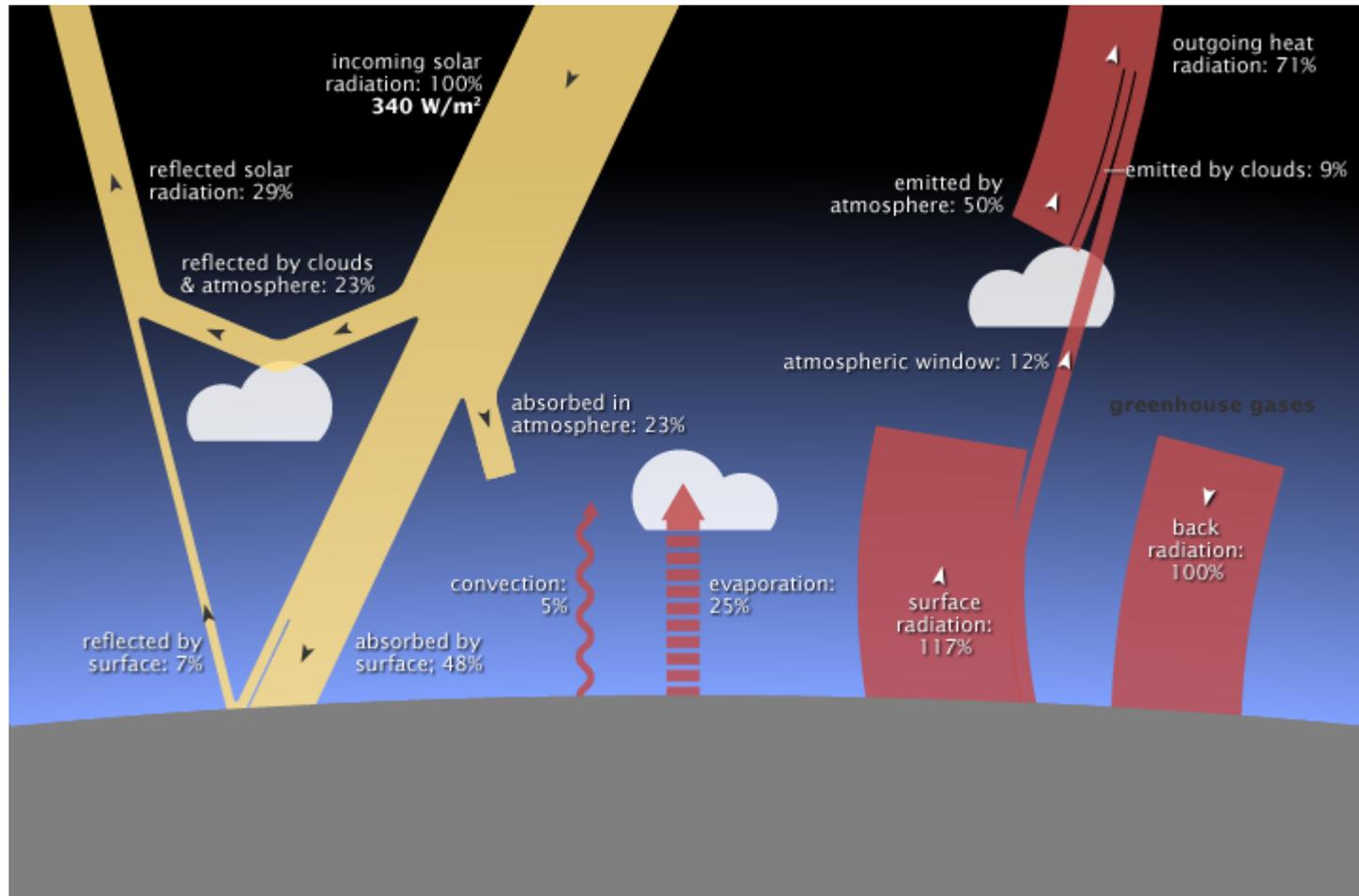


Vertical structure of earth's atmosphere obtained with radiative-convective equilibrium model.

- Inclusion of moist convective adjustment results in
- cooling of lower troposphere
  - warming of upper troposphere
  - increased depth of troposphere

Manabe and Strickler (1964)

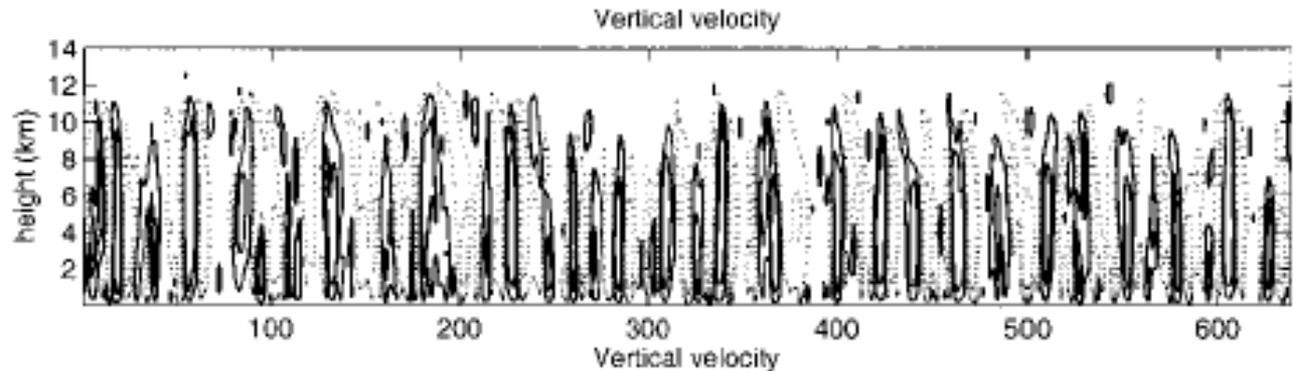
# “Latent” heat transport



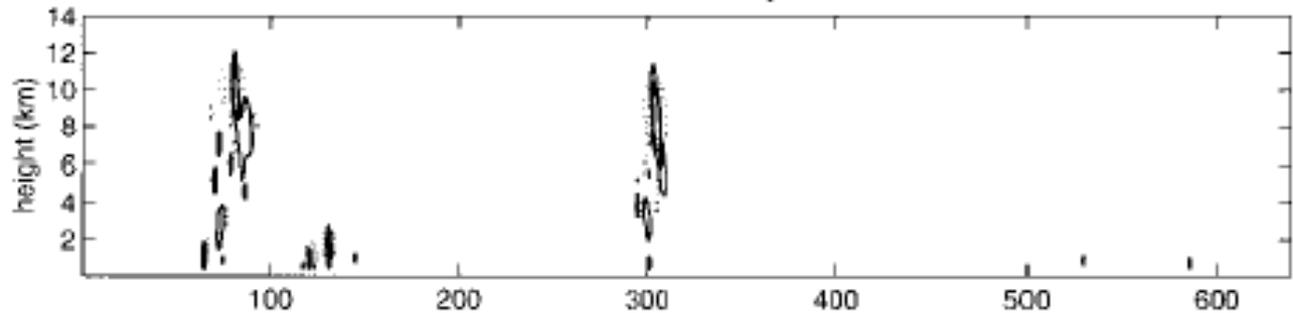
# Slow down of convective motion with fixed thermal forcing

Same thermal forcing (heating at the lower boundary and cooling aloft) drives the two systems below, but motion is much vigorous in dry convection!

Dry convection



Moist  
convection



Pauluis and Held (2002a,2002b)

# Cloud convection as a “dehumidifier” (moisture remover)

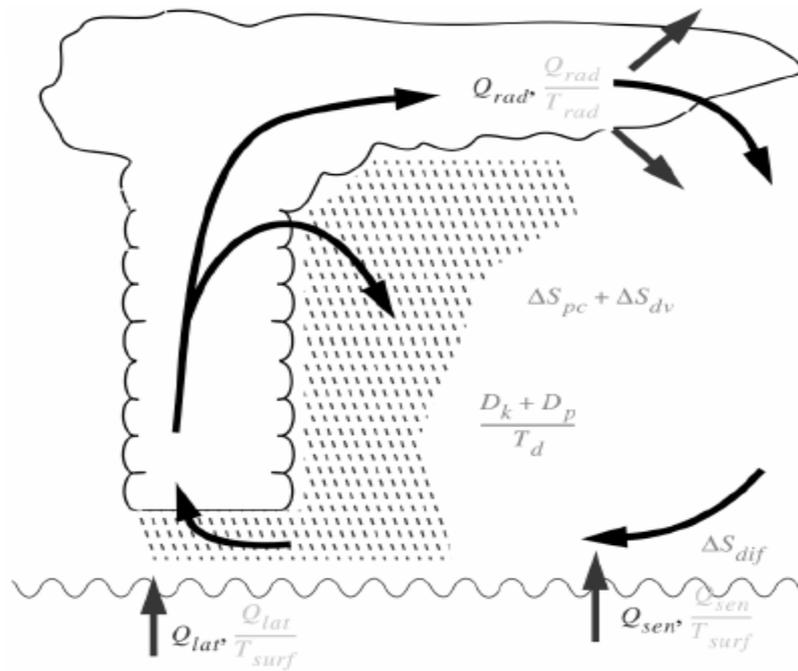


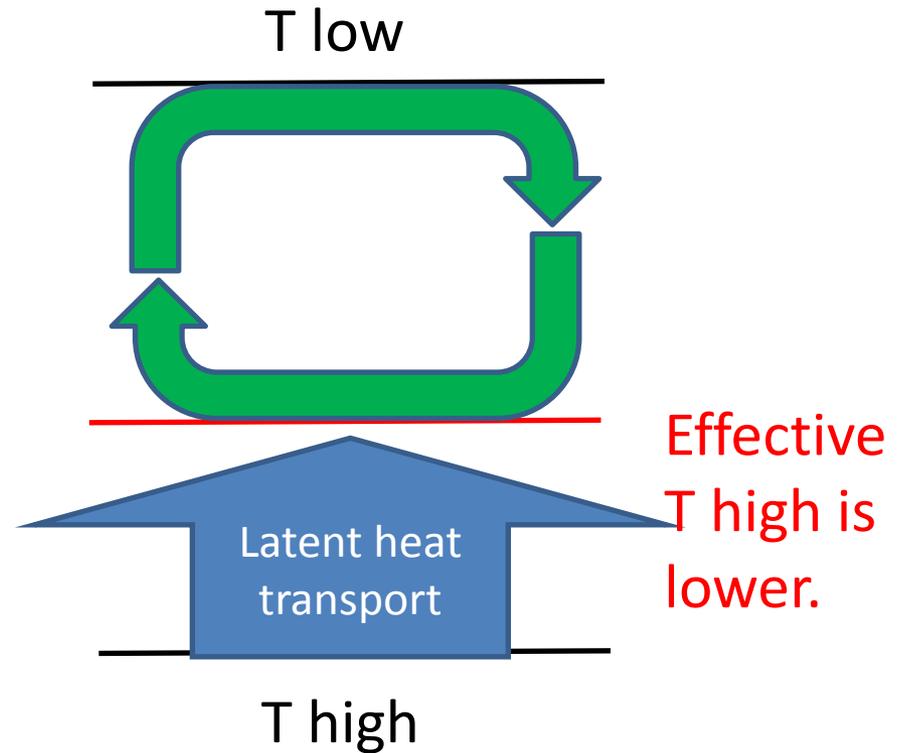
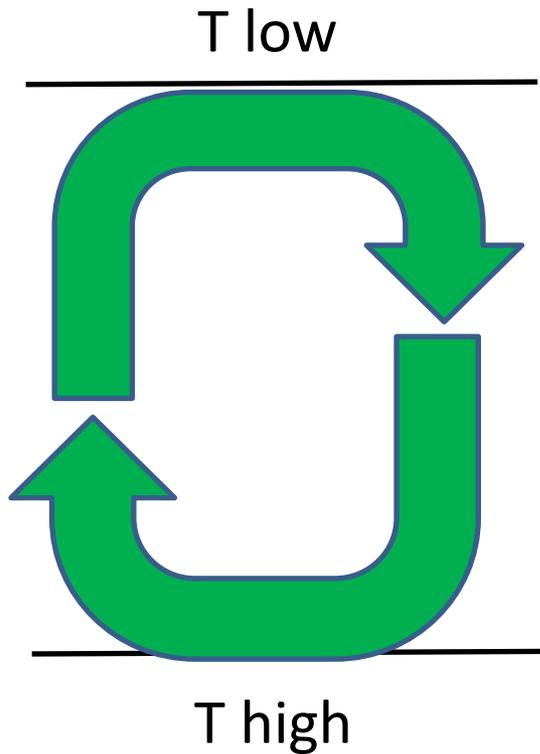
FIG. 1. Schematic representation of the energy and entropy budgets of an atmosphere in radiative-convective equilibrium. The heat sources and sinks are radiative cooling  $Q_{rad}$ , surface sensible heat flux  $Q_{sen}$ , and surface latent heat flux  $Q_{lat}$ . The irreversible entropy sources are frictional dissipation  $D/T_d$ , diffusion of heat  $\Delta S_{dif}$ , diffusion of water vapor  $\Delta S_{dv}$ , and irreversible phase changes  $\Delta S_{pc}$ .

Non-equilibrium evaporation lowers the thermodynamic efficiency to 1/3.

$$\Delta S = M_{evap} R_v \log(R_h)$$

Relative humidity at the sea surface

# The view focusing on non-condensable component



# Decrease of $\Delta T$ is quite significant for Earth's atmosphere

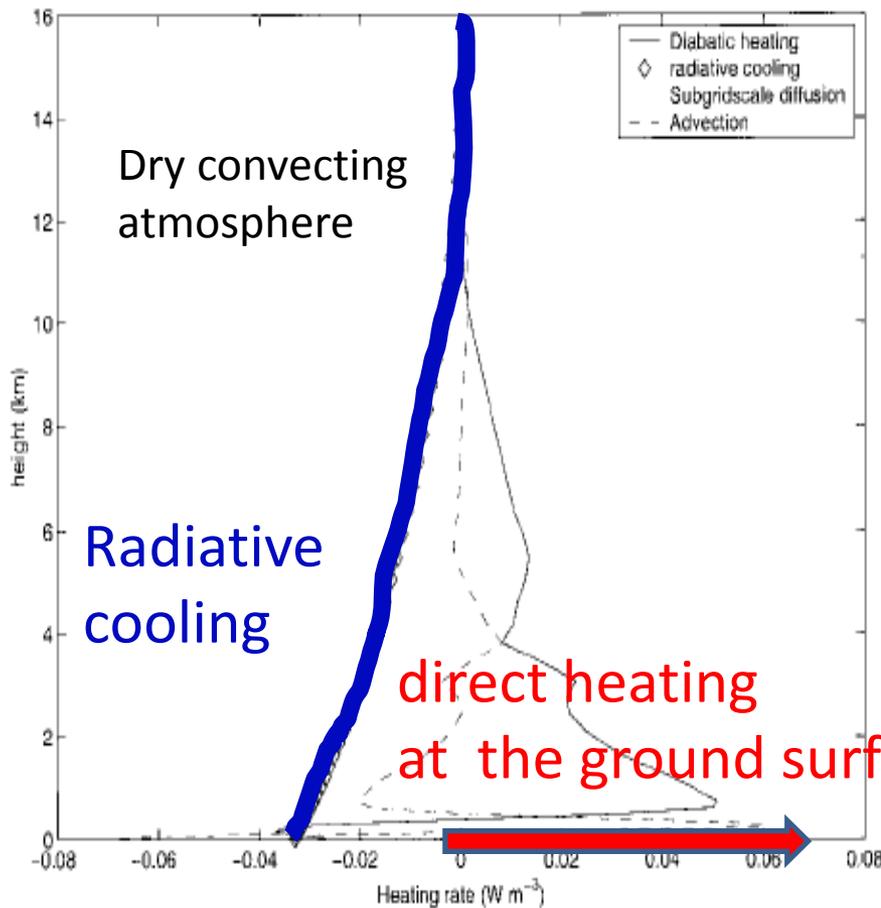


FIG. 5. Horizontally averaged heating rates.

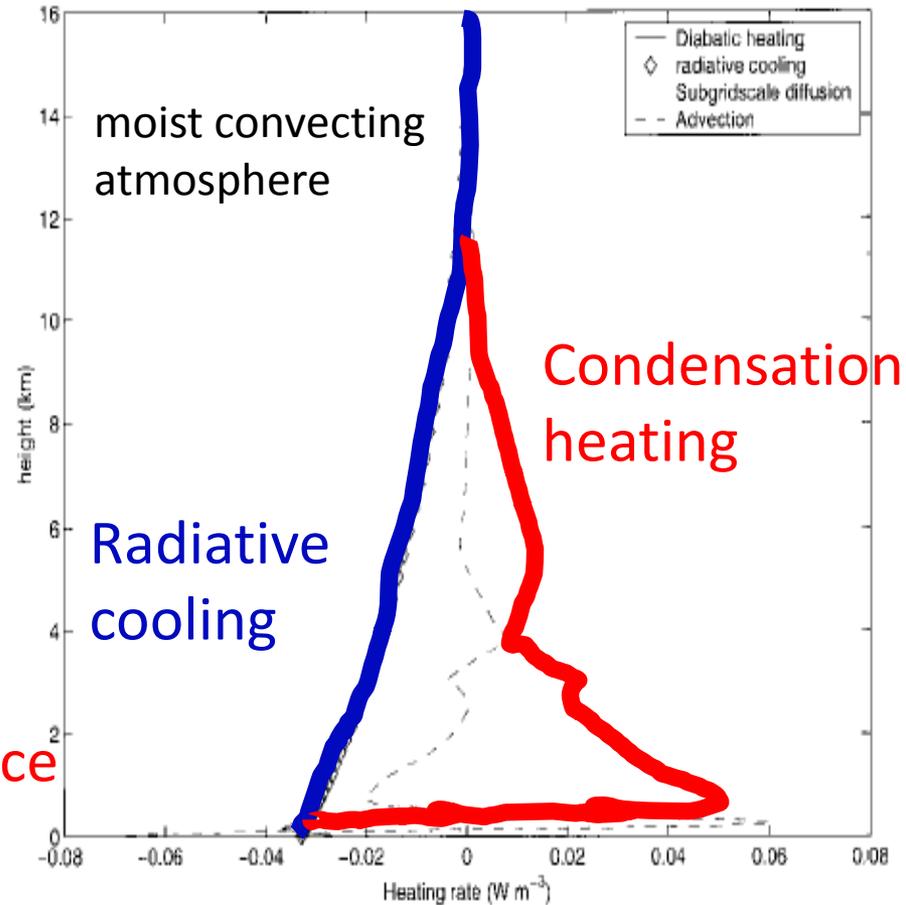


FIG. 5. Horizontally averaged heating rates.

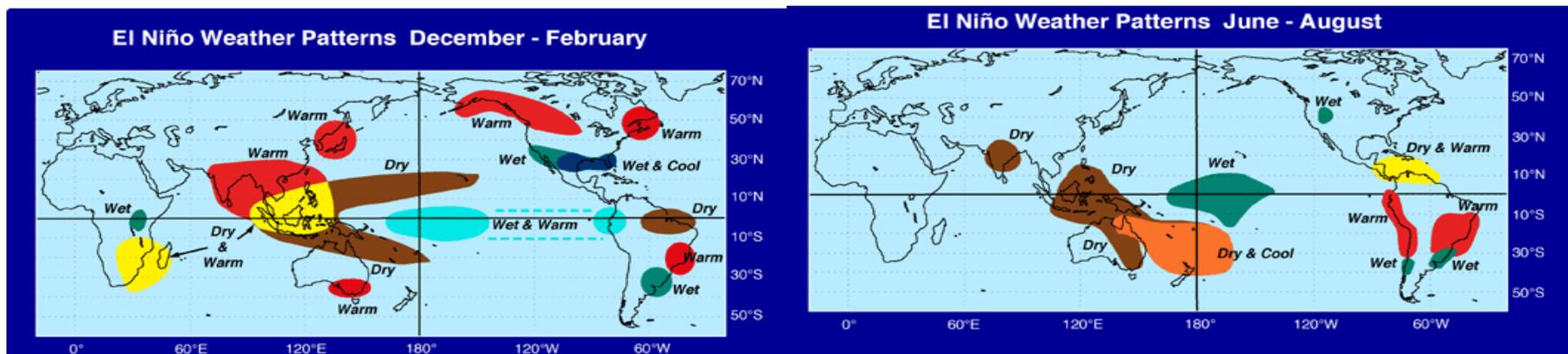
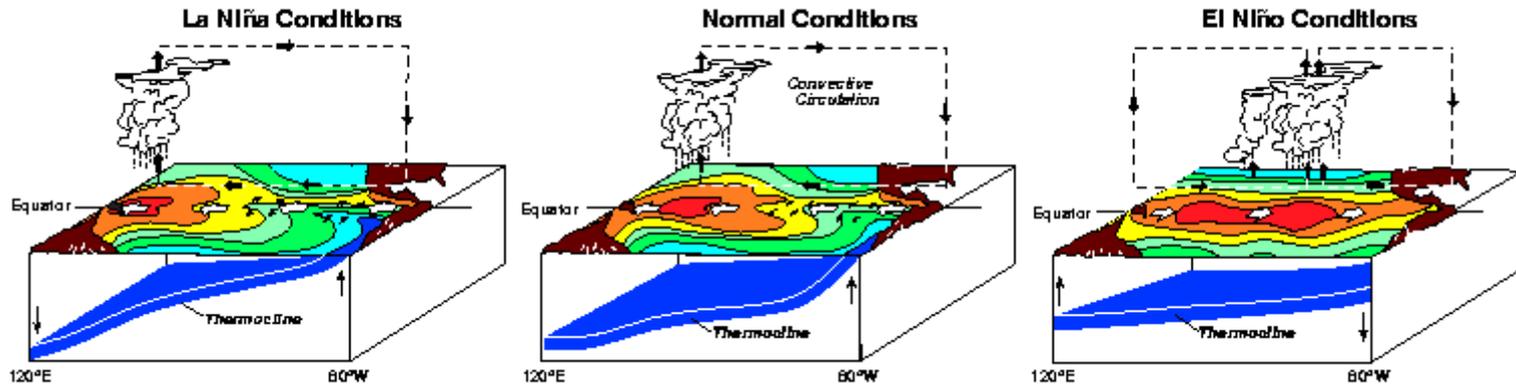
Pauluis and Held (2002a,2002b)

# Additional effect may increase the thermodynamic efficiency

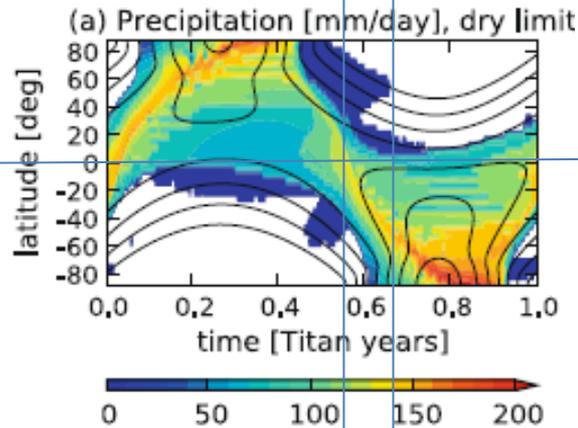
- Vertical distribution of radiative forcing may be modified, so that the depth (and the temperature difference) of the convecting layer may increase with moist convection.
- Large-scale structure may increase the temperature of “high-temperature heat source”.
- Even if the efficiency is low, intermittency (in space and time) results in vigorous motion, sometime somewhere.

# Result of enhanced vertical coupling by moist convection example 1:

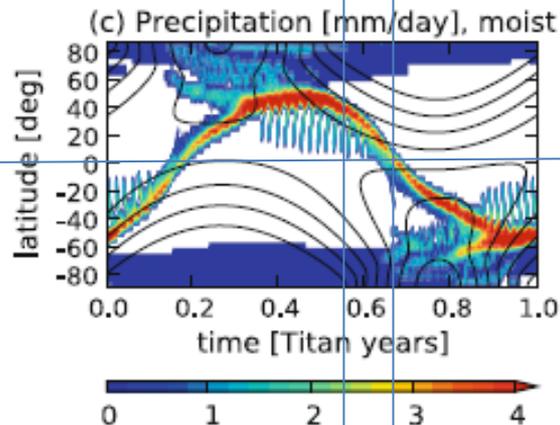
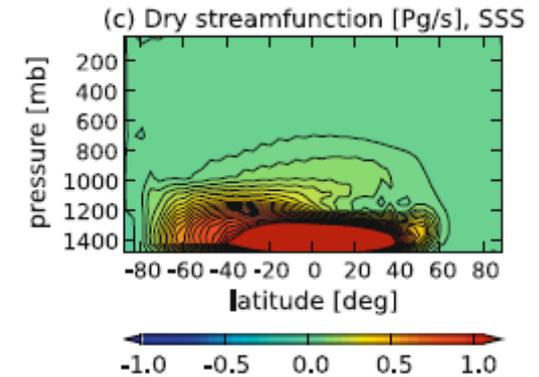
## *El Niño*



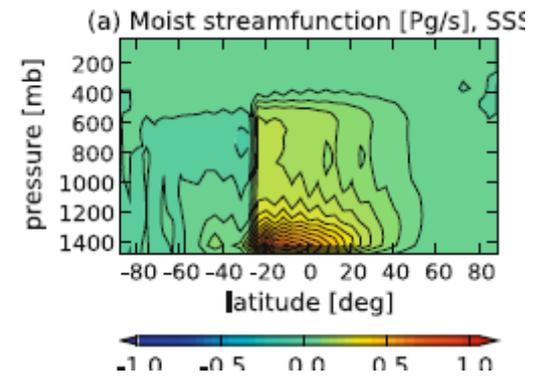
# Delay of seasonal cycle (Titan) by enhanced land-atmosphere coupling



dry  
model

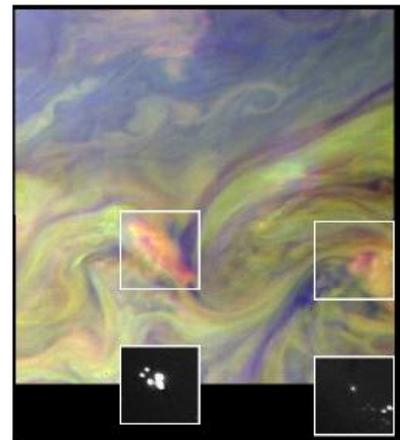
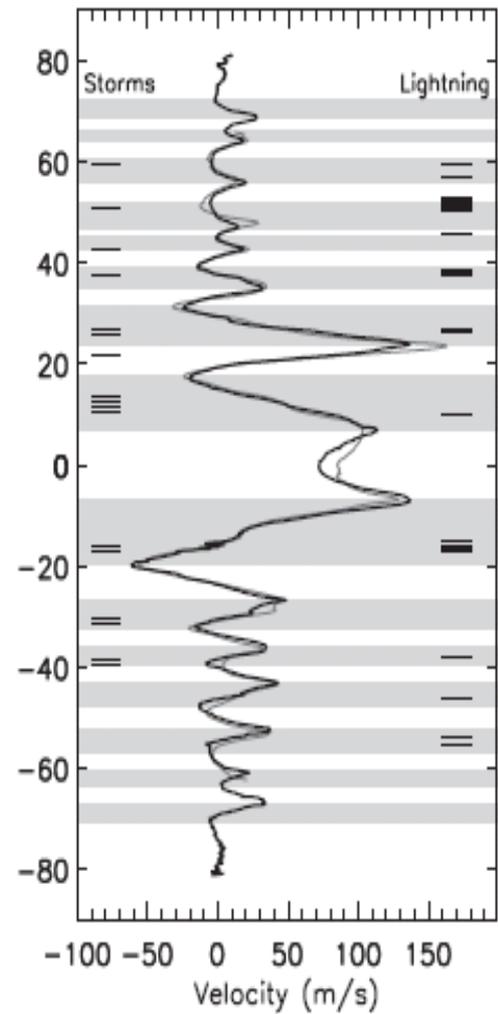
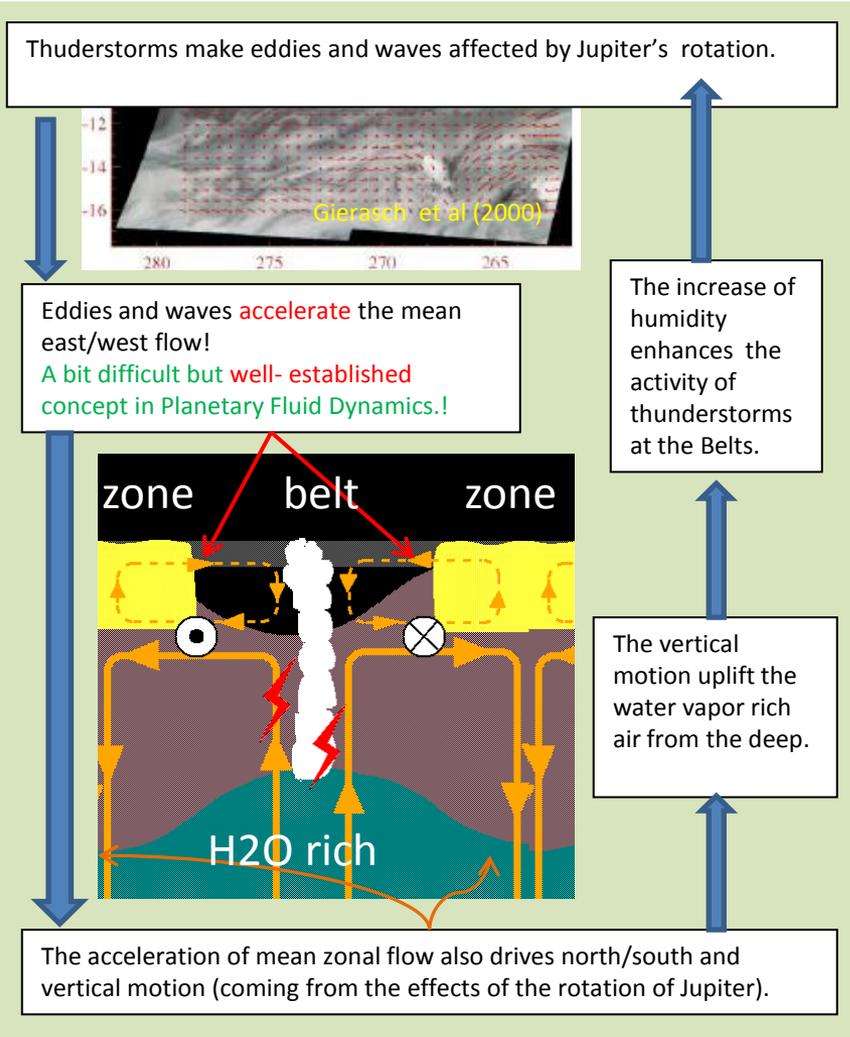


moist  
model



Mitchell et al, Icarus 203 (2009) 250–264

# Possible interaction between cloud and zonal-flow



# Concluding Remarks

- Moist convection is working in various planetary atmospheres.
- Properties of convection differ considerably depending on composition, thermal forcing etc.
- Detail of the cloud physics may be important.
- Moist convection affects various aspects of the structure, dynamics, and evolution of the atmosphere.

**Thank you for your attention!**

# References

- Abe, Y., and Matsui, T., 1988: Evolution of an Impact-Generated H<sub>2</sub>O-CO<sub>2</sub> Atmospheric and Formation of a Hot Proto-Ocean on Earth. *J. Atmos. Sci.*, 45, 3081-3101.
- Atreya, S. K., Adams, E. Y., Niemann, H. B., Demick-Montelara, J. E., Owen, T. C., Fulchignoni, M., Ferri, F., Wilson, E. H., 2006: Titan's methane cycle. *Planet. Space Sci.*, 54, 1177-1187.
- Baines, K. H., Carlson, R. W., and Kamp, L. W., 2002: Fresh Ammonia Ice Clouds in Jupiter: I. Spectroscopic Identification, Spatial Distribution, and Dynamical Implications. *Icarus*, 159, 74-94, doi:10.1006/icar.2002.6901.
- Bretherton, C. S., 1987: A Theory for Nonprecipitating Moist Convection between Two parallel Planes. Part I: Thermodynamics and "Linear" Solutions. *J. Atmos. Sci.*, 44, 1809-1827.
- Burrow, A., Marley, M., Hubbard, W. B., Lunine, J. I., Guillot, T., Saumon, D., Freedman, R., Sudarsky, D., and Sharp, C., 1997: A NONGRAY THEORY OF EXTRASOLAR GIANT PLANETS AND BROWN DWARFS. *The Astrophysical Journal*, 491, 856-875.
- Colaprete, A., Haberle, R. M., and Toon, O. B., 2003: Formation of convective carbon dioxide clouds near the south pole of Mars. *J. Geophys. Res.*, 108(E7), 17.1-17.19.
- Fitscher, G., Kurth, W. S., Dyudina, U. A., Kaiser, M. L., Zarka, P., Lecacheux, A., Ingersoll, A. P., Gurnett, D. A., 2007: Analysis of a giant lightning storm on Saturn. *Icarus*, 190, 528-544.

# References

- Flasar, F. M., 1998: The composition of Titans atmosphere : a meteorological perspective. Planet. Space Sci., Vol. 46, 1109-1124.
- Forget, F. and Pierrehumbert, R. T., 1997: Warming Early Mars with Carbon Dioxide Clouds That Scatter Infrared Radiation. Science, 278, 1273-1276.
- Guillot, T., 1995: Condensation of methane, ammonia and water and the inhibition of convection in giant planets. Science, 269, 16997-99.
- Manabe, S., and Strickler, R. F., 1964: Thermal Equilibrium of the Atmosphere with a Convective Adjustment. J. Atmos. Sci., 21, 361-385.
- McDonald, J. E., 1964: On a Criterion Governing the Mode of Cloud Formation in Planetary Atmospheres. J. Atmos. Sci., 21, 76-82,
- Mitchell, J. L., Pierrehumbert, R. T., Frierson, D. M. W., Caballero, R., 2009: The impact of methane thermodynamics on seasonal convection and circulation in a model Titan atmosphere. Icarus 203, 250-254.
- Montmessin, F., Gondet, B., Bibring, J.-P., Langevin, Y., Drossart, P., Forget, F., and Fouchet T., 2007: Hyperspectral imaging of convective CO<sub>2</sub> ice clouds in the equatorial mesosphere of Mars. J. Geophys. Res., 112, E11S90.
- Nakajima, K., Takehiro, S., Ishiwatari, M., and Hayashi, Y.-Y., 1998: "Cloud convections" in Geophysical and planetary fluids. Nagare Multimedia. (in Japanese)  
<http://www2.nagare.or.jp/mm/98/nakajima/index.htm>

# References

- Nakajima, K., Takehiro, S., Ishiwatari, M., and Hayashi, Y.-Y., 2000: Numerical modeling of Jupiter's moist convection layer. *Geophys. Res. Lett.*, 27, 19, 3129-3132.
- Pauluis, O., and I. M. Held, 2002: Entropy Budget of an Atmosphere in Radiative-Convective Equilibrium. Part I: Maximum Work and Frictional Dissipation. *J. Atmos. Sci.*, 59, 125-139.
- Pauluis, O., and I. M. Held, 2002: Entropy Budget of an Atmosphere in Radiative-Convective Equilibrium. Part II: Latent Heat Transport and Moist Processes. *J. Atmos. Sci.*, 59, 140-149.
- Pierrenumbert, R. T., and Erlick, C., 1998: On the Scattering Greenhouse Effect of CO<sub>2</sub> Ice Clouds. *J. Atmos. Sci.*, 147, 1897-1903.
- Seinfeld, J. H., and Pandis, S. N., 1998: *Atmospheric Chemistry and Physics*. Wiley-Interscience.
- Sugiyama, K., Odaka, M., Nakajima, K., and Hayashi, Y.-Y., 2009: Development of a Cloud Convection Model to Investigate the Jupiter's Atmosphere. Nagare Multimedia, <http://www.nagare.or.jp/mm/2009/sugiyama/>.
- Sugiyama, K., Odaka, M., Nakajima, K., and Hayashi, Y.-Y., Numerical Modeling of Moist Convection in Jupiter's Atmosphere, CPS 6th International School of Planetary Sciences, P-27, 4-9 January, 2010, Kobe, Japan.
- Tao, W.-K., and Moncrieff, M. W., 2009: Multiscale clouds system modeling. *Rev. Geophys.*, 47, RG4002.
- Vasavada, A. R., and Showman, A. P., 2005: Jovian atmospheric dynamics: an update after Galileo and Cassini. *Rep. Prog. Phys.*, 68, 1935-1996.

# References

Wallace, J. M., and Hobbs, P. V., 2006: *Atmospheric Science 2nd ed.* Academic Press.

Yamashita, T., Odaka, M., Sugiyama, K., Nakajima, K., Ishiwatari, M., and Hayashi, Y.-Y.,  
Two-dimensional numerical experiments of Martian atmospheric convection with  
condensation of the major component, CPS 6th International School of Planetary  
Sciences, P-37, 4-9 January, 2010, Kobe Japan.

<http://www.gfd-dennou.org/arch/prepri/2010/pschool6/yamasita/presen/pub/>.

中島健介, 1998: 木星の大気構造と雲対流. 日本惑星学会誌「遊・星・人」, 7, 143-153.